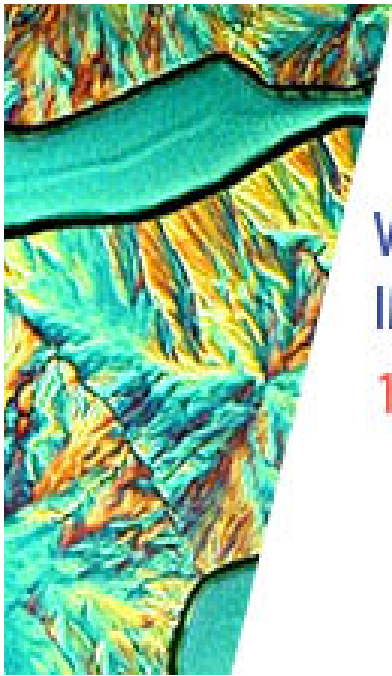


The OSA NonImaging Optical Design Technical Group Welcomes You



WHAT IS ETENDUE, AND WHY IS IT
IMPORTANT?

17 July 2019 • 12:00 EDT

OSA NonImaging
Optical Design
Technical Group

Technical Group Leadership 2019



Maryna L. Meretska
Chair



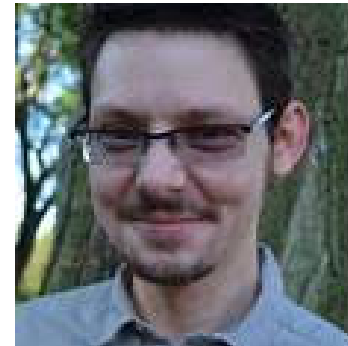
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Vice Chair



Furkan E. Sahin
Webinar Officer



Thien-An Nguyen
Event Officer



Richard J. Williams
Social Media Officer

Technical Group at a Glance

- **Focus**

- Design and characterization of illumination systems using modeling techniques.
- Non-sequential design techniques, including both software and tailoring methods provide the tools to design efficient optical components that provide the desired distribution at the target.
- Typical applications include solar energy, lighting, and displays.

- **Mission**

- To benefit *YOU* and to strengthen *OUR* community
- Webinars, podcasts, publications, technical events, business events, outreach
- Interested in presenting your research? Have ideas for TG events? Contact us at TGactivities@osa.org.

- **Find us here**

- Website: https://www.osa.org/en-us/get_involved/technical_groups/fdi/nonimaging_optical_design/
- Facebook: <https://www.facebook.com/groups/OSAnonimagingopticaldesign/>
- LinkedIn: <https://www.linkedin.com/groups/4766842/>

Today's Webinar



What is etendue, and why is it important?

Julius Muschaweck

CEO, JMO GmbH

julius@jmoptics.de

Speaker's Short Bio:

Julius Muschaweck, a German physicist, has been working on optical design for illumination for over twenty years. After a stay as Visiting Scholar at the University of Chicago with Prof. Roland Winston (well known as the originator of Nonimaging Optics), he was co-founder and CEO of OEC, an optical engineering service which pioneered freeform optics. Later, at OSRAM, where he held the position of Senior Principal Key Expert (the highest rank in the OSRAM/Siemens expert career), he coordinated the over 100 optical designers within OSRAM world-wide. He then joined ARRI, the leading movie camera and lamp head maker, as Principal Optical Scientist. Julius Muschaweck now works as an independent consultant, providing illumination optics solutions to industry clients, teaching courses on illumination optics, and writing about the subject.



Étendue

What is it? And why is it so useful?


Julius Muschaweck

OSA Webinar, July 17th, 2019

What is étendue?

A French word:

étendue

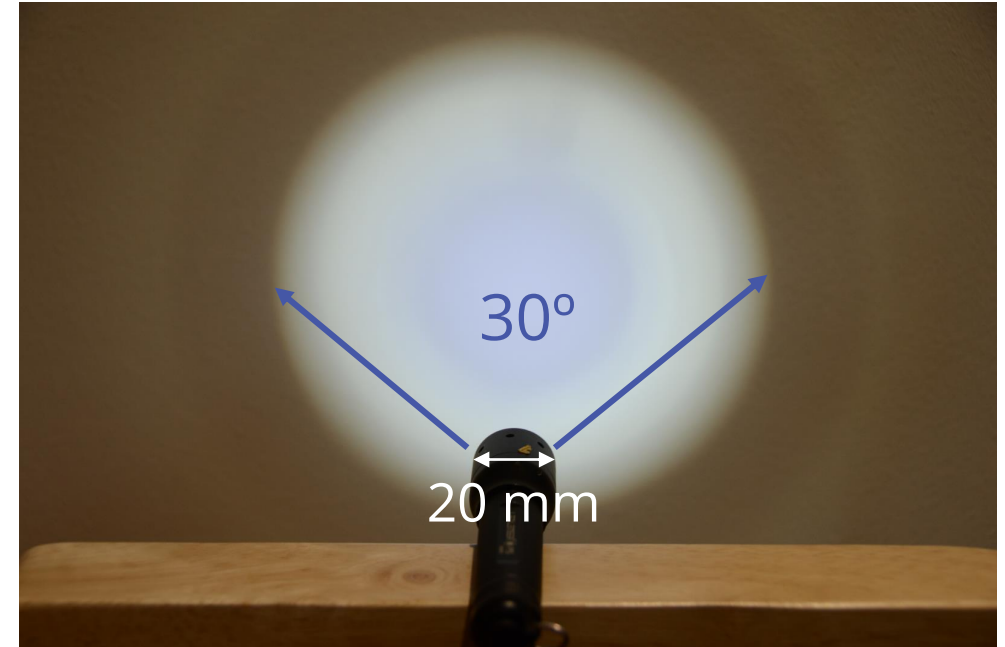
[etãdy ]

FEMININE NOUN

1. *[d'eau, sable]* stretch ♦ **expanse**
2. *[de problème]* **extent**

What is étendue?

- A purely geometric quantity
- The expanse, extent of a beam of light
- „Large“ beam \Leftrightarrow large cross section area
 \Leftrightarrow large angular spread
- Étendue = something like (area \times solid angle)

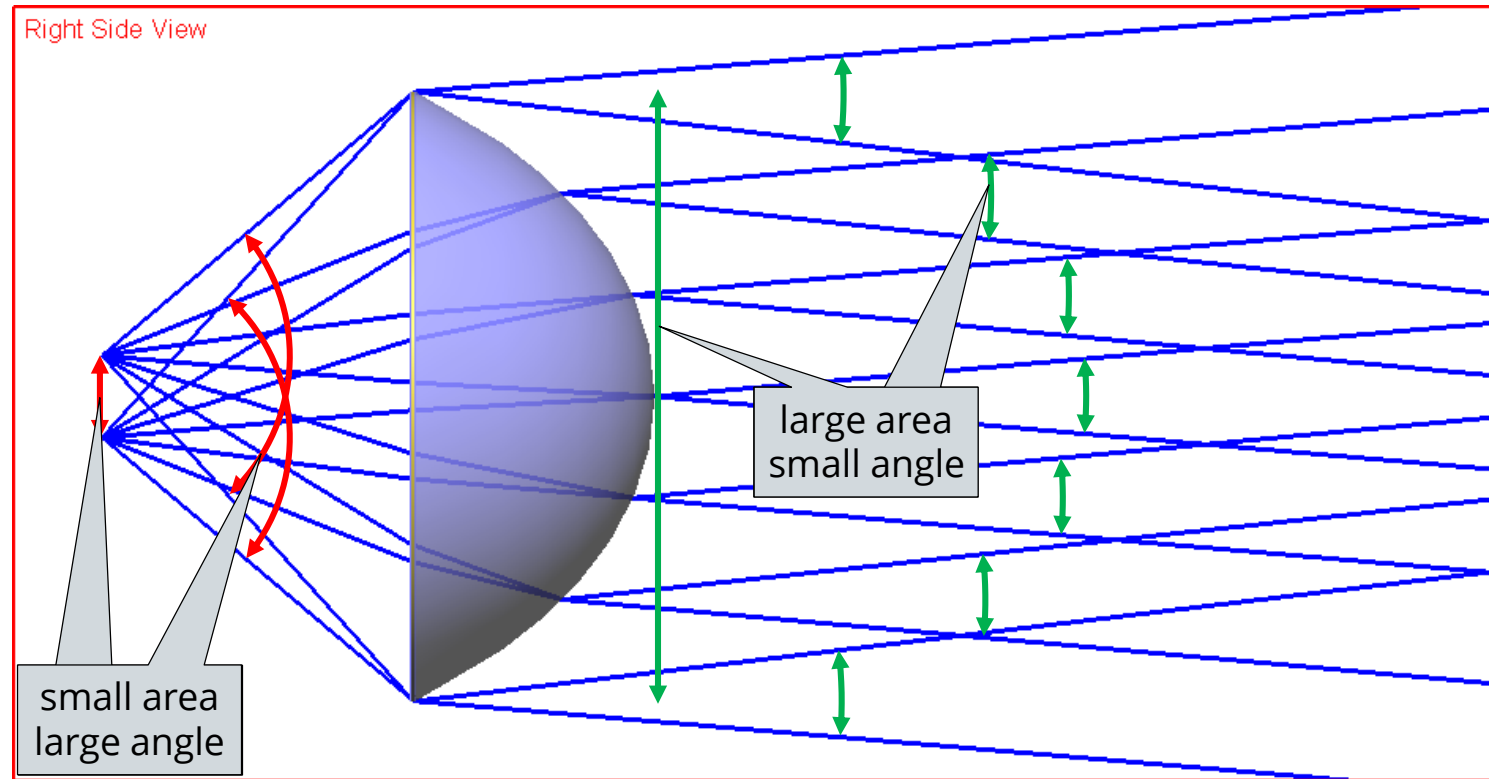


What is special about étendue?

„Étendue is conserved“

That's what some people say.

And it's true, in a sense...



