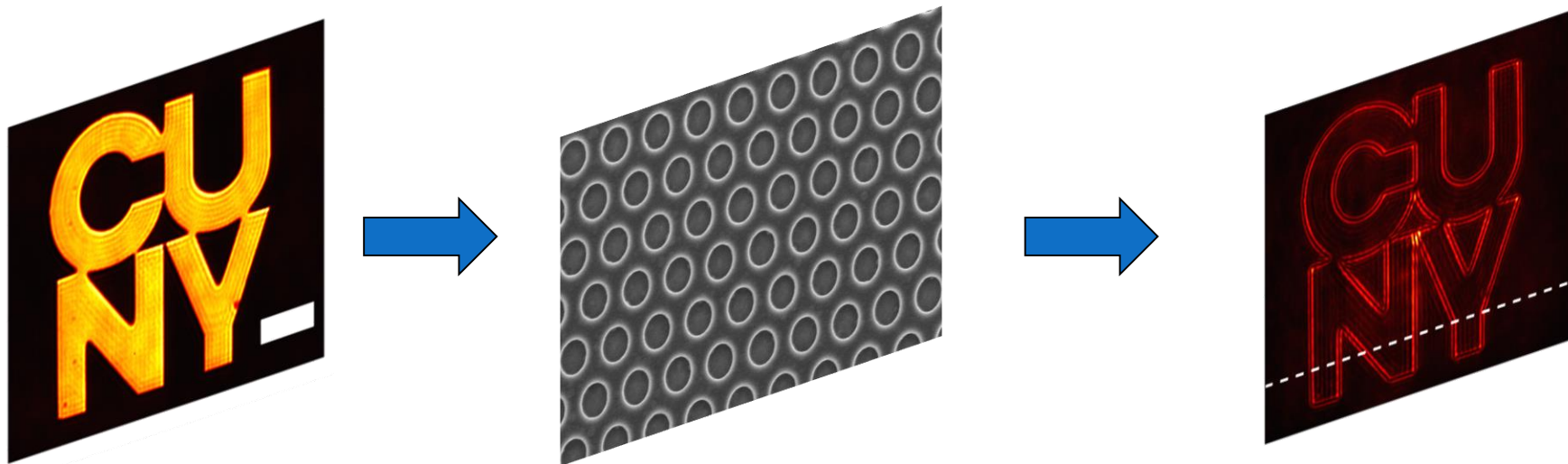




ANALOG IMAGE PROCESSING WITH METAMATERIALS

Michele Cotrufo, Advanced Science Research Center (CUNY), New York



OUTLINE

1. Introduction

- Why do we need analog computing and image processing?
- How can metamaterials and metasurfaces perform image processing?

2. Spatial Image Processing: State of the art and Main challenges

- What are the different approaches used?
- Which figures of merit we need to improve to go from proof-of-principles to useful devices?
- How to overcome the need for coherent illumination?

3. What's next?

- Spatio-temporal image processing
- More complex mathematical operations
- Reconfigurable devices

4. (Open) Discussion

- Beyond the hype: What are (if any) the real benefits of metasurfaces in image processing?
- Are metasurface-based image-processing devices always worth the effort?

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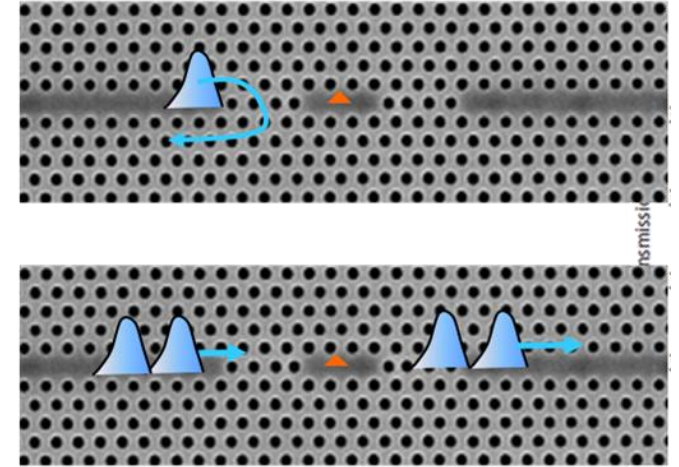
DIGITAL VS. ANALOG COMPUTING



Valve body of an automatic transmission
Hydraulic Analog Computer

- Digital computers dominate our world, from data centers to personal computers, cell phones...
- They also require enormous amounts of power. ***Information processing and communications consume >10% of total energy in the US, and growing...***
- On average a single Google search produces ***0.2-0.3 grams of CO₂ emissions***
- Analog computers use continuous variations of a physical quantity to process signals – typically electrical, mechanical or hydraulic quantities.
- Their use faded out because of sensitivity to noise and other non-idealities.
- ***Today there is renewed interest (neuromorphic computing, hardware acceleration...), especially because of improved nanofabrication skills***

USING LIGHT FOR ANALOG COMPUTING



- Light is *ubiquitous*, and *cheap*
- We have learned how to control it very accurately *at the nanoscale* using *photonic crystals* and *metamaterials*
- Light provides an ideal platform for *ultrafast*, *ultralow-energy* signal processing and analog computing

USING LIGHT FOR ANALOG COMPUTING

$$f_{\text{in}}(x, y, t, \dots) \rightarrow \mathbf{E}_{\text{in}}(r, t)e^{i\omega_0 t}$$



Optical Components,
Metamaterials

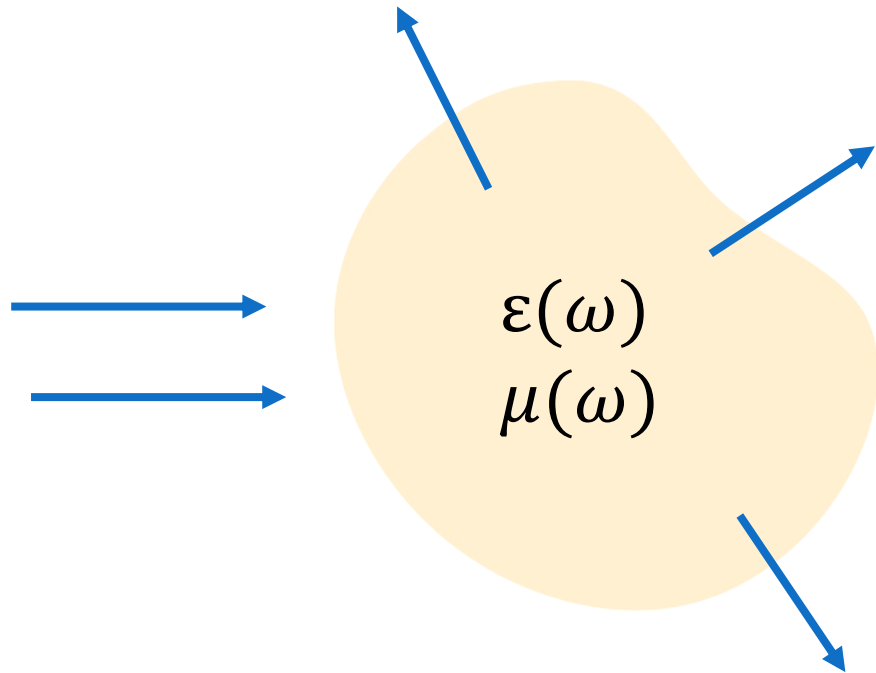
$$\mathbf{E}_{\text{out}}(r, t)e^{i\omega_0 t} \rightarrow f_{\text{out}}(x, y, t, \dots)$$



- Light is ***ubiquitous***, and ***cheap***
- We have learned how to control it very accurately ***at the nanoscale*** using ***photonic crystals*** and ***metamaterials***
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ELECTROMAGNETIC METAMATERIALS

Meta (from the Greek, “beyond”)-Material

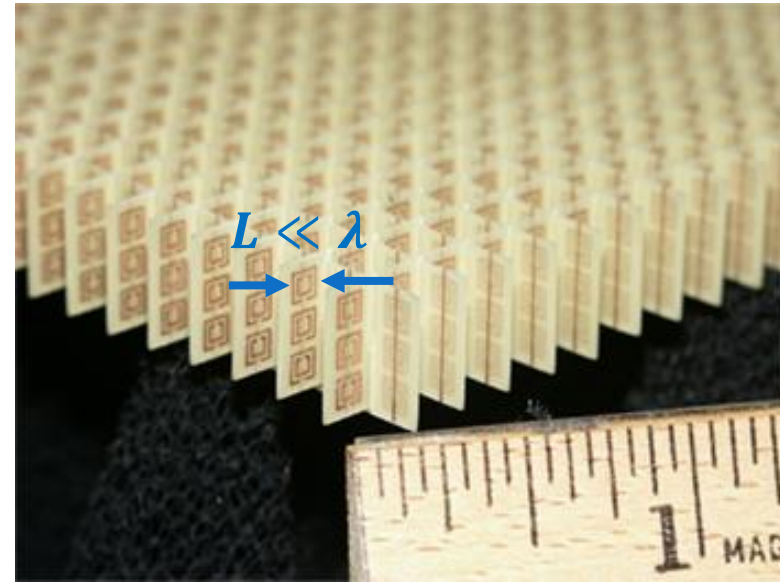


“Natural” materials

Limited sets of material properties:

- Refractive Index
- Frequency-Dependence
- Chirality
- Bianisotropy

-

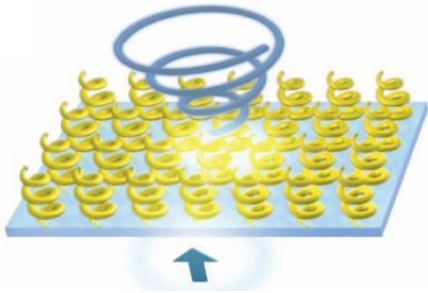


Shelby et al., *Applied Physics Letters* **78** (4): 489 (2001)

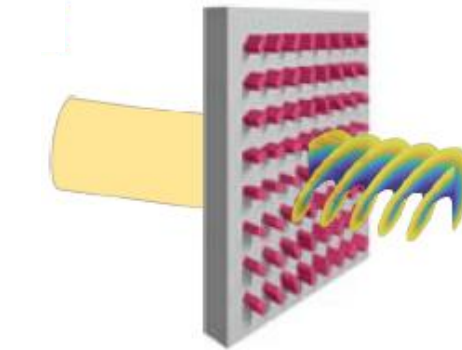
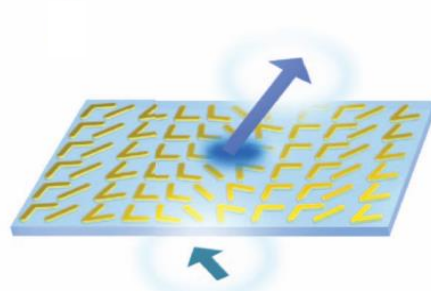
- Artificial materials made by “**meta-atoms**” $\ll \lambda$
- Electromagnetic Radiation sees only an “**average**” response
- Materials with **optical responses not available in nature**

PHOTONIC METAMATERIALS

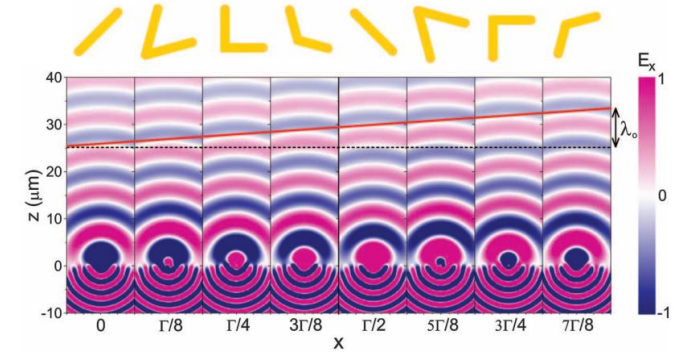
Optical Metamaterials and Metasurfaces



A.F. Koenderink, A. Alù, and A. Polman, *Science* (2015)



K. Wang et al., *Phys. Today* (2022).

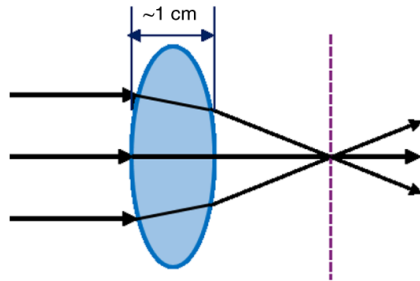


N. Yu et al., *Science* (2011).

Advanced Optical Functionalities in very Compact Footprints

Conventional Lens

- Phase delay from **thickness and shape**
- Response mainly dictated by **intrinsic material properties**



Metalens

- Phase delay by **scattering from sub-wavelength inclusions**
- Response dictated by **shape, orientation and arrangement of inclusions**

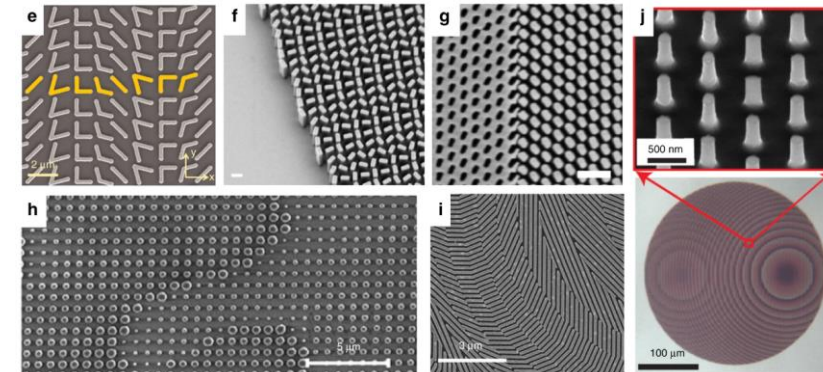
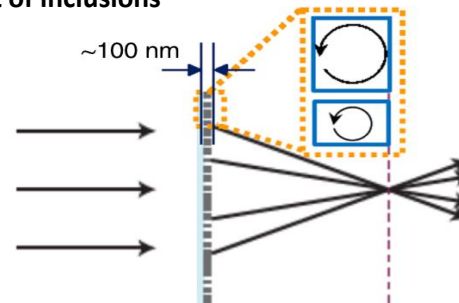
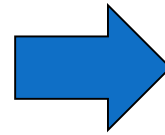
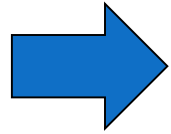


IMAGE PROCESSING

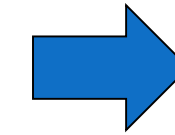
Digital Image Processing



$$f(x, y)$$

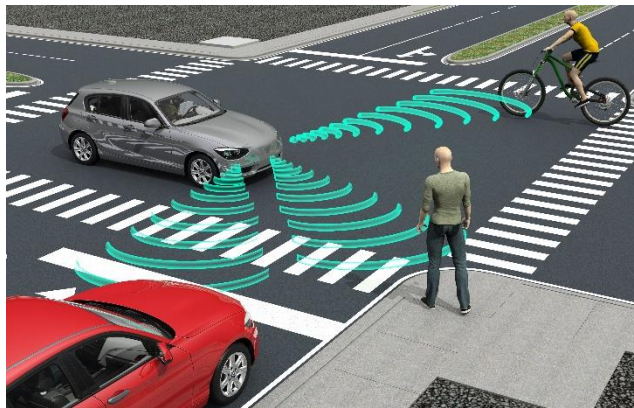


$$\nabla^2 .$$



$$\nabla^2 f(x, y)$$

Self-driving cars



<https://www.rdworldonline.com/>

Enhance edges to simplify object detection



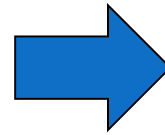
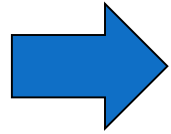
<https://towardsdatascience.com/>

IMAGE PROCESSING

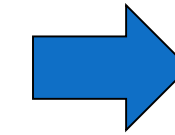
Digital Image Processing



$$f(x, y)$$



$$\nabla^2 .$$



$$\nabla^2 f(x, y)$$

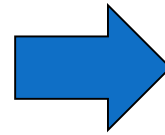
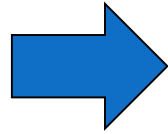
- Medical Imaging
- Fingerprint Recognition
- Satellite Images
- Robotic Vision
- ...

IMAGE PROCESSING

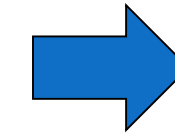
Digital Image Processing



$$f(x, y)$$



$$\nabla^2 .$$



$$\nabla^2 f(x, y)$$

Pros:

- Programmable
- Highly versatile.

Cons:

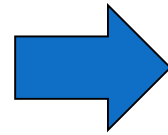
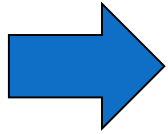
- Require hardware for computation.
- Might be “too slow” for certain applications.
- Energy consumption.

IMAGE PROCESSING

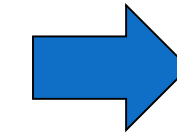
Digital Image Processing



$$f(x, y)$$



$$\nabla^2 .$$

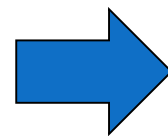
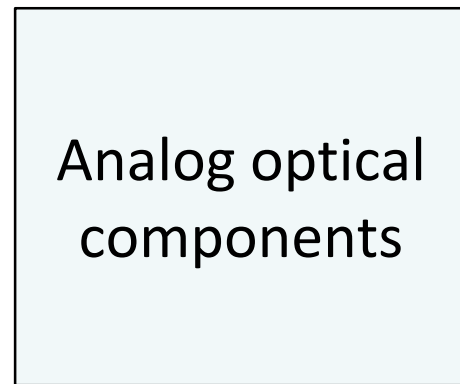
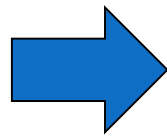


$$\nabla^2 f(x, y)$$

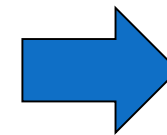
Analog Image Processing



$$E_{\text{in}}(x, y, t) = f(x, y)e^{i\omega_0 t} \hat{e}$$

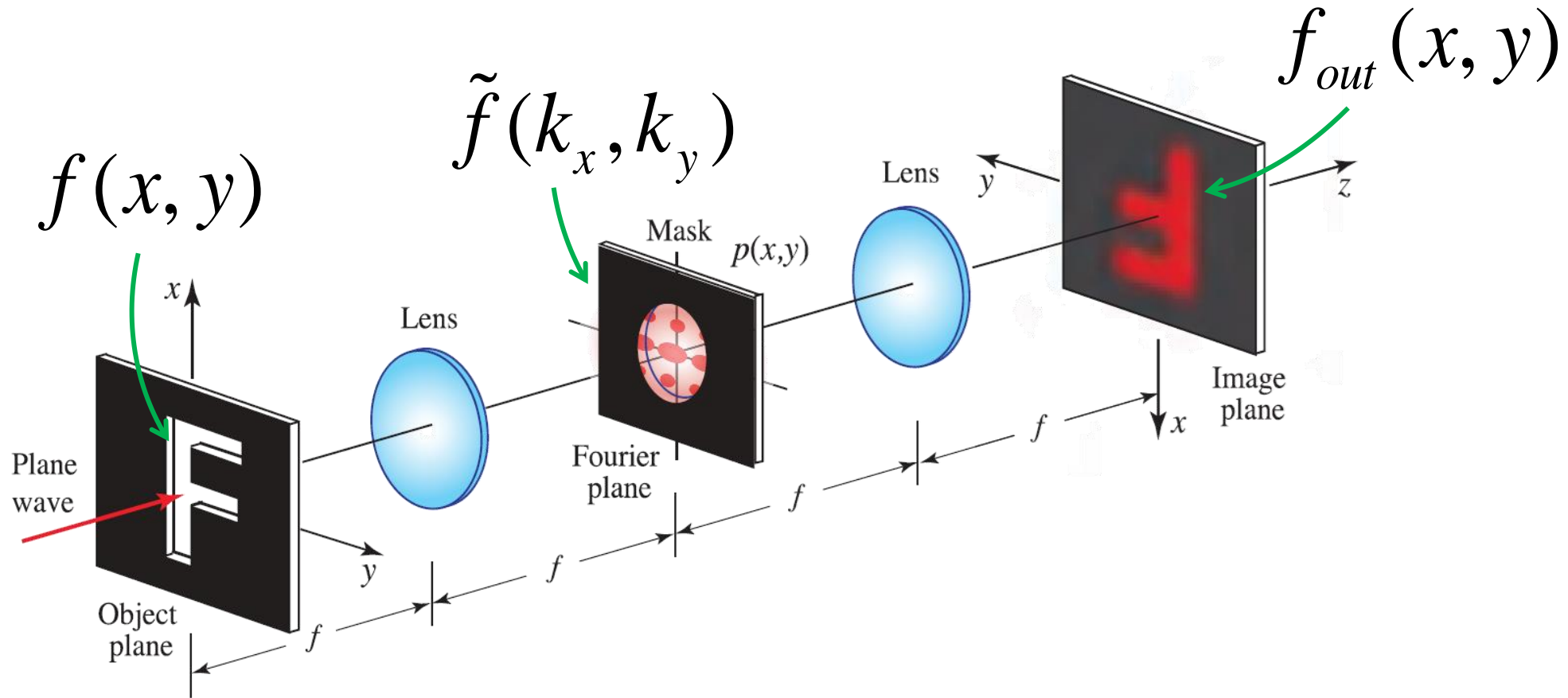


$$E_{\text{out}}(x, y, t) = \nabla^2 f(x, y)e^{i\omega_0 t} \hat{e}$$



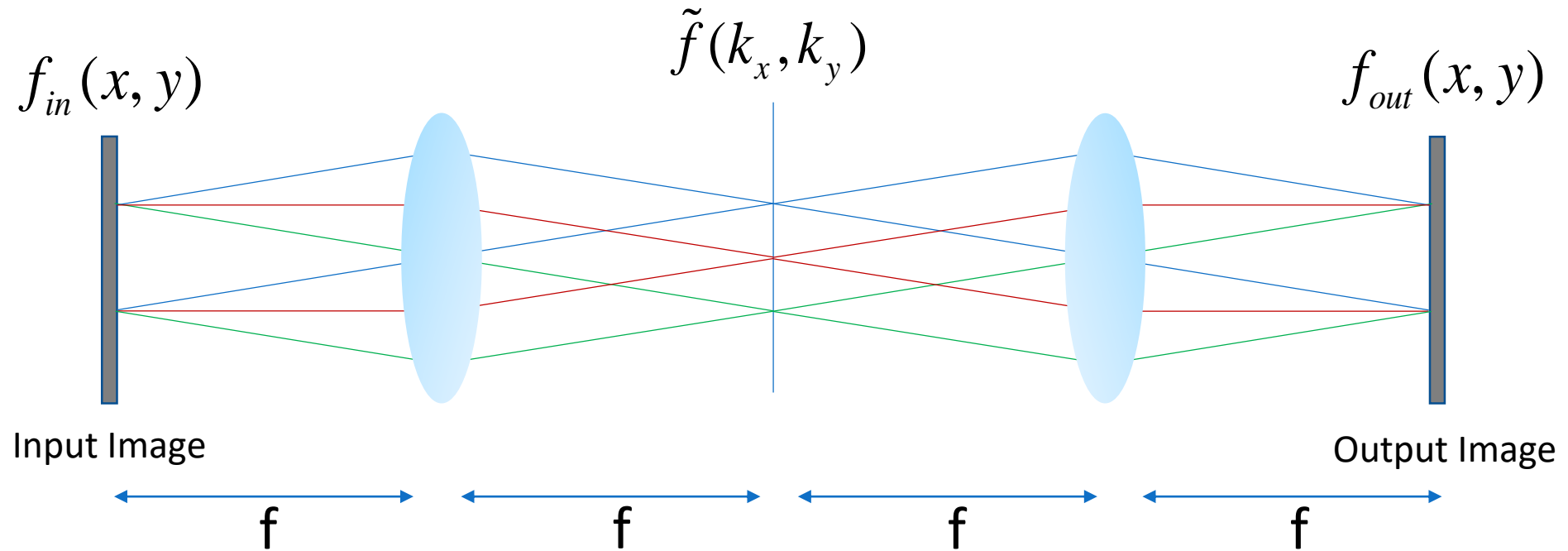
ANALOG IMAGE PROCESSING: FOURIER OPTICS

Standard Method for K-Space Filtering



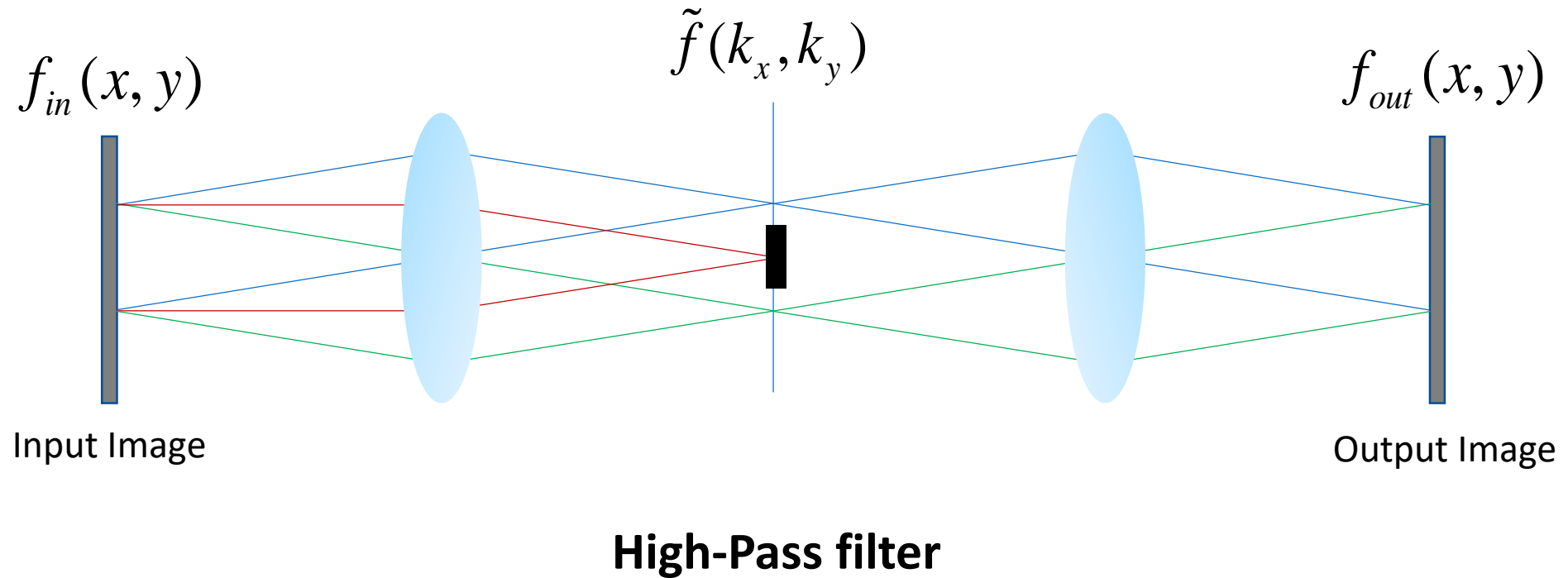
ANALOG IMAGE PROCESSING: FOURIER OPTICS

K-space filtering with a 4F system



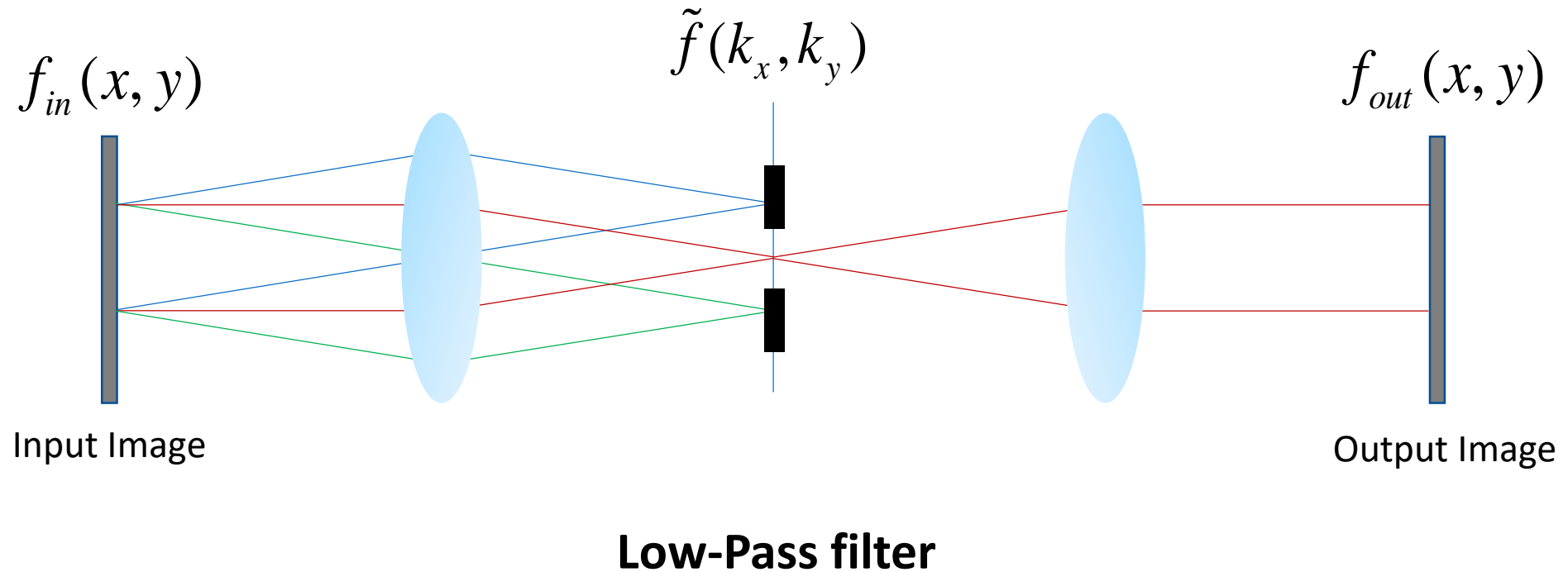
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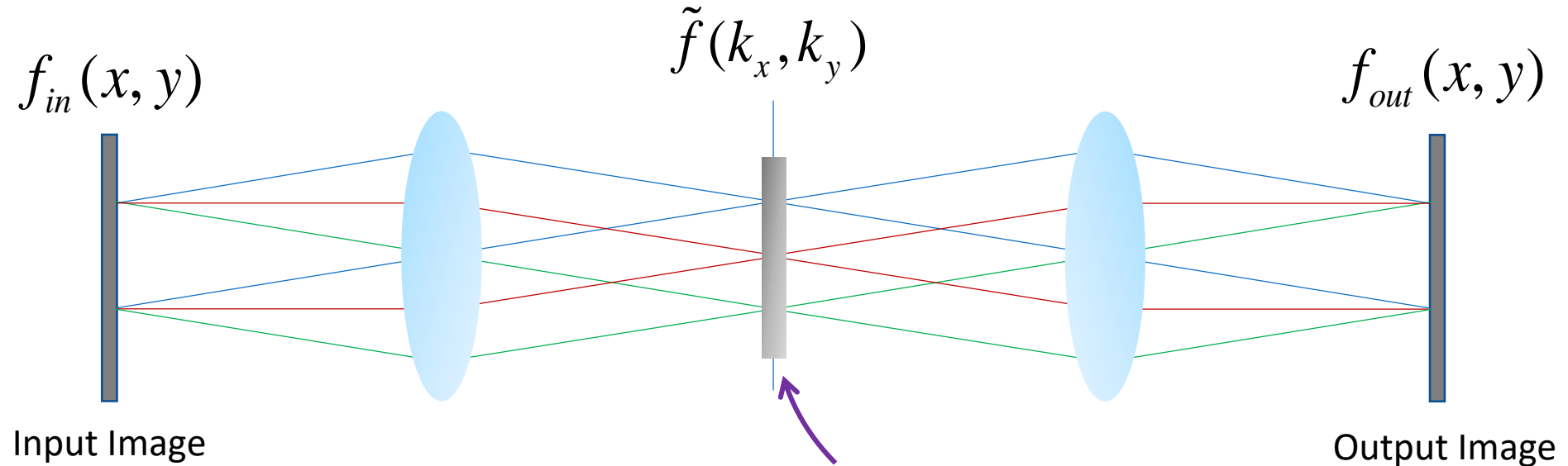
ANALOG IMAGE PROCESSING: FOURIER OPTICS

