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Combining chirality with Parity-Time (PT) symmetry in metamaterials

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hotonic Metamaterials





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Outline

- Introduction
 - Parity-Time (PT) symmetry
 - chirality and chiral metamaterials
- Combining chirality with PT symmetry
 - conditions for PT symmetry with chirality
 - **scattering** by a PT chiral double-slab
 - normal incidence
 - oblique incidence
- Practical implementations
- PT symmetry for **molecular chirality sensing**



The concept of Parity-Time (PT) symmetry

Schrödinger Equation: $\hat{H}\Psi(x) = E\Psi(x)$

Hamiltonian

$$\hat{H} = -\frac{\hbar^2}{2m}\frac{d^2}{dx^2} + V(x)$$

Parity-Time-symmetric Hamiltonians <u>can have</u> real eigenvalues even if not-Hermitian

Bender, Phys. Rev. Lett. 80, 5243, 1998

PT-symmetric Hamiltonian: $[\hat{P}\hat{T}, \hat{H}] = 0 \Rightarrow \hat{P}\hat{T}\hat{H} = \hat{H}\hat{P}\hat{T}$

Parity: spatial inversion

$$\hat{P}: \begin{cases}
\mathbf{r} \to -\mathbf{r} \\
\mathbf{p} \to -\mathbf{p} \\
\mathbf{E} \to -\mathbf{E} \text{ polar vector} \\
\mathbf{H} \to \mathbf{H} \text{ axial vector}
\end{cases}
\quad
\hat{T}: \begin{cases}
t \to -t \\
i \to -i \\
\mathbf{r} \to \mathbf{r} \\
\mathbf{E} \to \mathbf{E} \\
\mathbf{H} \to -\mathbf{H}
\end{cases}$$

The concept of Parity-Time (PT) symmetry

PT-symmetric Hamiltonians can have real eigenvalues even if not-Hermitian

$$\hat{H}\Psi(x) = E\Psi(x)$$

$$[\hat{P}\hat{T}, \hat{H}] = 0 \Rightarrow \hat{P}\hat{T}\hat{H} = \hat{H}\hat{P}\hat{T}$$

$$\hat{H} = -\frac{\hbar^2}{2m}\frac{d^2}{dx^2} + V(x)$$
Condition: $V(x) = V^*(-x)$

$$\begin{bmatrix} \operatorname{Re}[V(x)] = \operatorname{Re}[V(-x)] \text{ (even in } x) \\ \operatorname{Im}[V(x)] = -\operatorname{Im}[V(-x)] \text{ (odd in } x) \end{bmatrix}$$
Example of PT-symmetric potential

$$\int \frac{\mathsf{Re}}{\bigcup_{i=1}^{1} - \frac{1}{5}} \int_{S} \frac{\mathsf{Re}}{\operatorname{Im}} \int_{S} \frac{\mathsf{Re}}{\operatorname{Im}$$

Parity-Time (PT) symmetry in optics

In optics, wave propagation in paraxial approximation is governed by a Schrödinger-like equation



Novel effects in PT symmetric optical systems





Coherent perfect absorption (CPA) and lasing at same frequency

PRA 82, 031801(R) (2010), PRL 106, 093902 (2011) Science 346 (6212), 975 (2014)



How can we extend these effects in chiral systems?

Chirality and chiral metamaterials

Chiral structure: not identical to its mirror image



chirality is expressed via the parameter к

$$\boldsymbol{D} = \varepsilon \varepsilon_0 \boldsymbol{E} + i(\kappa / c) \boldsymbol{H}$$
$$\boldsymbol{B} = \mu \mu_0 \boldsymbol{H} - i(\kappa / c) \boldsymbol{E}$$

magneto-electric coupling

Consequences of chirality:

- 1. eigenmodes: circularly polarized waves
 - Right Circularly Polarized (RCP or +)
 - Left Circularly Polarized (LCP or)

 $E_{\pm}(\hat{x}\pm i\hat{y})$

2. *different index* for RCP (+) and LCP (-) waves!

$$n_{\pm} = \sqrt{\varepsilon \mu} \pm \kappa$$

Chirality-originated effects



Questions

Can we achieve Parity-Time symmetry in chiral media?

if yes

Under what conditions?

See Droulias et. al., Phys. Rev. Lett 122, 213201 (2019) Katsantonis et. al., Photonics 7, 43 (2020)

To answer the questions...



Questions

Can we achieve Parity-Time symmetry in chiral media?