A riddle

Xenon flash tube



cylinder surface area = 1320 mm²
beam angle $\pm 90^\circ$

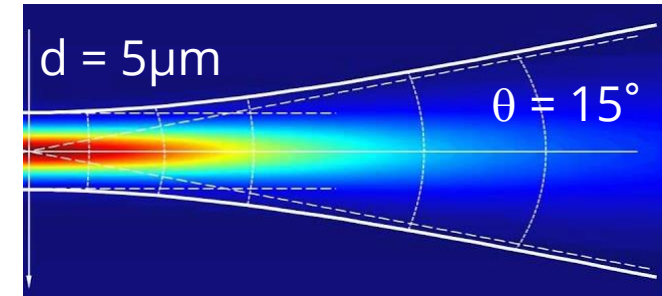
Lenses, mirrors,
prisms, beam splitters



+

=

Narrow (Gaussian) beam
Optical efficiency > 20%



area = 0.00002 mm²
beam angle $\pm 7.5^\circ$



A riddle

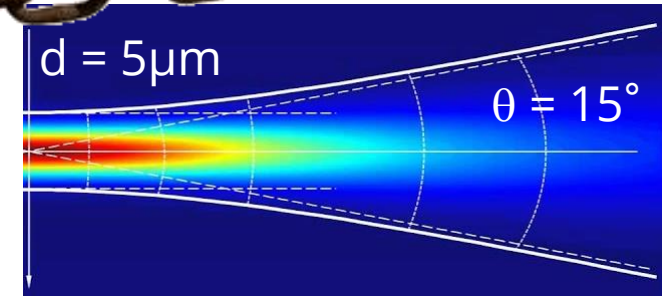


cylinder surface area = 1320 mm²
beam angle $\pm 90^\circ$

Lenses, mirrors,
prisms, beam splitters



Narrow (Gaussian beam)
Optical efficiency $\approx 20\%$



area = 0.00002 mm²
beam angle $\pm 7.5^\circ$

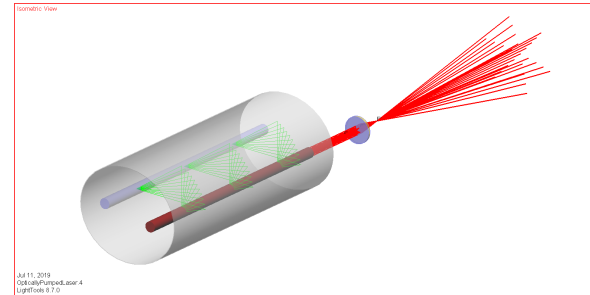
A riddle

Xenon flash tube

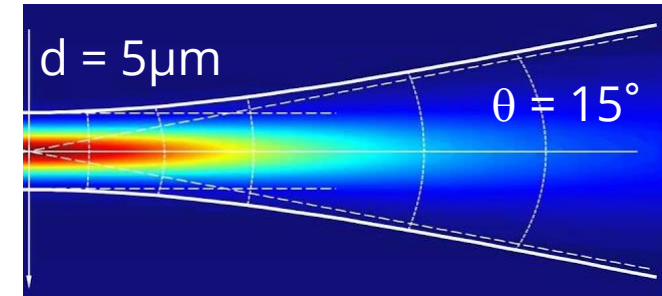


cylinder surface area = 1320 mm²
beam angle $\pm 90^\circ$

Elliptical mirror,
Nd-YAG rod, lens

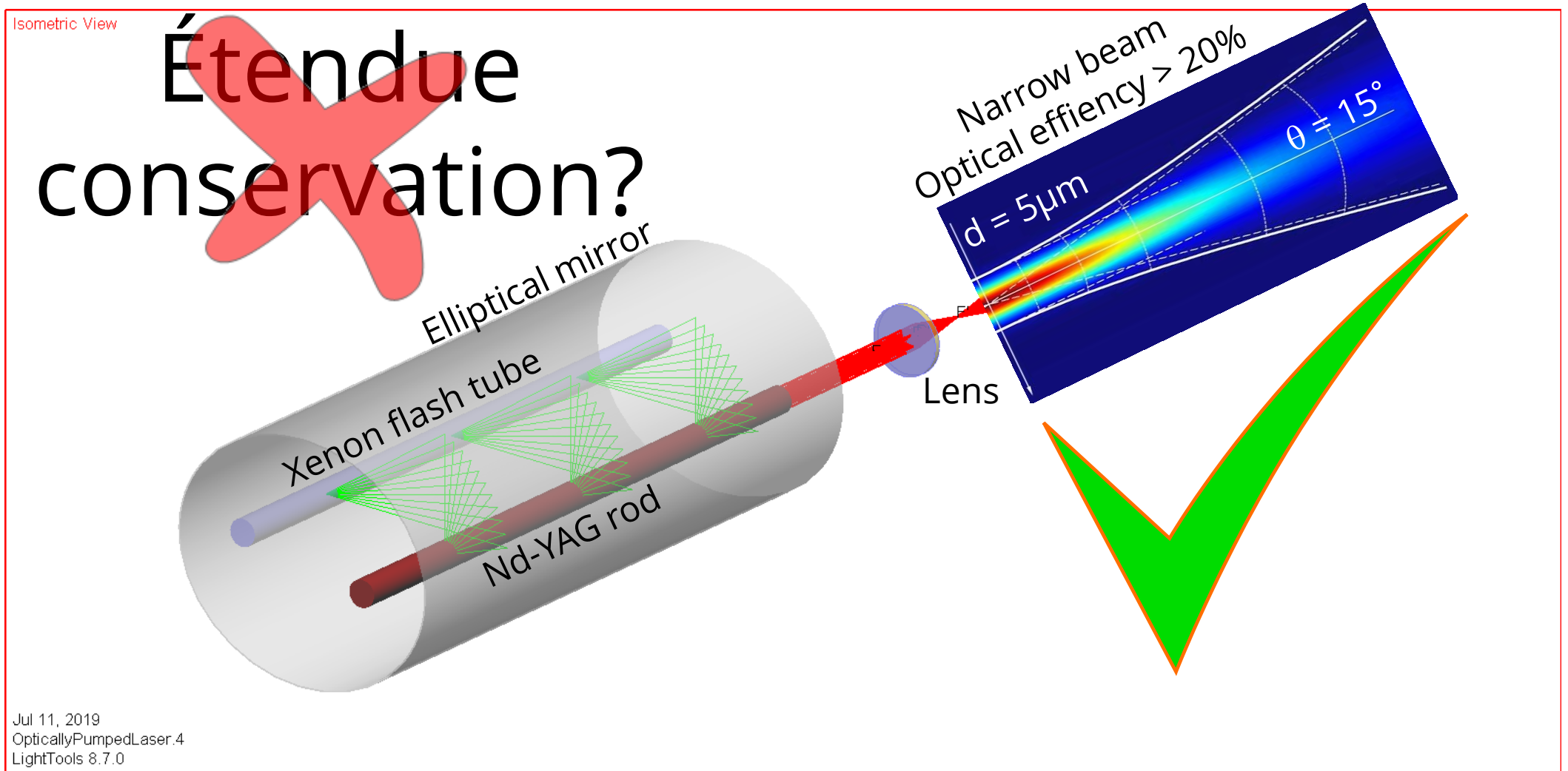


Narrow beam
Optical efficiency > 20%



area = 0.00002 mm²
beam angle $\pm 7.5^\circ$



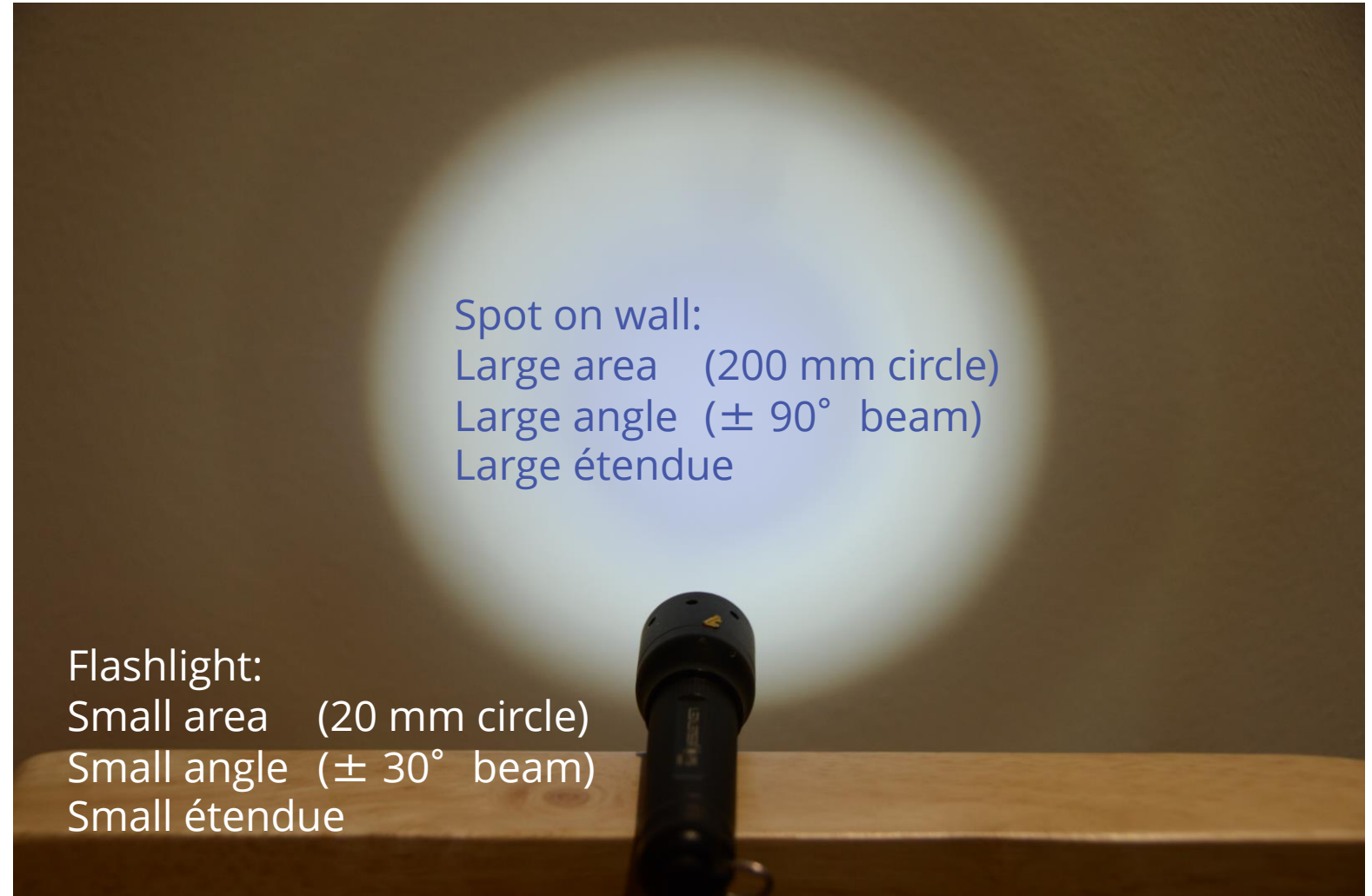


Jul 11, 2019
OpticallyPumpedLaser.4
LightTools 8.7.0

Another riddle

Just a flashlight and a wall

Étendue
conservation?



A third riddle

At X-Prism:

Three sides input (R,G,B)

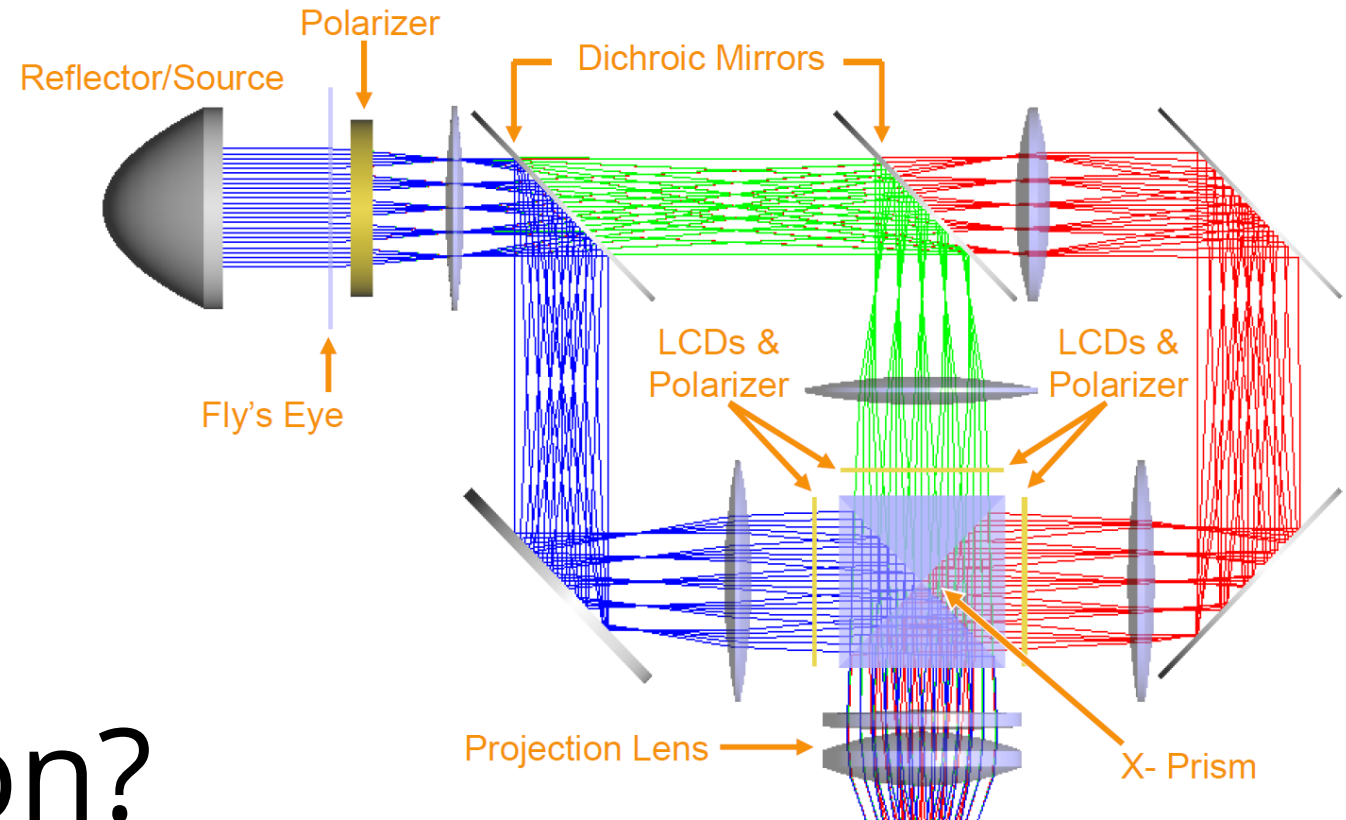
One side output (white)

All four areas equal

All beam

Étendue

~~Étendue~~
conservation?



So what's the story about étendue?



Ray coordinates: Starting point

Starting point in space:

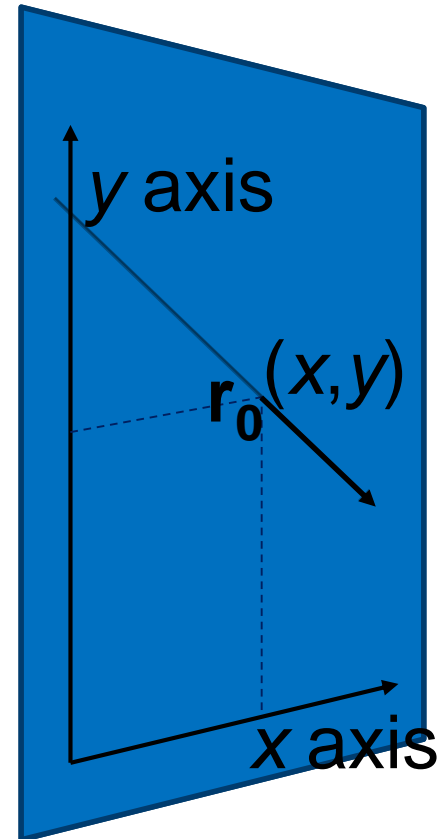
Global coordinates

Three numbers: $\mathbf{r}_0 = (x_{g'}, y_{g'}, z_{g'})$

Starting point on screen:

Local surface coordinates

Two numbers (x, y)



Ray coordinates: Starting point

Starting point in space:

Global coordinates

Three numbers: $r_0 = (x, y, z)$

Starting point on surface:

Local surface coordinates

Two numbers (x, y)

For location:
Two numbers,

x, y



Ray coordinates: Direction vector

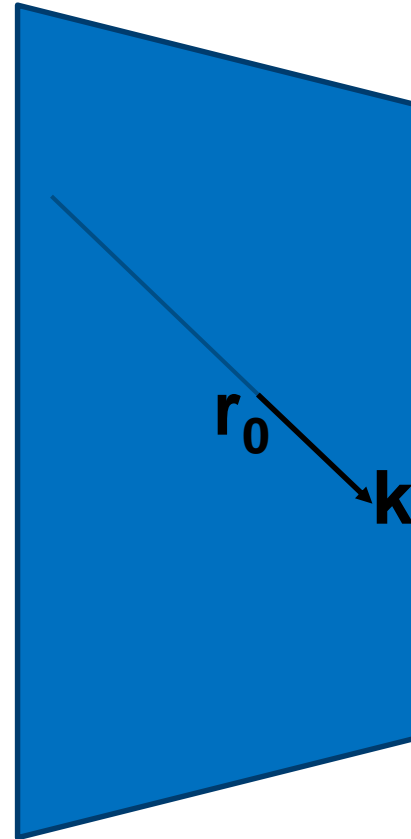
Direction vector in space:

Global coordinates

Three numbers: $\mathbf{k} = (k_x, k_y, k_z)$

Two should suffice!

But which two?



Normalized direction vector, local surface coordinates

Normalization by refractive index:

$|\mathbf{k}| = n$ in material $\Rightarrow |\mathbf{k}| = 1$ in vacuum

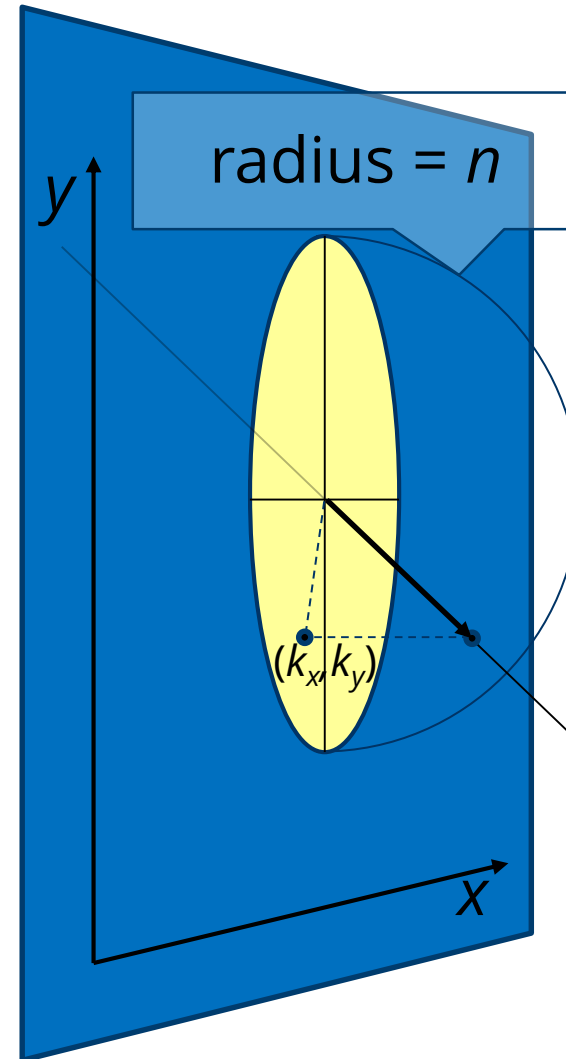
Local surface coordinates:

$k_x \parallel x$ $k_y \parallel y$ $k_z \parallel z$

No need for $k_z = \pm \sqrt{n^2 - k_x^2 - k_y^2}$

with **oriented** surface ($k_z > 0$)

k_x, k_y sufficient!