K-space filtering with a 4F system



ANALOG IMAGE PROCESSING: FOURIER OPTICS

K-space filtering with a 4F system



Mask with arbitrary spatially dependent profile

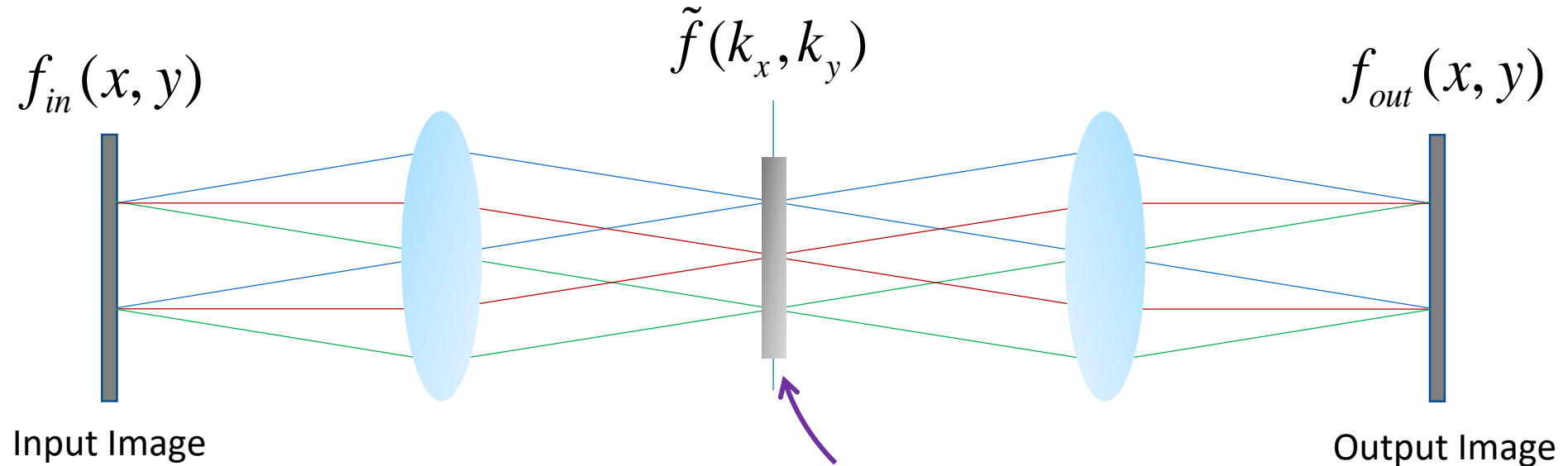
$$t(x, y) \rightarrow t(k_x, k_y)$$

Transfer Function

$$f_{out}(x, y) = \iint dx dy t(k_x, k_y) \tilde{f}(k_x, k_y) e^{-i(k_x x + k_y y)}$$

ANALOG IMAGE PROCESSING: FOURIER OPTICS

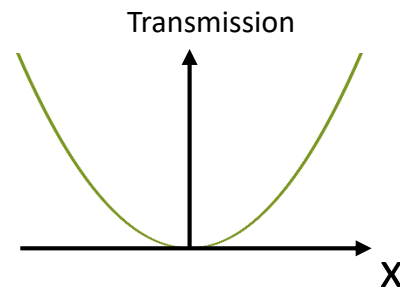
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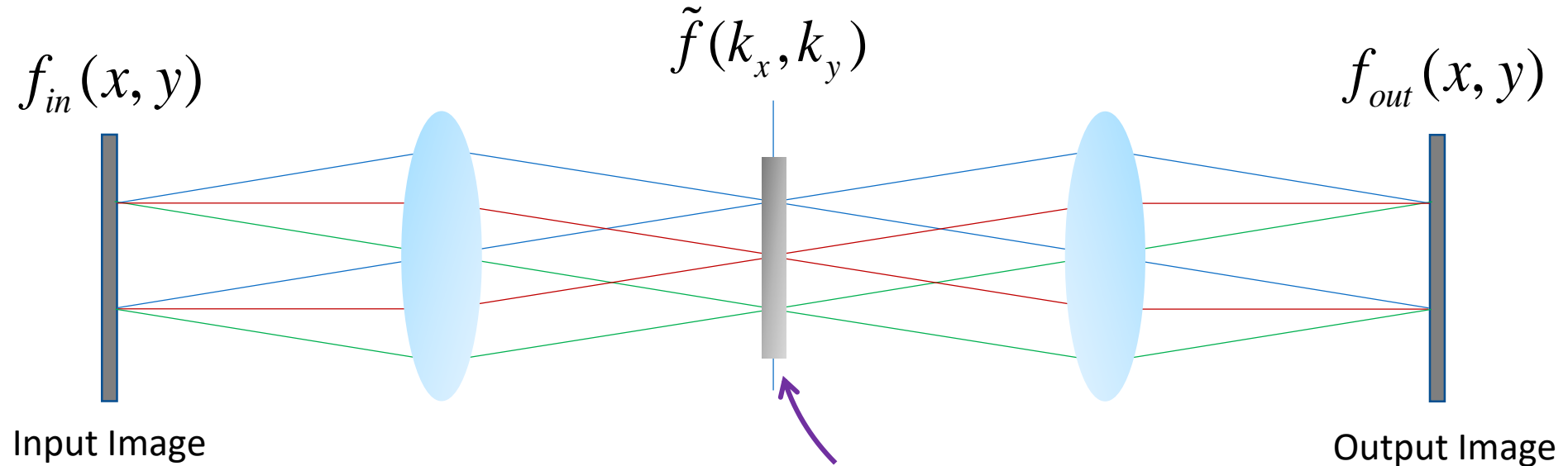
**Example:
Laplacian operation**



$$t(k_x, k_y) \propto (k_x^2 + k_y^2) \Rightarrow f_{out}(x, y) \propto (\partial_x^2 + \partial_y^2) f(x, y)$$

ANALOG IMAGE PROCESSING: FOURIER OPTICS

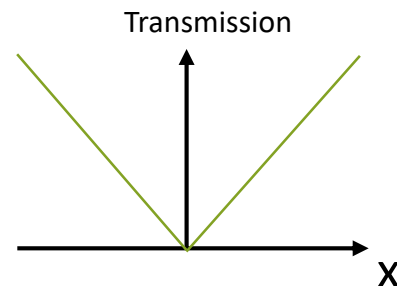
K-space filtering with a 4F system



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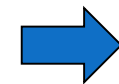
$$t(x, y) \rightarrow t(k_x, k_y)$$

Example:
Phase Contrast



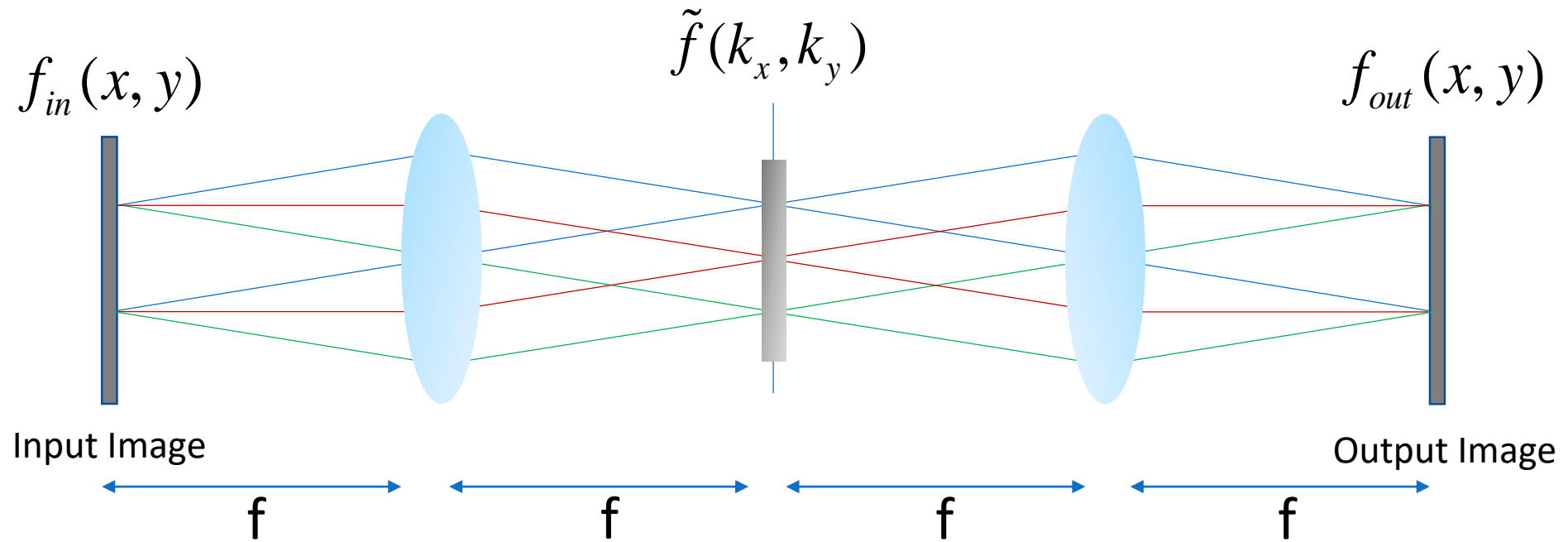
$$t(k_x, k_y) \propto k_x$$

$$f_{in}(x, y) = f_0 e^{i\phi(x, y)}$$



$$f_{out}(x, y) \propto \partial_x \phi(x, y)$$

ANALOG IMAGE PROCESSING: FOURIER OPTICS



Pros: very easy to target a desired k-vector

Cons: inherently **bulky technique**:

- Need to access the Fourier space
- Total footprint $\geq 4f$
- Not suited for integrated applications (smartphones, compact microscopes, etc.)

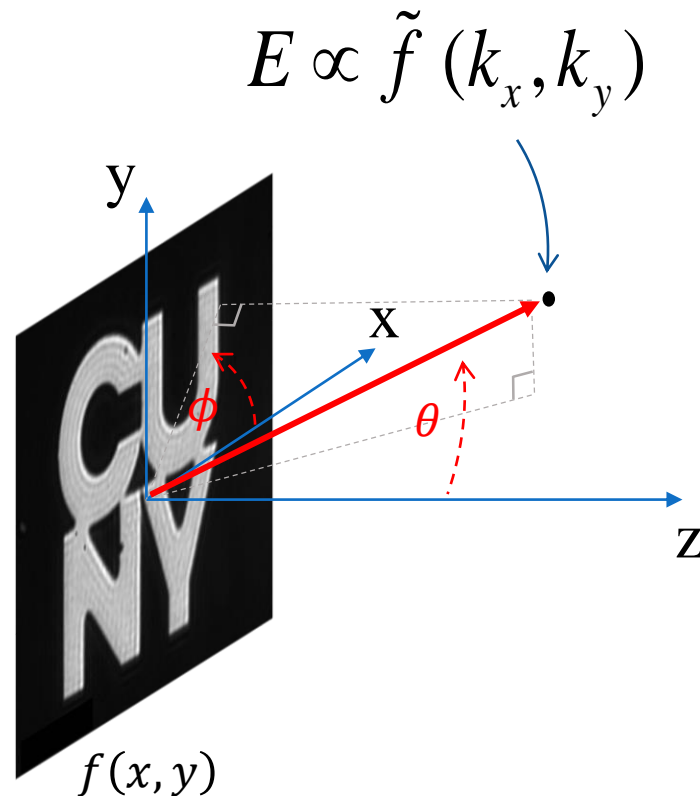
$$f_{out}(x, y) = \iint dx dy t(k_x, k_y) \tilde{f}(k_x, k_y) e^{-i(k_x x + k_y y)}$$



ANALOG SIGNAL PROCESSING WITH METASURFACES

We do not need to physically access the back focal plane to obtain the Fourier transform

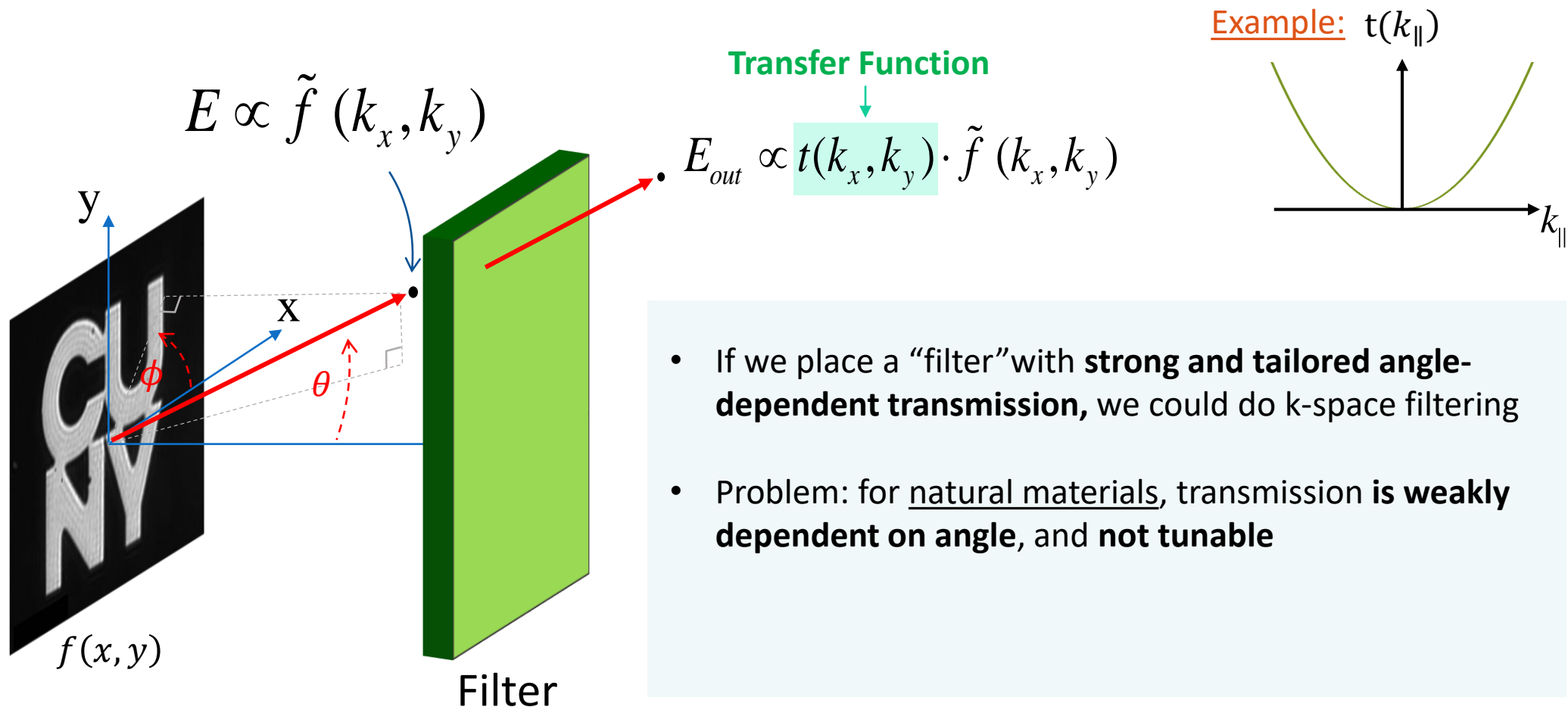
Optics gives us the Fourier transform for free (i.e., without lenses)



Each diffracted wave, propagating at a specific angle, “carries” a different Fourier component

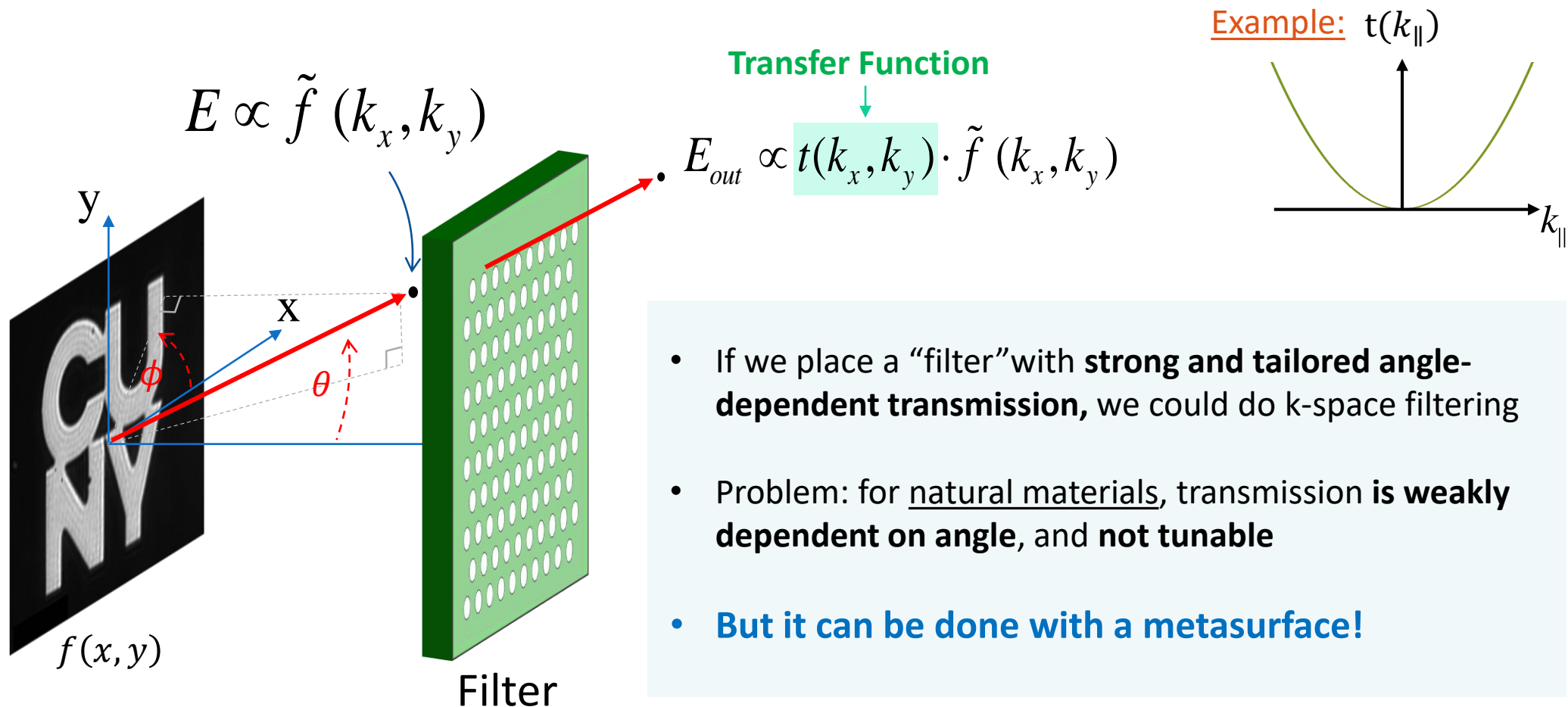
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ANALOG SIGNAL PROCESSING WITH METASURFACES

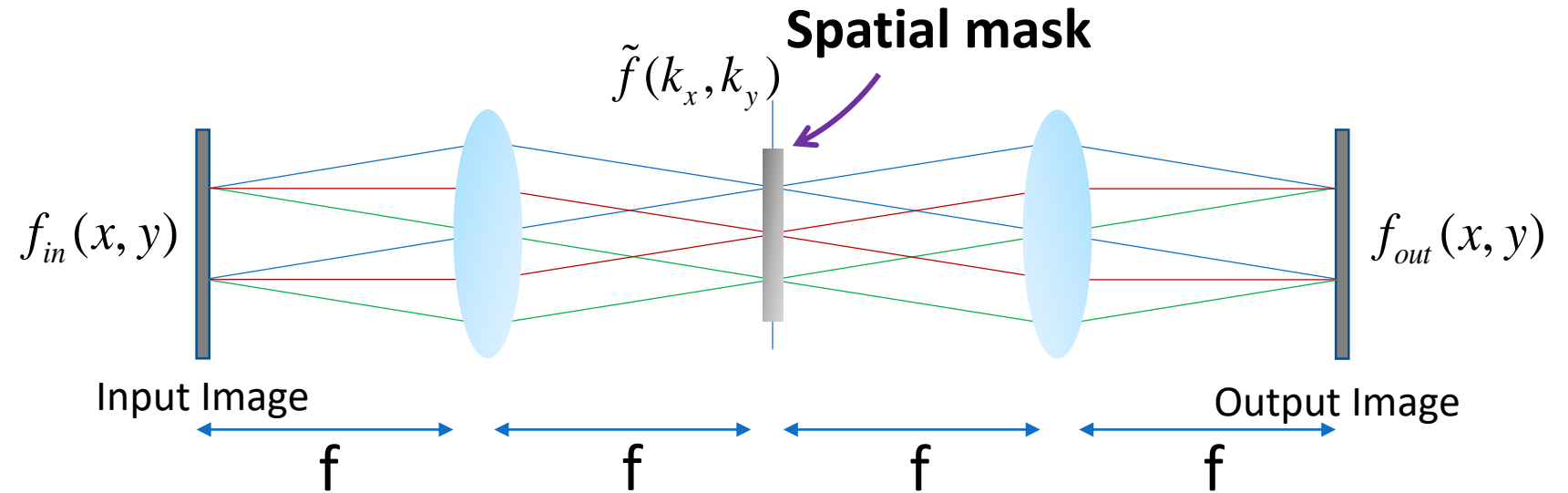
We do not need to physically access the back focal plane to obtain the Fourier transform



- If we place a “filter” with **strong and tailored angle-dependent transmission**, we could do k-space filtering
- Problem: for natural materials, transmission is **weakly dependent on angle**, and **not tunable**
- **But it can be done with a metasurface!**

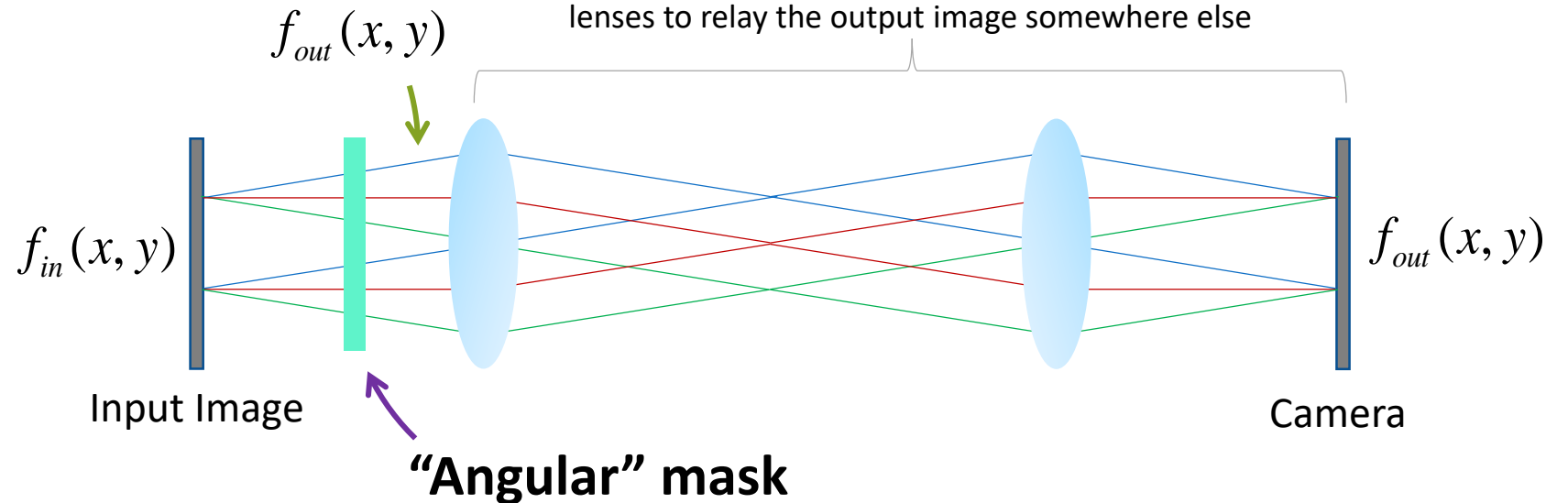
4F OR NOT 4F – THIS IS THE QUESTION

Standard 4F
k-space filtering

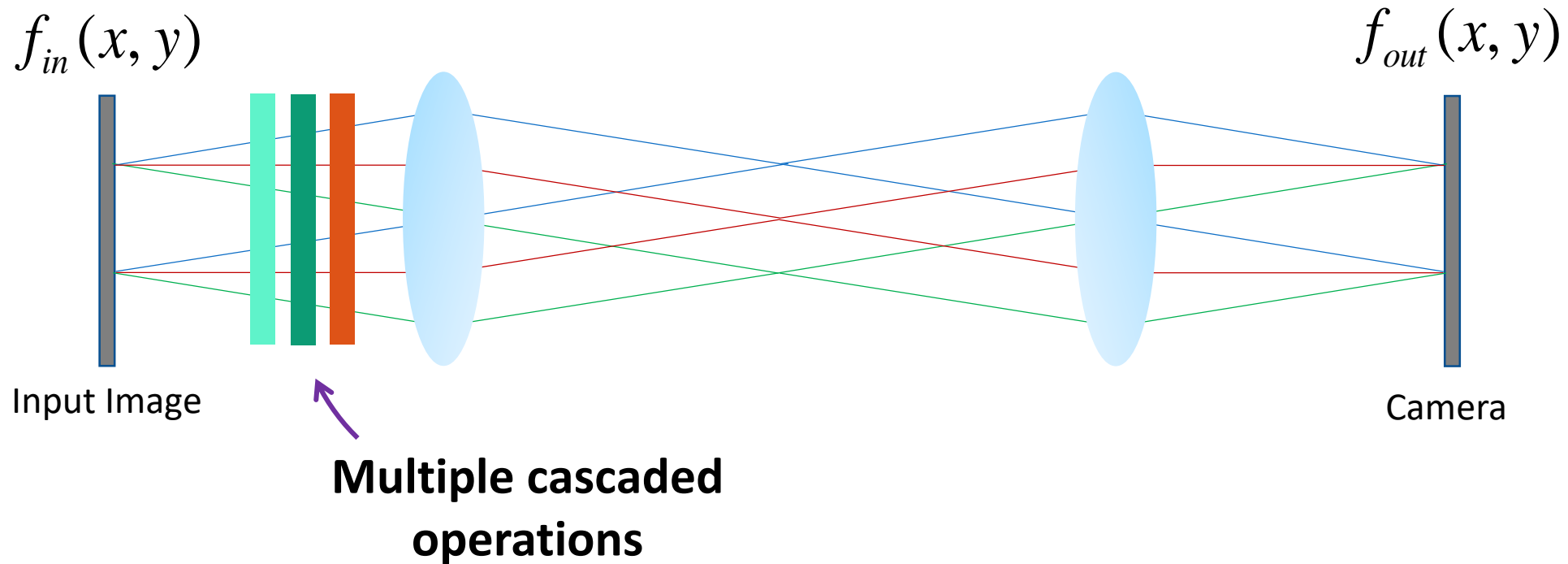


In practical scenarios, we might still need a pair of lenses to relay the output image somewhere else

The “metasurface”
approach



SCALABILITY OF THE 4F-LESS APPROACH



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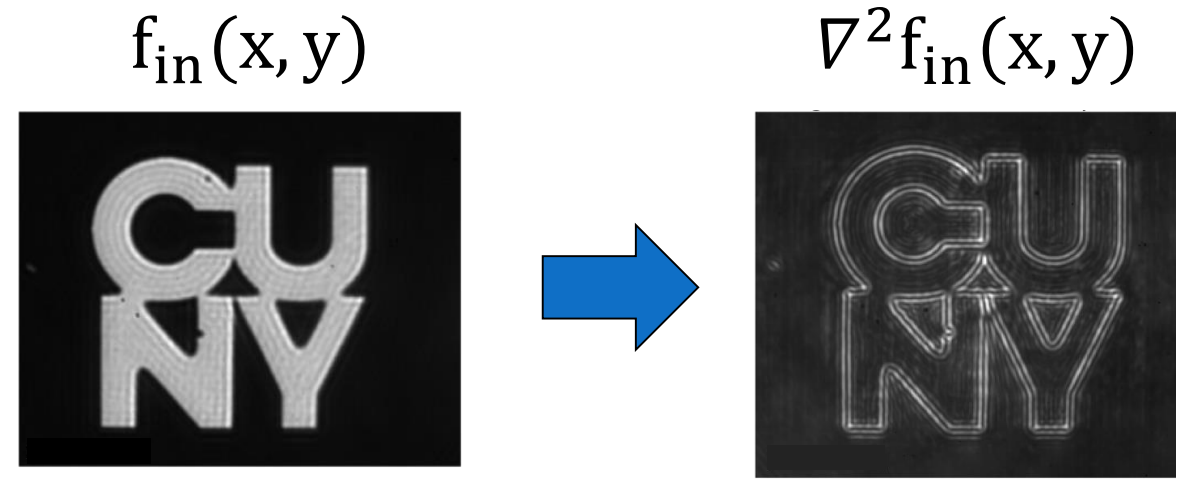
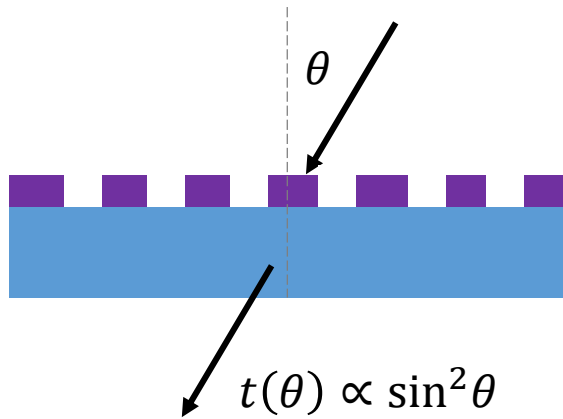
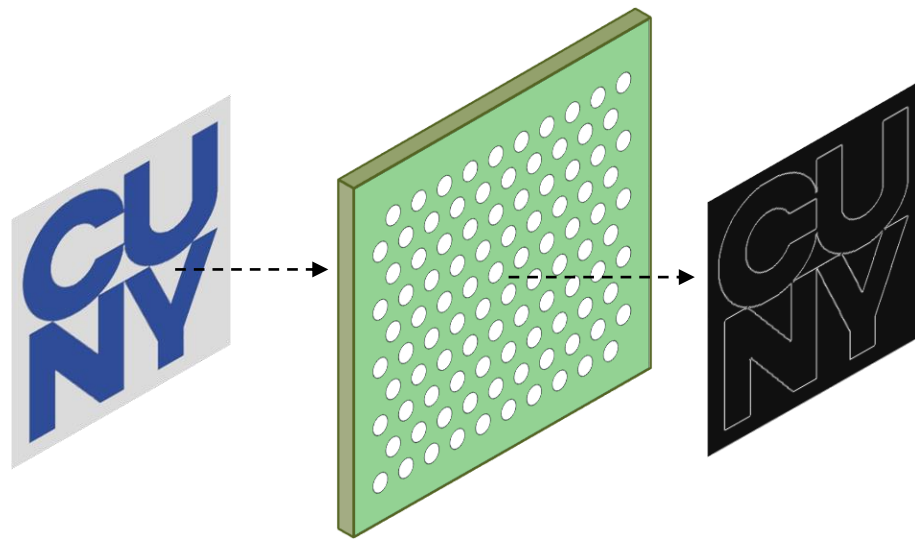
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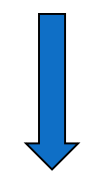
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Standard Approach to obtain a “Laplacian Response”