Under what conditions?

$$\begin{bmatrix} \varepsilon(\mathbf{r}) = \varepsilon^*(-\mathbf{r}) \\ \mu(\mathbf{r}) = \mu^*(-\mathbf{r}) \\ \kappa(\mathbf{r}) = -\kappa^*(-\mathbf{r}) \\ \leftarrow addi$$

as in non-chiral systems

additional condition

See Droulias et. al., Phys. Rev. Lett 122, 213201 (2019) Katsantonis et. al., Photonics 7, 43 (2020)

Our PT-chiral system/bilayer

Homogenous, non-dispersive, chiral media

Investigation of scattering (transmission/reflection) properties



Scattering by Parity-Time (PT) symmetric systems



The "chiral" scattering matrix, S



Subscripts: +: RCP wave, -: LCP wave a, b, c, d: amplitudes of incoming and outgoing waves

$$\begin{array}{l}
\mathbf{4} \\
\left(\begin{array}{c}
Left - \\
Right + \\
Left + \\
Right -
\end{array}\right) = S \begin{pmatrix}
Left + \\
Right - \\
Left - \\
Left - \\
Right +
\end{array}) \\
S = \begin{pmatrix}
r^{(L)} & t_{--} & 0 & 0 \\
t_{++} & r^{(R)} & 0 & 0 \\
0 & 0 & r^{(L)} & t_{++}
\end{array}$$

Superscripts: (L)/(R): Left/Right incidence

0

t

 $r^{(R)}$

Generalized unitarity relation for S

0

$$PTS(\omega^*)PT = S^{-1}(\omega)$$

See Droulias et. al., Phys. Rev. Lett 122, 213201 (2019) Katsantonis et. al., Photonics 7, 43 (2020)

L. Ge et al, Phys. Rev. A 85, 023802 (2012)

Transmission – Reflection for normal incidence

Analytical calculations for a general chiral bi-layer



S-matrix (4x4) features for normal incidence

Scattering matrix eigenvalues, σ (two degenerate pairs)

$$\begin{array}{c|c} & G & L & \leftarrow \\ & & & & \\ & & & \\ & & & &$$

$$- \sigma_{1,2} = \frac{1}{2} (r^{(L)} + r^{(R)} \pm \sqrt{(r^{(L)} - r^{(R)})^2 + 4t_{++}t_{--}}$$

Scattering matrix eigenvalues independent of chirality

Exceptional point, PT-phases, CPA-laser points **independent of chirality!!**

Conservation relation



Exceptional point location $\frac{R^{(L)} + R^{(R)}}{2} - \sqrt{T_{++}T_{-}} = 1$



Optical activity and ellipticity – normal incidence



Possibility for independent control of PT properties (exceptional point, reflection/transmission resonances, CPA-laser points) and transmitted wave polarization (θ, η) !

E.g. CPA-laser for circularly polarized waves!

 $\mathcal{E} = 3 \pm 0.4i, \mu = 1.1 \pm 0.1i, \kappa = \pm 0.04 - 0.04i$

Off-normal incidence: Mixed-PT phase



Eigenvalues depend on chirality, κ

Eigenvalues don't form two degenerate pairs

Appearance of a mixed-PT phase

Scattering matrix eigenvalues, σ

Non-chiral

Chiral-PT, κ=0.04(1+i)



Tuning the different phases and the exceptional points



Angle-dependent and asymmetric chiral effects



 $\varepsilon = 3 \pm 0.4i, \mu = 1.1 \pm 0.1i, \kappa = \pm 0.04 - 0.04i$

PT symmetric chiral metamaterial practical realization?

Bilayer-metal structures (unit cells)



PT-phase transition in a realistic system



Summarizing

Combining PT-symmetry with chirality:

Normal incidence → possibility of independent control of PT-effects and polarization

Off-normal incidence →

- mixed PT-phases
- multiple exceptional points
- angle-dependent and chirality-dependent PT and polarization features
- asymmetric (side-dependent) polarization features

For more info see

Droulias et. al., Phys. Rev. Lett **122**, 213201 (2019) Katsantonis et. al., Phy. Rev. B **101**, 214109 (2020) Katsantonis et. al., Photonics **7**, 43 (2020)

PT symmetry for molecular chirality sensing



Enantiomer detection and discrimination is of great importance for biology and pharmaceutical industry

Chirality effects used for sensing

$$n_{\pm} = \sqrt{\varepsilon\mu} \pm \kappa$$

Optical activity Rotation of linear polarization *Circular dichroism (CD)* Different absorption for RCP(+)/LCP(-) waves: *CD*: *A*₊-*A*₋

measured by:

$$CD = A_{+} - A_{-} = \left| t_{-} \right|^{2} - \left| t_{++} \right|^{2}$$

transmittance of transmittance of LCP (-) waves RCP (+) waves

In natural chiral media $\kappa^{-10^{-4}} \rightarrow$ weak chiro-optical signals, e.g. CD~10⁻⁵

Chirality effects used for sensing

 $n_{\pm} = \sqrt{\varepsilon \mu \pm \kappa}$

Kuhn's dissymmetry factor, g
Relative differential absorption
for RCP(+)/LCP(-) waves
$$g=(A_+-A_-)/[(A_++A_-)/2]$$

(percentage of enantioselectivity in
photoexcitations)

$$g = \frac{A_{+} - A_{-}}{(A_{+} + A_{-})/2} = \frac{CD}{(A_{+} + A_{-})/2}$$

Circular dichroism (CD) Different absorption for RCP(+)/LCP(-) waves: *CD*: *A*₊-*A*₋

measured by:

$$CD = A_{+} - A_{-} = \left| t_{-} \right|^{2} - \left| t_{++} \right|^{2}$$

Enhancing g → Enhanced enantioselectivtiy in photoionization, photolysis, fluorescence, photopolymerization, etc.