Normalization:

$|\mathbf{k}| = 1$ in vacuum $\Rightarrow |\mathbf{k}| = n$ in material

Local surface coordinates:

$k_x \parallel x$ $k_x \parallel y$ $k_z \parallel z$

No need for $k_z = \pm \sqrt{n^2 - k_x^2 - k_y^2}$

with oriented surface

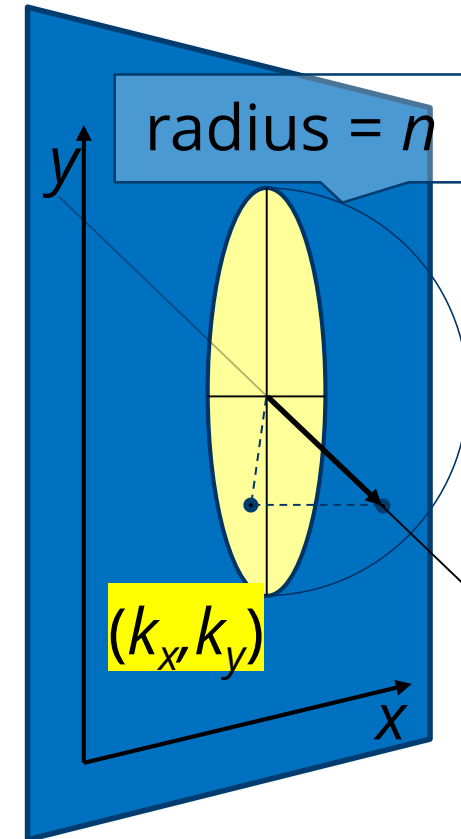
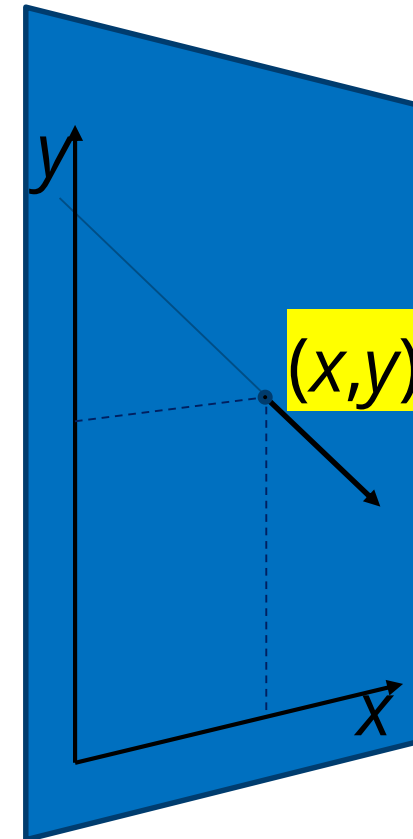
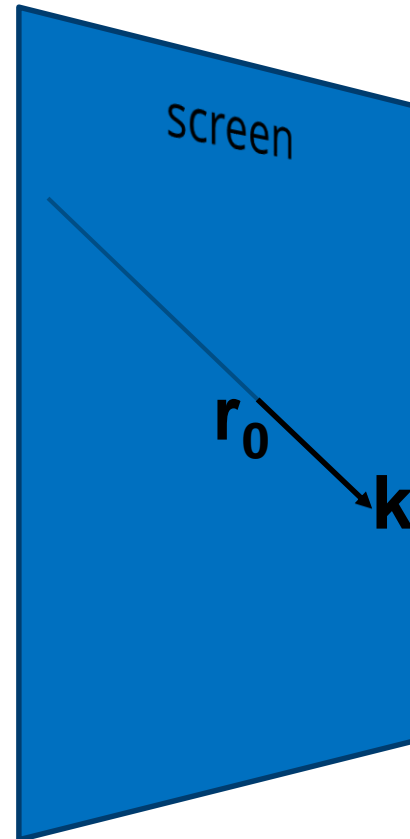
$\Rightarrow k_x, k_y$ sufficient

For direction: Two numbers,

k_x, k_y

From 3D ray to 4D ray coordinates

1. Select screen
2. Define x-y coordinate system
3. Use (x,y) of ray intersection as location coordinates
4. Attach tangent hemisphere, radius n
5. Define k vector,
 $k = (k_x, k_y, k_z)$, $|k| = n$
 by intersecting hemisphere
6. Obtain (k_x, k_y) by projection,
 use as direction coordinates
7. Voilà: Ray coordinates: (x, y, k_x, k_y)



From 3D ray to 4D ray coordinates

1. Select screen
2. Define x-y coordinate system
3. Use (x, y) of ray intersection as location coordinates
4. Attach tangent disk, radius n
5. Define k vector, $k = (k_x, k_y, k_z)$, by intersecting hemisphere
6. Use (k_x, k_y) by projection as direction coordinate
7. Voilà: Ray coordinates: (x, y, k_x, k_y)

Ray coordinates on a certain screen:

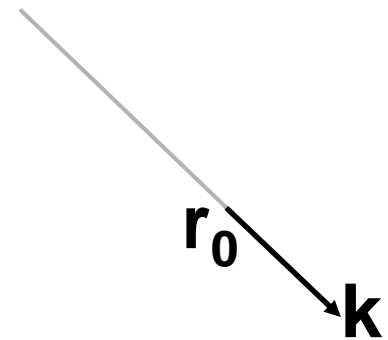
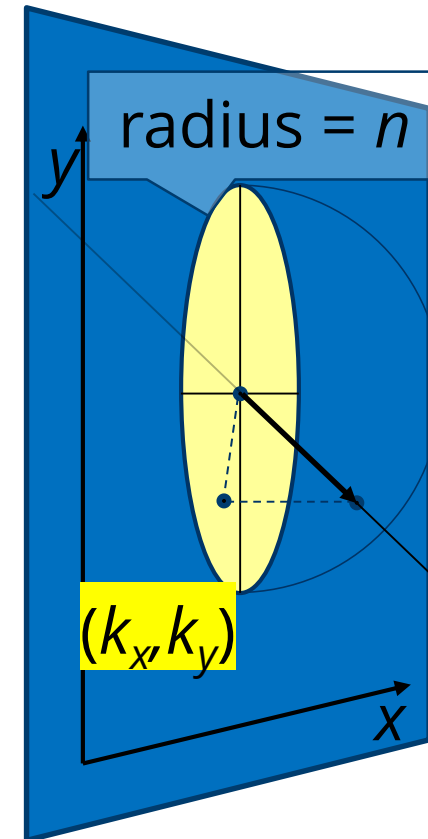
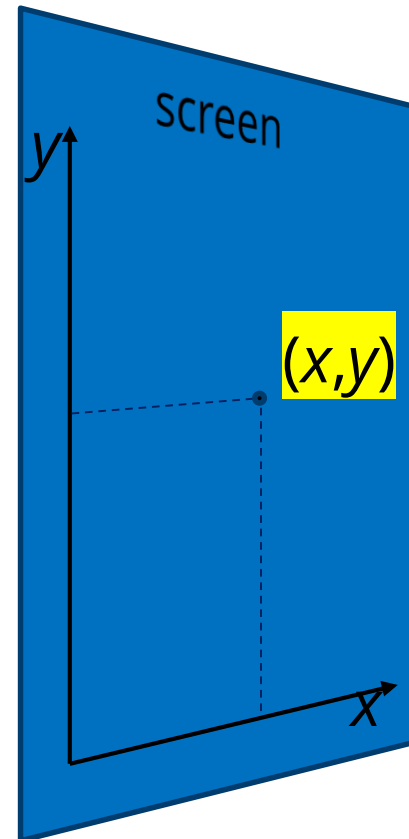
$$(x, y, k_x, k_y)$$



From 4D ray coordinates to 3D ray

1. A ray is given by a screen and ray coordinates (x, y, k_x, k_y)
2. Determine starting point \mathbf{r}_0 from surface geometry, coordinate system and (x, y)
3. Attach tangent disk at \mathbf{r}_0 , radius= n
4. Find point on disk with (k_x, k_y)
5. Raise this point up to hemisphere to find \mathbf{k}
6. 3D Ray:

$$\mathbf{r} = \mathbf{r}_0 + \mu \mathbf{k} \quad (\mu \in \mathbb{R}, \mu \geq 0)$$



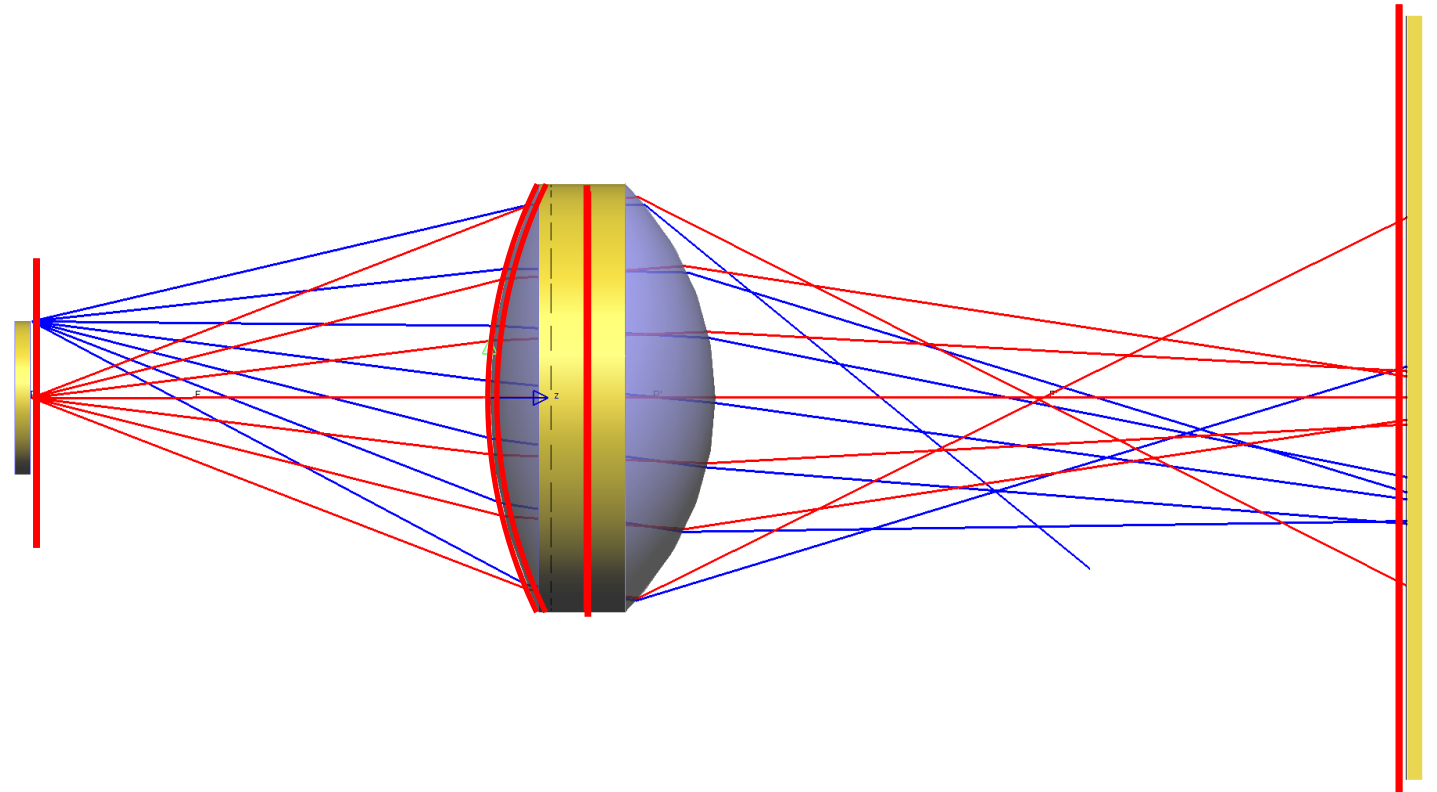
A closer look at screens

Screen \neq optical surface (!!)

Choose freely, choose wisely

As many as you like

Not necessarily planar



Nov 17, 2018
RayOptics 1
LightTools 9.6.0

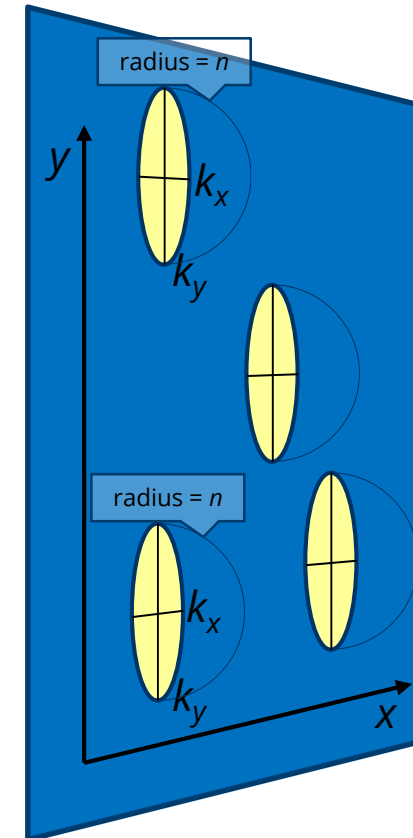
What is phase space?