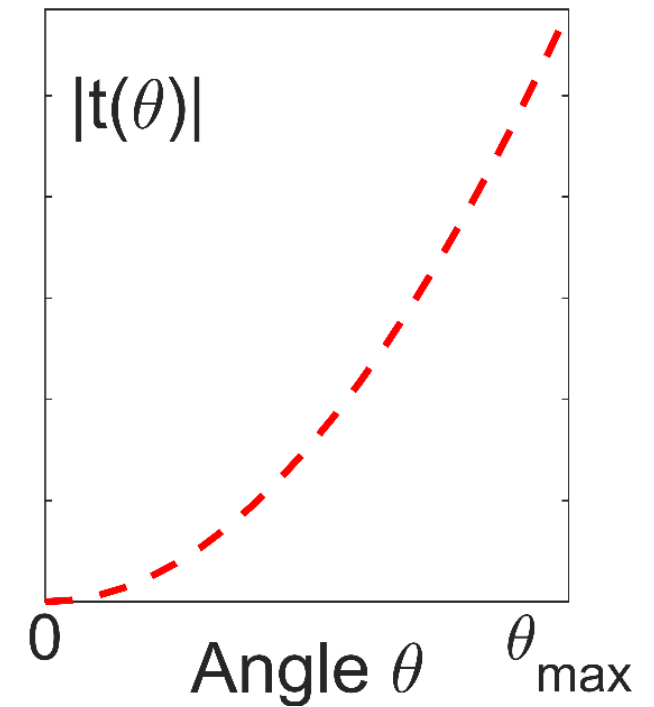
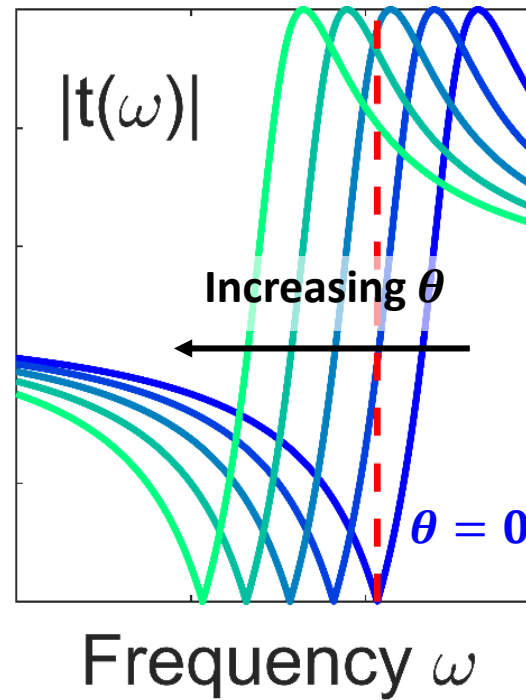
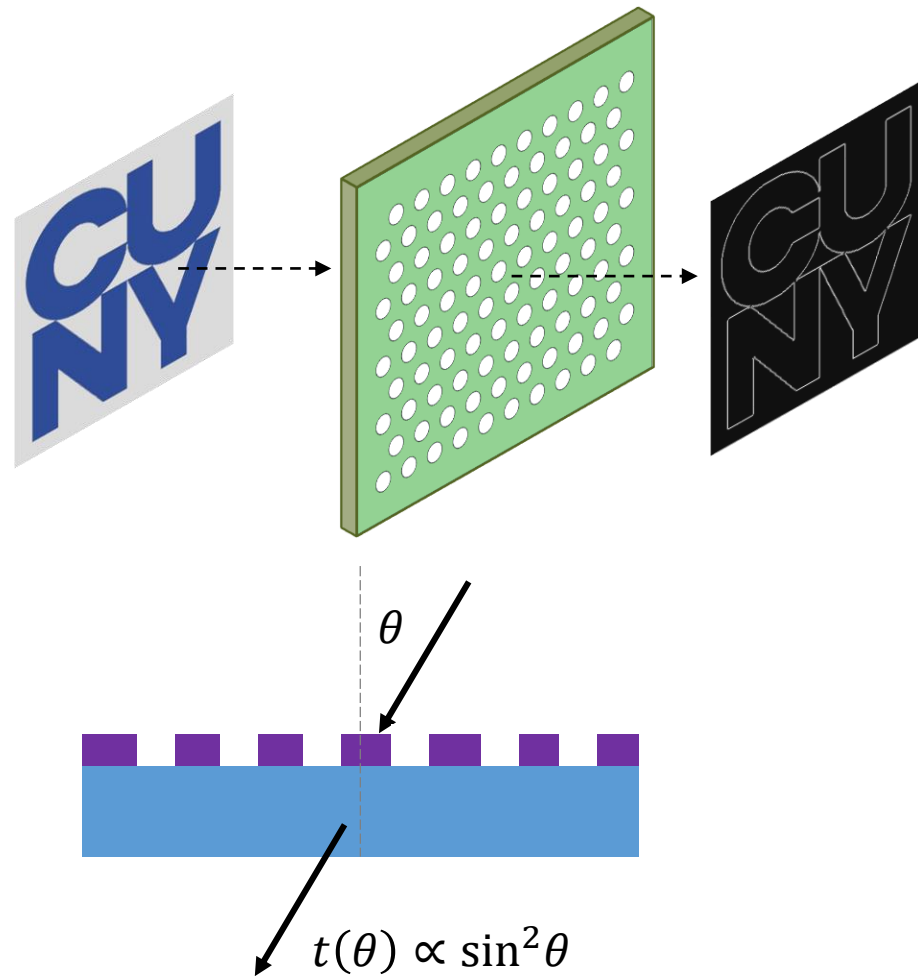
$$f_{out}(x, y) = (\partial_x^2 + \partial_y^2) f_{in}(x, y)$$



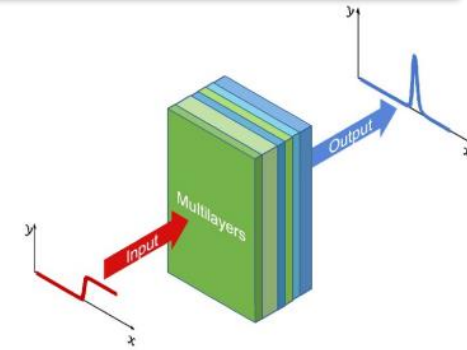
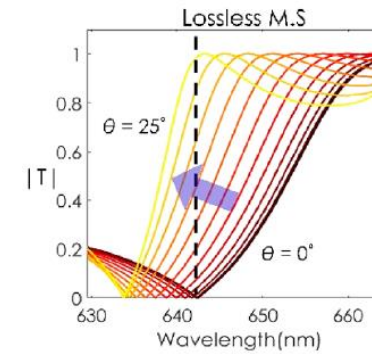
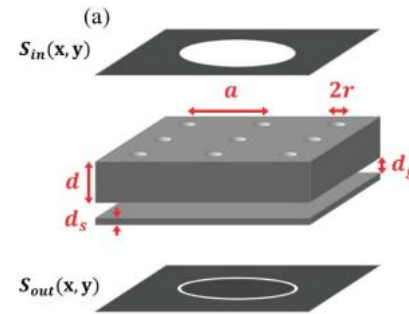
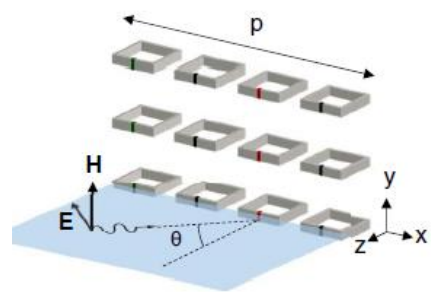
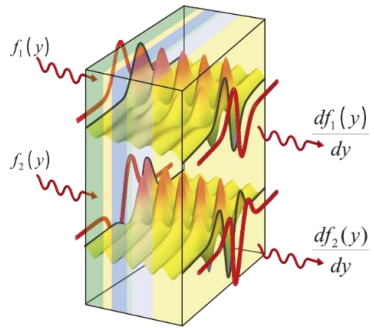
$$f_{out}(k_x, k_y) = -(k_x^2 + k_y^2) f_{in}(k_x, k_y)$$

ANALOG SIGNAL PROCESSING WITH METASURFACES

Standard Approach to obtain a “Laplacian Response”



ANALOG IMAGE PROCESSING WITH METASURFACES



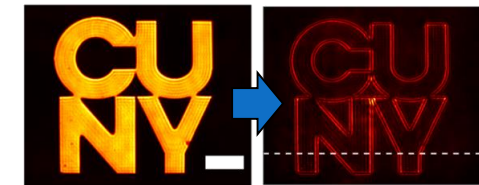
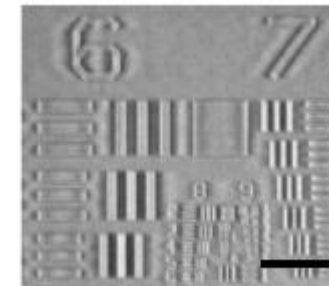
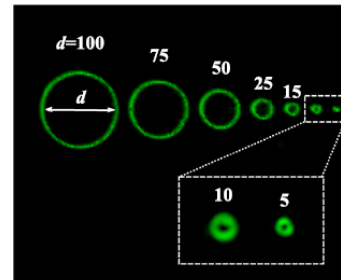
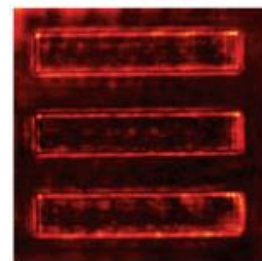
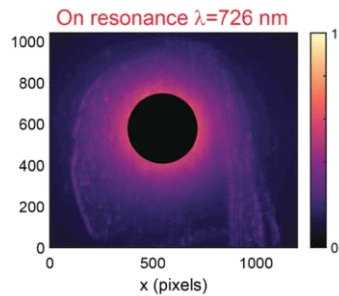
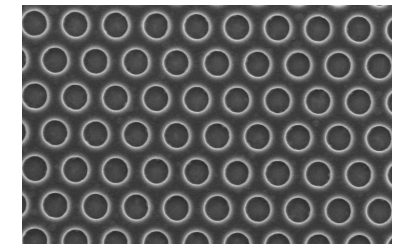
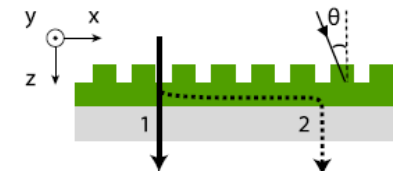
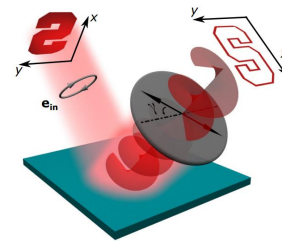
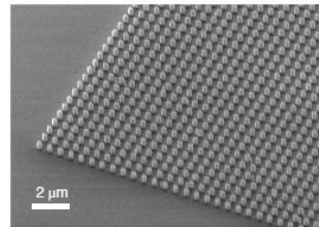
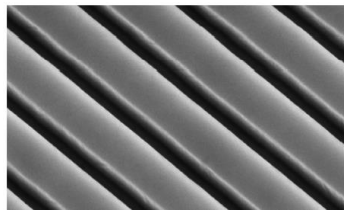
Silva, et al., **Science** 343(6167), 160-163 (2014)

Kwon et al., **Phys. Rev. Lett.** 121(17), 173004 (2018)

Guo et al., **Optica** 5(3), 251-256 (2018)

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Xue et al., **J. of Optics** 23(12), 125004 (2021)



Cordaro et al., **Nano Letters** 19(12), 8418-8423(2019)

Zhou et al., **Nature Photonics** 14(5), 316-323(2020)

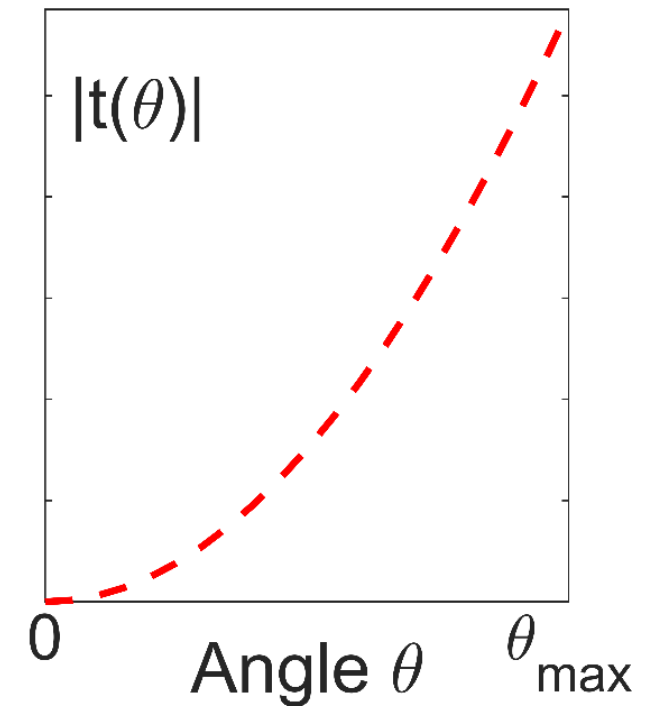
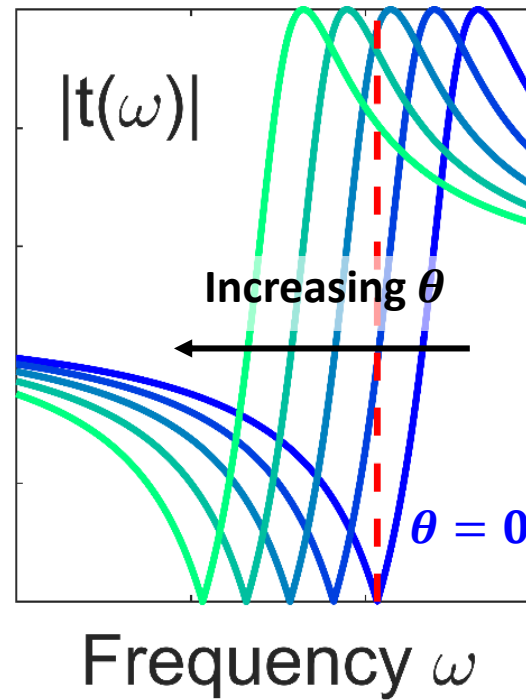
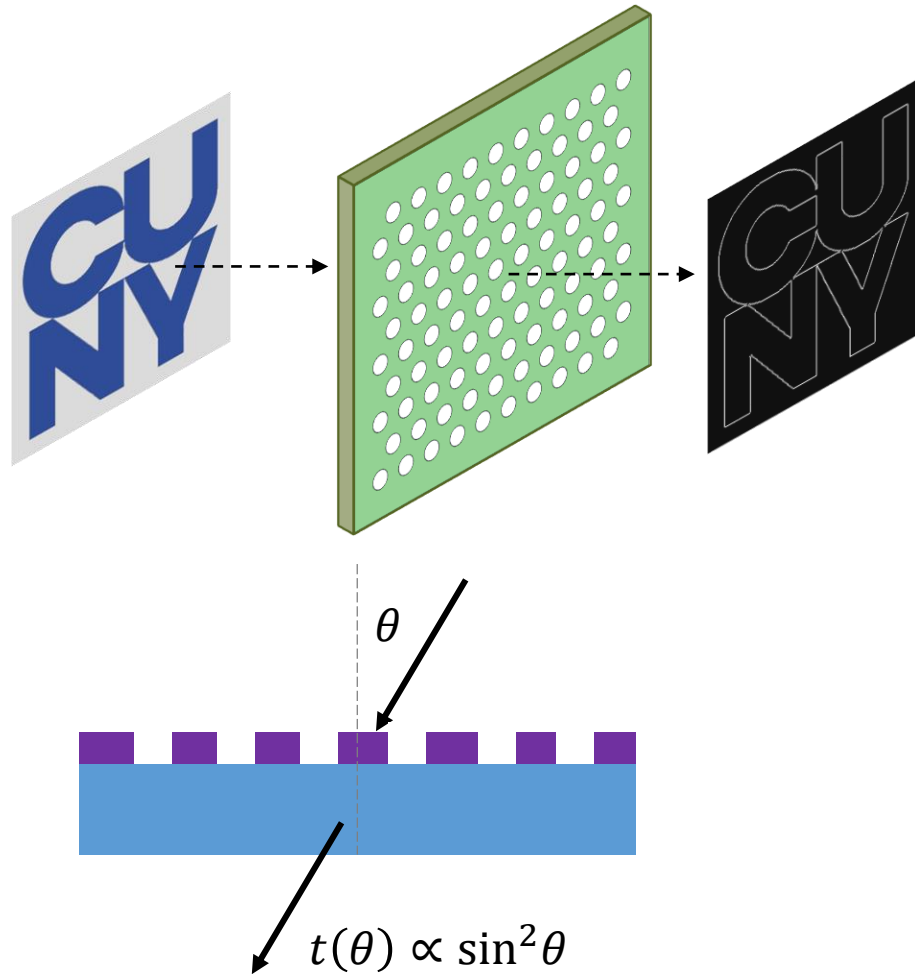
Zhu et al., **Nat. Comm.** 12:680 (2021)

Ji et al., **Nat. Comm.** 13.1, 7848 (2022)

Cotrufo et al., *under review*
arXiv : 2212.03468

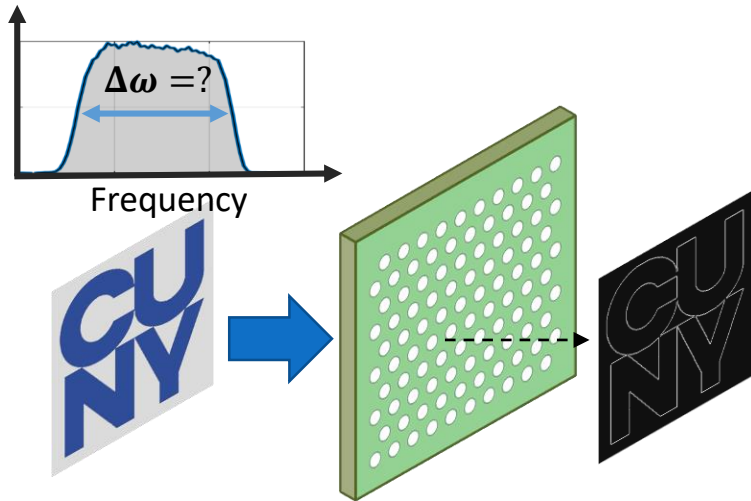
ANALOG IMAGE PROCESSING WITH METASURFACES

Standard Approach to obtain a “Laplacian Response”

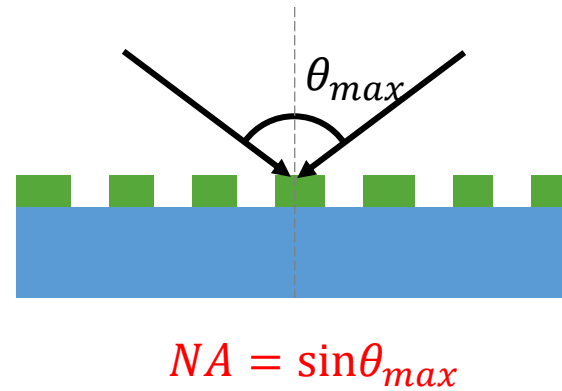


IMPORTANT FIGURES OF MERIT

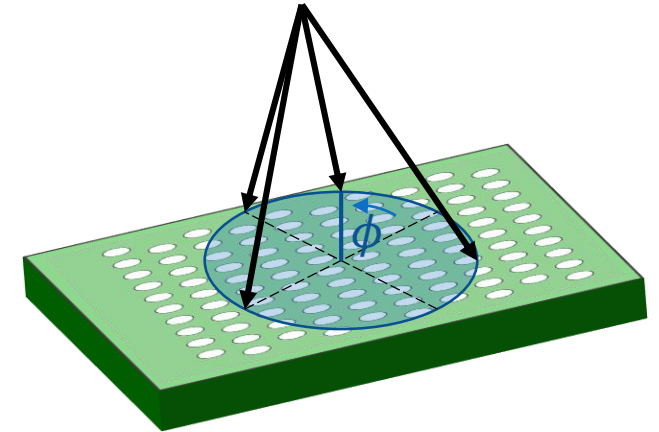
1. Spectral Bandwidth



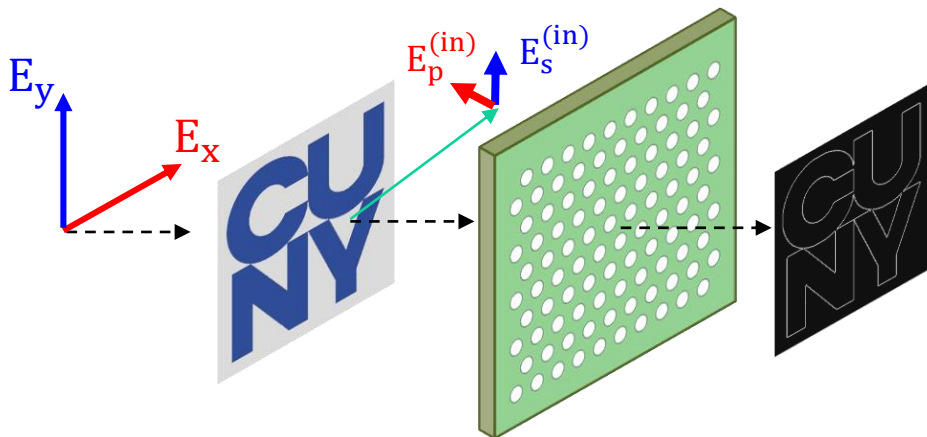
2. Numerical Aperture



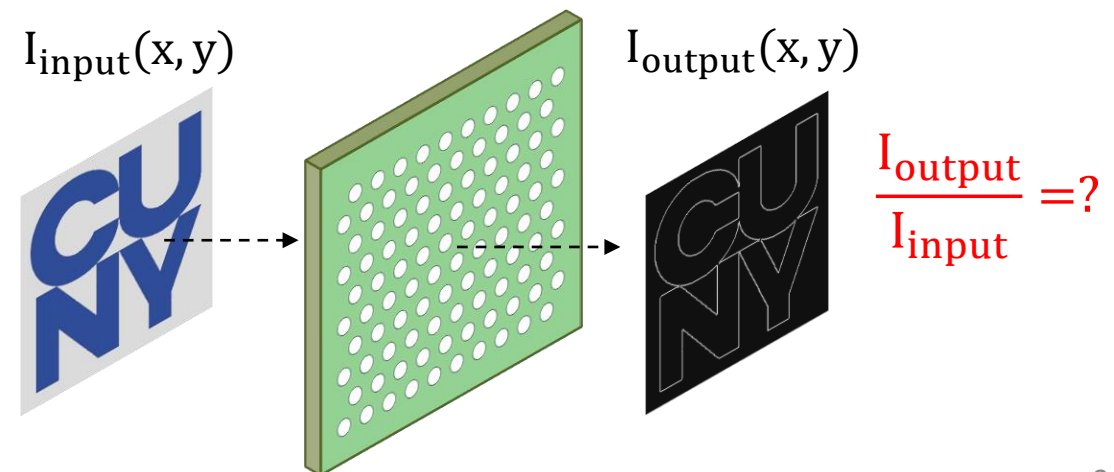
3. Azimuthal Isotropy



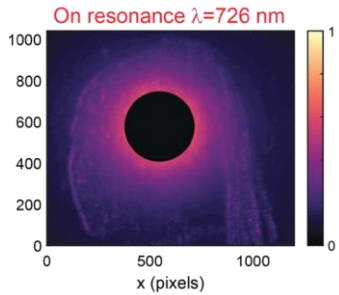
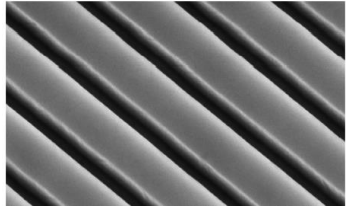
4. Polarization (in)dependence



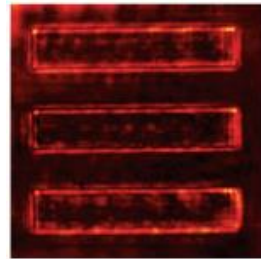
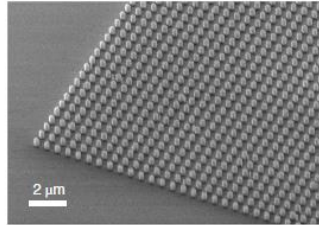
5. Efficiency



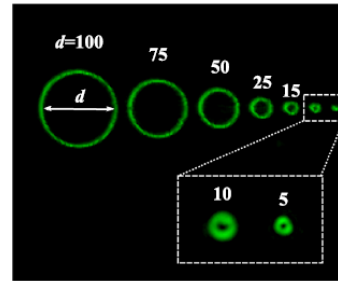
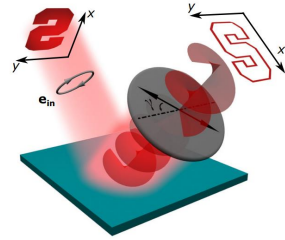
ANALOG IMAGE PROCESSING WITH METASURFACES



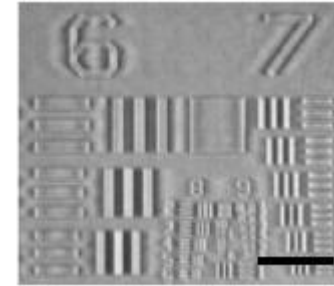
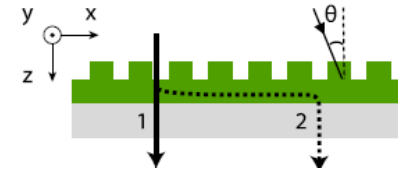
Cordaro et al., **Nano Letters**
19(12), 8418-8423(2019)
Polman's & Alu's group



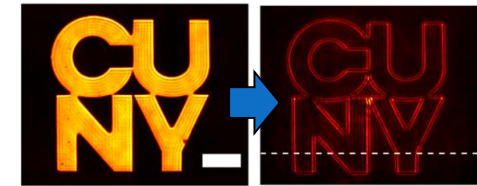
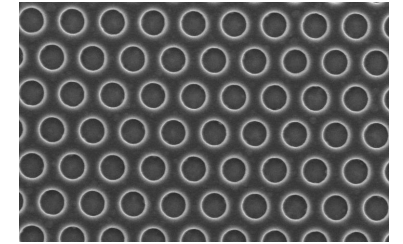
Zhou et al., **Nature Photonics**
14(5), 316-323(2020)
Valentine's group



Zhu et al., **Nat. Comm.**
12:680 (2021)
Fan's group

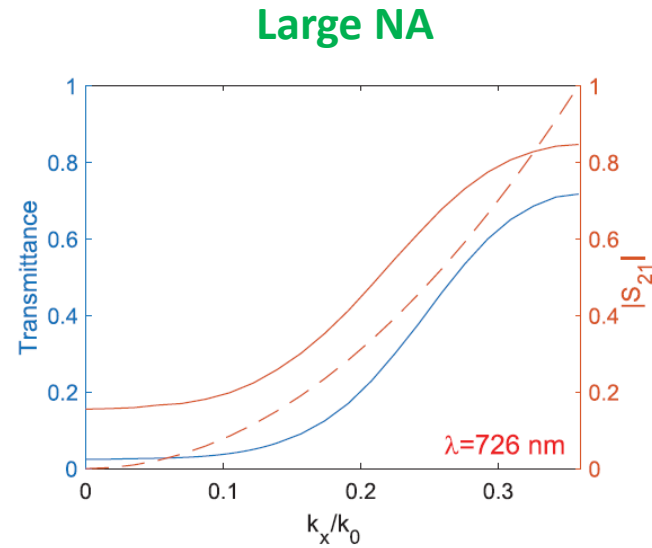
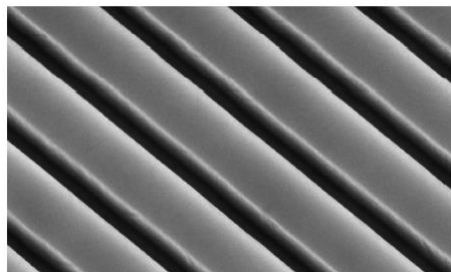
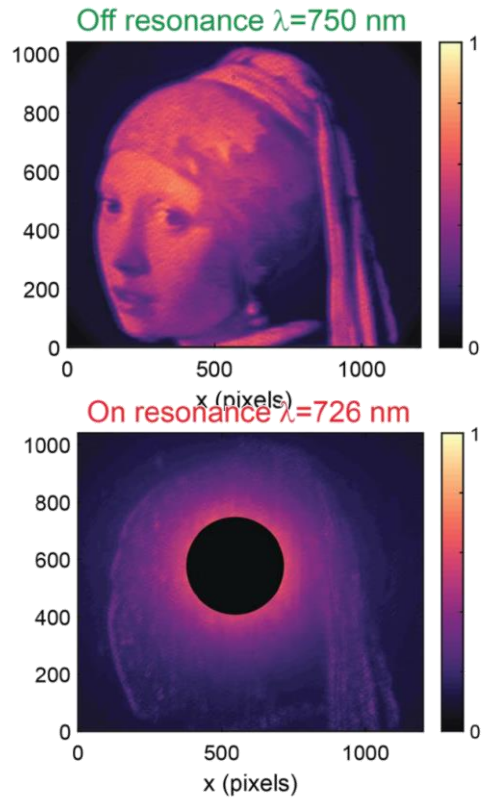


Ji et al., **Nat. Comm.**
13.1, 7848 (2022)
Brongersma's group

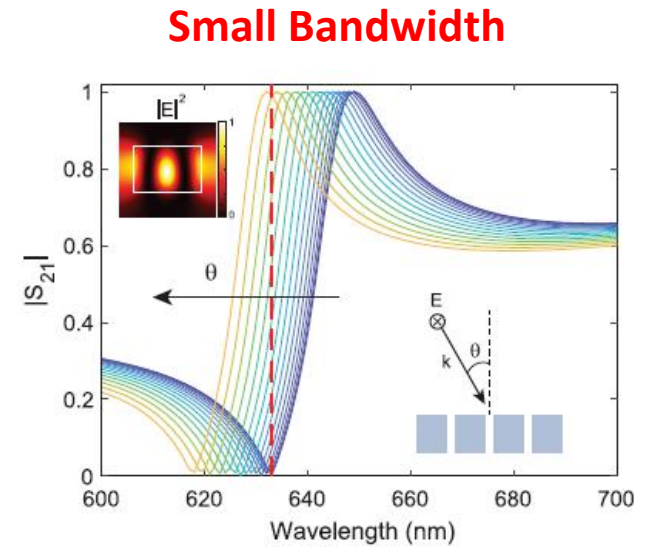
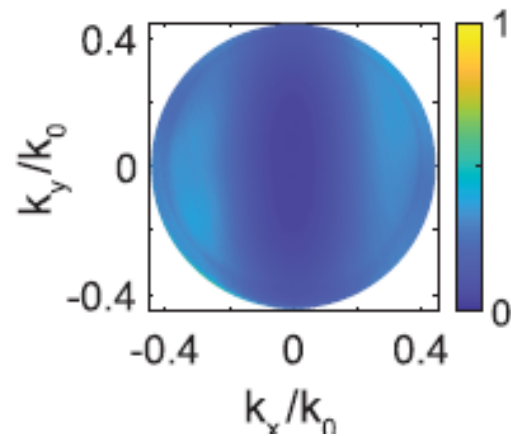


Cotrufo et al., *under review.*
arXiv : 2212.03468
Alu's group

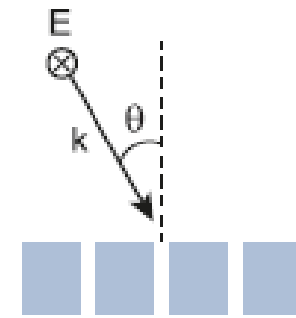
EXPERIMENTAL WORKS ON 4F-LESS EDGE DETECTION



Very anisotropic (C2 symmetry)

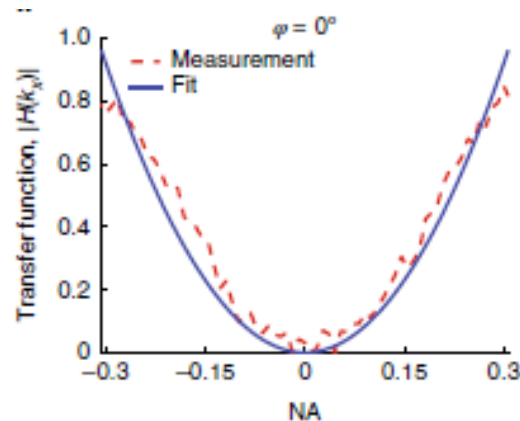
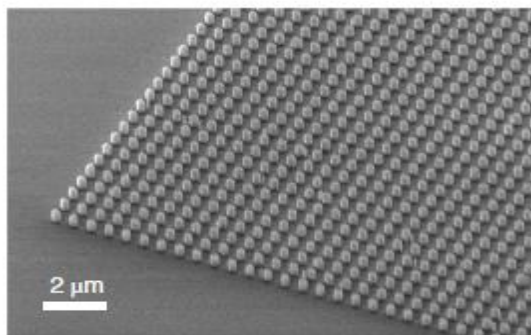


Strongly Polarization-Dependent

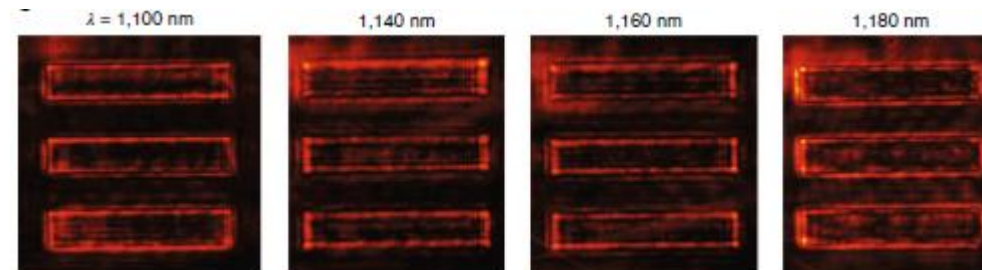


EXPERIMENTAL WORKS ON 4F-LESS EDGE DETECTION

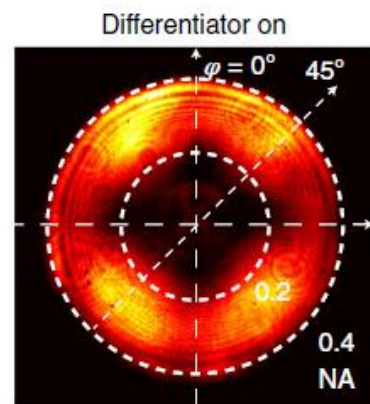
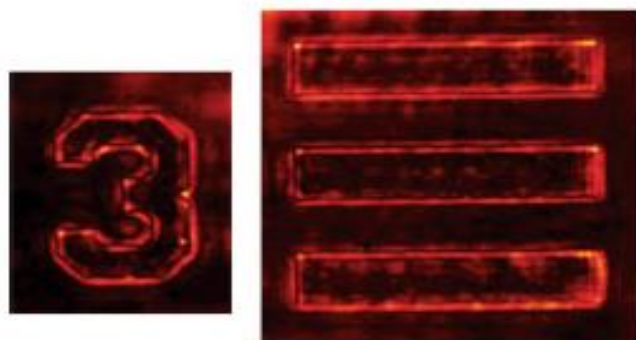
Large NA (0.32)