In natural chiral media $\kappa^{-10^{-4}} \rightarrow$ weak chiro-optical signals, e.g. CD~10⁻⁵

Absorption in chiral media

Absorbed power density of a CP (+/-) wave by a thin chiral layer of parameters ε , μ , κ (Poynting's th.

$$A_{\pm} \sim \frac{\omega}{2} [\operatorname{Im}(\varepsilon) | \mathbf{E} |^{2} + \operatorname{Im}(\mu) | \mathbf{H} |^{2}] \pm \frac{2\omega}{c} \operatorname{Im}(\kappa) \operatorname{Im}(\mathbf{E} \cdot \mathbf{H}^{*}) \xrightarrow{\text{LCP}} \mathbf{E}$$

$$CD = A_{+} - A_{-} = 4c \operatorname{Im}(\kappa) \left(\frac{\omega}{2c^{2}} \operatorname{Im}(\mathbf{E} \cdot \mathbf{H}^{*}) \right) \xrightarrow{\text{Field chirality}} \mathbf{f}_{c}$$

$$CD = A_{+} - A_{-} = 4c \operatorname{Im}(\kappa) \left(\frac{\omega}{2c^{2}} \operatorname{Im}(\mathbf{E} \cdot \mathbf{H}^{*}) \right) \xrightarrow{\text{Field chirality}} \mathbf{f}_{c}$$

$$C = -\frac{\omega}{2c^{2}} \operatorname{Im}(\mathbf{E} \cdot \mathbf{H}^{*})$$

$$Tang \& \text{Cohen, PRL 104, 163901}$$

(2010)

Nanophotonics for enhancing circular dichroism





Alu, Nat. Commun. 8, 14180 (2017)



Superiority of achiral structures – Overlapping resonances – up to 150x CD enhancement

Absorption in chiral media

Absorbed power density of a CP wave by a thin chiral layer of parameters ε , μ , κ

$$A_{\pm} \sim \frac{\omega}{2} [\operatorname{Im}(\varepsilon) | \mathbf{E} |^{2} + \operatorname{Im}(\mu) | \mathbf{H} |^{2}] \pm \frac{2\omega}{c} \operatorname{Im}(\kappa) \operatorname{Im}(\mathbf{E} \cdot \mathbf{H}^{*}) \xrightarrow[\text{LCP}]{} \longrightarrow$$

$$CD = A_{+} - A_{-} = 4c \operatorname{Im}(\kappa) \left[\frac{\omega}{2c^{2}} \operatorname{Im}(\mathbf{E} \cdot \mathbf{H}^{*})\right]$$

Enhancement through proper resonances – enhanced local fields

Tang & Cohen, PRL 104, 163901 (2010)

Field chirality

$$g = \frac{2(A_+ - A_-)}{A_+ + A_-} \propto \frac{8c \operatorname{Im}(\kappa)C}{\omega[\operatorname{Im}(\varepsilon) | E|^2 + \operatorname{Im}(\mu) | H|^2]}$$

Nodes of standing wave in specially designed cavity Tang & Cohen, PRL104, 163901 (2010)

11-fold g-enhancement (fluorescence) ^{11-fold g-enhancement (fluorescence)} ^{11-fold g-enhancement (fluorescence)} ^{11-fold g-enhancement (fluorescence)} ^{10-fold g-enhancement (fluorescence)} ^{10-fold}

He et al., Nature Comm. (2018) (Photopolymerization dissymmetry)

 $\operatorname{Im}(\boldsymbol{E}\cdot\boldsymbol{H}^*)$

 \overrightarrow{d}_{C}

Our approach: Combine loss and gain media



• Balanced loss and gain $Im(\varepsilon_{gain})=-Im(\varepsilon_{loss})$

 $\varepsilon(z) = \varepsilon^*(-z)$ $\mu(z) = \mu^*(-z)$

- Strong fields at gain-loss interface
- Peculiar, potentially useful electromagnetic effects

 (unidirectional invisibility, simultaneous coherent perfect
 absorption & lasing)
 I. Katsantonis et. al., Phys. Rev. B 105, 174112 (2022)

CD enhancement in the PT-symmetric 3-layer system



Transmission / reflection / scattering matrix for the 3-layer PT system

Electric field at the CD peak of 3-layer PT system

g-enhancement in the PT-symmetric 3-layer system

q-enhancement investigation for the PTsymmetric 3-layer system Gain

Loss

2

g enhancements @ R=0, T≈1

Conclusions/summary

PT-symmetric media provide a promising avenue for molecular chirality sensing and enantioselective field-molecule interactions

In such systems:

Large Circular Dichroism enhancements

Large dissymmetry factor (g) enhancements with appreciable field intensities

For details: I. Katsantonis et. al., Phys. Rev. B 105, 174112 (2022)