- Choose screen
- Define coordinate system for x, y, k_x, k_y
- „Allowed“ values:
 x, y such that (x,y) within surface boundary
 k_x, k_y such that $\sqrt{k_x^2 + k_y^2} < n$ i.e. within disk

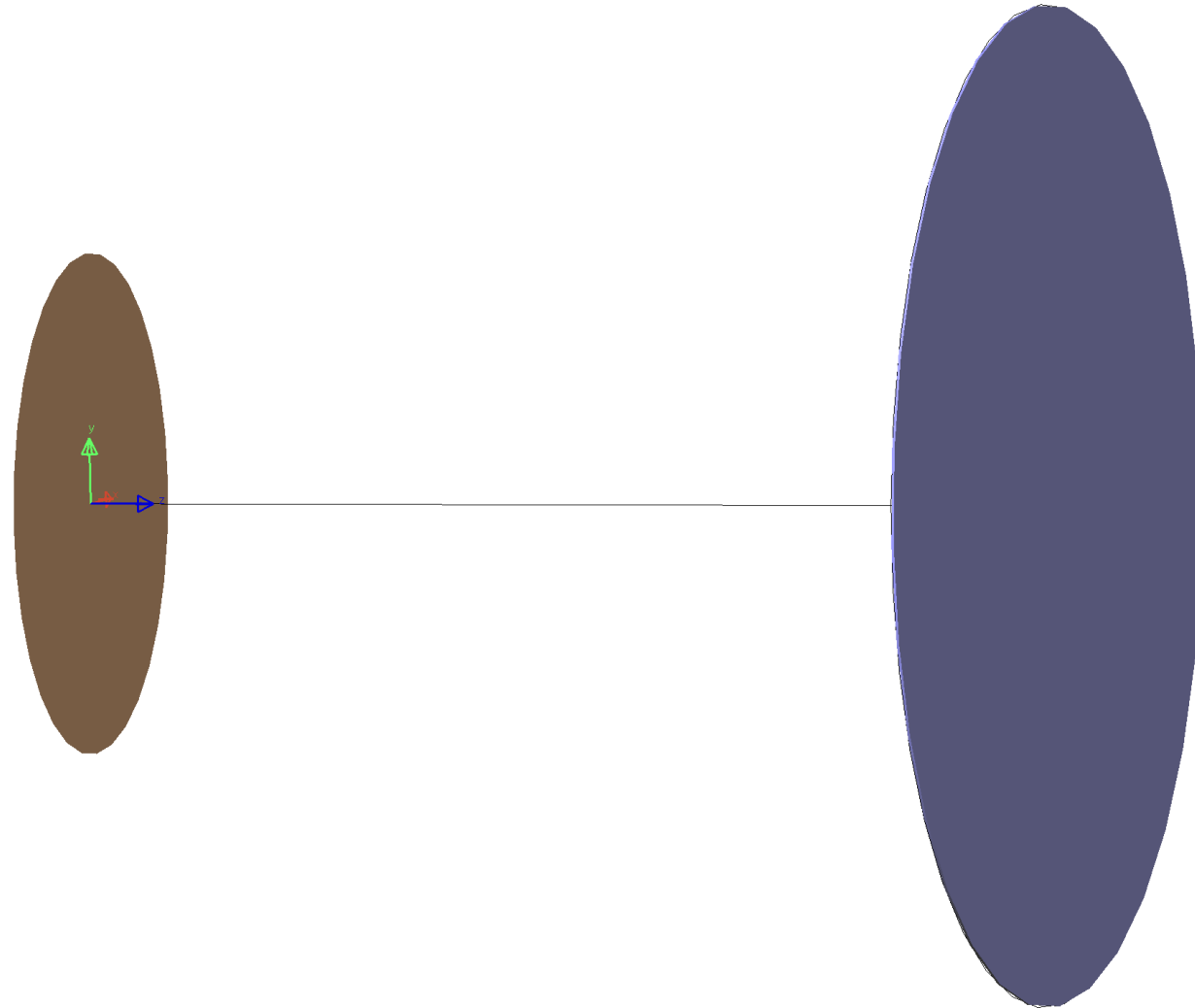
All allowed (x, y, k_x, k_y) naturally form a 4D space

Each allowed (x, y, k_x, k_y) corresponds to a 3D ray

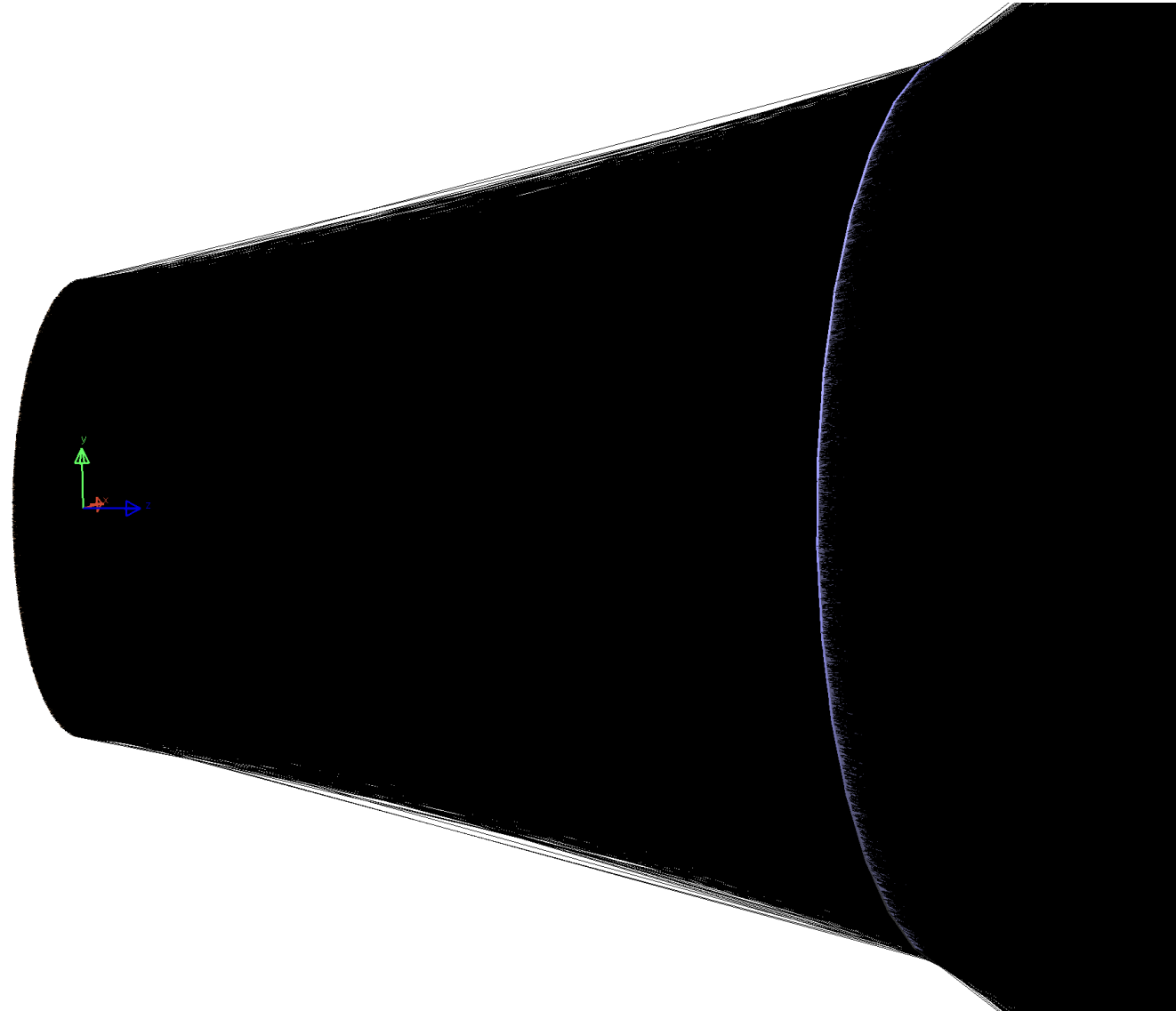
3D rays are points in 4D phase space



3D space: pretty crowded

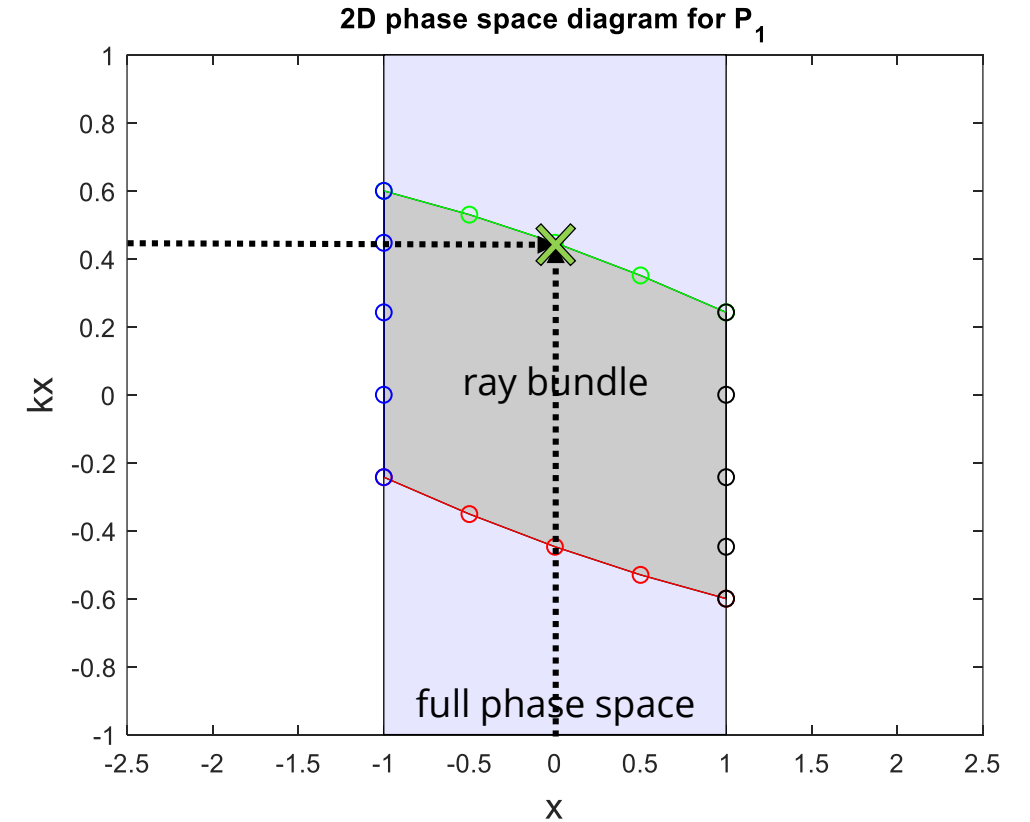
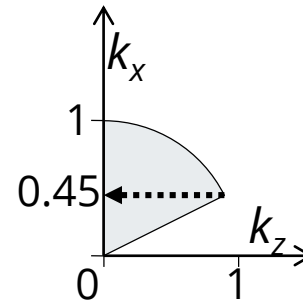
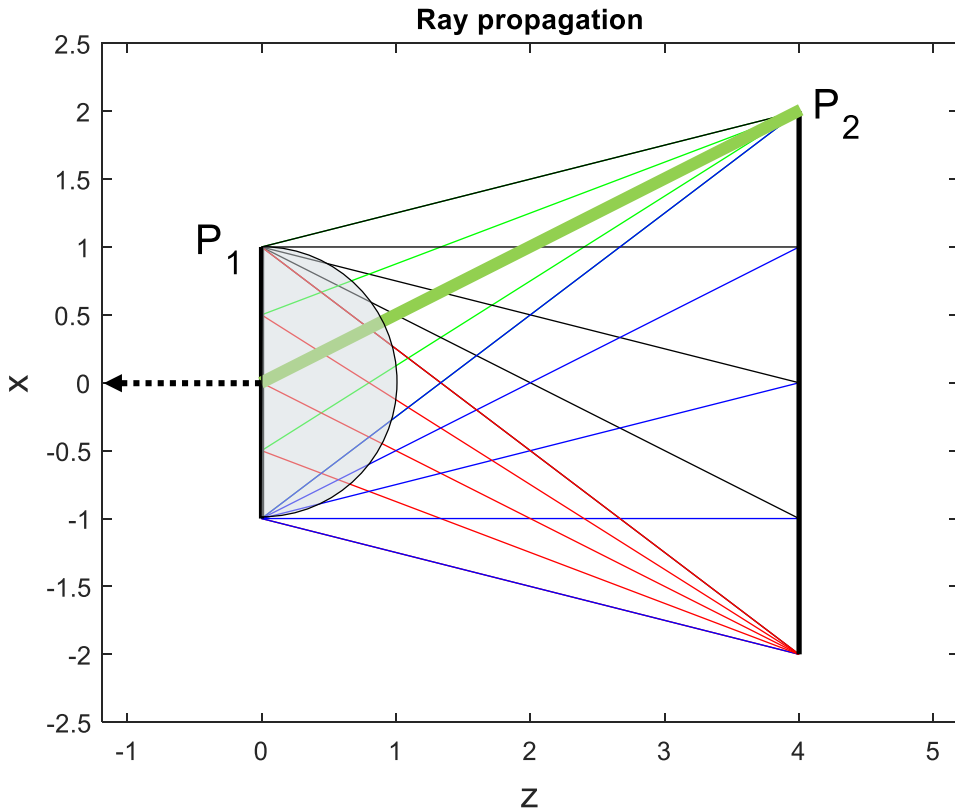


3D space: pretty crowded



Jul 16, 2019
Crowded3D 2
LightTools 8.7.0

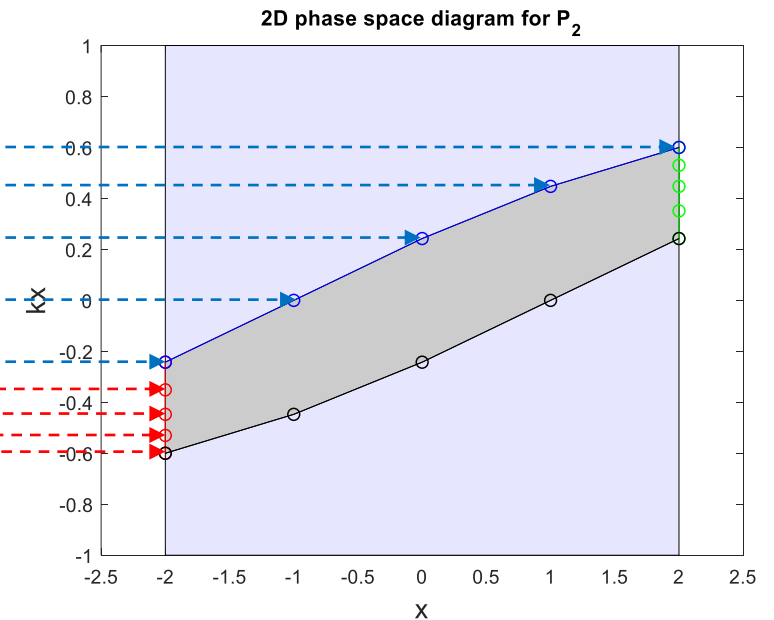
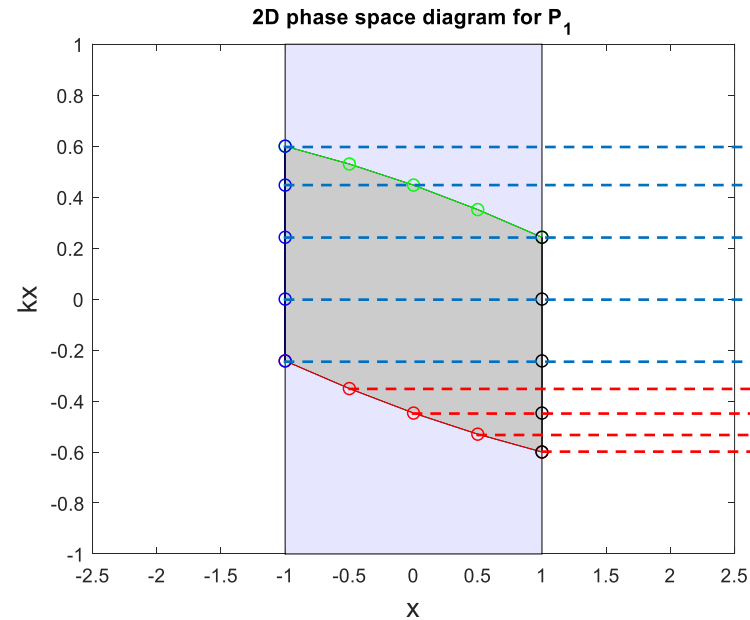
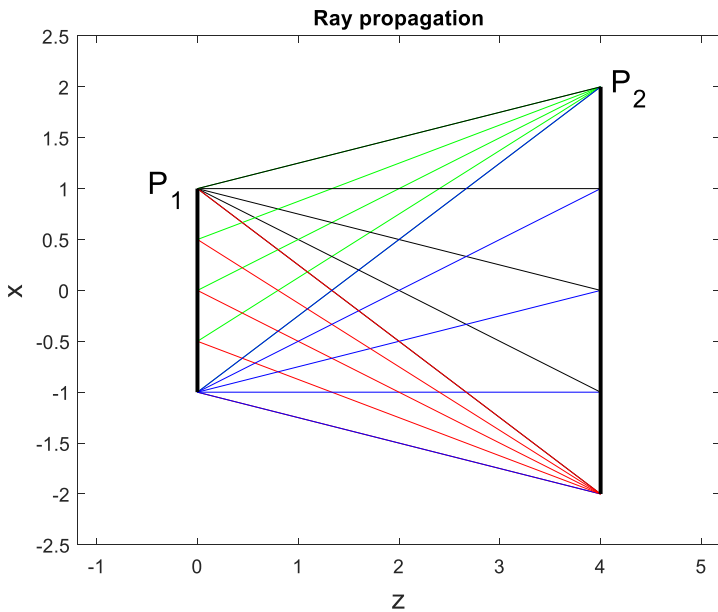
Visualizing 4D: 2D phase space diagrams