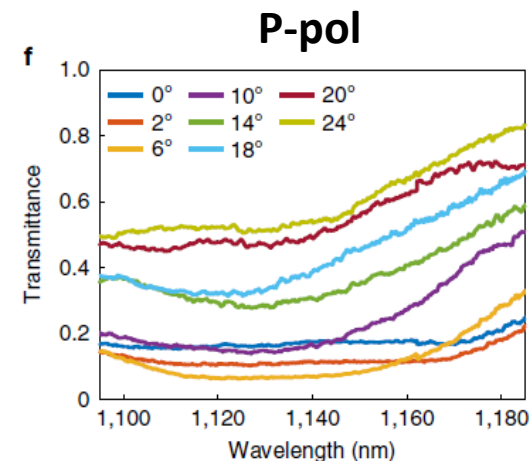
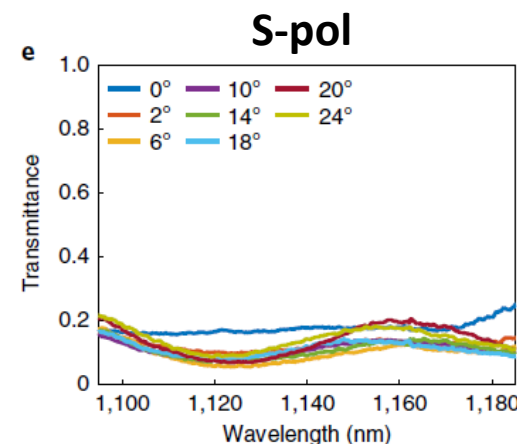
Large Bandwidth (~80nm)



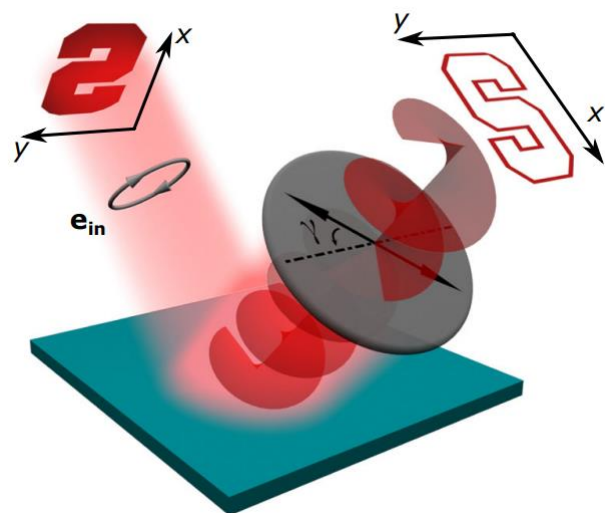
Improved Isotropy (C4 symmetry)



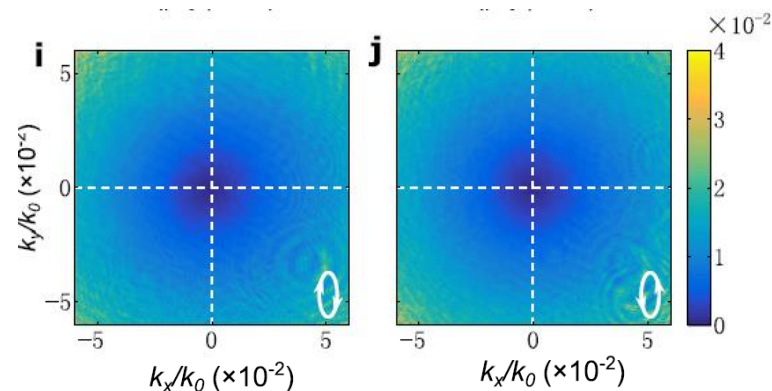
Polarization-Dependent



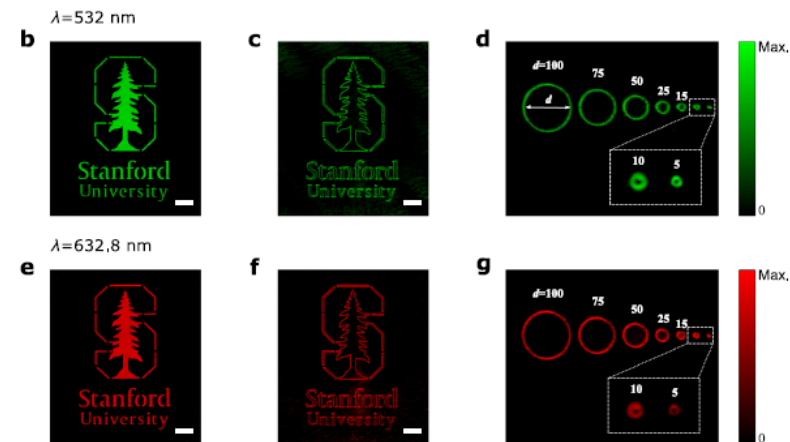
EXPERIMENTAL WORKS ON 4F-LESS EDGE DETECTION



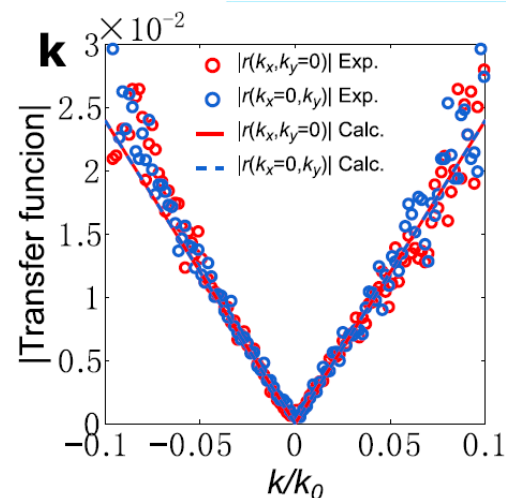
Excellent Isotropy



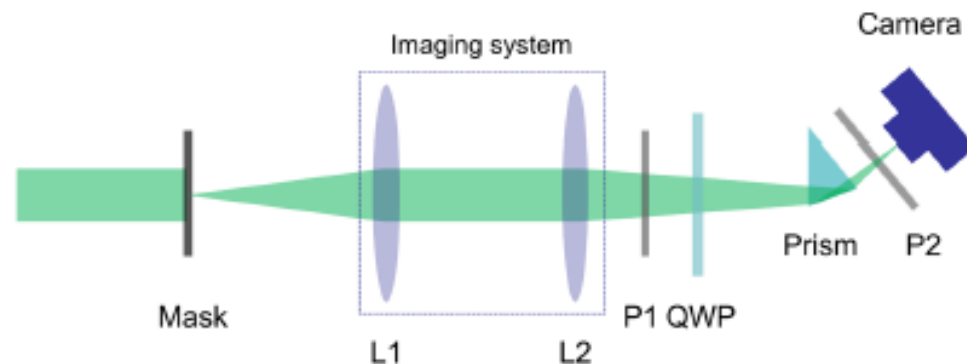
Very Large Bandwidth



Limited NA and Efficiency

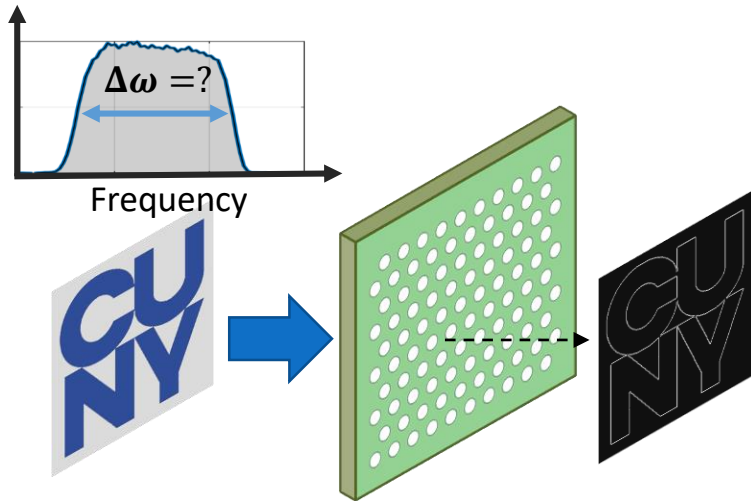


Polarization-Dependent, and need for polarization optics

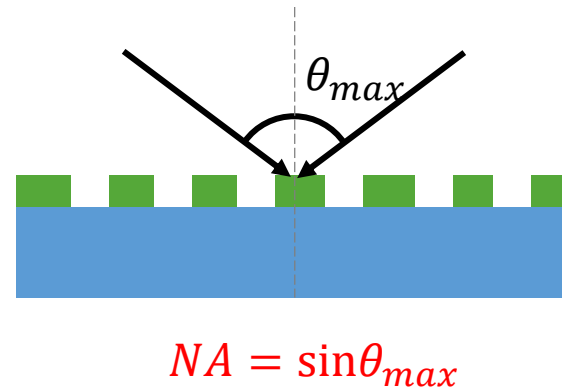


IMPORTANT FIGURES OF MERIT

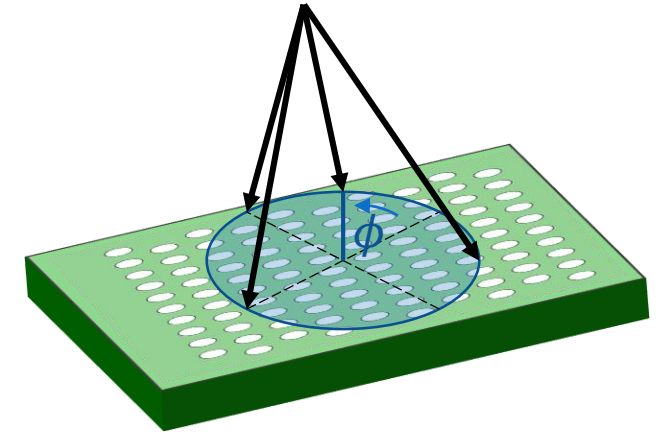
1. Spectral Bandwidth



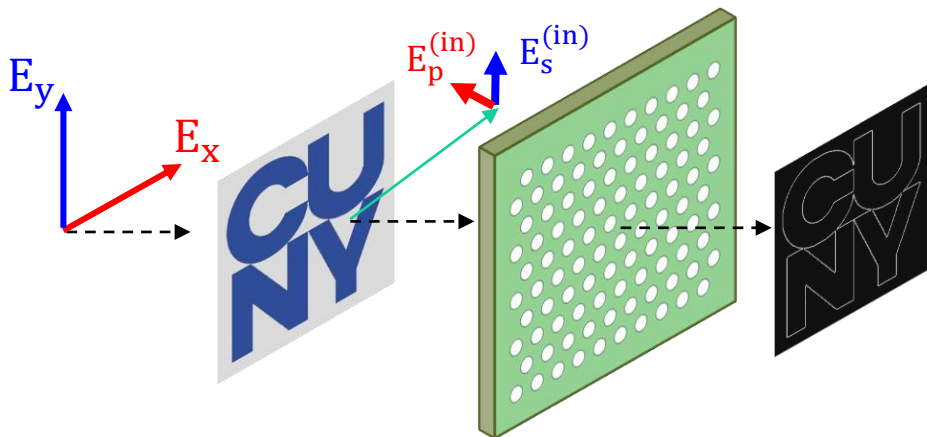
2. Numerical Aperture



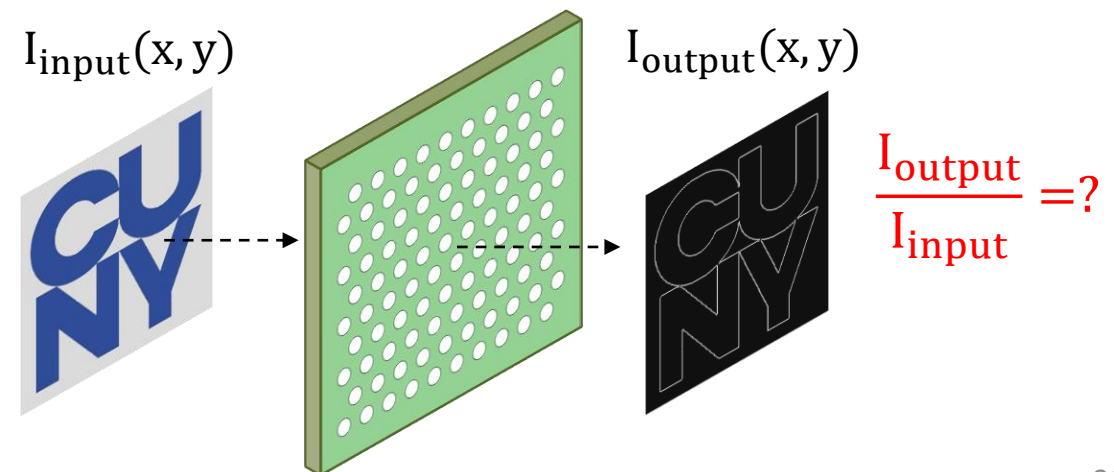
3. Azimuthal Isotropy



4. Polarization (in)dependence



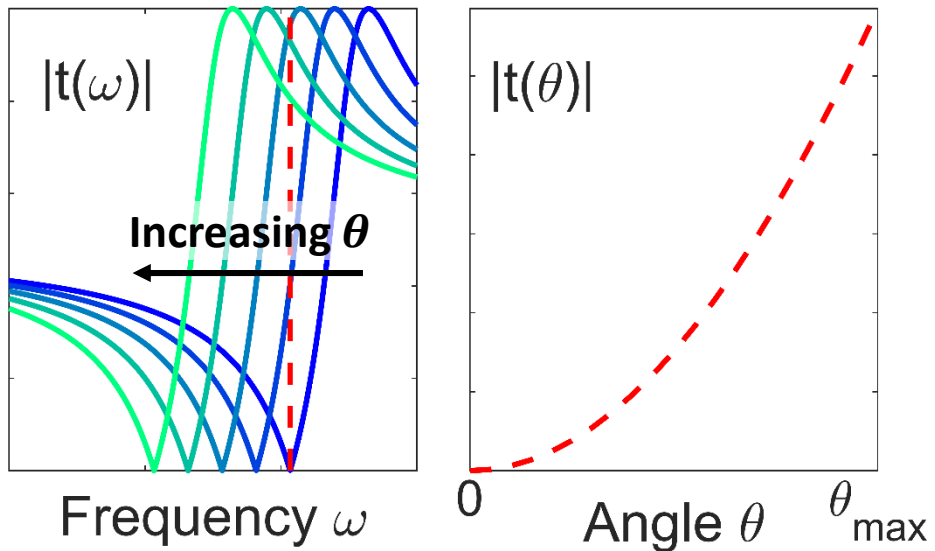
5. Efficiency



BROADBAND, HIGH-EFFICIENCY AND HIGH-NA EDGE DETECTION

Ideal transfer function: $t(\theta, \phi) \propto \sin^2 \theta$

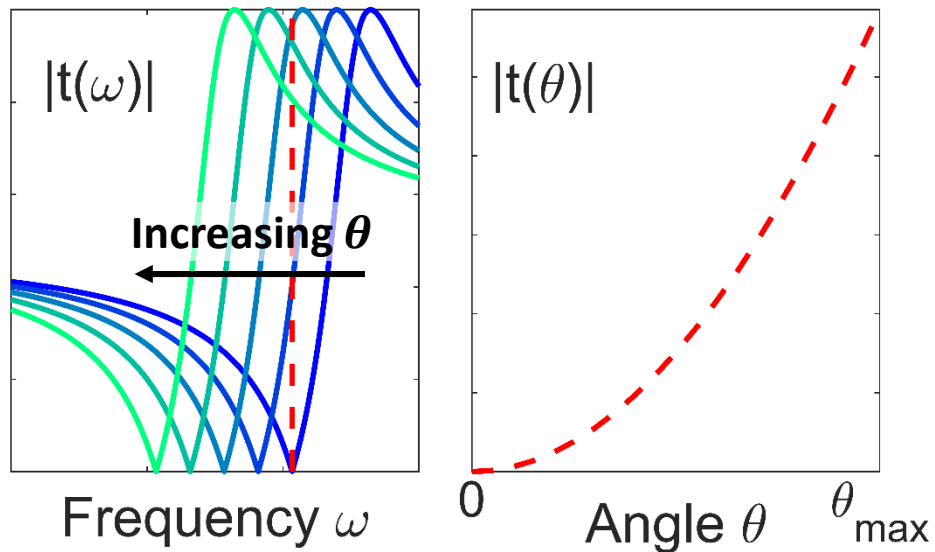
Standard Approach



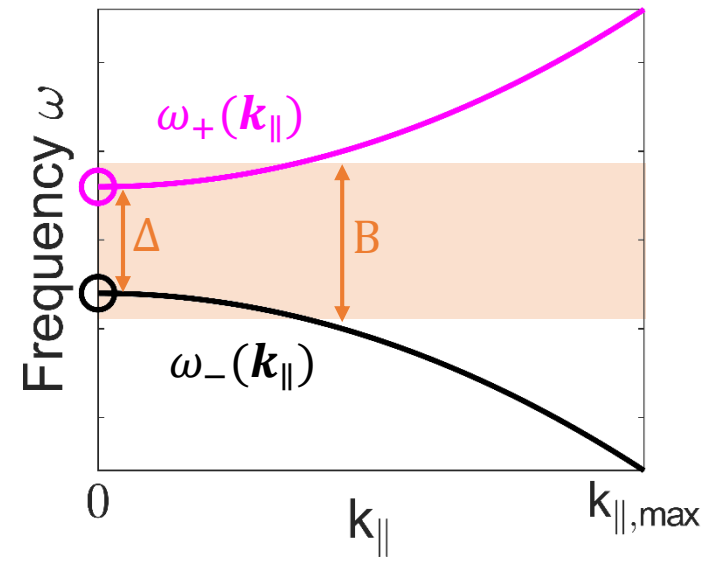
BROADBAND, HIGH-EFFICIENCY AND HIGH-NA EDGE DETECTION

Ideal transfer function: $t(\theta, \phi) \propto \sin^2 \theta$

Standard Approach



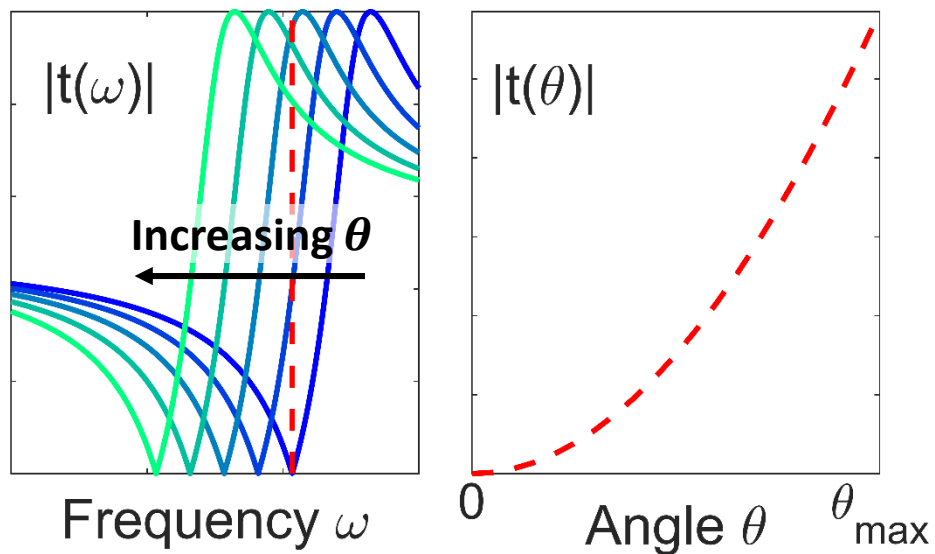
Our Approach: Dispersion Engineering



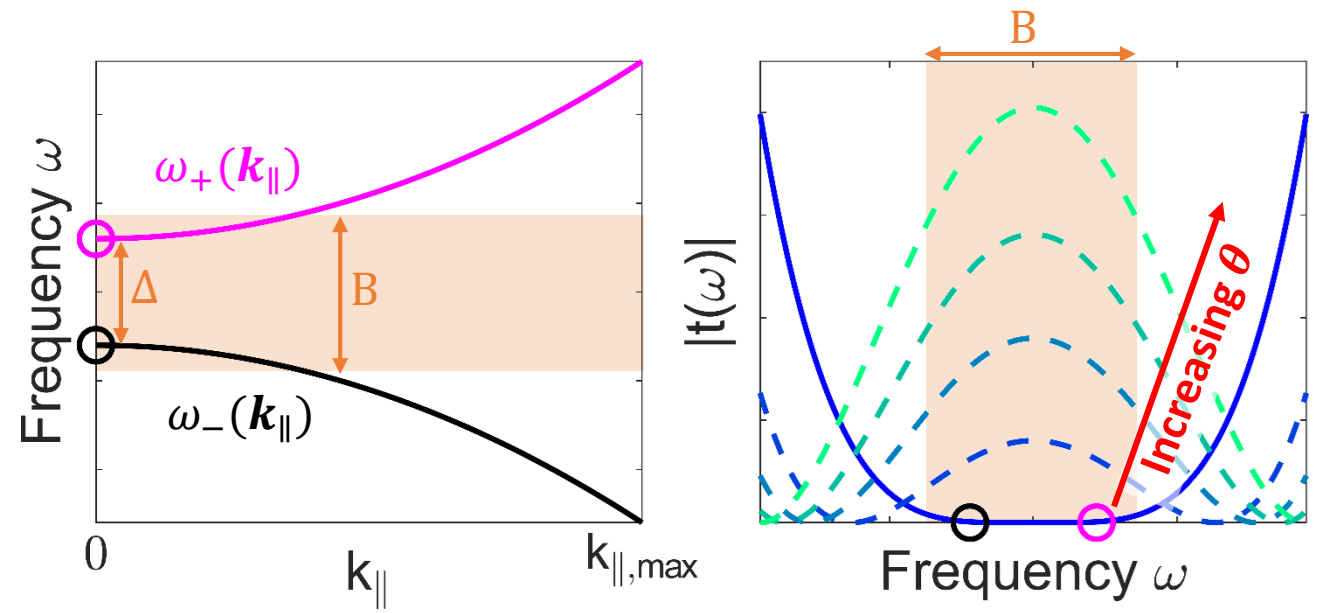
BROADBAND, HIGH-EFFICIENCY AND HIGH-NA EDGE DETECTION

Ideal transfer function: $t(\theta, \phi) \propto \sin^2 \theta$

Standard Approach

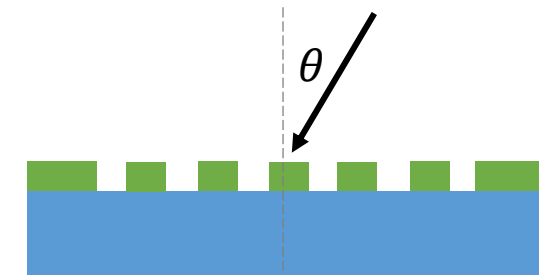
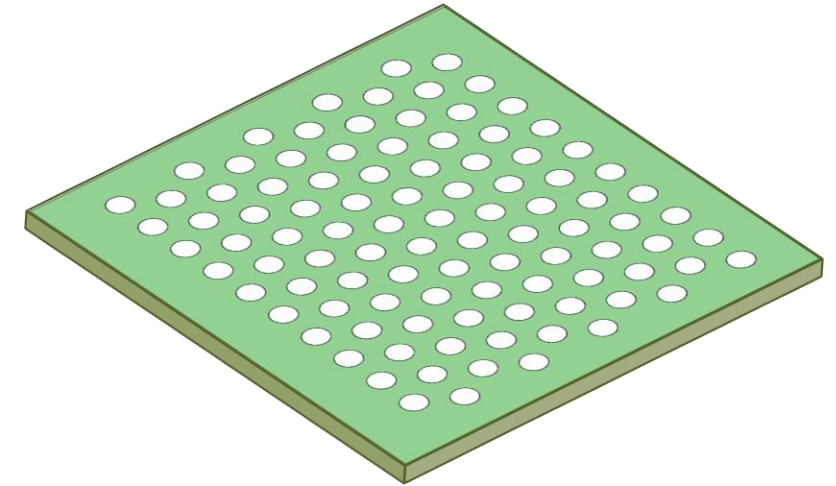
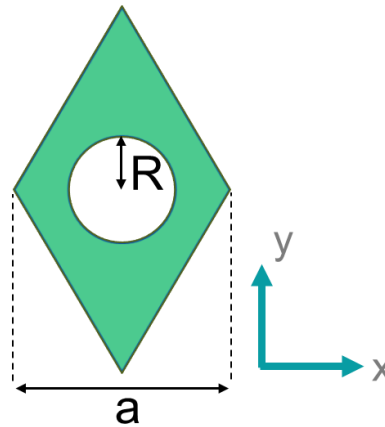
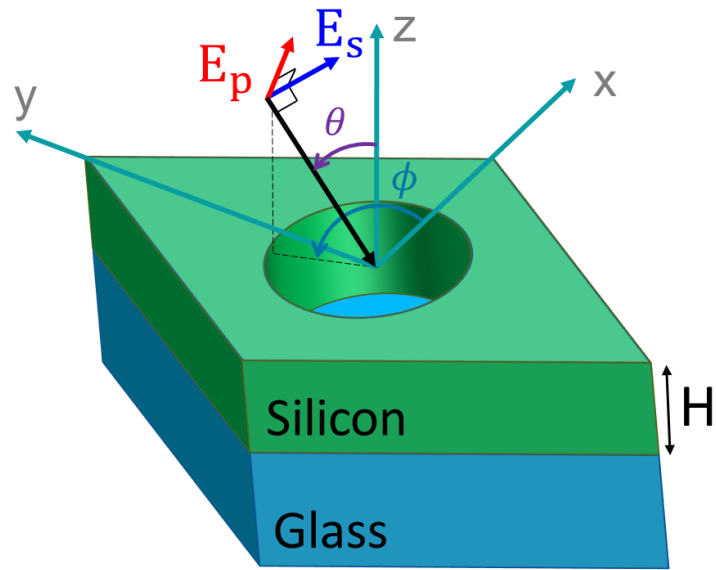


Our Approach: Dispersion Engineering



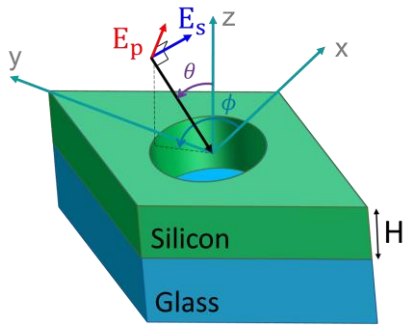
BROADBAND, HIGH-EFFICIENCY AND HIGH-NA EDGE DETECTION

(amorphous) Silicon Metasurface on Glass



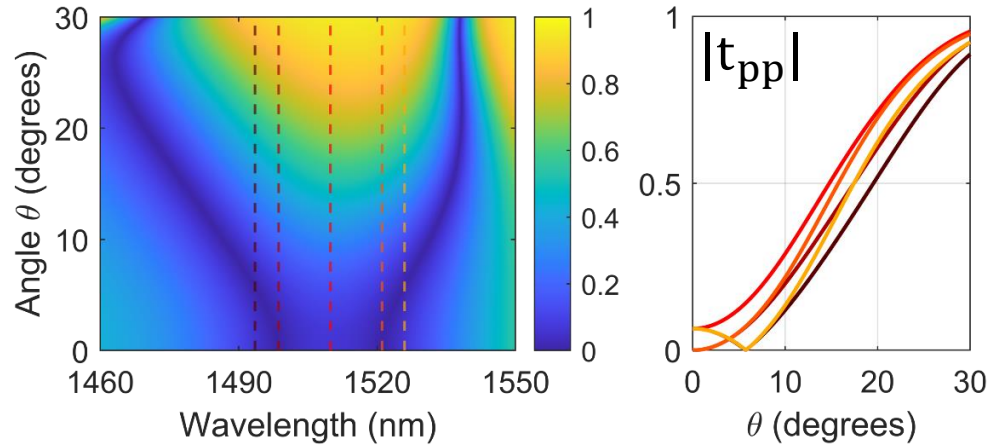
$$t(\theta) \propto \sin^2 \theta$$

BROADBAND, HIGH-EFFICIENCY AND HIGH-NA EDGE DETECTION

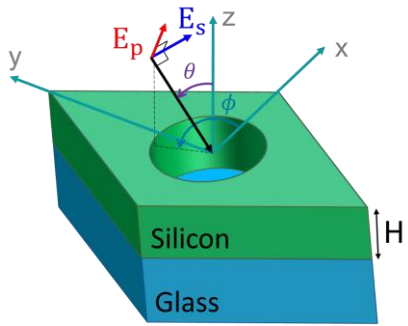


Calculations

$|t_{pp}|$

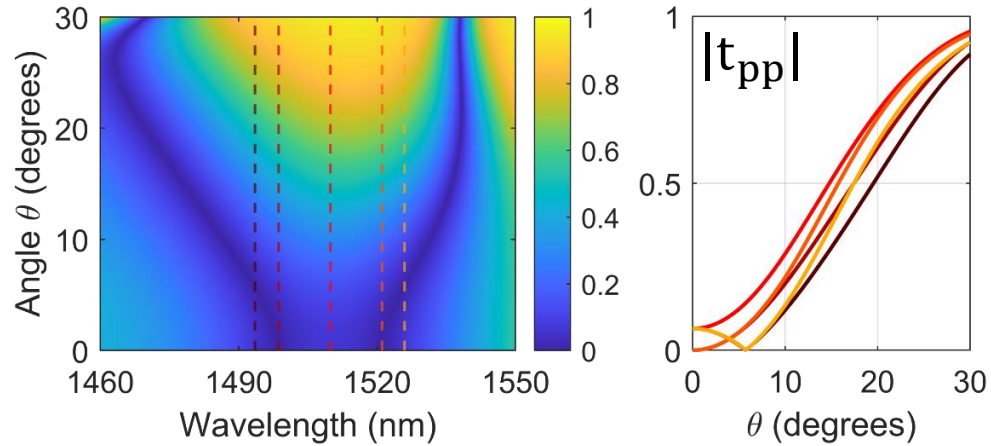


BROADBAND, HIGH-EFFICIENCY AND HIGH-NA EDGE DETECTION

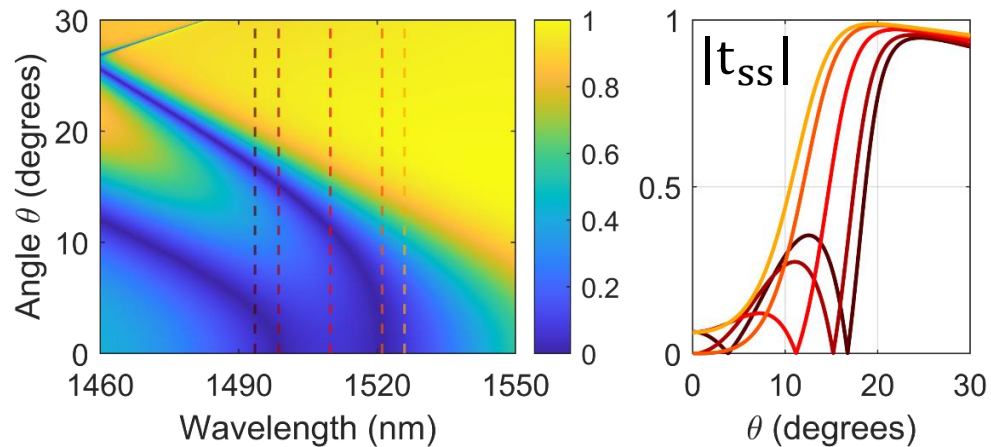


Calculations

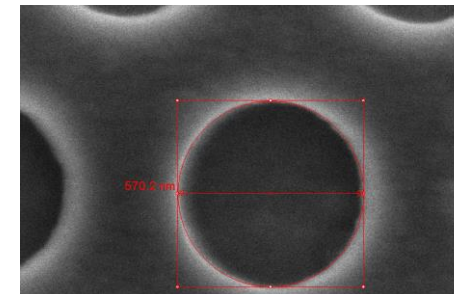
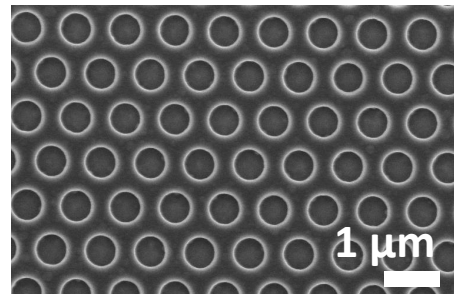
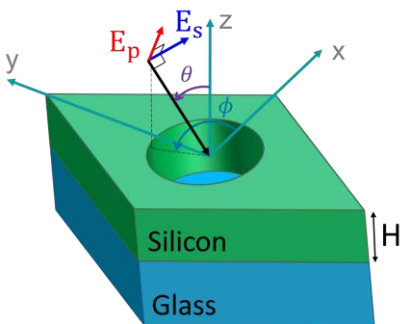
$|t_{pp}|$



$|t_{ss}|$



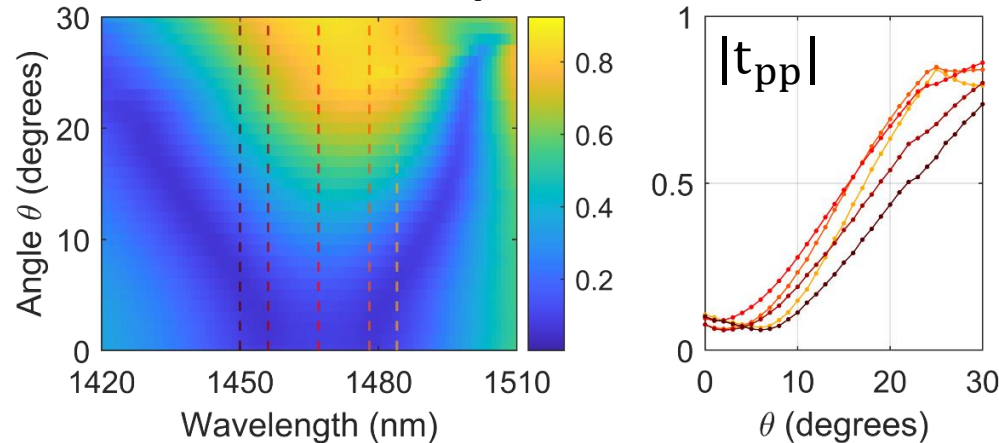
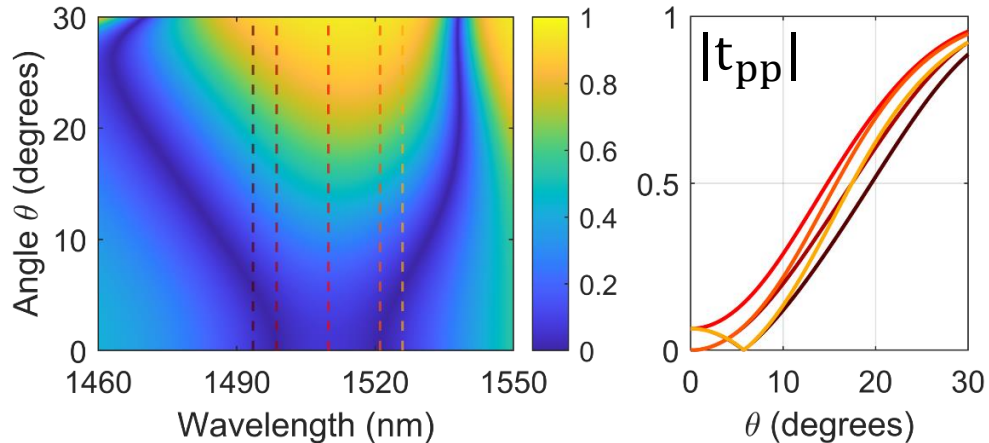
BROADBAND, HIGH-EFFICIENCY AND HIGH-NA EDGE DETECTION



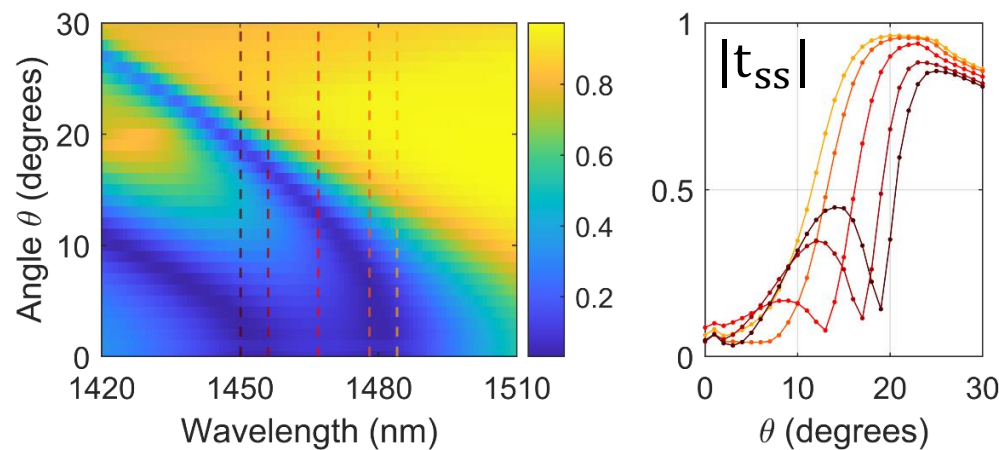
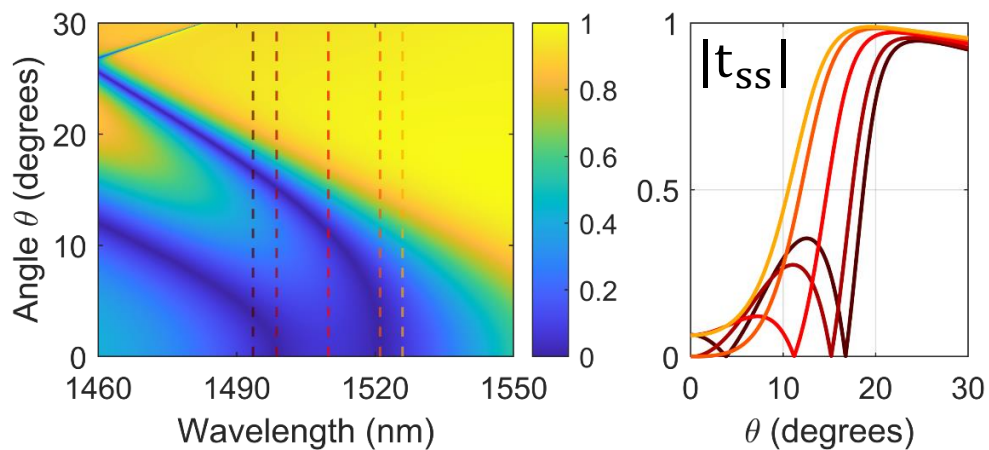
Calculations

Experiments

$|t_{pp}|$

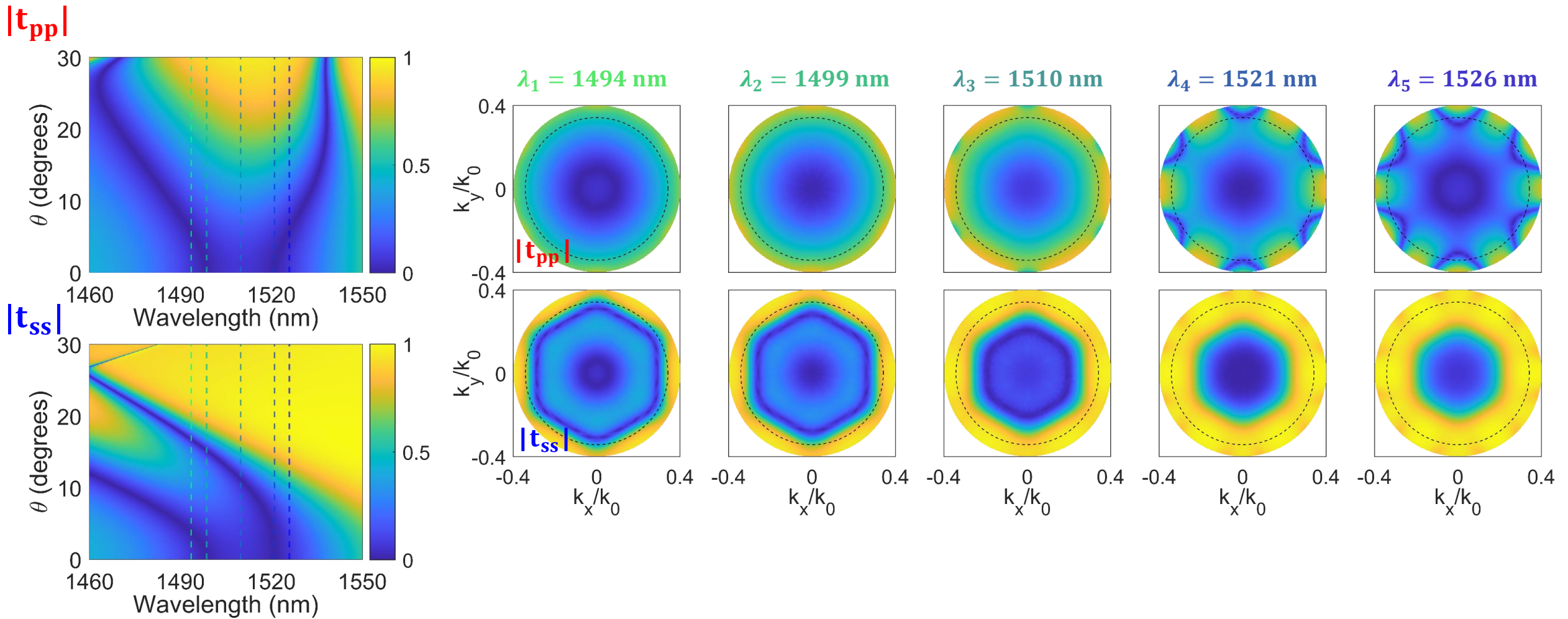


$|t_{ss}|$

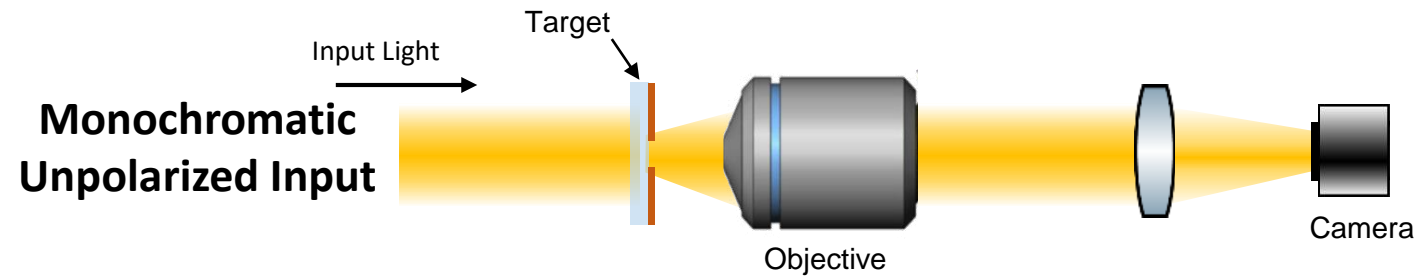


NA > 0.35

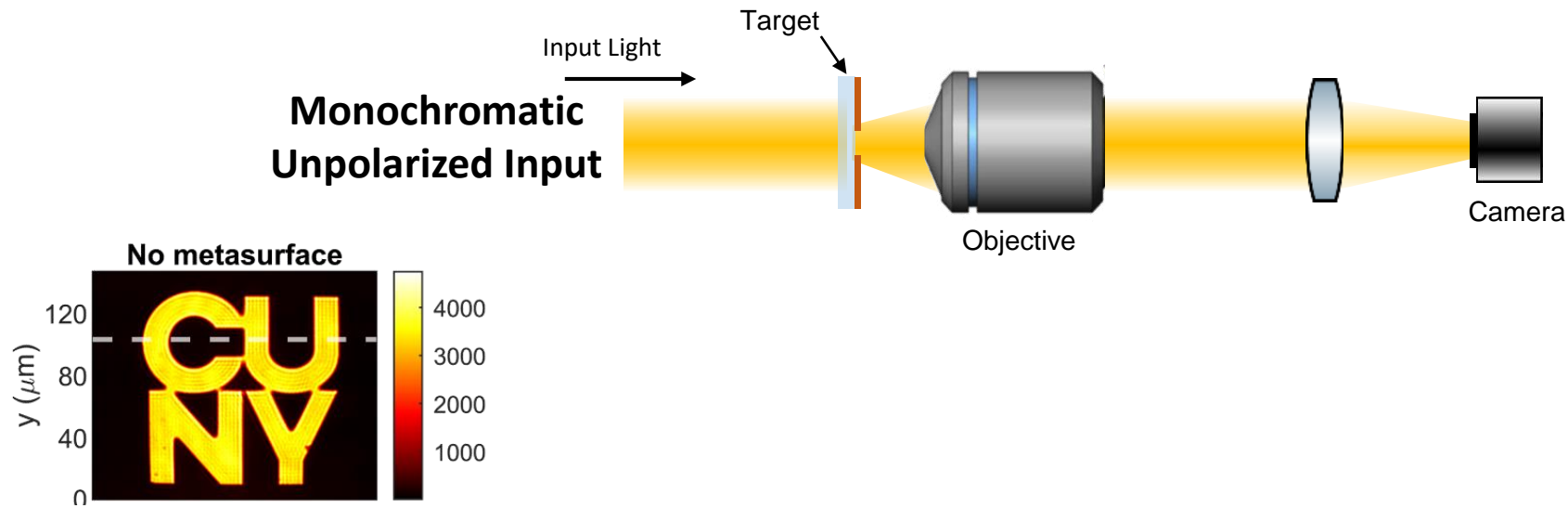
BROADBAND, HIGH-EFFICIENCY AND HIGH-NA EDGE DETECTION



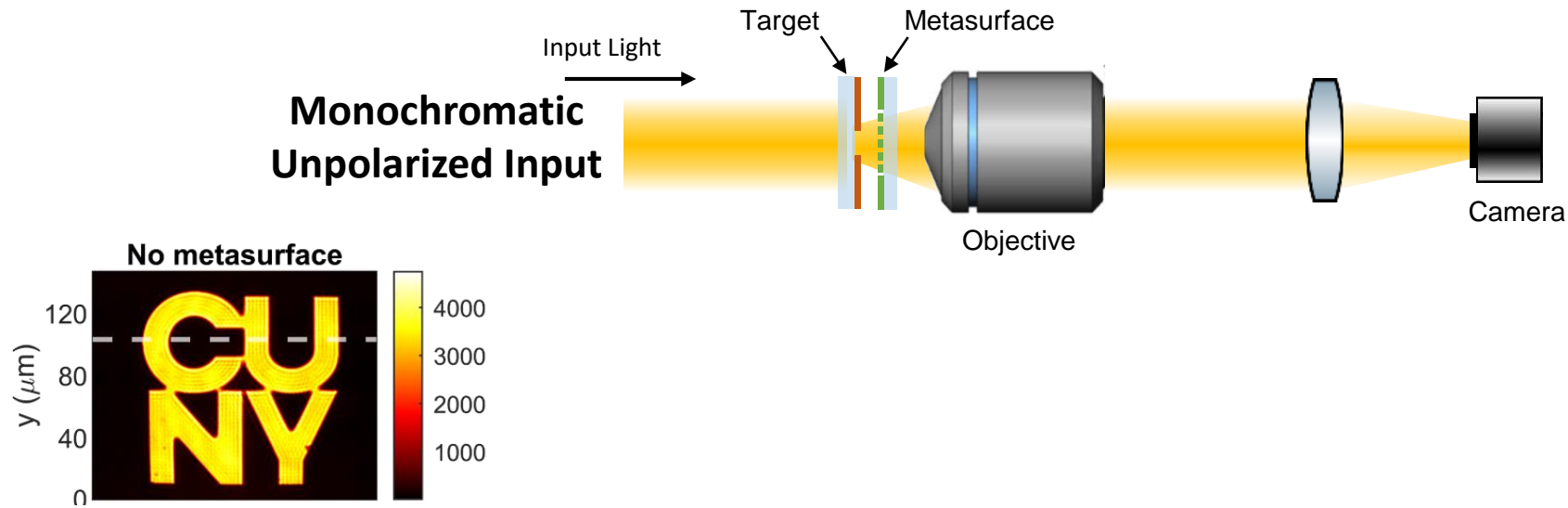
BROADBAND, HIGH-EFFICIENCY AND HIGH-NA EDGE DETECTION



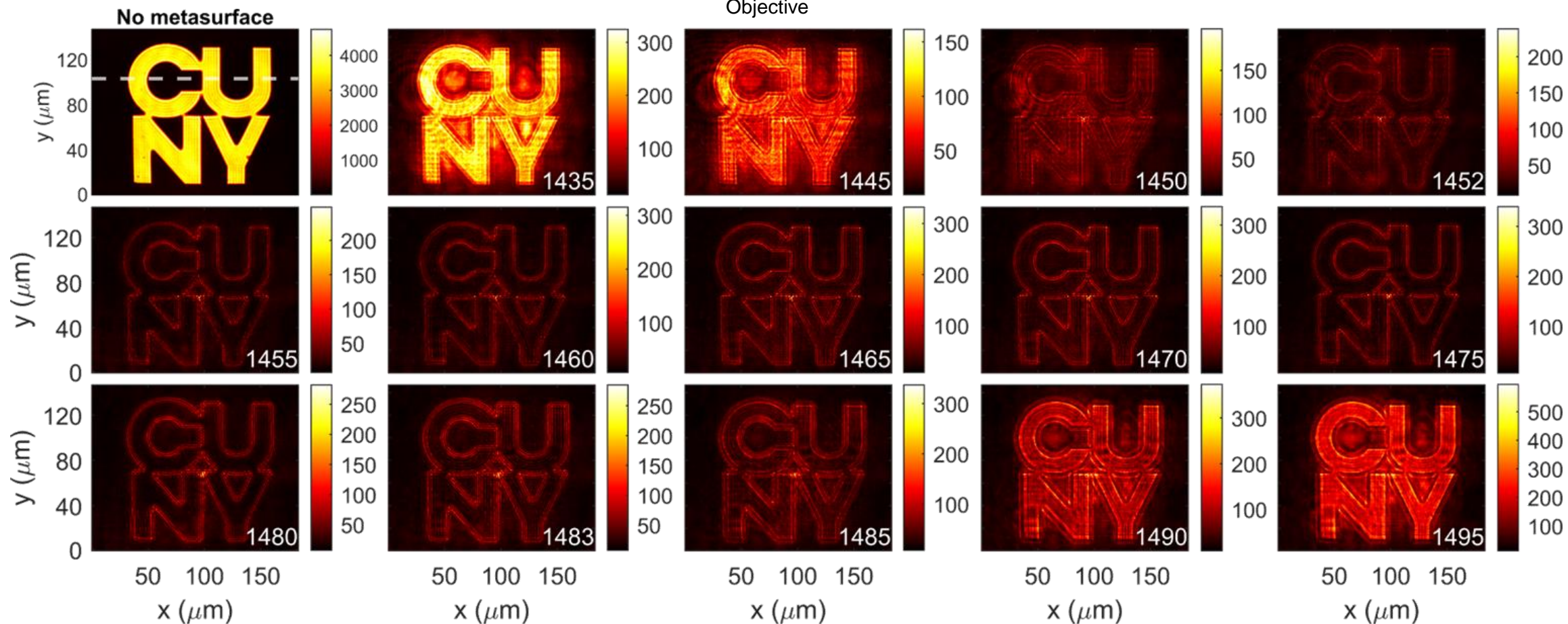
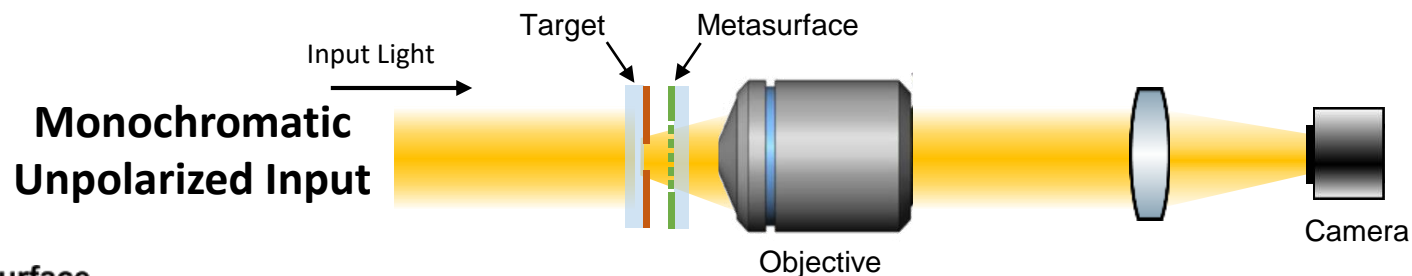
BROADBAND, HIGH-EFFICIENCY AND HIGH-NA EDGE DETECTION



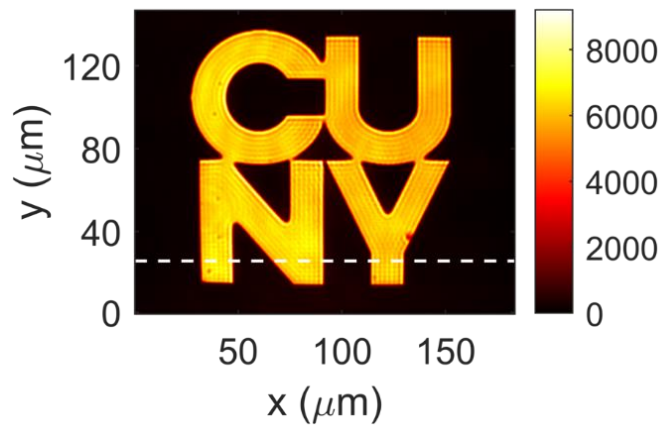
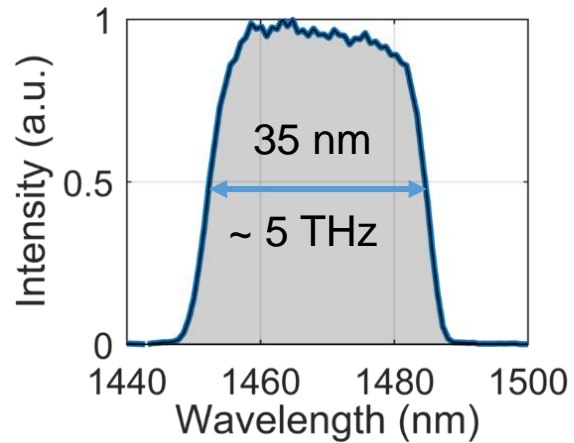
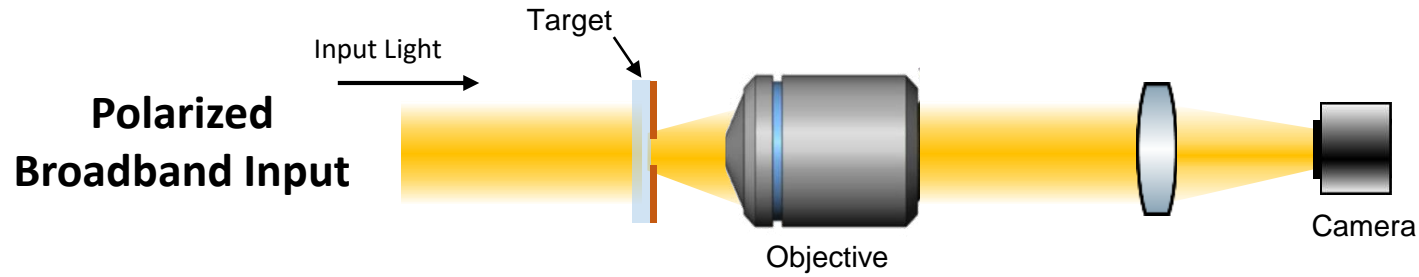
BROADBAND, HIGH-EFFICIENCY AND HIGH-NA EDGE DETECTION



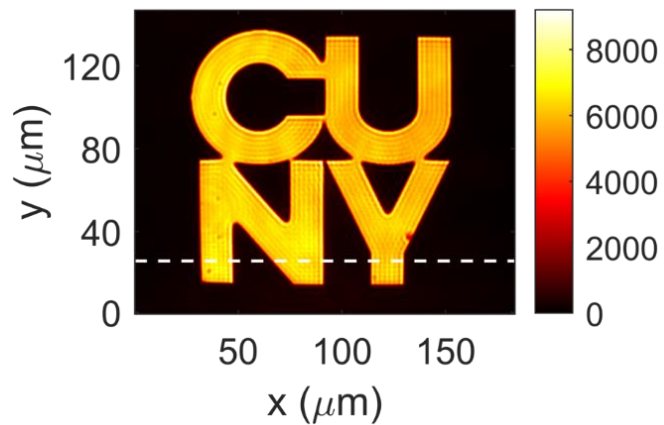
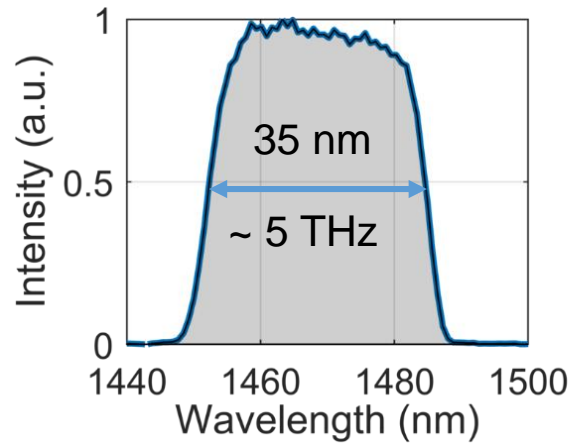
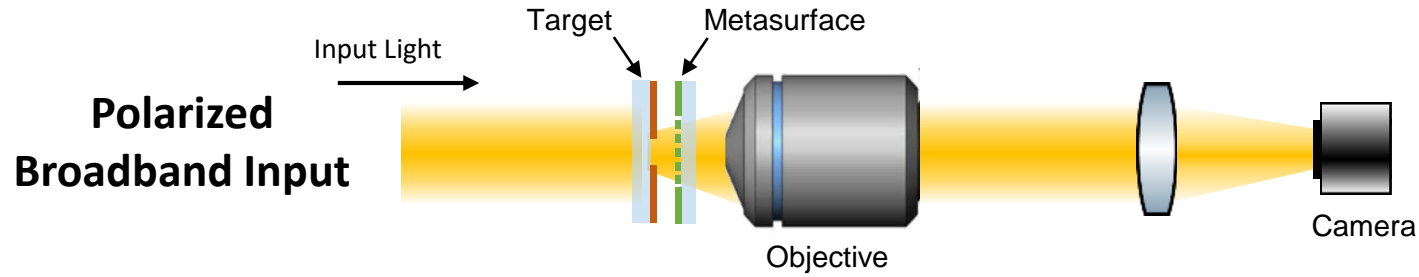
BROADBAND, HIGH-EFFICIENCY AND HIGH-NA EDGE DETECTION



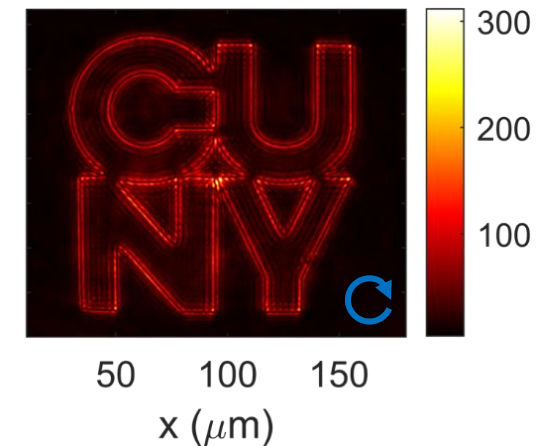
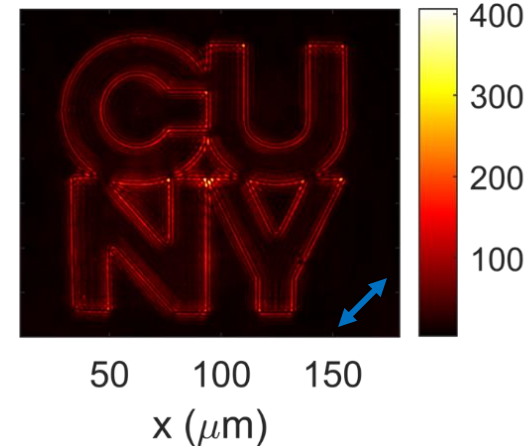
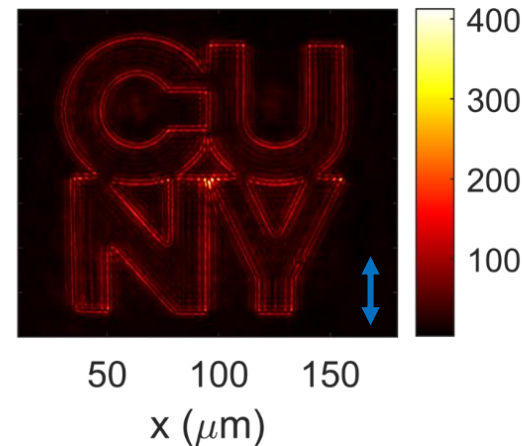
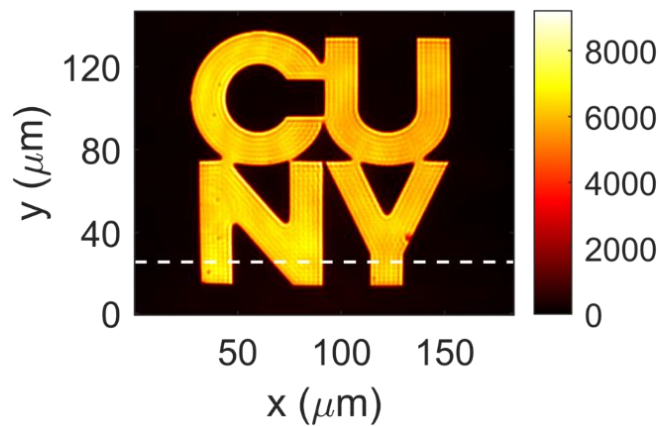
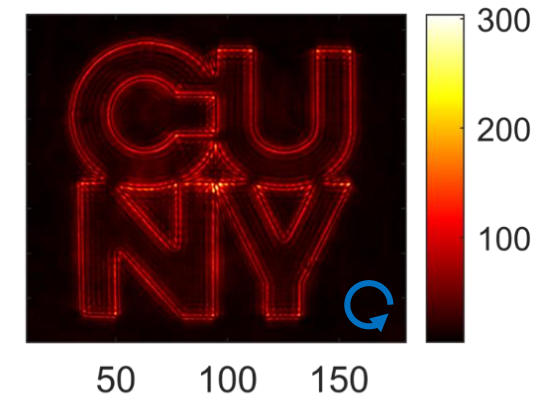
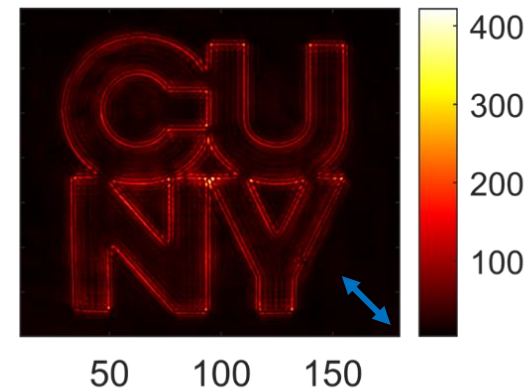
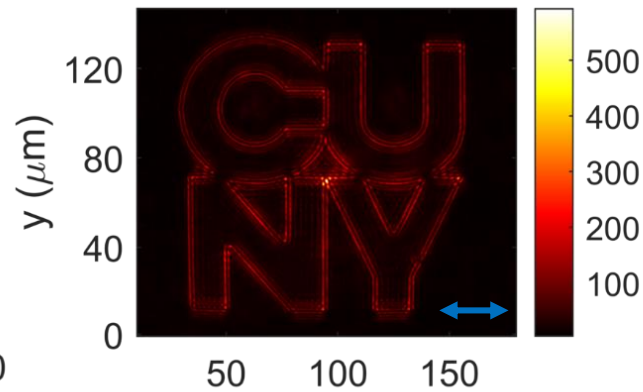
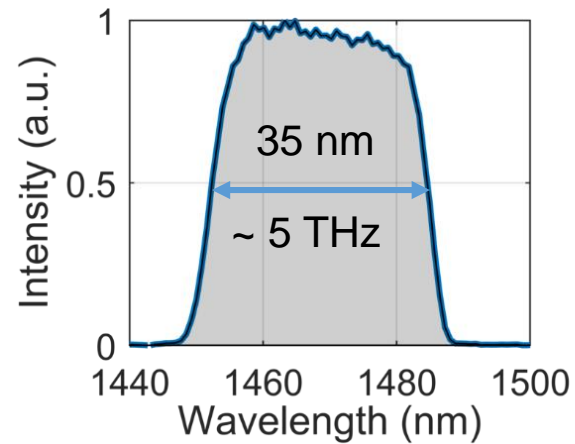
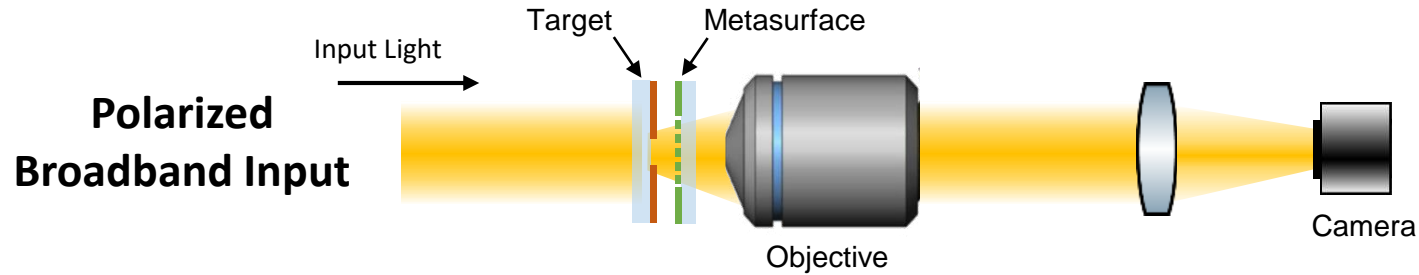
BROADBAND, HIGH-EFFICIENCY AND HIGH-NA EDGE DETECTION