Ray bundles: Nonzero volume regions of phase space

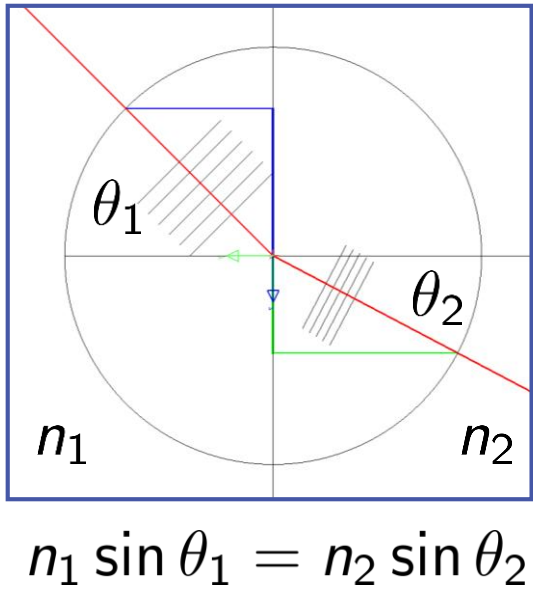
2D phase space diagrams: propagation

Free propagation in 3D = **shear** in 2D / 4D

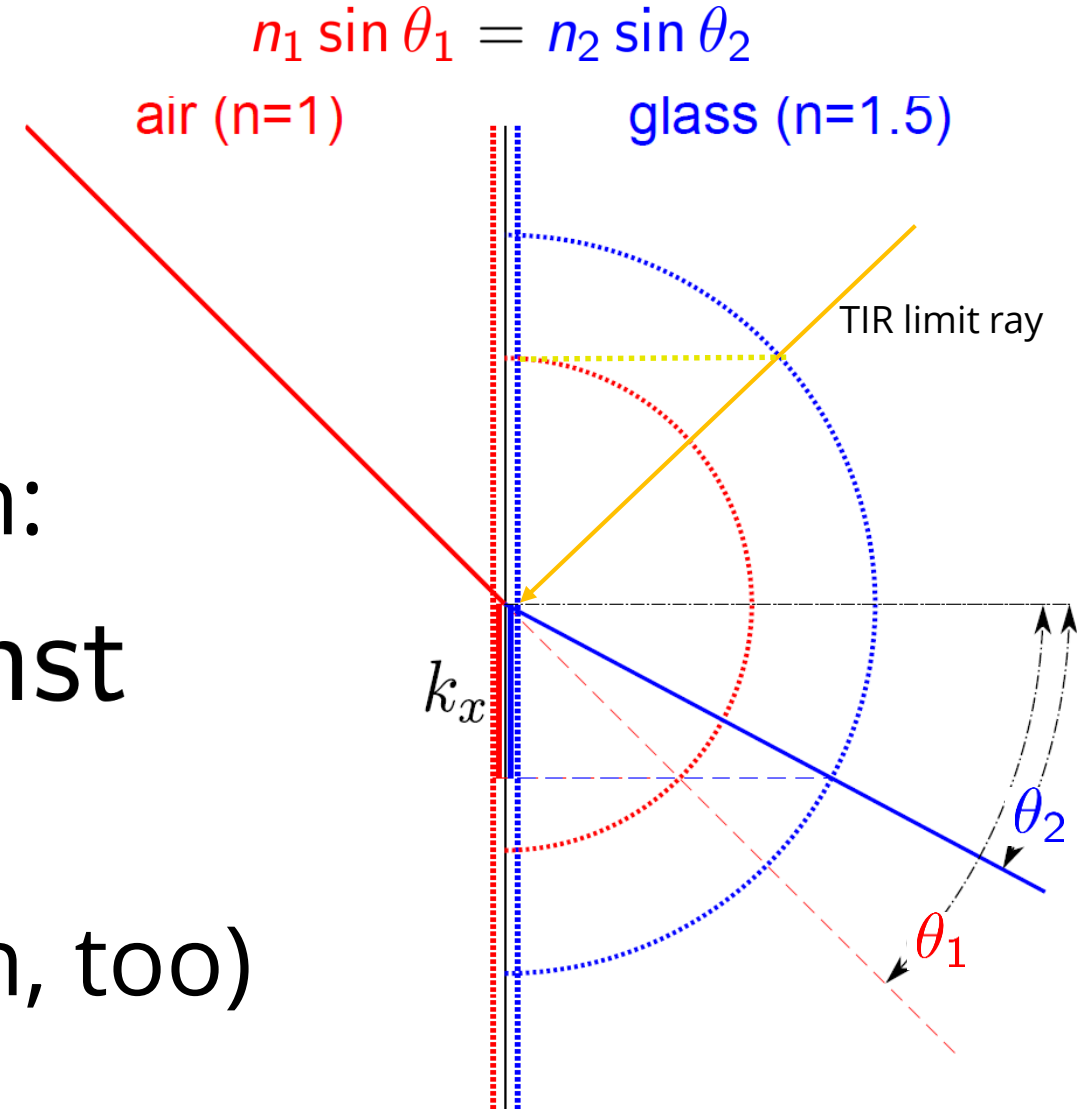


2D area: conserved under free propagation

Refraction in phase space



Under refraction:
 $(k_x, k_y) = \text{const}$
 (under reflection, too)

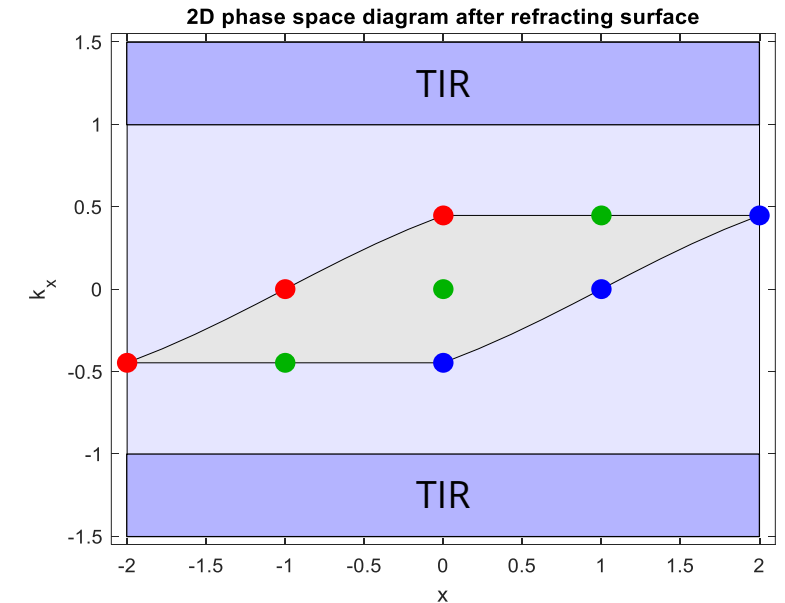
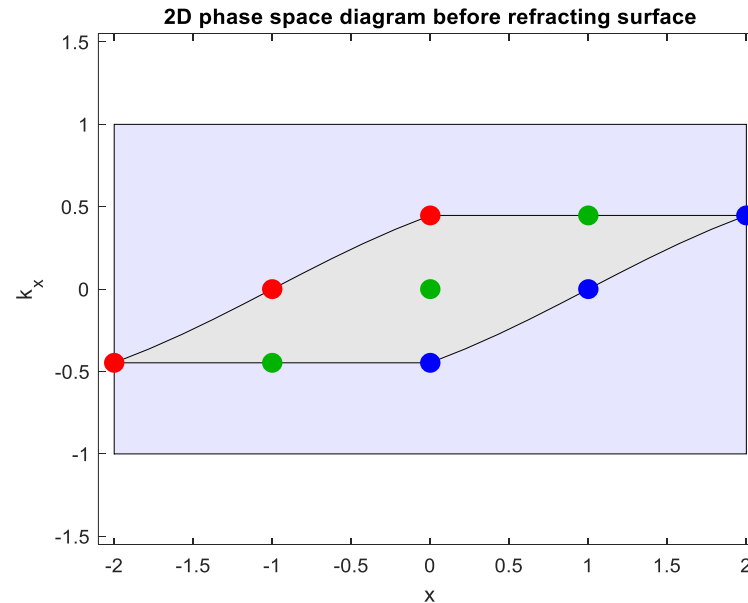
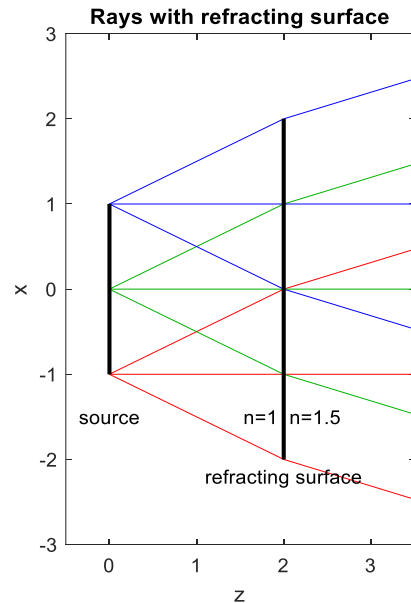


Refraction: 2D phase space diagram

No change of ray coordinates in phase space \Rightarrow identical ray bundles

Ray directions change, k_x values change not!

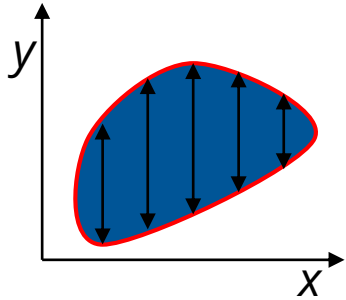
Total phase space volume changes, ray bundle volume changes not!



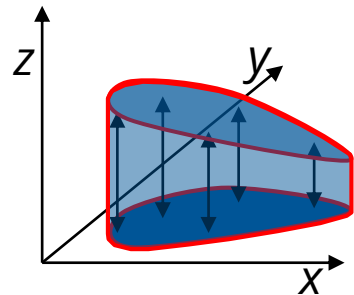
Volumes in 1D, 2D, 3D, ...