BROADBAND, HIGH-EFFICIENCY AND HIGH-NA EDGE DETECTION

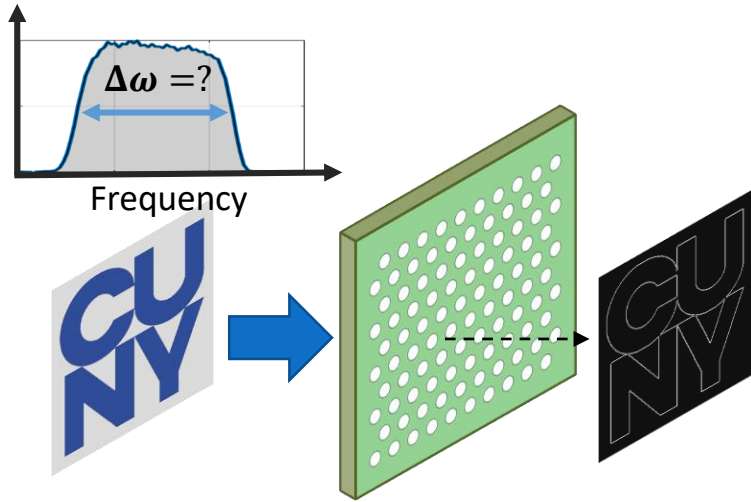


BROADBAND, HIGH-EFFICIENCY AND HIGH-NA EDGE DETECTION

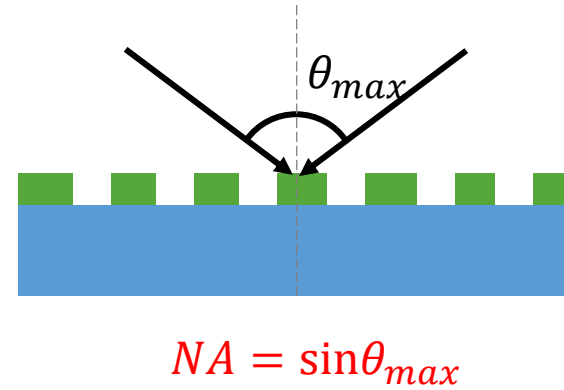


IMPORTANT FIGURES OF MERIT

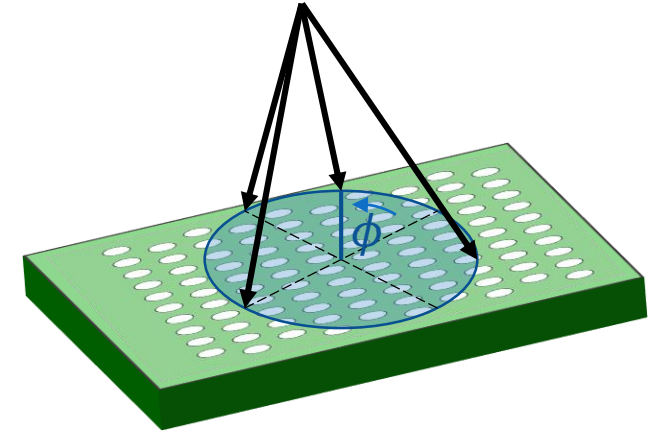
1. Spectral Bandwidth



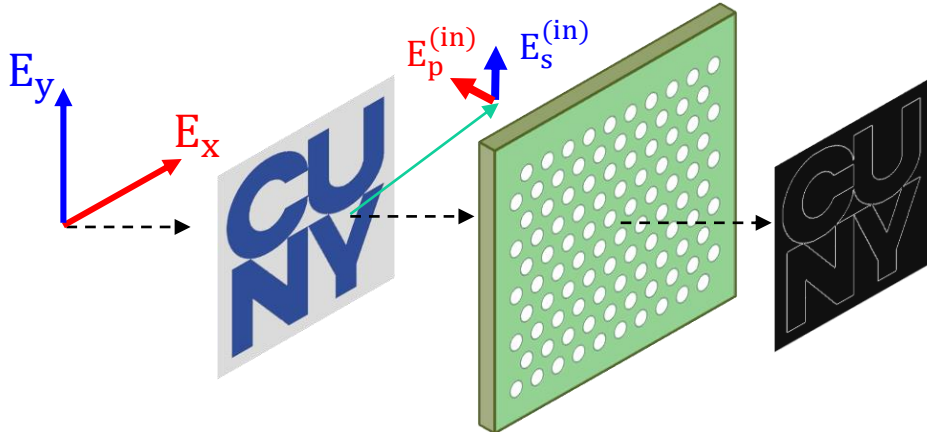
2. Numerical Aperture



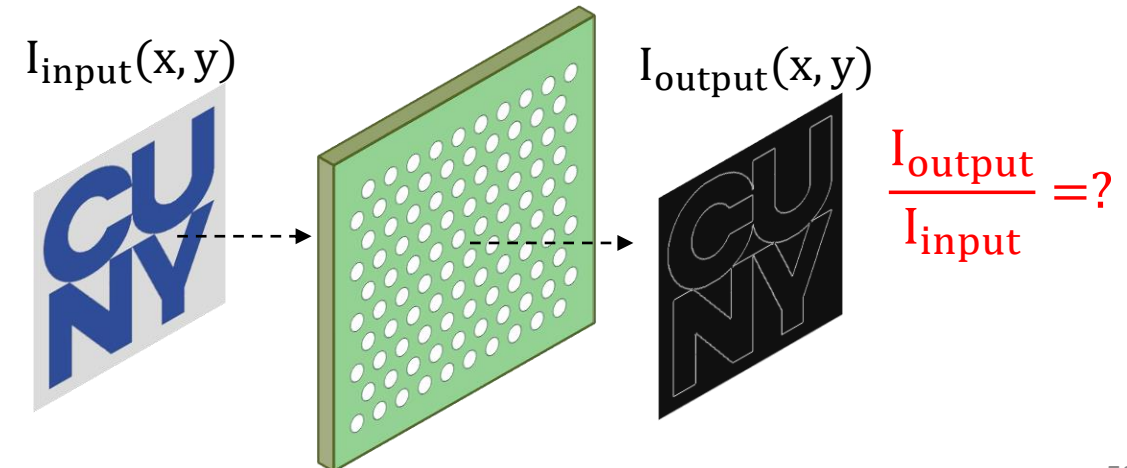
3. Azimuthal Isotropy



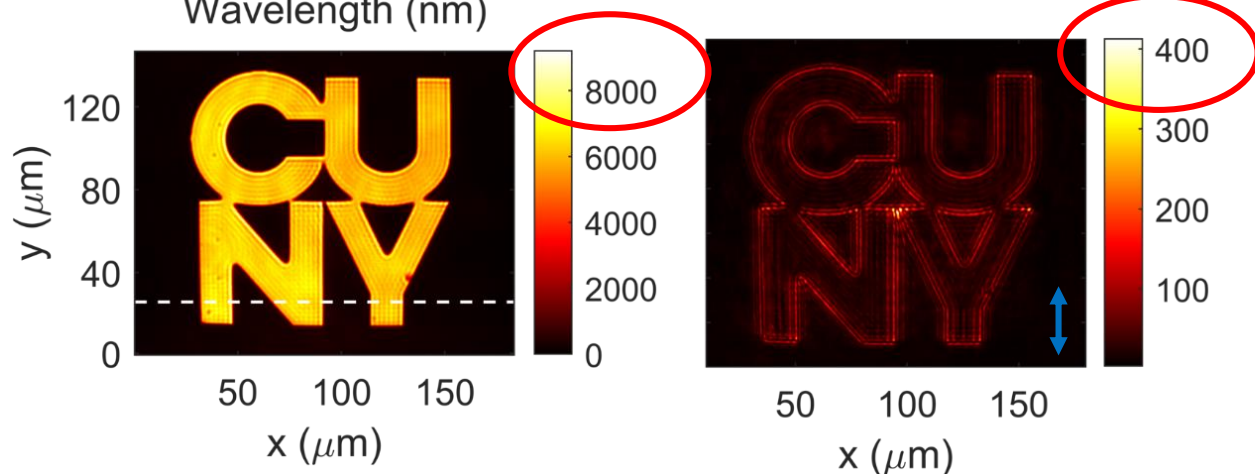
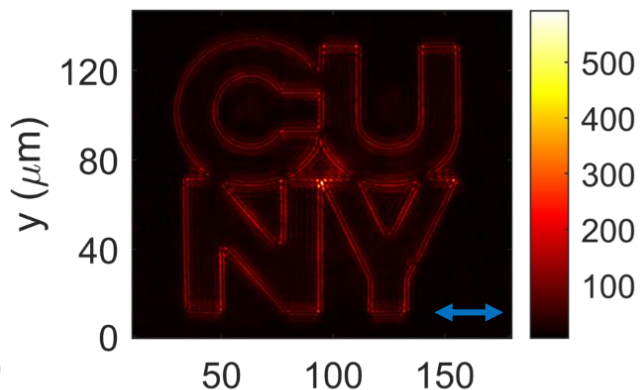
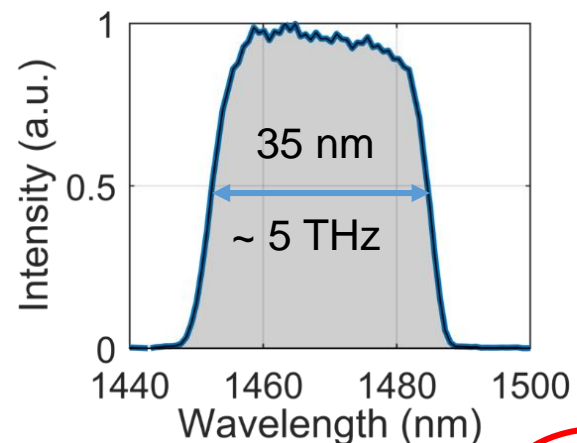
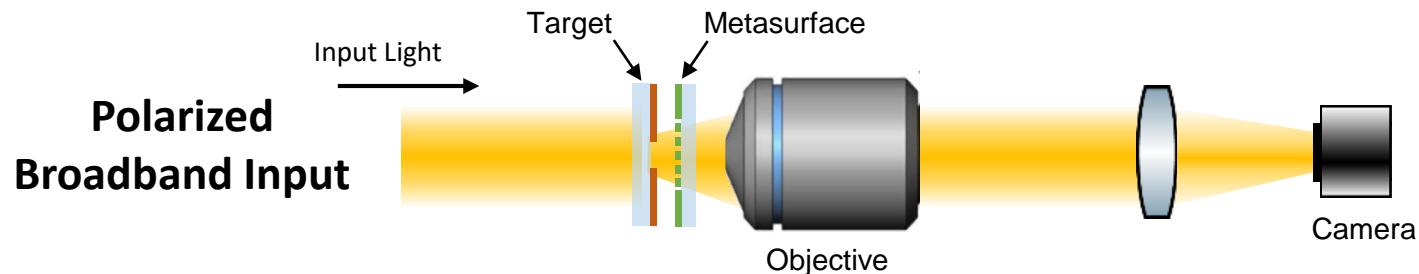
4. Polarization (in)dependence



5. Efficiency



BROADBAND, HIGH-EFFICIENCY AND HIGH-NA EDGE DETECTION



In each measurement, counts are normalized by **camera integration time** and **laser power**

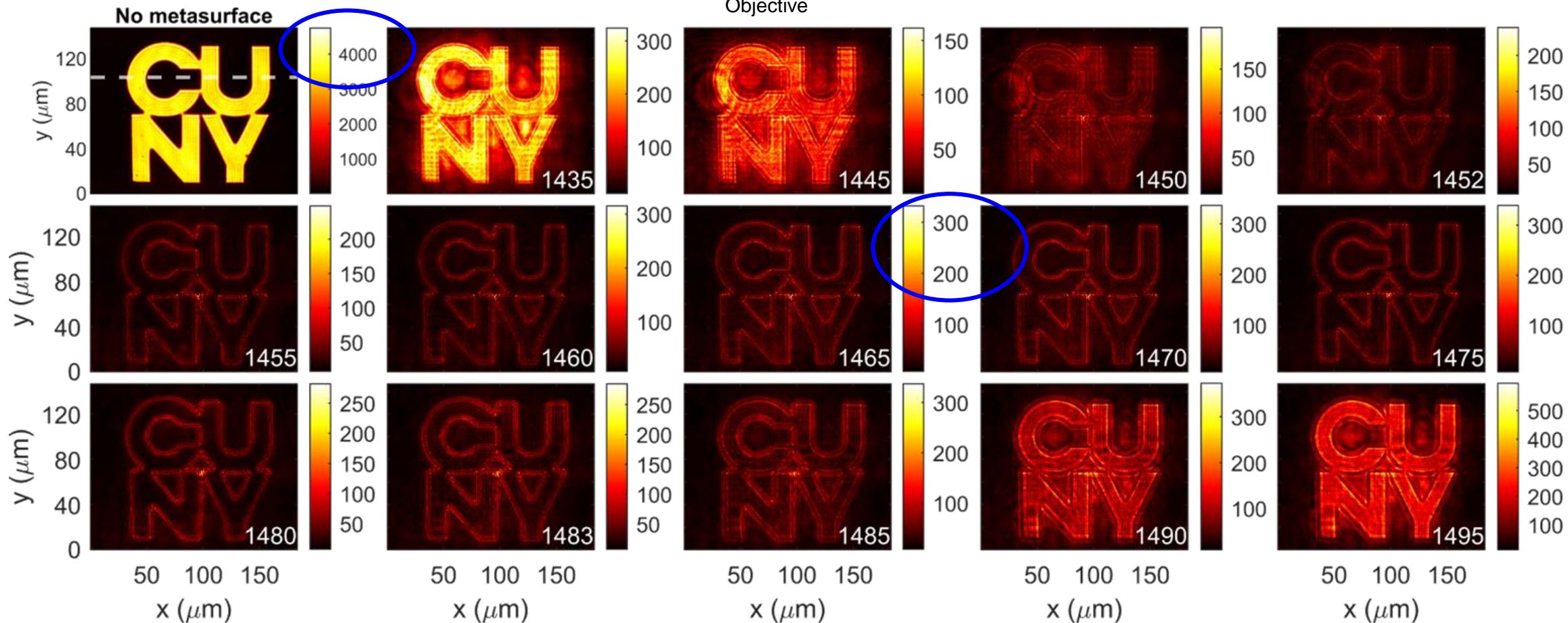
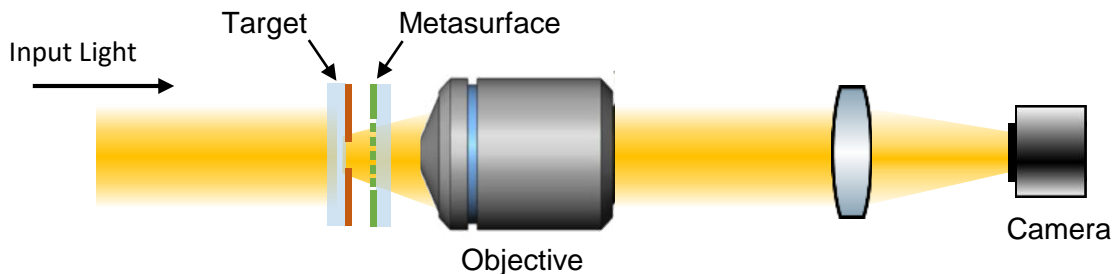
Efficiency:

$$\eta_{peak} \equiv \frac{\max(I_{filtered})}{\max(I_{input})} \approx 4\% - 5\%$$

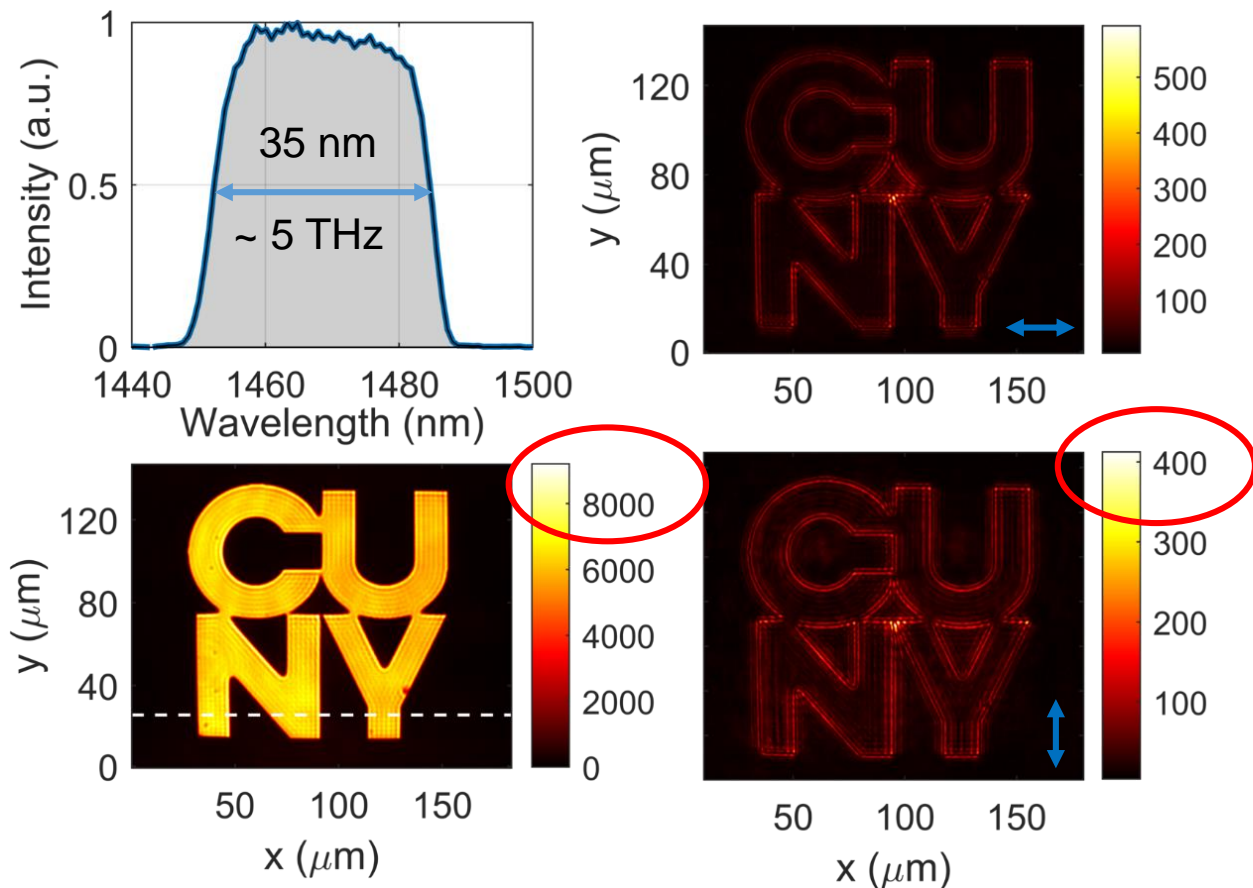
$$\eta_{avg} \equiv \frac{\text{avg}_{edge}(I_{filtered})}{\max(I_{input})} \approx 1 - 2\%$$

BROADBAND, HIGH-EFFICIENCY AND HIGH-NA EDGE DETECTION

Monochromatic
Unpolarized Input



BROADBAND, HIGH-EFFICIENCY AND HIGH-NA EDGE DETECTION



Efficiency:

$$\eta_{peak} \equiv \frac{\max(I_{filtered})}{\max(I_{input})} \approx 4\% - 5\%$$

$$\eta_{avg} \equiv \frac{\text{avg}_{edge}(I_{filtered})}{\max(I_{input})} \approx 1 - 2\%$$

How good are these efficiencies?

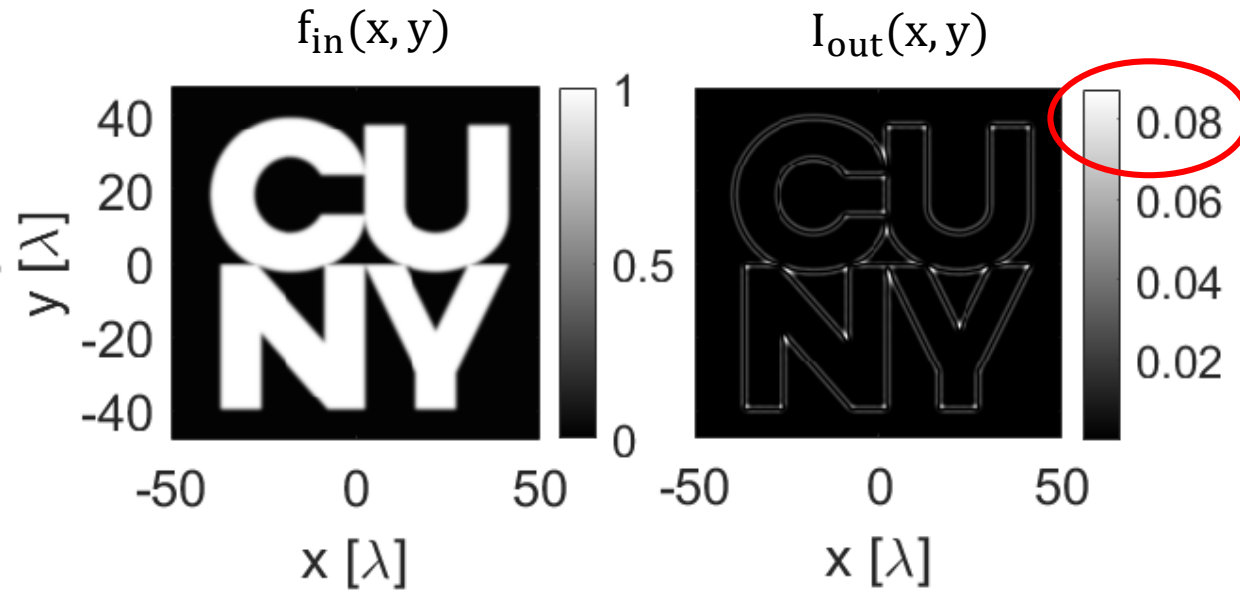
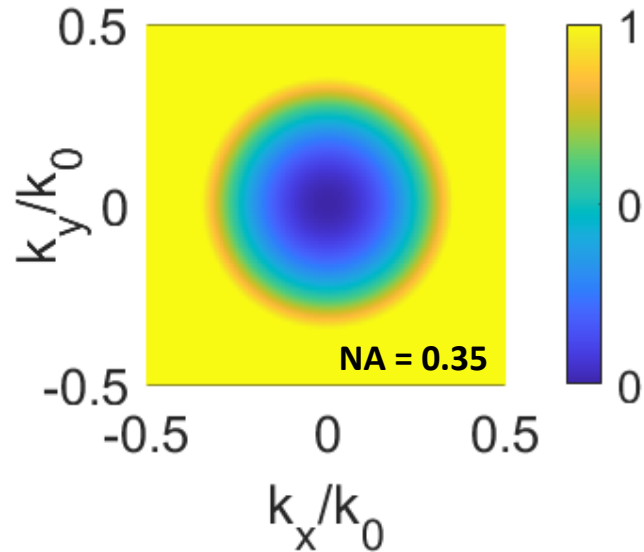
- Efficiencies of 1% - 5% sound small...
- (Reviewers do not seem to like 1-digit numbers)

COMPARISON WITH IDEAL EDGE DETECTOR

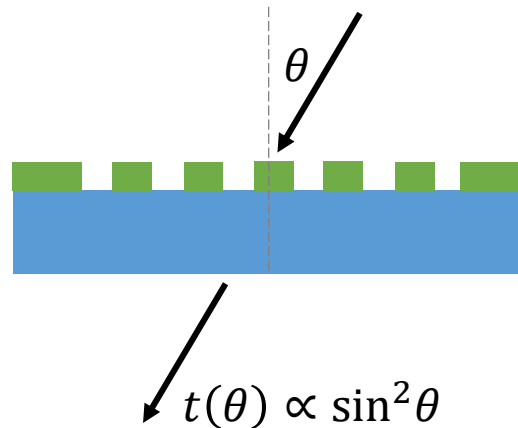
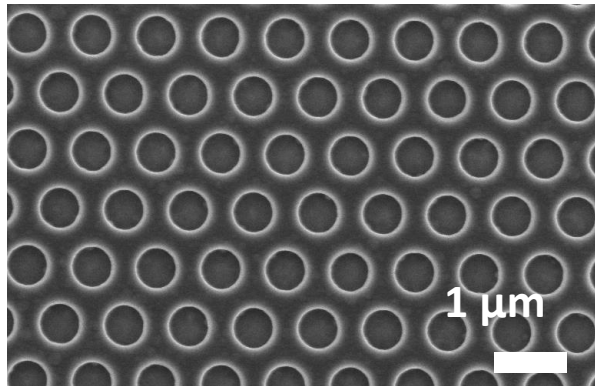
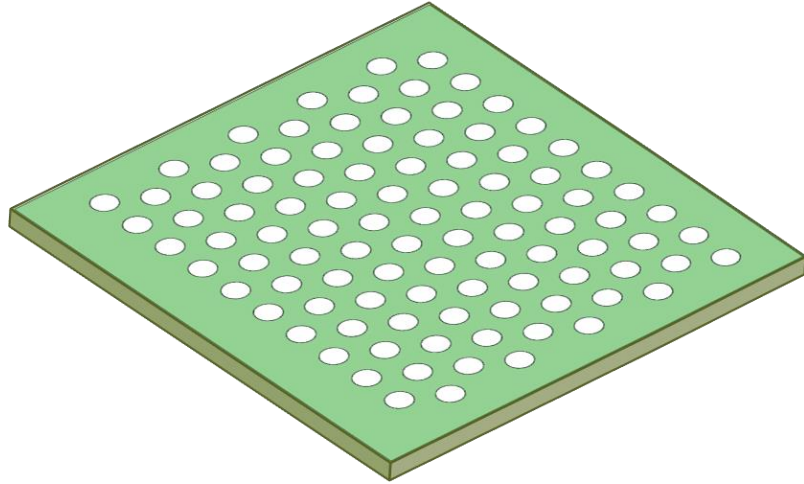
How good are these efficiencies?

$$t_{pp}(k_x, k_y) = t_{ss}(k_x, k_y) = t_{ideal}(k_x, k_y) = \begin{cases} \left(\frac{1}{k_0^2 NA^2}\right) \cdot (k_x^2 + k_y^2) & \text{if } k_x^2 + k_y^2 \leq k_0^2 NA^2 \\ 1 & \text{otherwise} \end{cases}$$

Ideal Detector



SIMULTANEOUS OPTIMIZATION OF ALL FIGURES OF MERIT



- **Full Polarization-Independent**

- **High NA** ($NA > 0.35$)

- **Large bandwidths**
($\Delta\lambda \geq 35 \text{ nm @ } 1500 \text{ nm}$)

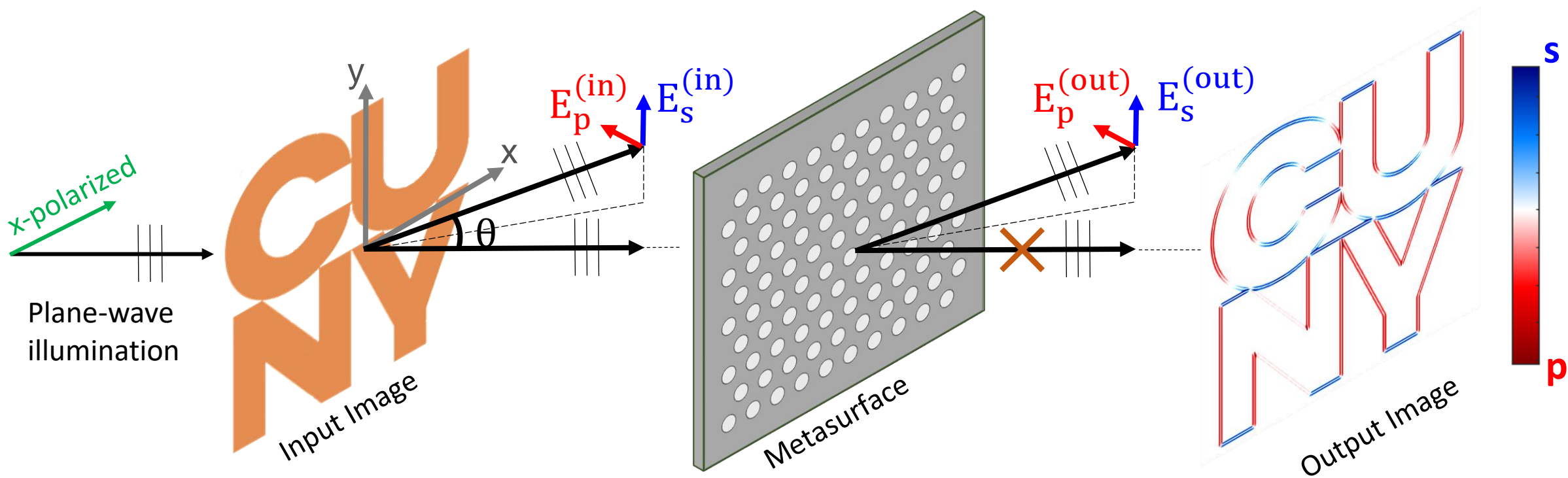
- **Very high Efficiencies**

Close to the maximum allowed by math!

- **High Isotropy**

C6 symmetry → Largest isotropy allowed by a period metasurface

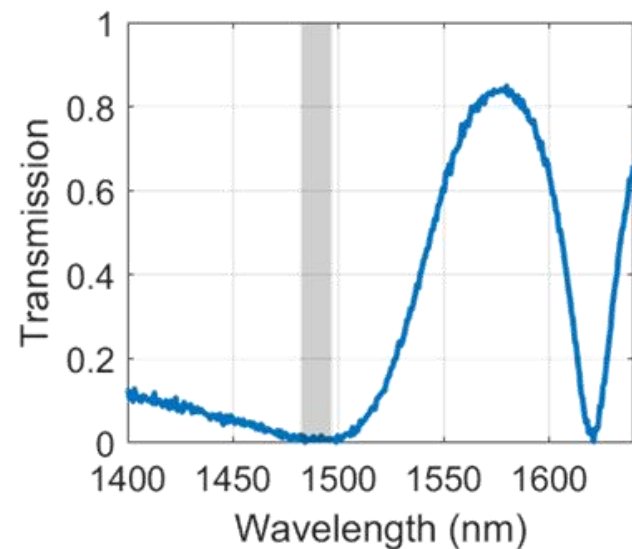
POLARIZATION-DEPENDENT EDGE-DETECTION



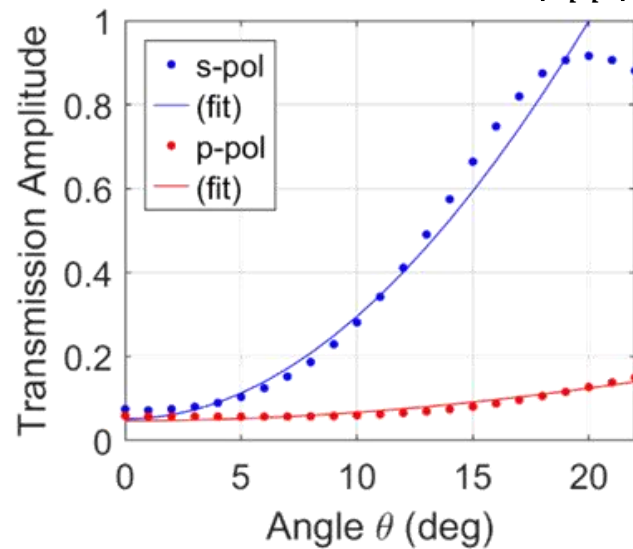
POLARIZATION-DEPENDENT EDGE DETECTION

Single-Polarization Metasurface

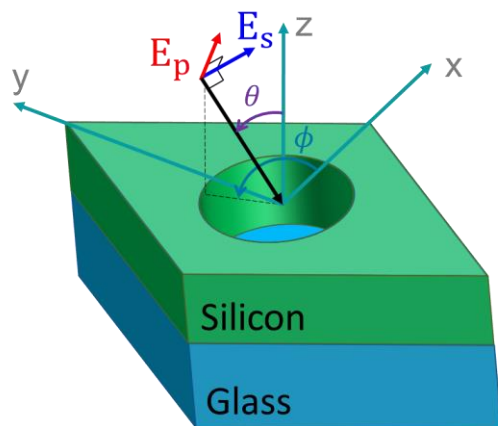
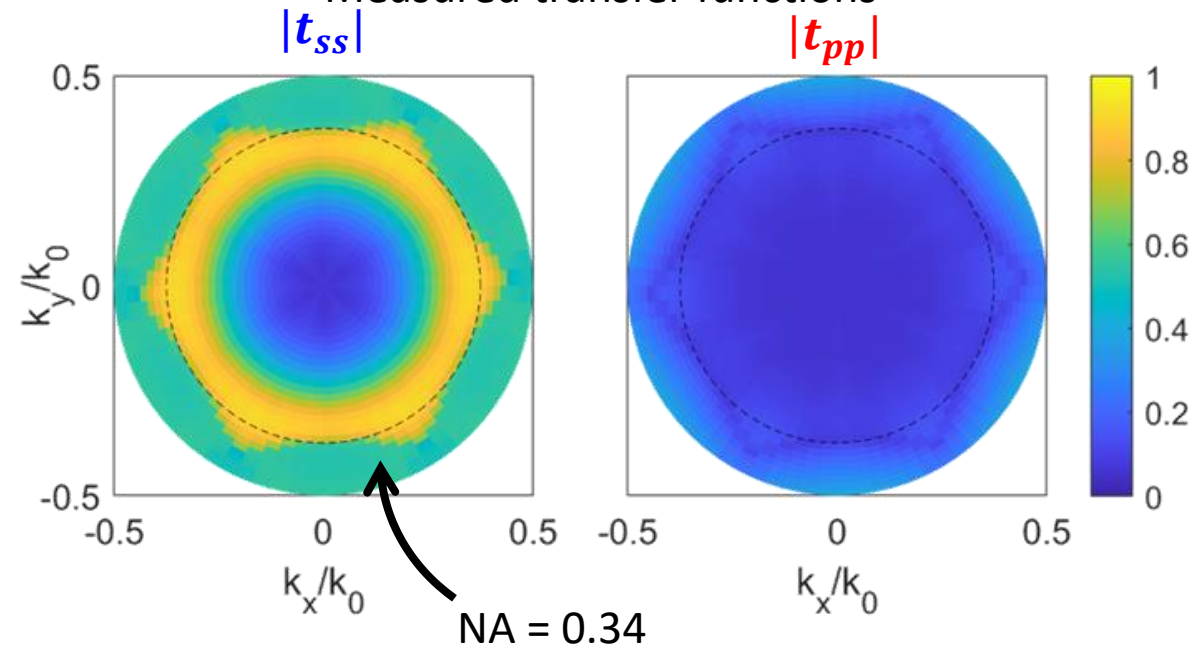
Normal-incidence transmission



Measured $|t_{ss}|$ and $|t_{pp}|$

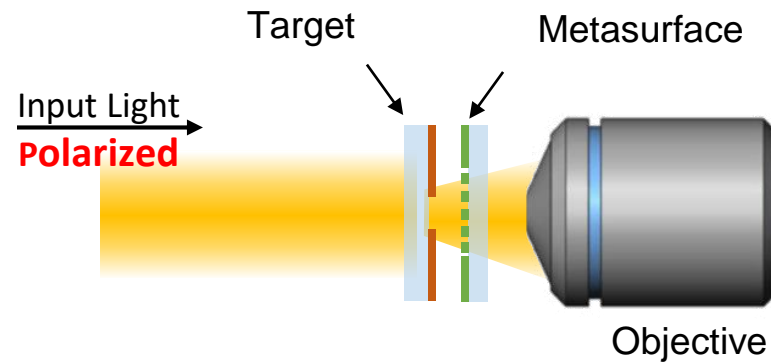


Measured transfer functions



Same metasurface pattern as before (i.e. same C_6 symmetry)
but different geometrical parameters

POLARIZATION-DEPENDENT EDGE DETECTION

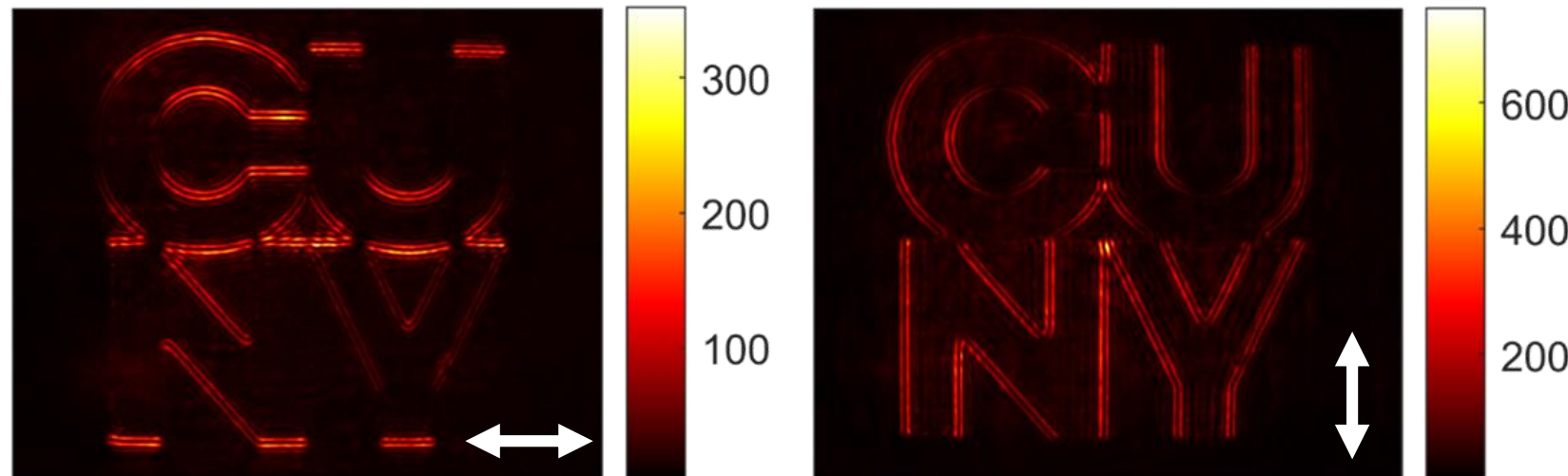


Unfiltered image



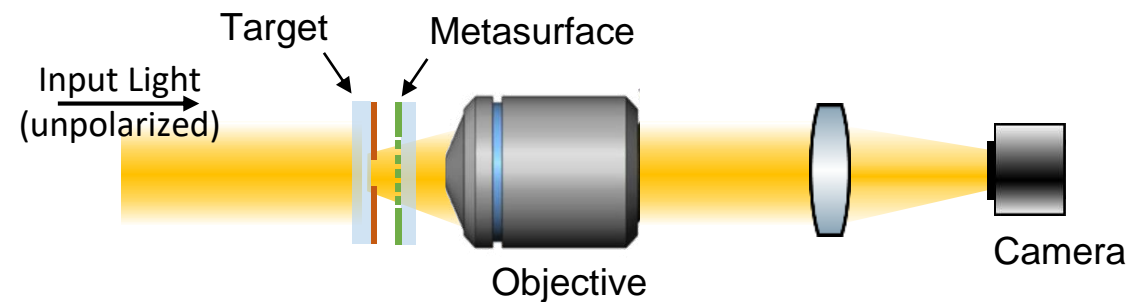
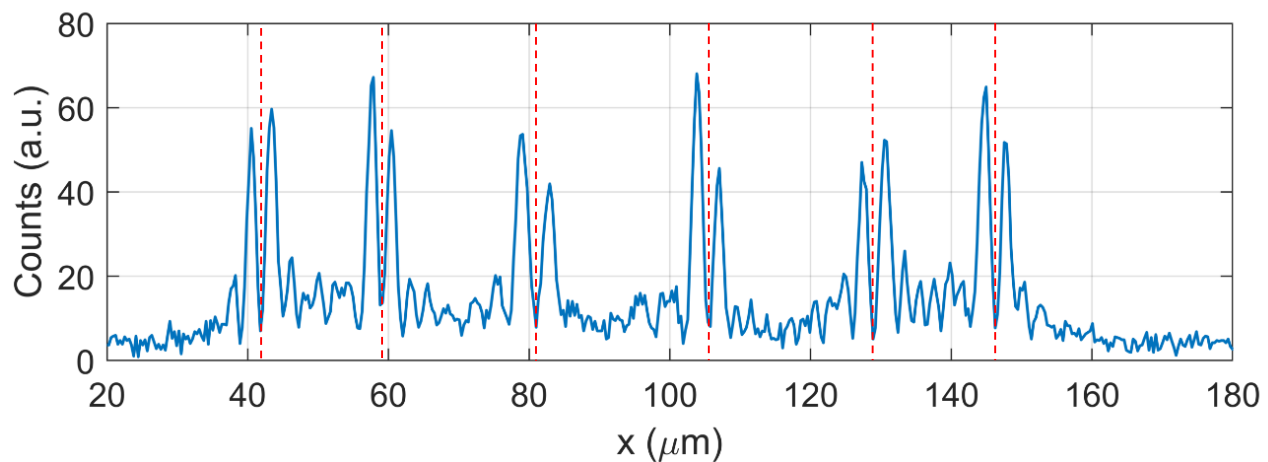
Scale bar = 30 μm

Direction-Dependent Edge Detection

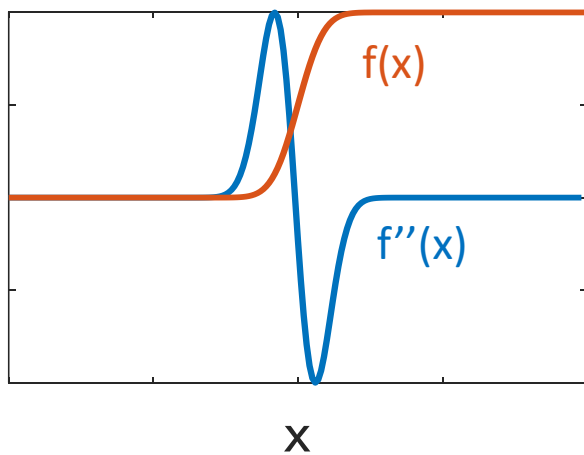


$$\eta_{\text{peak}} > 3 \%$$

SECOND-ORDER DERIVATIVE

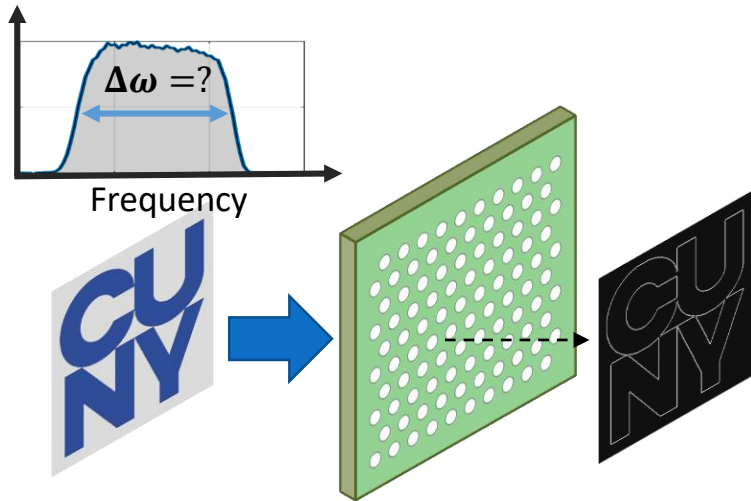


Filtered image, unpolarized excitation

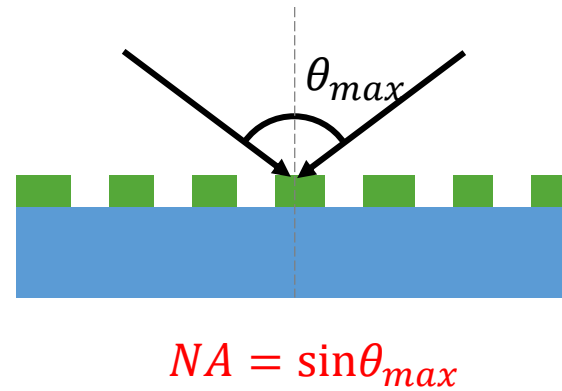


IMPORTANT FIGURES OF MERIT

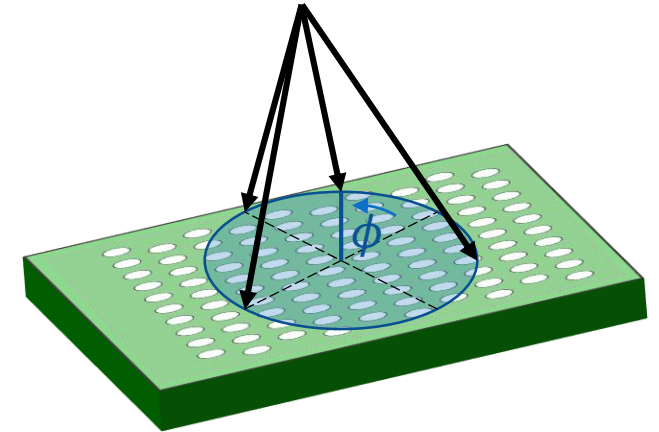
1. Spectral Bandwidth



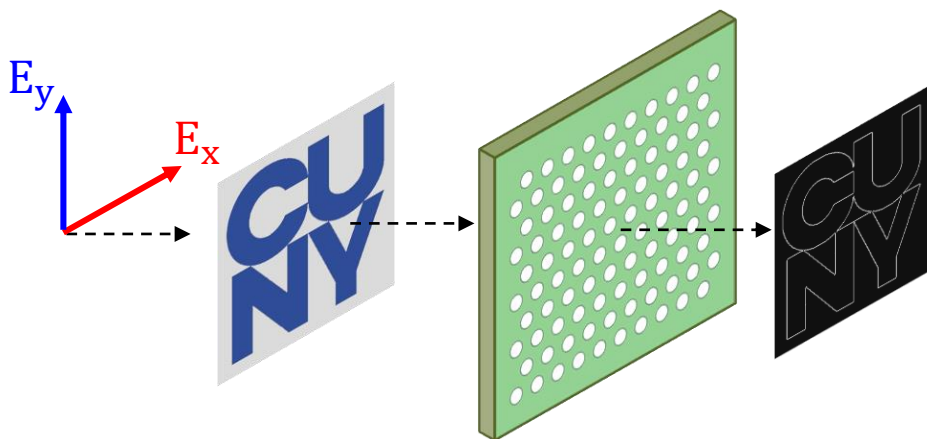
2. Numerical Aperture



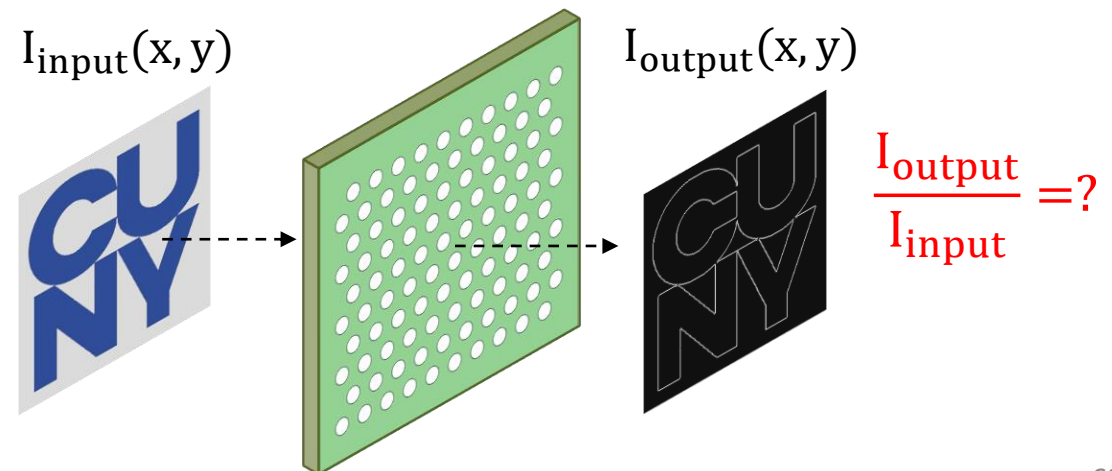
3. Azimuthal Isotropy



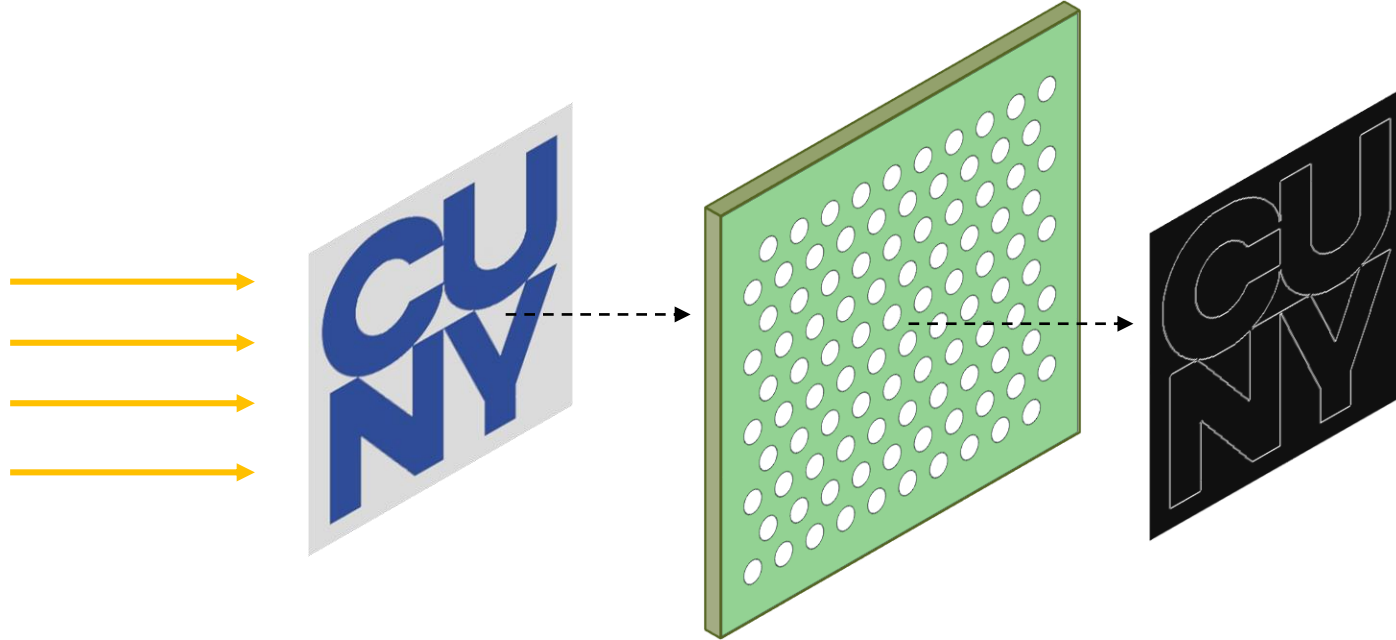
4. Polarization (in)dependence



5. Efficiency

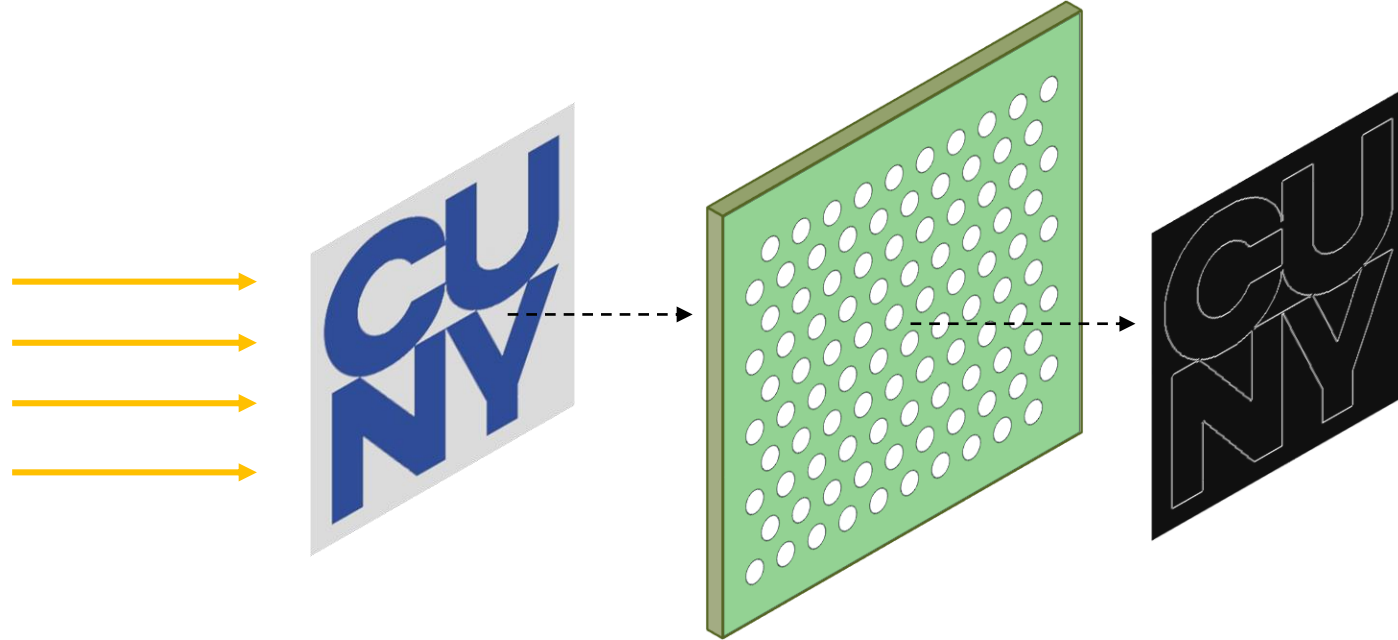


COHERENT VS INCOHERENT ILLUMINATION



- The image processing is obtained via coherent superposition of several waves diffracted by the image
- The input illumination must have some degree of spatial coherence

COHERENT VS INCOHERENT ILLUMINATION



Coherent illumination:

we can manipulate the field amplitude

$$E_{\text{in}}(\mathbf{k}_{\parallel}) \rightarrow E_{\text{out}}(\mathbf{k}_{\parallel}) = t(\mathbf{k}_{\parallel})E_{\text{in}}(\mathbf{k}_{\parallel})$$

$$t(\mathbf{k}_{\parallel}) \propto |\mathbf{k}_{\parallel}|^2$$

Transmission
amplitude

Incoherent illumination:

we need to work “directly” with the intensity

$$I_{\text{in}}(\mathbf{k}_{\parallel}) \rightarrow I_{\text{out}}(\mathbf{k}_{\parallel}) = T(\mathbf{k}_{\parallel})I_{\text{in}}(\mathbf{k}_{\parallel})$$

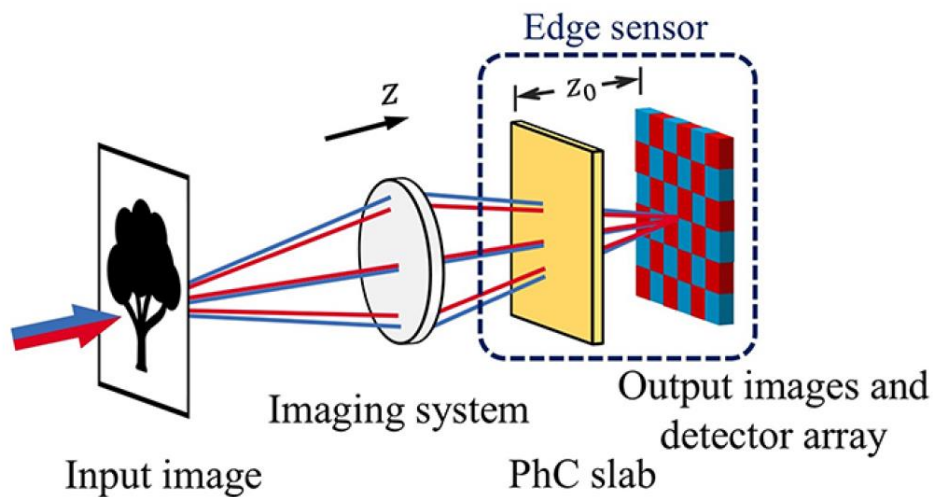
Can we get $T(\mathbf{k}_{\parallel}) \propto |\mathbf{k}_{\parallel}|^2$?

$$T(\mathbf{k}_{\parallel}) \propto \int t^*(\mathbf{q})t(\mathbf{k}_{\parallel} + \mathbf{q})d\mathbf{q} \Rightarrow T(\mathbf{k}_{\parallel}) \text{ always maximizes at } \mathbf{k}_{\parallel} = \mathbf{0}$$

- Wang et al., *Compact incoherent image differentiation with nanophotonic structures*. **ACS Photonics**, 7(2), pp.338-343 (2020)
- Zhang et al. *Incoherent Optoelectronic Differentiation Based on Optimized Multilayer Films*. **Laser & Photonics Reviews** 16.9 : 2200038 (2022)

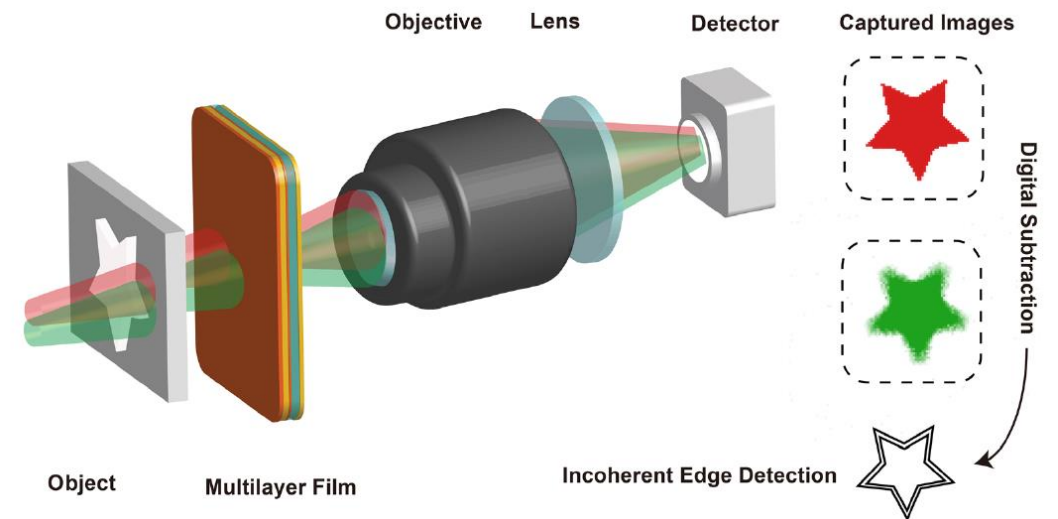
EDGE DETECTION UNDER INCOHERENT ILLUMINATION

Key idea: Process the same image with two different tailored transfer functions (e.g. same metasurface but different wavelengths), and then digitally subtract the two images



Wang et al., *Compact incoherent image differentiation with nanophotonic structures*. **ACS Photonics**, 7(2), pp.338-343 (2020).

Shanhui Fan's group



Zhang et al. *Incoherent Optoelectronic Differentiation Based on Optimized Multilayer Films*. **Laser & Photonics Reviews** 16.9 : 2200038 (2022).

Jason Valentine's group

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- Beyond the hype: What are (if any) the real benefits of metasurfaces in image processing?
- Are metasurface-based image-processing devices always worth the effort?

ADDING TEMPORAL PROCESSING

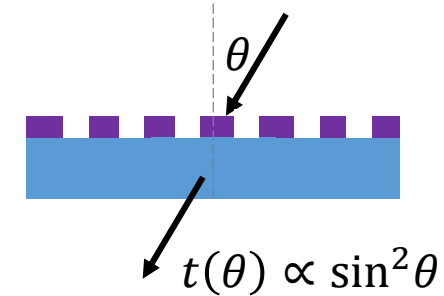
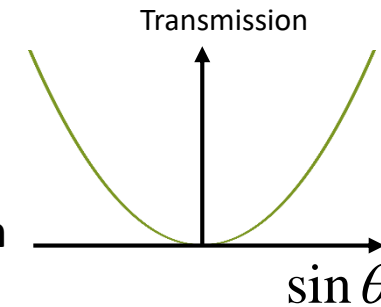
So far we have considered only spatial operations

$$f(x) \rightarrow \frac{\partial^m}{\partial x^m} f(x)$$



$$t(k_x) \propto k_x^m$$

Metasurface's transfer function



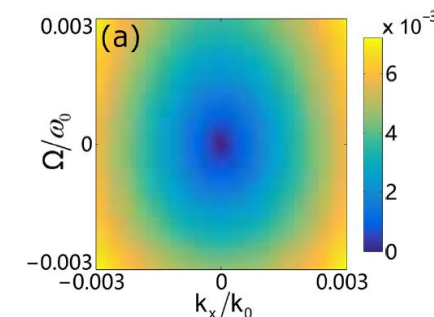
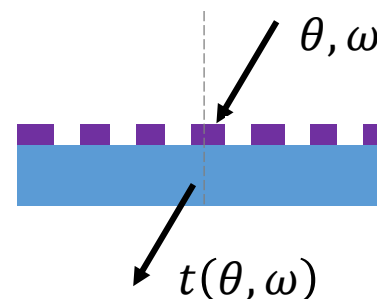
$$f(x, t) \rightarrow \hat{L}_{x,t} f(x, t)$$

$$\hat{L}_{x,t} = C_t \partial_t^m + C_x \partial_x^n$$



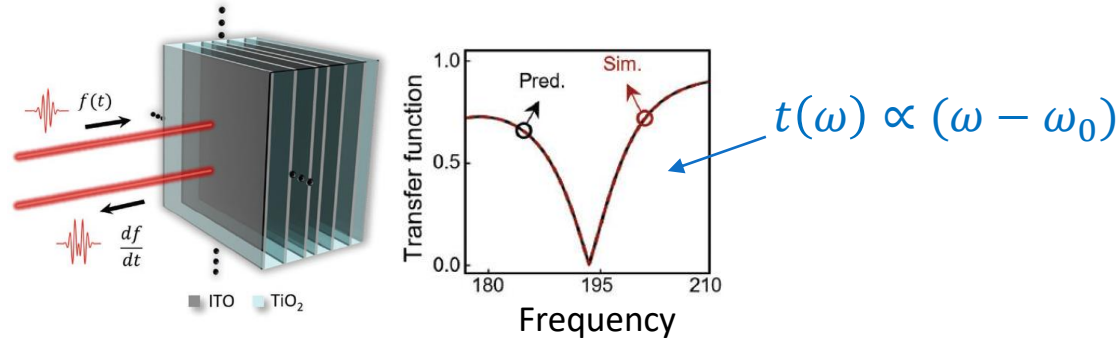
$$t(k_x, \omega) \propto C_x k_x^m + C_t \omega^n$$

$$\hat{L}_{x,t} = \begin{cases} \partial_t^m \\ C_t \partial_t^m + C_x \partial_x^n \\ \vdots \end{cases}$$



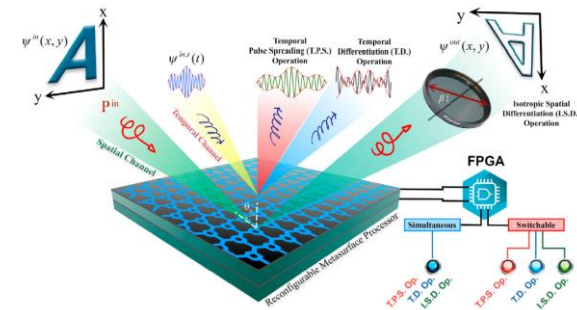
ADDING TEMPORAL PROCESSING

Analog Temporal Derivation ∂_t



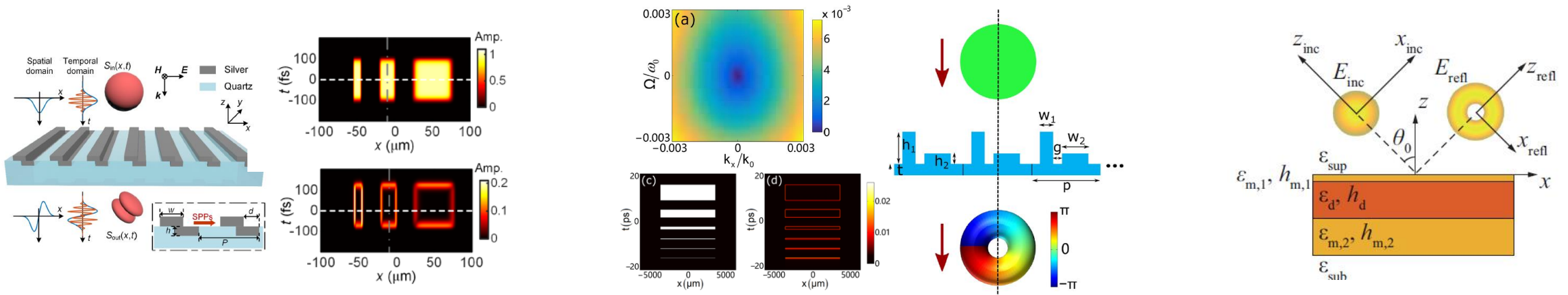
T. Knightley et al., **Advanced Optical Materials** 11.5: 2202351 (2023).