$$V_{1D} = \text{path length} = \int dl$$

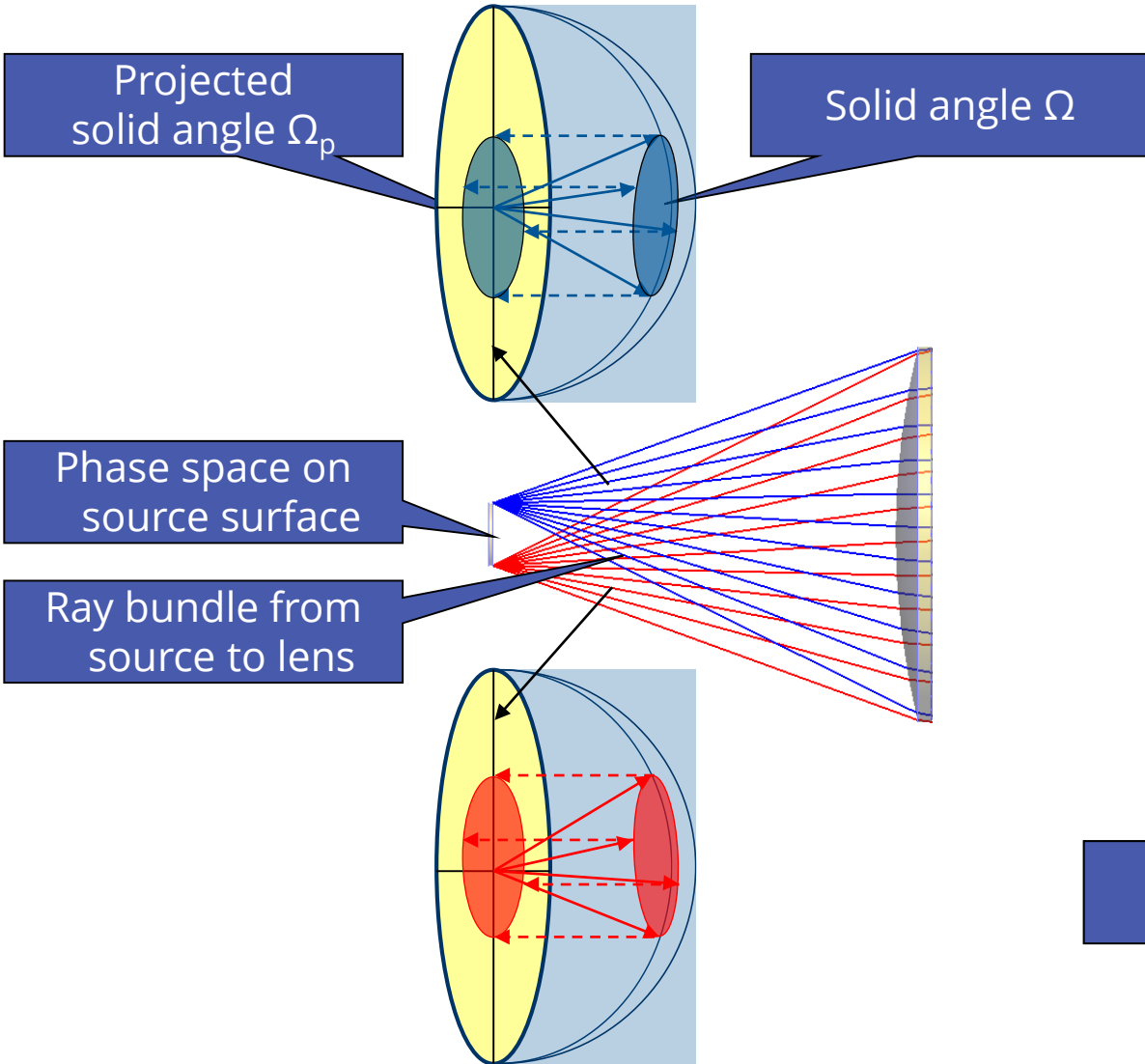


$$V_{2D} = \text{area} = \iint dA = \iint dx dy = \int h(x) dx$$

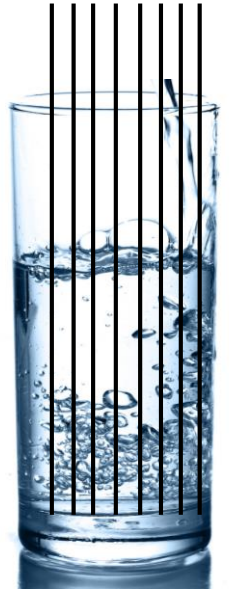
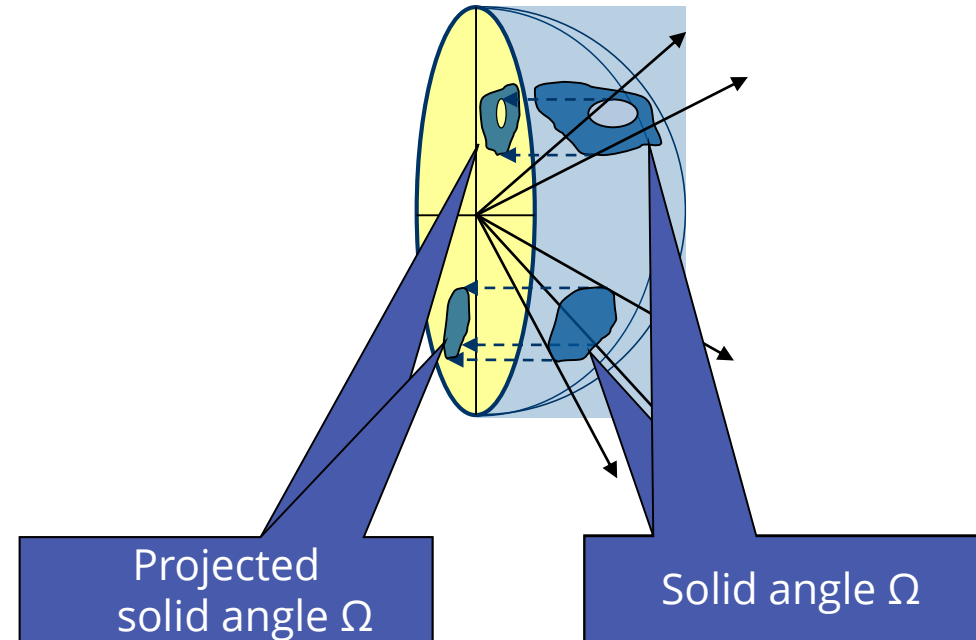


$$V_{3D} = \text{volume} = \iiint dV = \iint h(x, y) dA$$

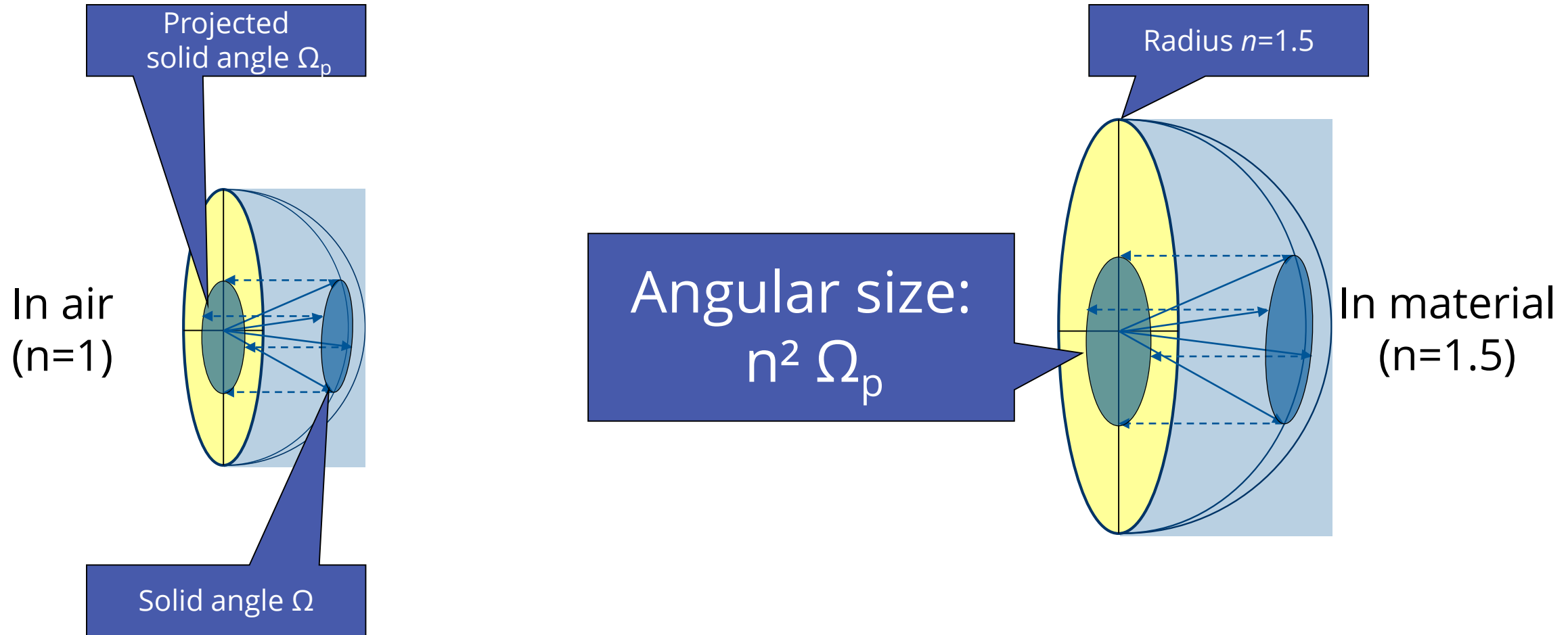
From 2D to 4D: Projected solid angle Ω_p



In general: anything



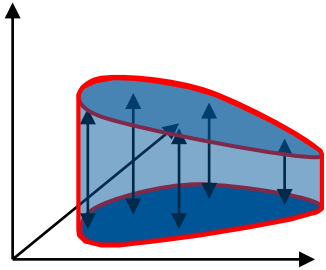
From 2D to 4D: Refractive index



Volume in 4D

Classical volume in 3D:

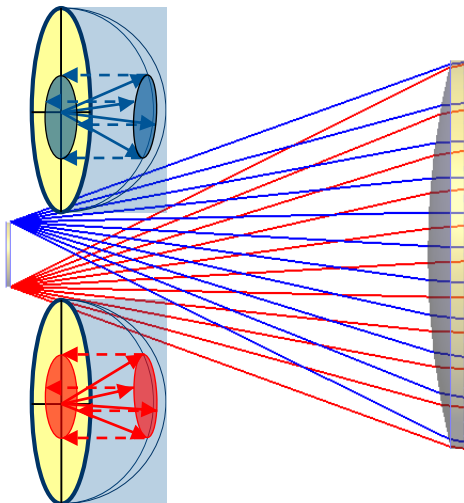
Integrate **height $h(x,y)$** over area



$$V_{3D} = \text{volume} = \iiint dV = \iint h(x, y) dA = \iiint dx dy dz$$

Phase space volume in 4D:

Integrate **angular size $n^2 \Omega_p(x,y)$** over area

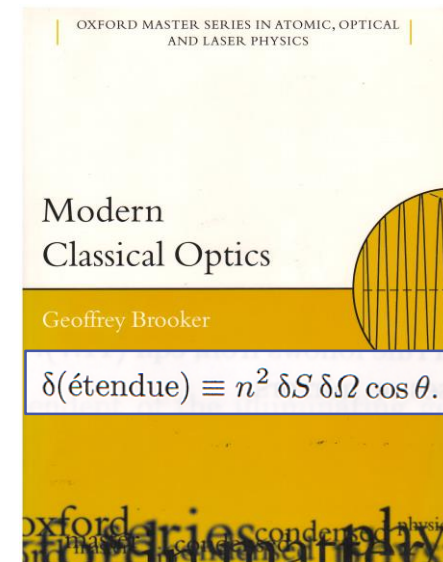
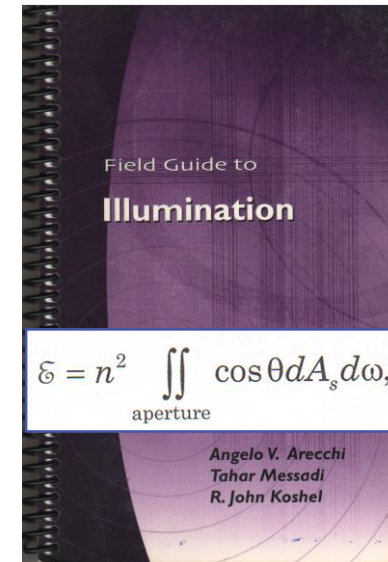
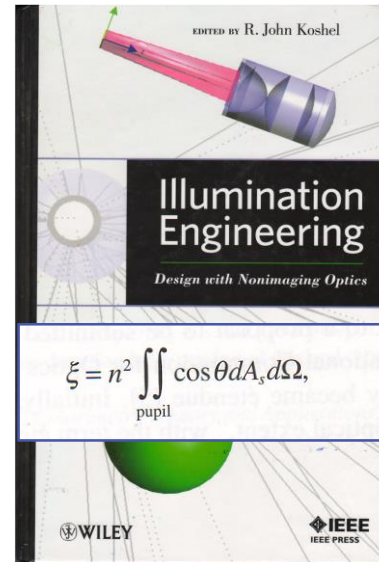
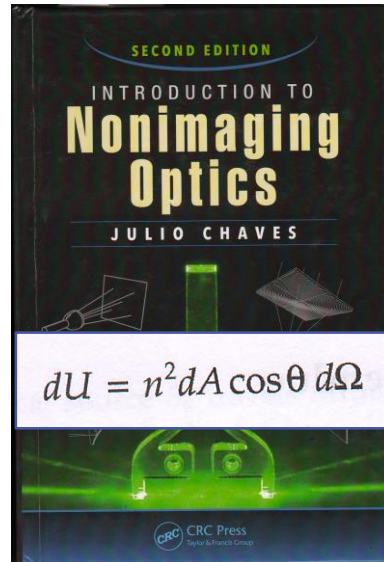
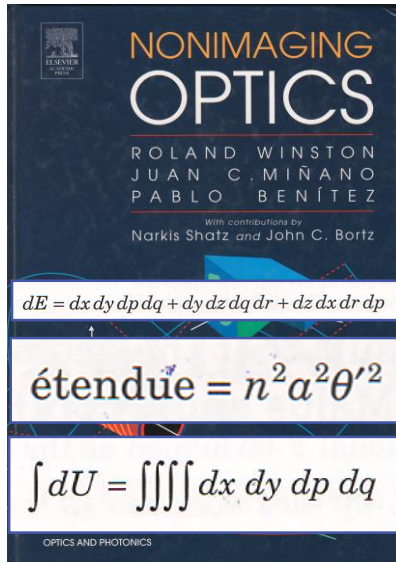
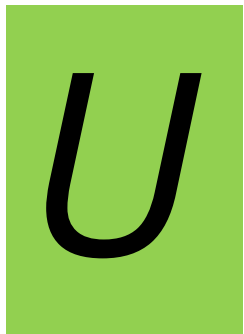


$$V_{4D} = \iiint \iiint dU = \iint n(x, y)^2 \Omega_p(x, y) dA = \iiint \iiint dx dy dk_x dk_y$$

The name of this 4D volume: Étendue

Physical units: $\text{m}^2 \text{sr}$ or $\text{mm}^2 \text{sr}$

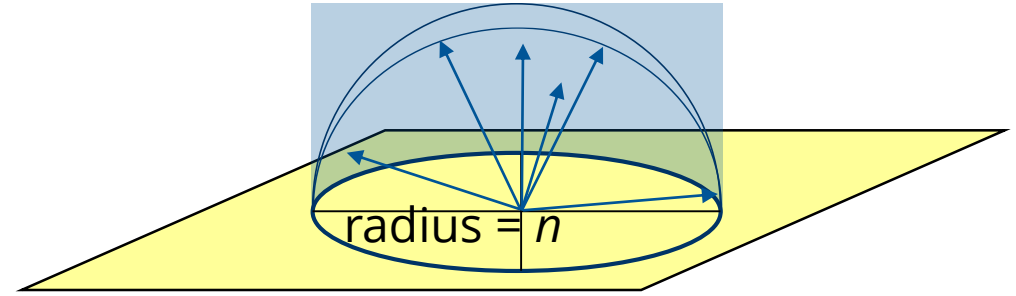
The symbol?



Étendue in simple cases: constant angular range

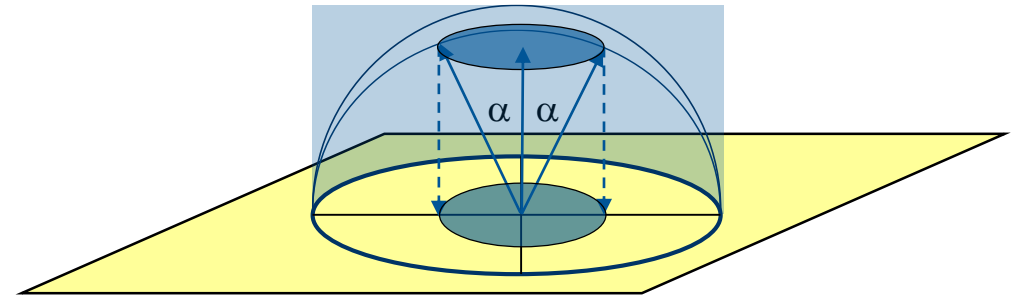
The full phase space volume
(from screen into full hemisphere)

$$U = \pi n^2 A$$



Far field collimator: From screen
into cone with half opening angle α

$$U = \pi (n \sin \alpha)^2 A$$



NB: „into cone with $\pm \alpha$ “ applies to **each screen point individually**

Example: A zoomable flashlight

Question: What LED size is ok?

- Answer:
1. Compute beam étendue (large area, small angle)
 2. Assume equal LED étendue
 3. Assume $\pm 90^\circ$ LED emission
 4. Compute LED area



Example: A zoomable flashlight: flood mode

Étendue of beam

```
d_Beam = 20; % mm
alpha_Beam = 30 * pi/180 % radians
alpha_Beam = 0.5236
```

Max. LED size:
10 mm circle

```
A_Beam = (d_Beam/2)^2 * pi % mm^2
A_Beam = 314.1593
```

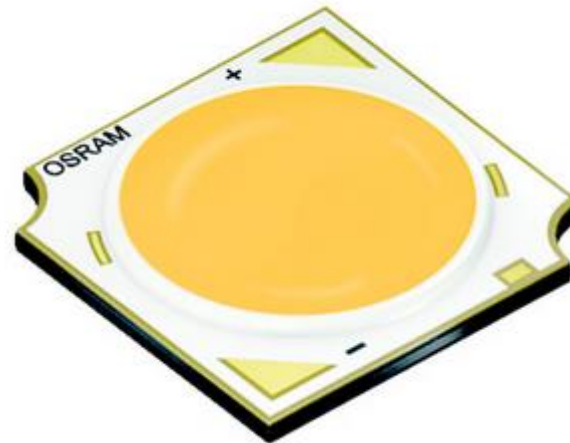
```
n_Beam = 1; % refractive index
angularRange_Beam = (n_Beam * sin(alpha_Beam))^2 * pi;
U_Beam = A_Beam * angularRange_Beam % mm^2 sr
U_Beam = 246.7401
```

Area of LED

Assume LED and beam have equal étendue

Assume LED has chip in air

```
n_LED = 1; % refractive index
angularRange_LED = n_LED^2*pi; % sr
U_LED = U_Beam;
A_LED = U_LED / angularRange_LED % mm^2
A_LED = 78.5398
```



```
d_LED = 2 * sqrt(A_LED/pi) % mm diameter of circular LED
d_LED = 10
```



Example: A zoomable flashlight: spot mode

Étendue of beam

```
d_Beam = 20; % mm
alpha_Beam = 5 * pi/180 % radians

alpha_Beam = 0.0873
```

Max. LED size:
1.55 mm square

```
A_Beam = (d_Beam/2)^2 * pi % mm^2

A_Beam = 314.1593
```

```
n_Beam = 1; % refractive index
angularRange_Beam = (n_Beam * sin(alpha_Beam))^2 * pi;
U_Beam = A_Beam * angularRange_Beam % mm^2 sr

U_Beam = 7.4971
```

Area of LED

Assume LED and beam have equal étendue

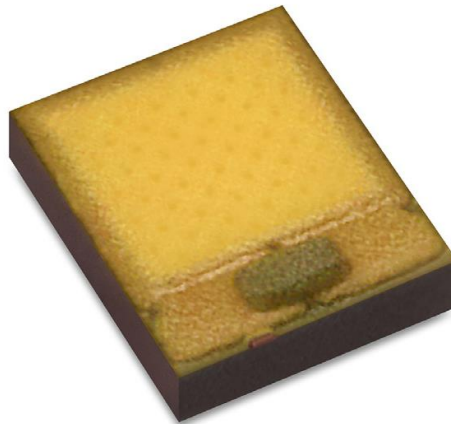
Assume LED has chip in air

```
n_LED = 1; % refractive index
angularRange_LED = n_LED^2*pi; % sr
U_LED = U_Beam;
A_LED = U_LED / angularRange_LED % mm^2
```

```
A_LED = 2.3864
```

```
d_LED = sqrt(A_LED) % mm edge length of square LED
```

```
d_LED = 1.5448
```



Flashlight:
Aperture: 20 mm circle
Beam angle: $\pm 5^\circ$

Example: A zoomable flashlight: LED with dome

Étendue of beam

```
d_Beam = 20; % mm
alpha_Beam = 5 * pi/180 % radians

alpha_Beam = 0.0873
```

```
A_Beam = (d_Beam/2)^2 * pi % mm^2
```

```
A_Beam = 314.1593
```

```
n_Beam = 1; % refractive index
angularRange_Beam = (n_Beam * sin(alpha_Beam))^2 * pi;
U_Beam = A_Beam * angularRange_Beam % mm^2 sr
```

```
U_Beam = 7.4971
```

Max. LED size:
1.1 mm square

Area of LED

Assume LED and beam have equal étendue

Assume LED has chip in silicone dome

```
n_LED = 1.41; % refractive index
angularRange_LED = n_LED^2*pi; % sr
U_LED = U_Beam;
A_LED = U_LED / angularRange_LED % mm^2
```

```
A_LED = 1.2003
```

```
d_LED = sqrt(A_LED) % mm edge length of square LED
```

```
d_LED = 1.0956
```



Flashlight:
Aperture: 20 mm circle
Beam angle: $\pm 5^\circ$

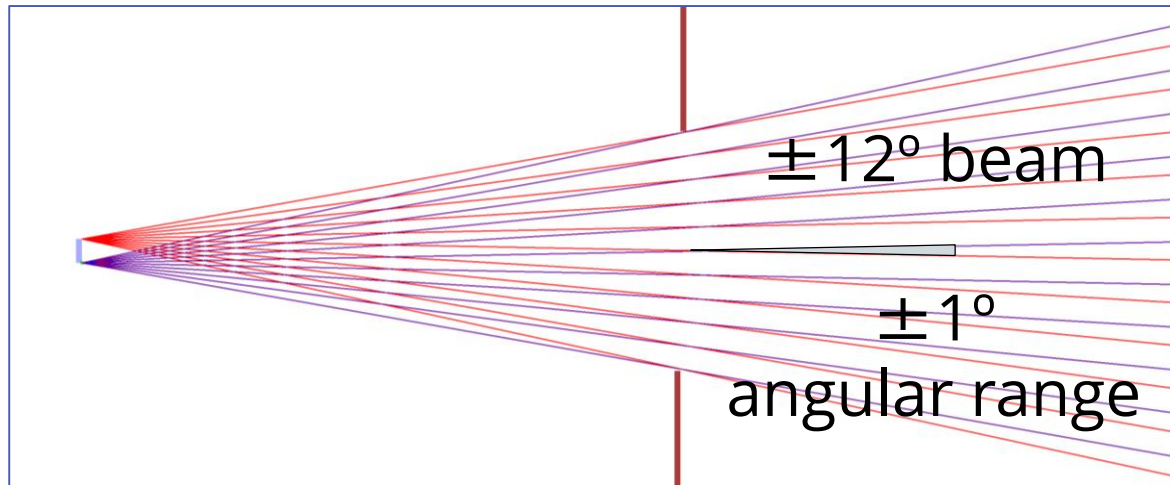


The actual LED choice

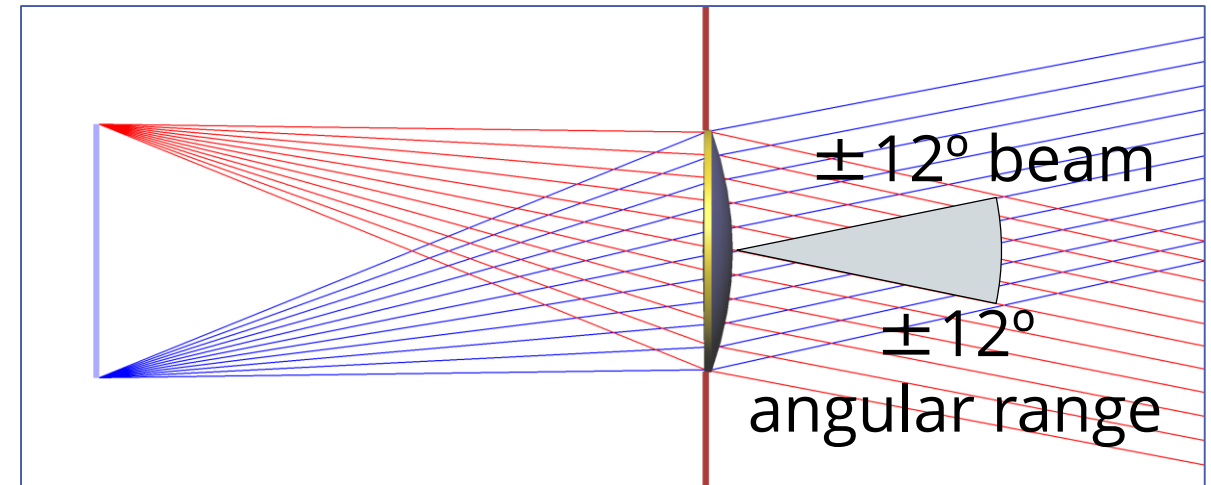


Look at angular range at each point – not overall

Small étendue

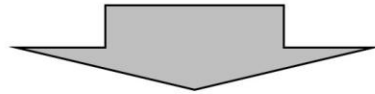


Large étendue



Spillage, match and dilution

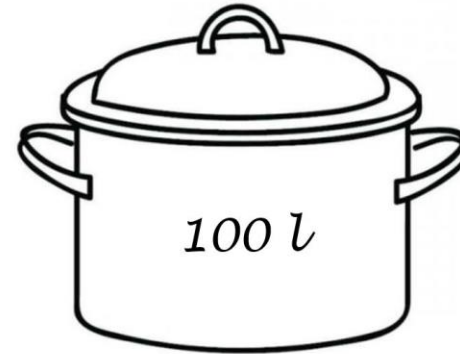
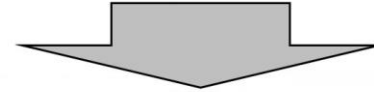
Source



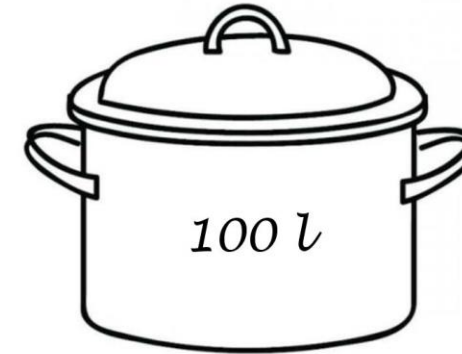
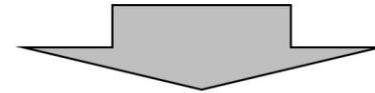
Target