Switching between ∂_t and ∂_x



A. Momeni et al., **Carbon**, 186, 599–611 (2022)

Linear combination: $C_t \partial_t + C_x \partial_x$

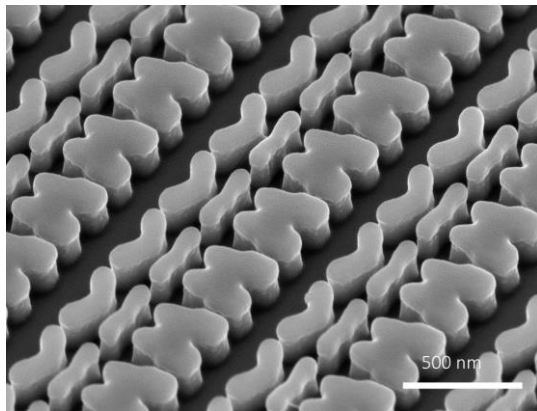
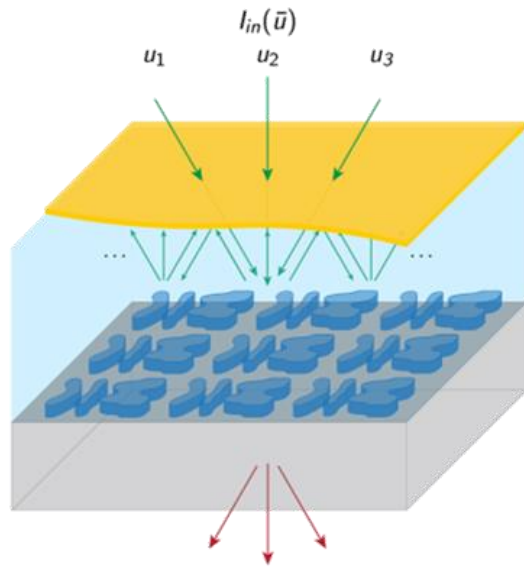


C. Xu, et al., **Optics Letters**, 46, 17, 4418–4421 (2021)

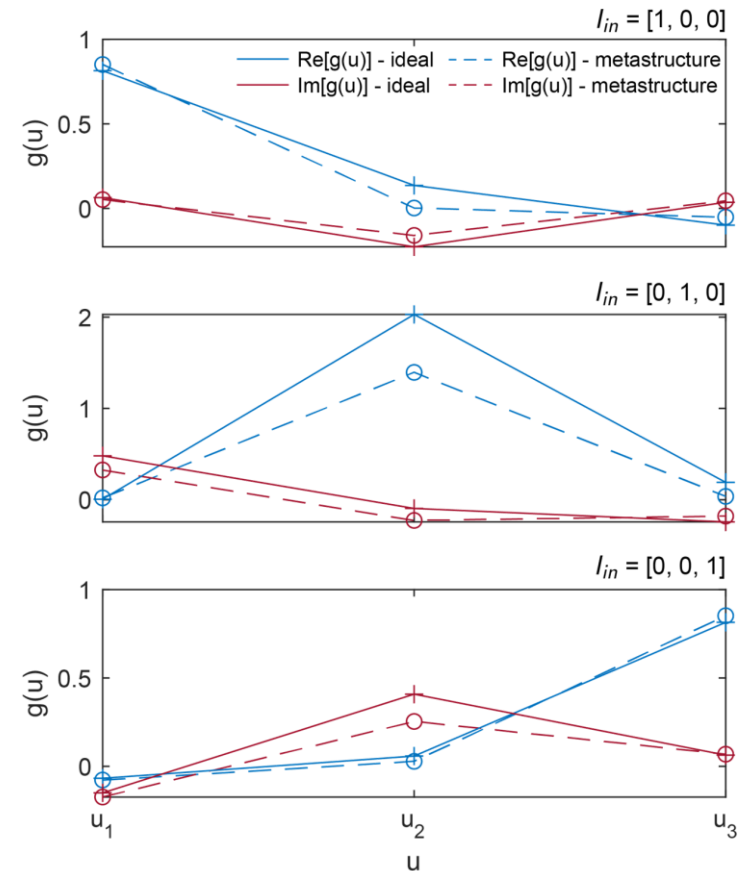
J. Huang et al., **Laser & Photonics Reviews**, 16, 5, p. 2100357 (2022)

L. L. Daskalovich, et al., **Phys. Rev. A**, 106, 3, 033523 (2022)

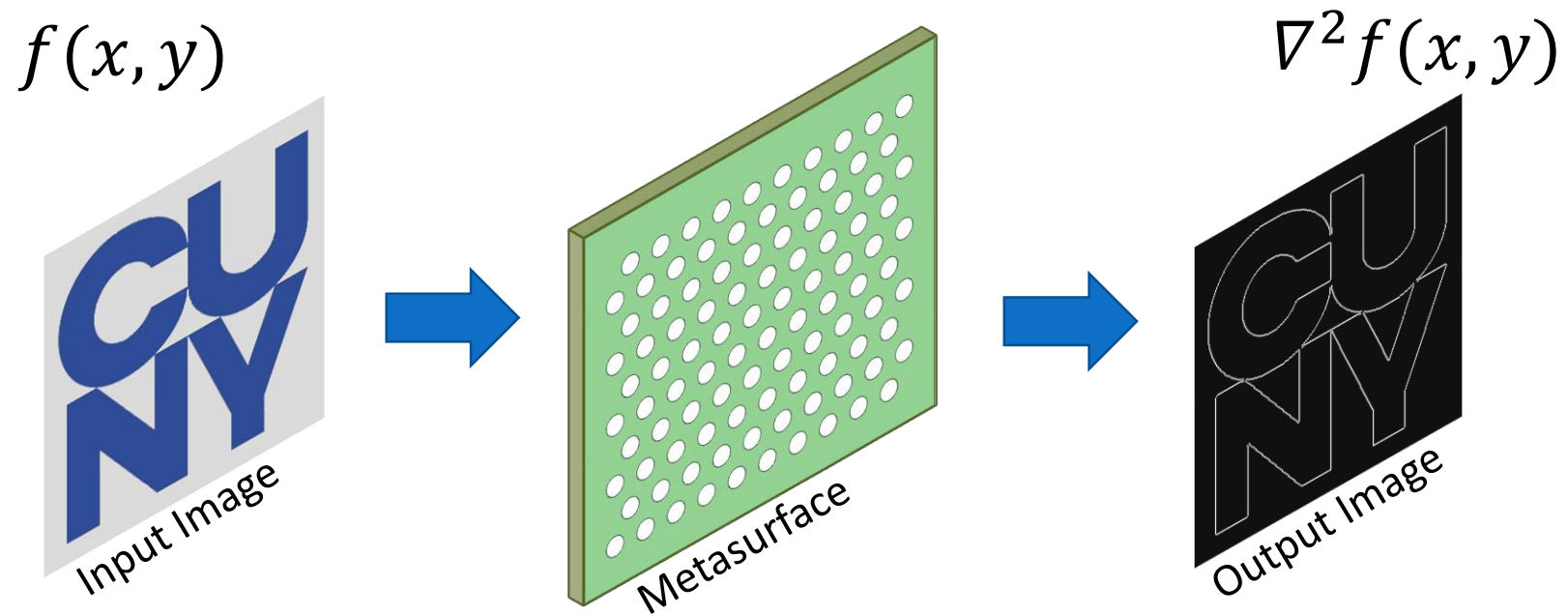
MORE COMPLEX OPERATIONS



$$g(u) = I_{in}(u) + \int_a^b K(u, v)g(v)dv$$



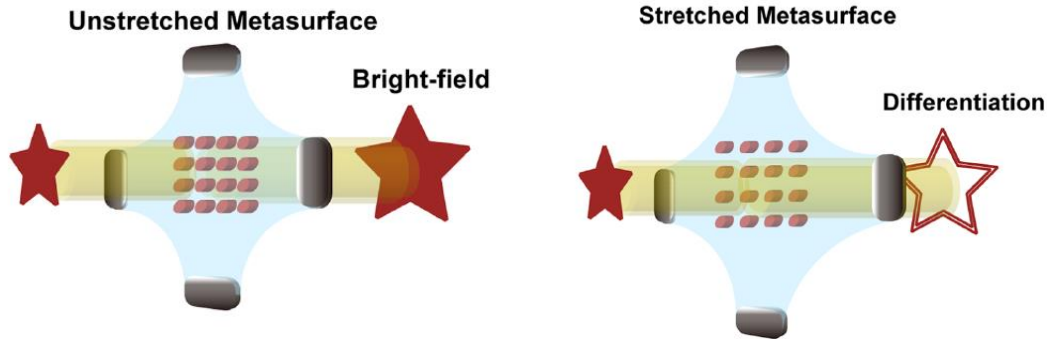
RECONFIGURABLE METASURFACES



- Most of the devices discussed so far are “static”: once fabricated, they will always perform the same operation
- For practical applications, we need some reconfigurability

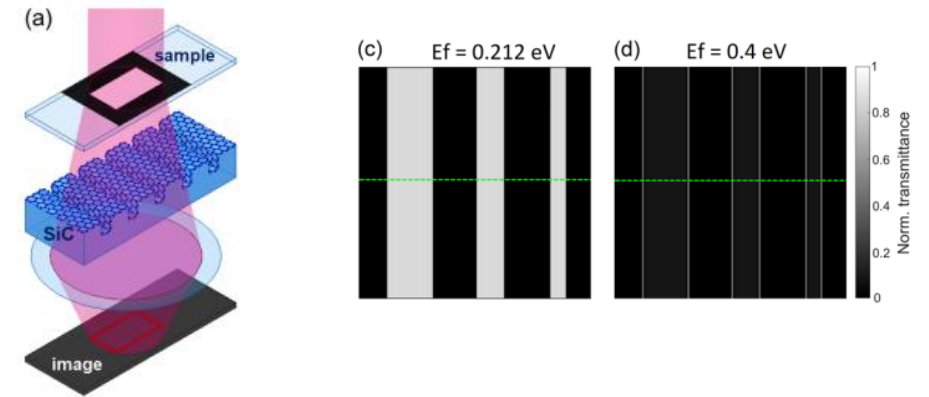
RECONFIGURABLE METASURFACES

Strain



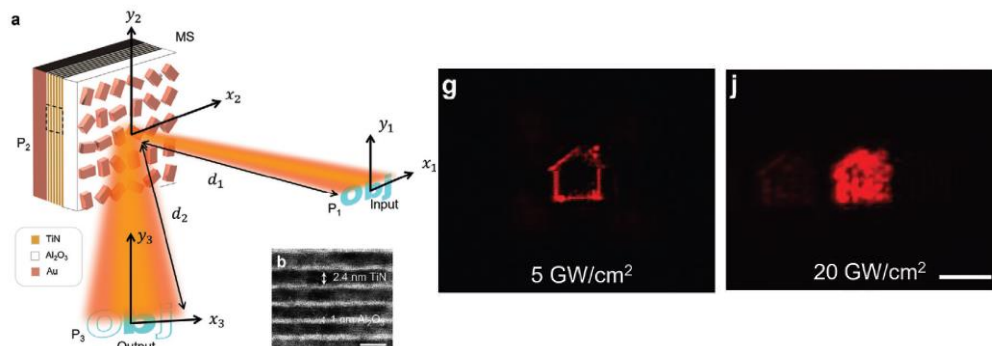
Zhang et al. Nano Letters 21.20: 8715-8722 (2021).

Electrical Tuning

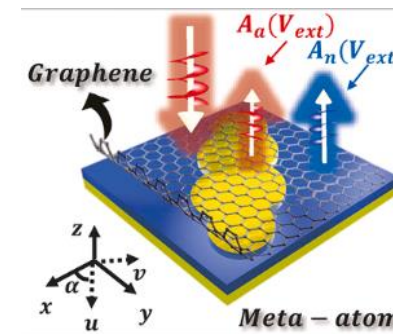


Khodasevych et al. Optical Materials Express 13.5: 1475-1487 (2023).

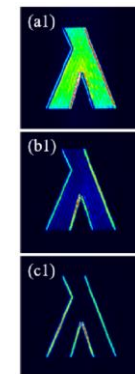
Nonlinear tuning



Zhou et al., Advanced Functional Materials 32.34, 2204734 (2022).



Qiushi, et al., Nanophotonics 11.9: 2085-2096 (2022).



Xiao et al. Optics Letters 47.4: 925-928 (2022)

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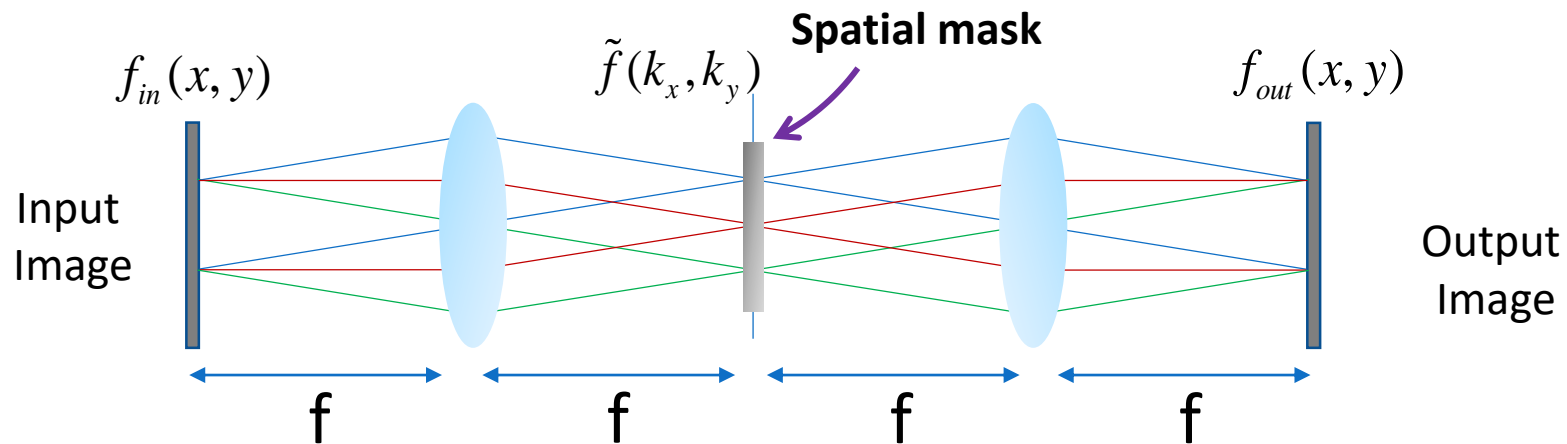
- Spatio-temporal image processing
- More complex mathematical operations
- Reconfigurable devices

4. (Open) Discussion

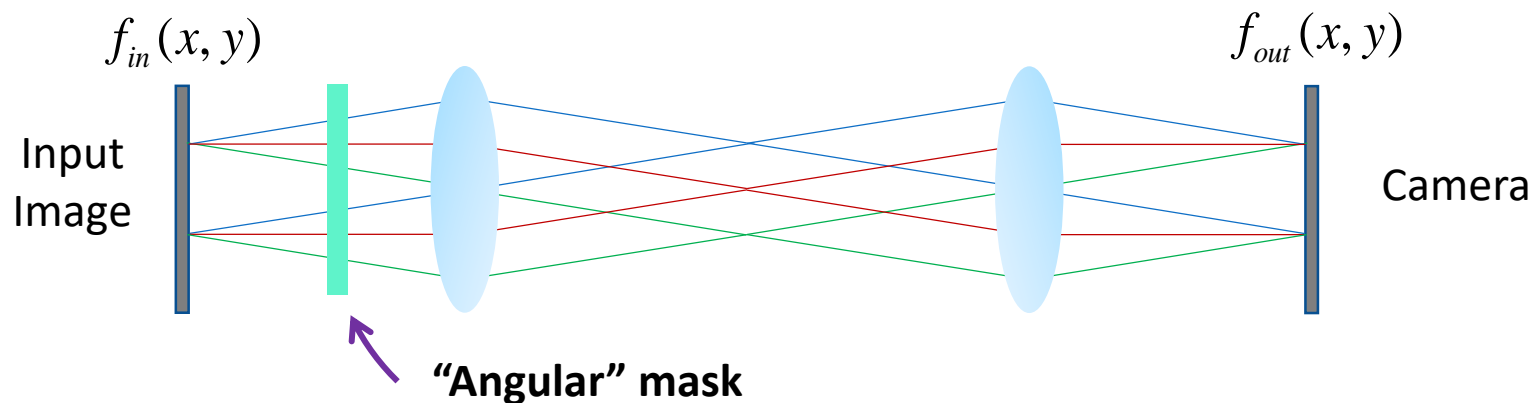
- Beyond the hype: What are (if any) the real benefits of metasurfaces in image processing?
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4F OR NOT 4F? – THIS IS THE QUESTION

Standard 4F
k-space filtering



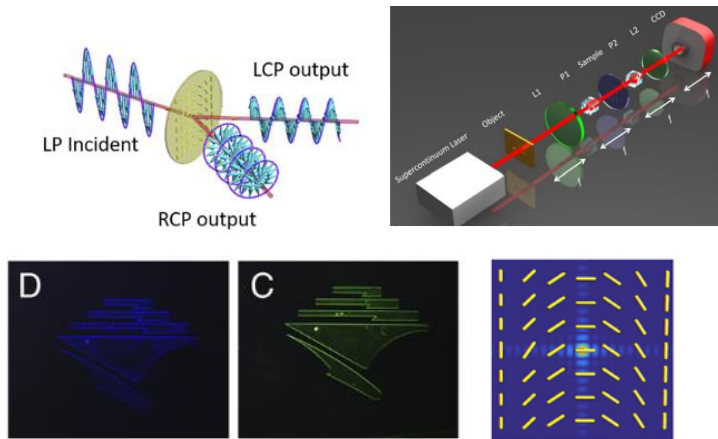
The “metasurface”
approach



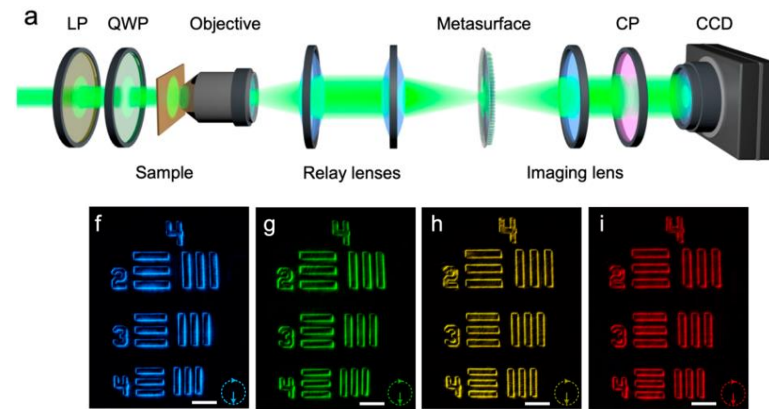
Transfer Function

$$f_{out}(x, y) = \iint dx dy t(k_x, k_y) \tilde{f}(k_x, k_y) e^{-i(k_x x + k_y y)}$$

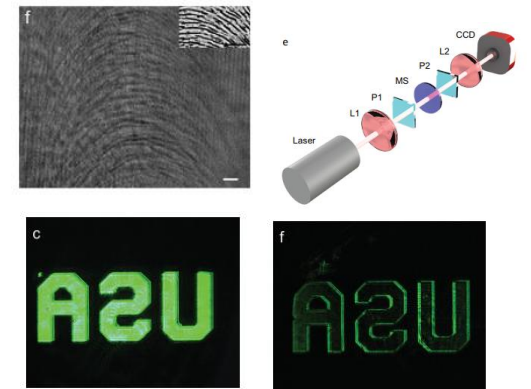
EDGE DETECTION WITH 4F + METASURFACES



Junxiao Zhou et al. PNAS 116.23 (2019): 11137-11140.



Pengcheng Huo et al., Nano Letters 20.4 (2020): 2791-2798.



Junxiao Zhou et al., National science review 8.6 (2021)

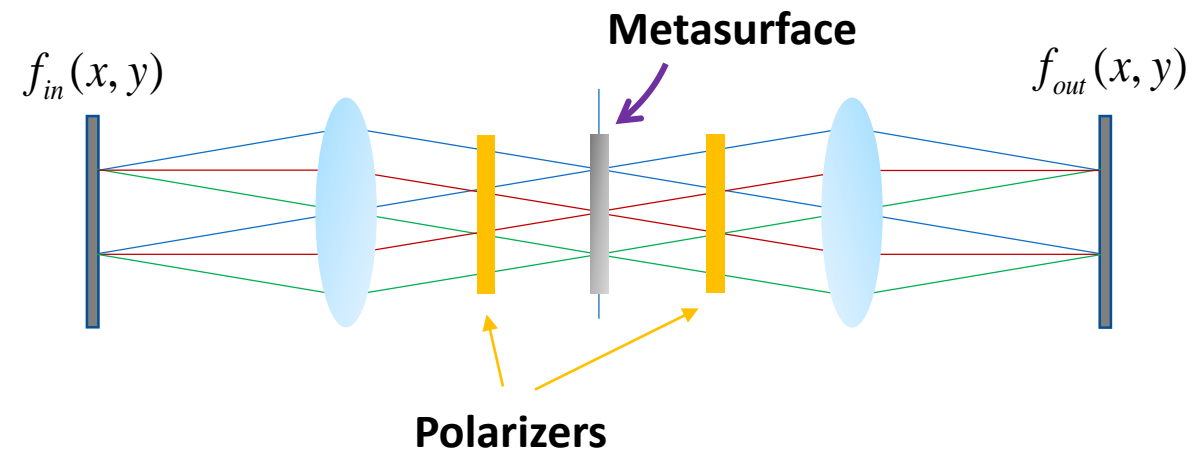
Pros:

- Metasurfaces offer **better control on amplitude and phase** with respect to a binary mask
- **Large bandwidths**, because spectral and angular response are “decoupled”

Cons:

- Require 4F → **cannot be miniaturized**
- Additional requirement of crossed polarizers

Pancharatnam–Berry-phase metasurfaces + Crossed polarizers



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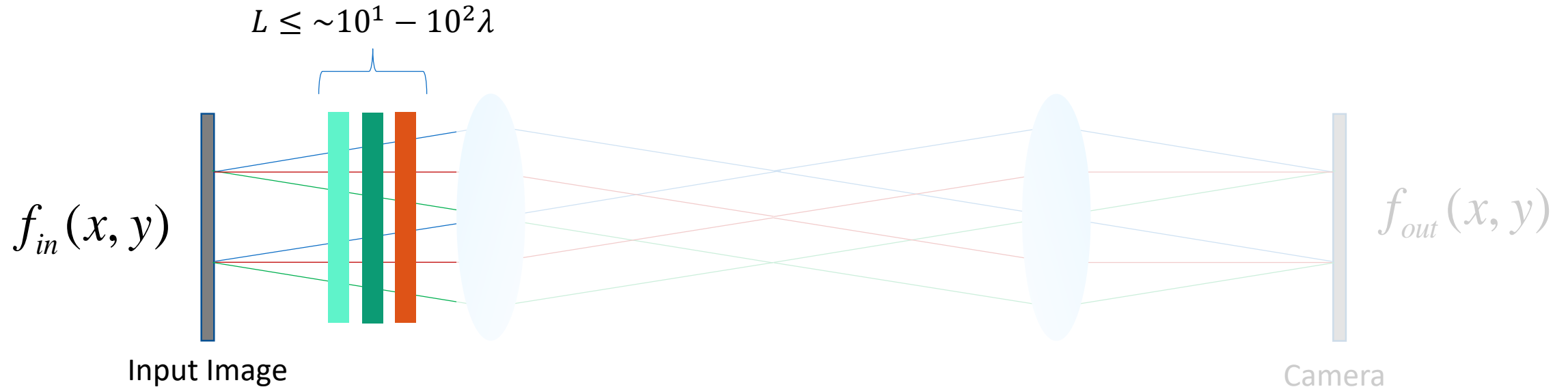
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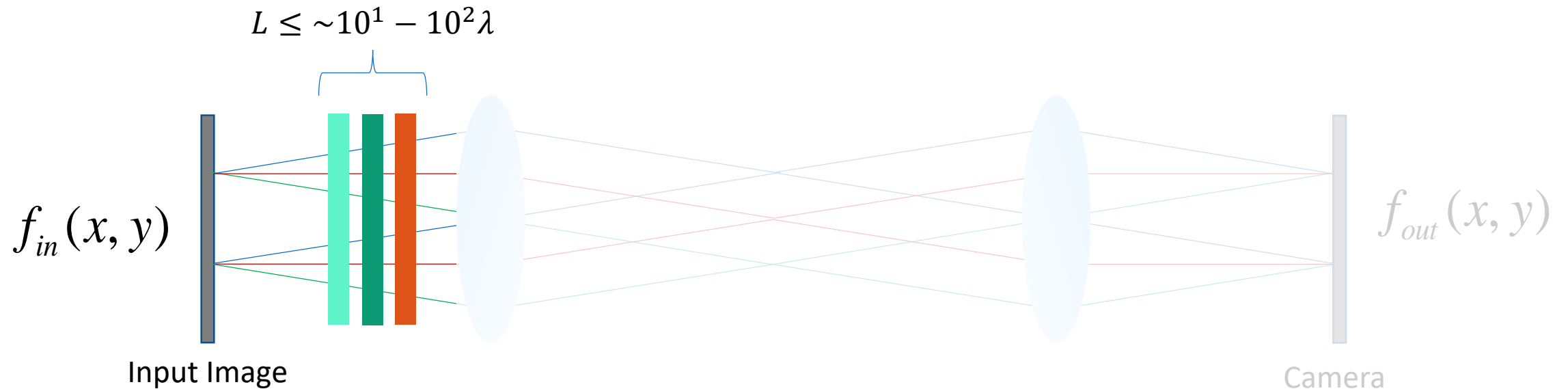
- Beyond the hype: What are (if any) the real benefits of metasurfaces in image processing?
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BEYOND THE HYPE



- **Compactness** → No need for a 4F system (in principle)
- **Scalability** → Multiple operations could be cascaded, without the need of additional optics
- **More tolerance on spatial alignment**
- More?

BEYOND THE HYPE



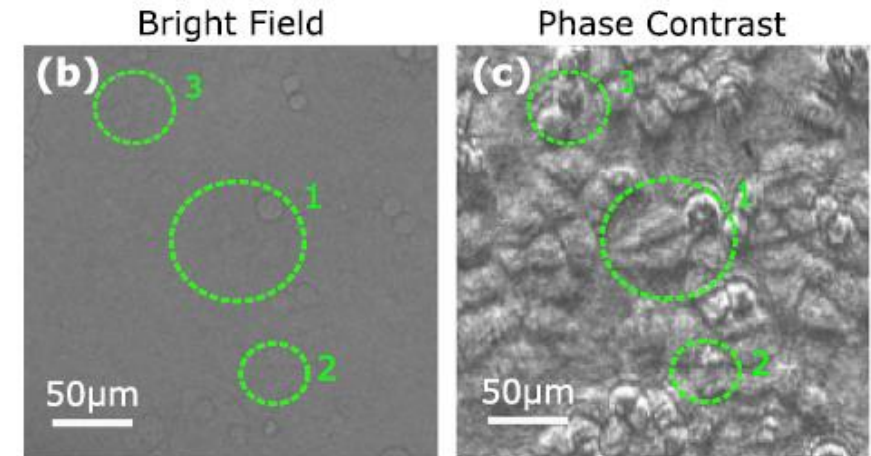
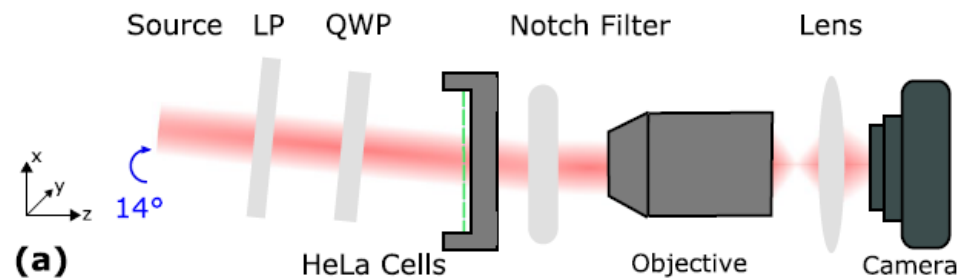
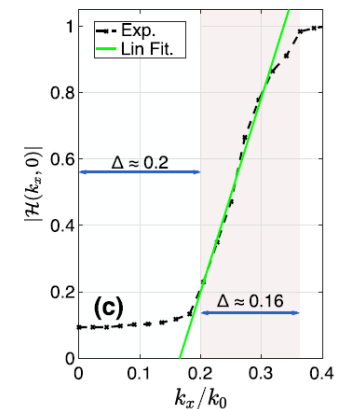
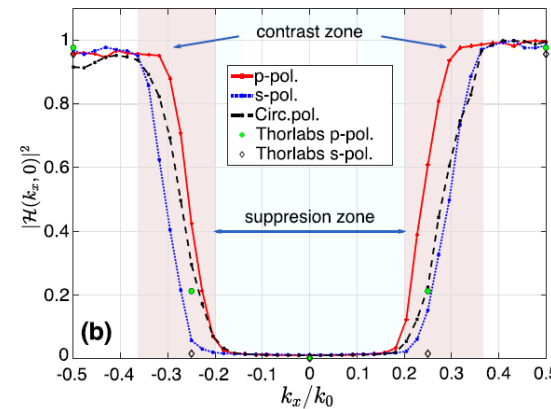
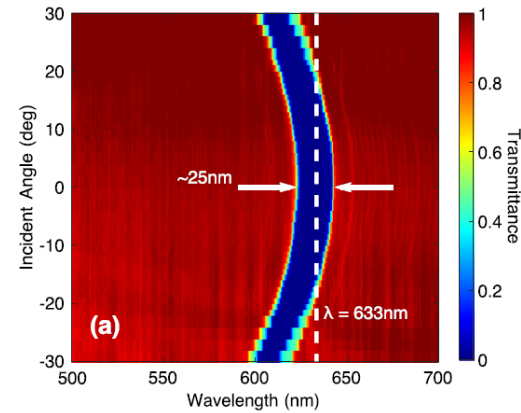
- **Compactness** → No need for a 4F system (in principle)
- **Scalability** → Multiple operations could be cascaded, without the need of additional optics
- **More tolerance on spatial alignment**
- More?

BULKIER APPROACHES

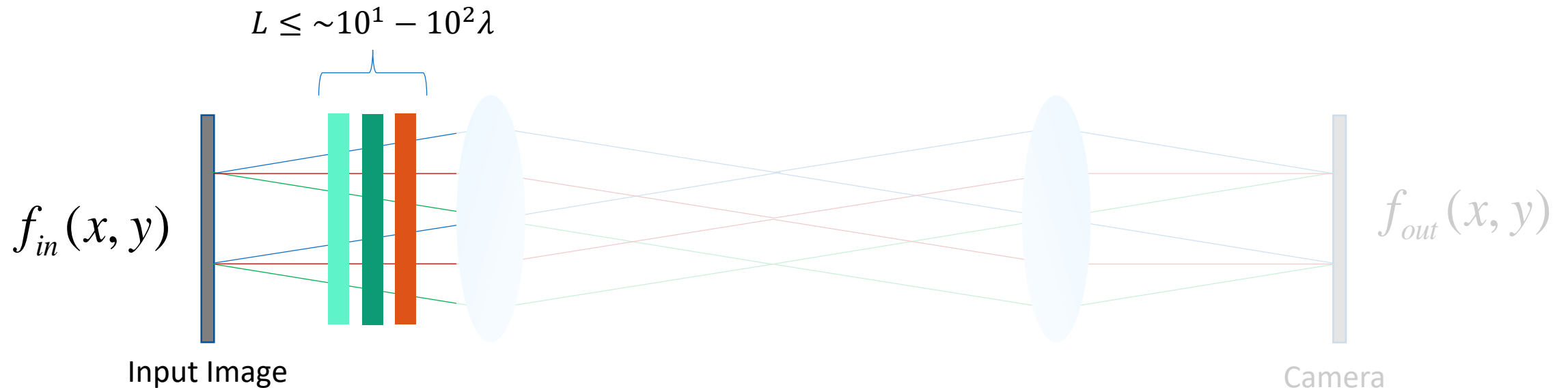
Are metasurface-based image-processing devices always worth the effort?



Commercially-available
Notch Filter



BEYOND THE HYPE



- **Compactness**
- **Scalability**
- **More tolerance on spatial alignment**

No free lunch in the universe:

- Many trade-offs between crucial figures of merit
- (so far) Limited set of operations demonstrated
- Limited reconfigurability

OUTLINE

1. Introduction

- Why do we need analog image processing?
- How can metamaterials and metasurfaces perform image processing?

2. Spatial Image Processing: State of the art and Main challenges

- What are the different approaches used?
- Which figures of merit we need to improve to go from proof-of-principles to useful devices?
- How to overcome the need for coherent illumination?

3. What's next?

- Spatio-temporal image processing
- More complex mathematical operations
- Reconfigurable devices

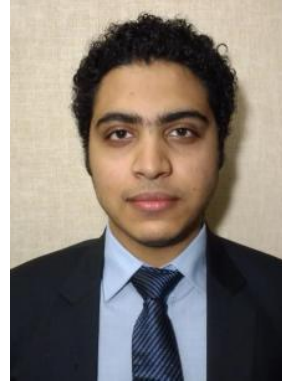
4. (Open) Discussion

- Beyond the hype: What are (if any) the real benefits of metasurfaces in image processing?
- Are metasurface-based image-processing devices always worth the effort?

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