Spillage



Match



Dilution

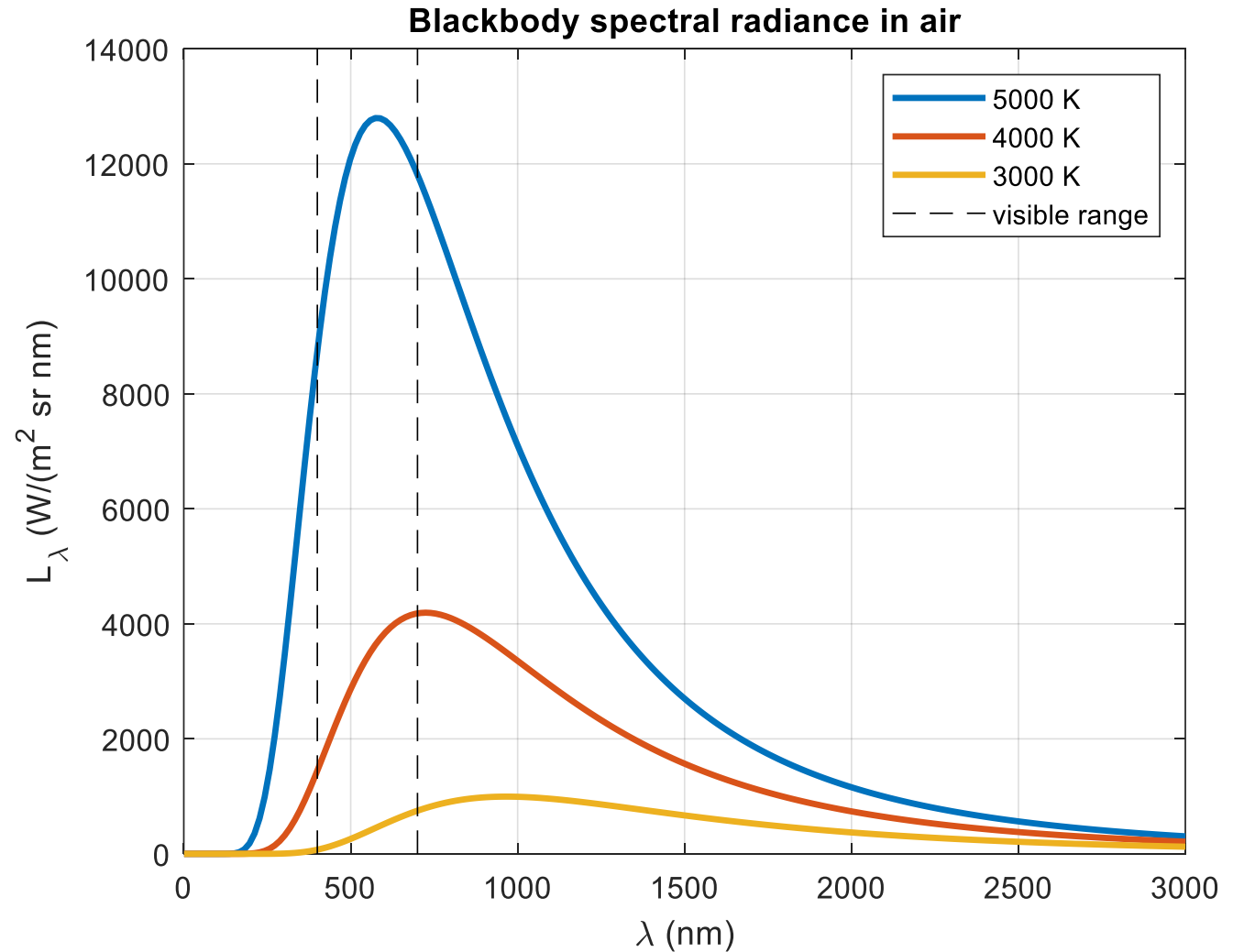
Planck's blackbody spectrum

Planck: Spectral radiance

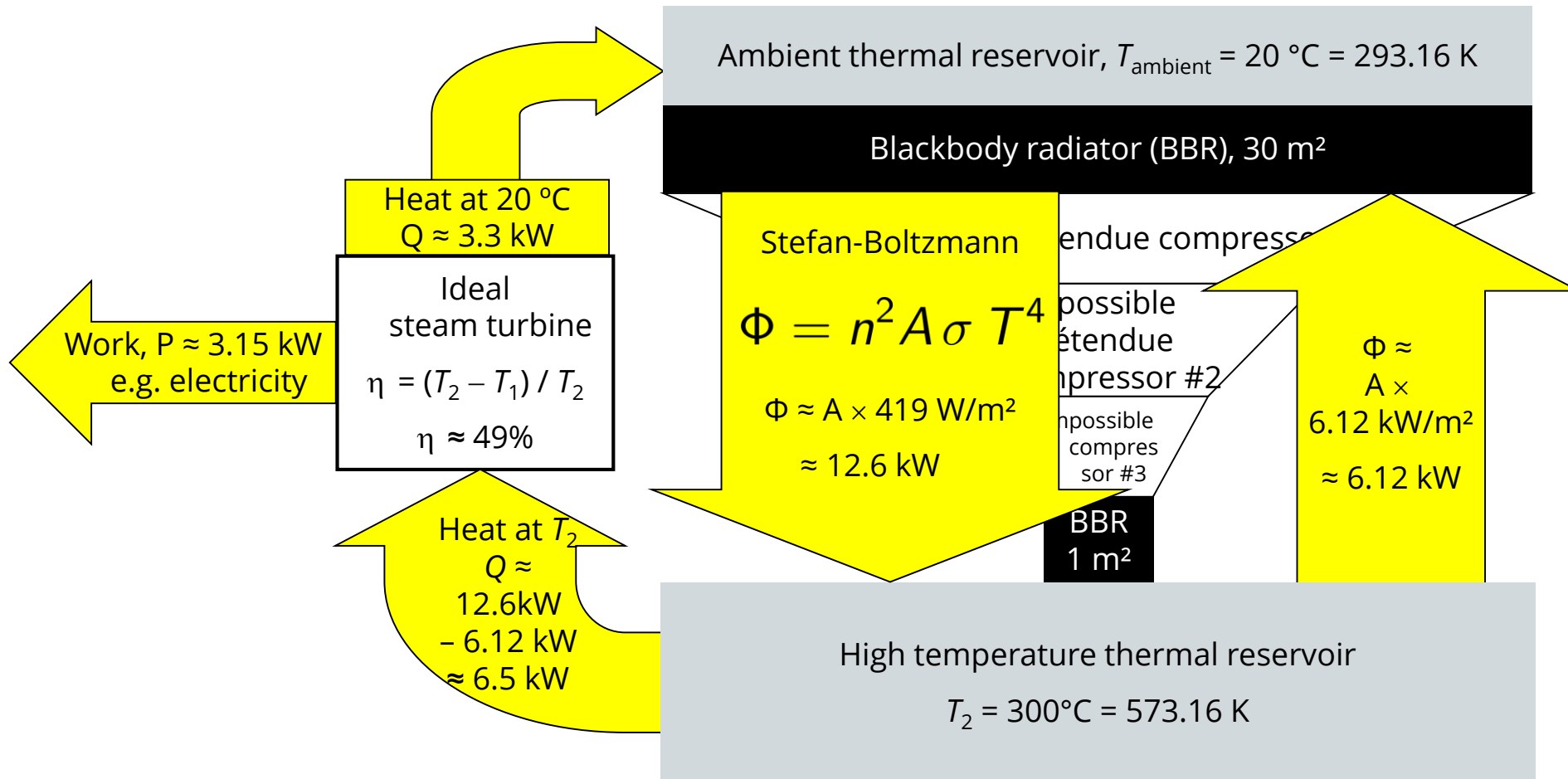
$$L_{\lambda}(\lambda, T)$$

Units: $W / (m^2 \text{ sr nm})$

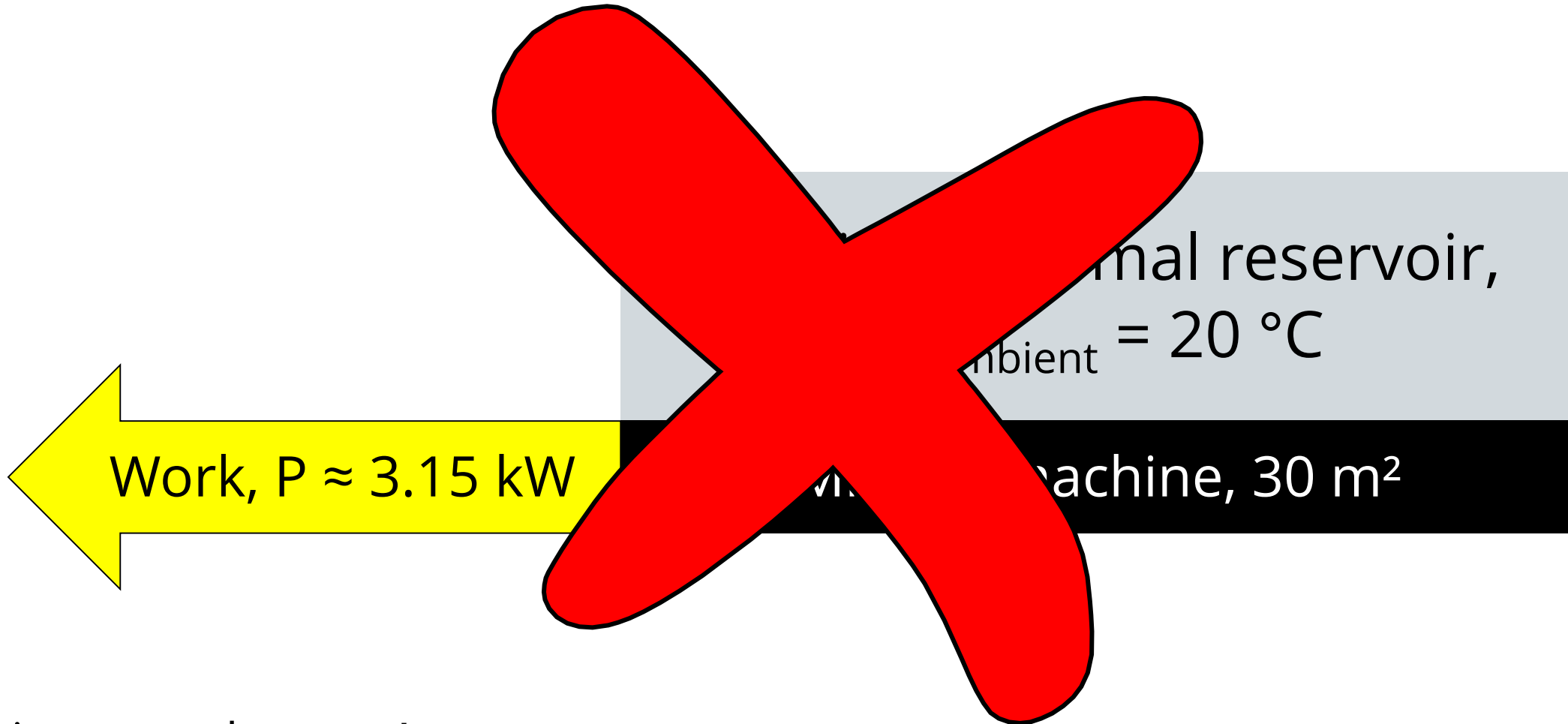
Flux per wavelength per étendue



Étendue conservation and the Second Law



Etendue conservation and the Second Law



This cannot happen!

For more details, see e.g. www.nature.com/articles/s41598-017-01622-6 www.entropyofradiation.com

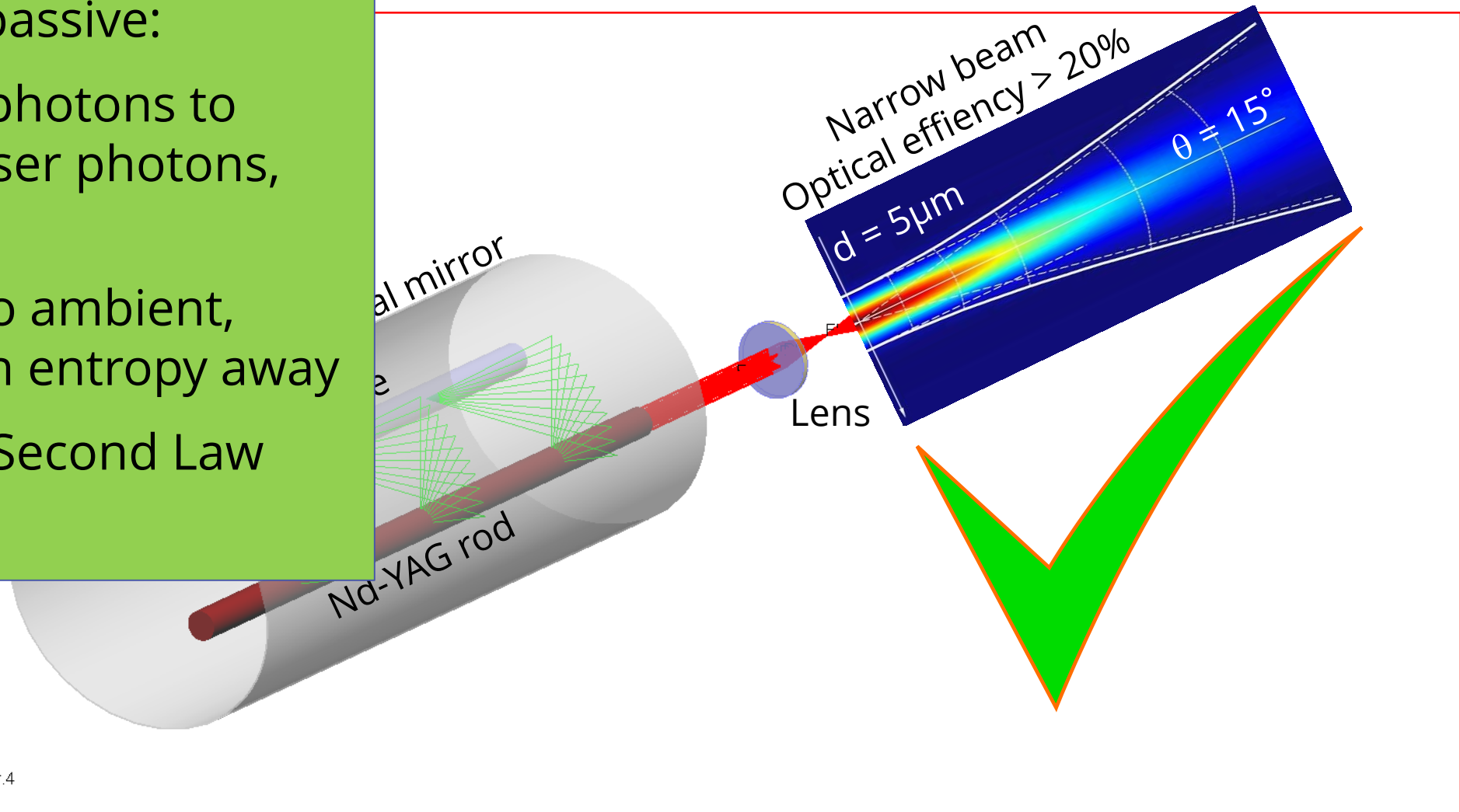
The Second Law of Thermodynamics

„Spectral radiance cannot increase in passive systems“

Definition of passive system:
Anything that does not (re-)emit photons

Solving riddle #1

Lasers are not passive:
 Convert pump photons to lower energy laser photons, creating heat
 Heat dumped to ambient, carries radiation entropy away
 No violation of Second Law



Jul 11, 2019
 OpticallyPumpedLaser.4
 LightTools 8.7.0

Solving riddle #2

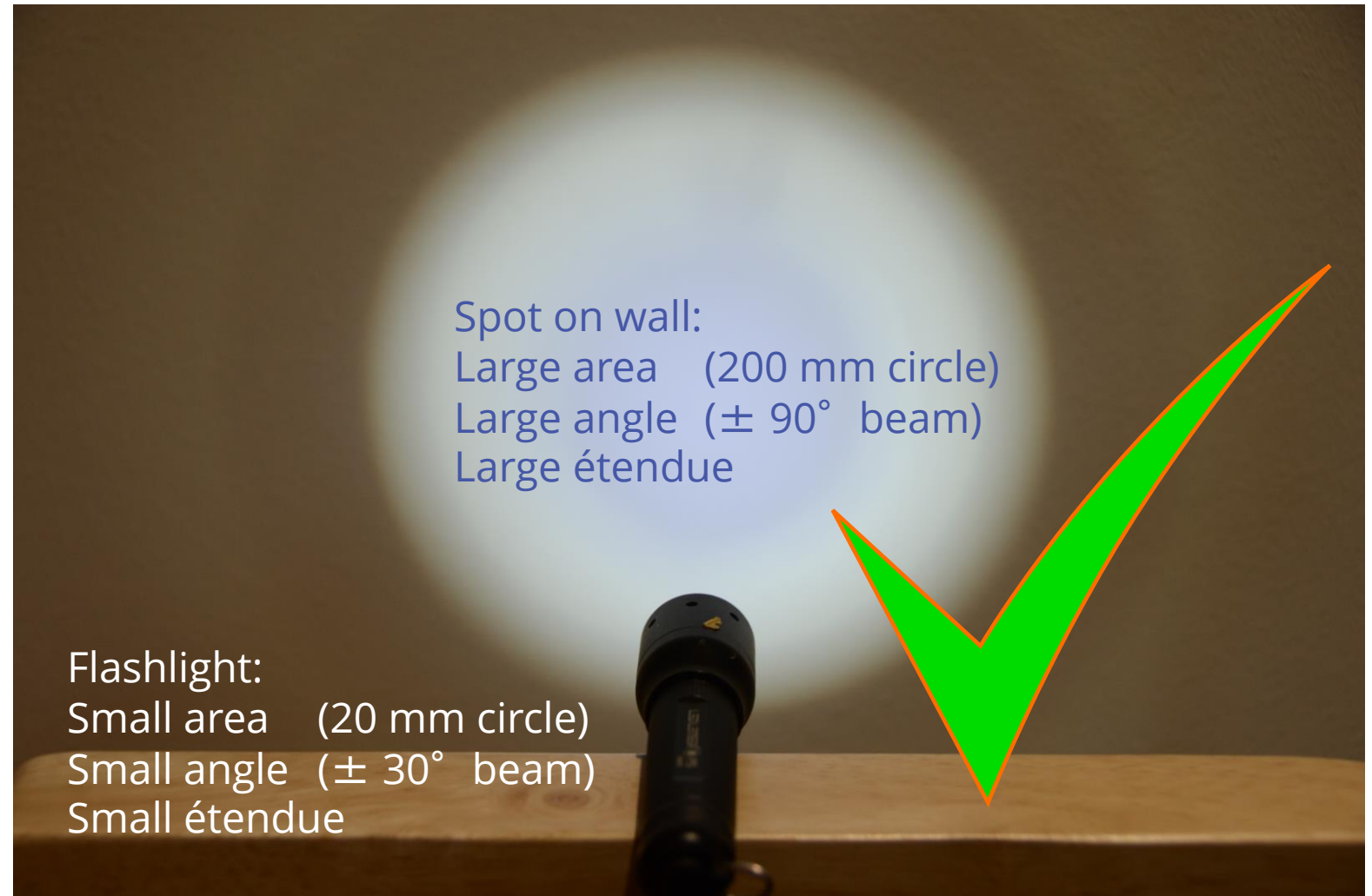
Just a flashlight and a wall

Radiation diluted at wall
by scattering into
previously (nearly) empty
phase space

Spectral radiance
decreases

Entropy is generated

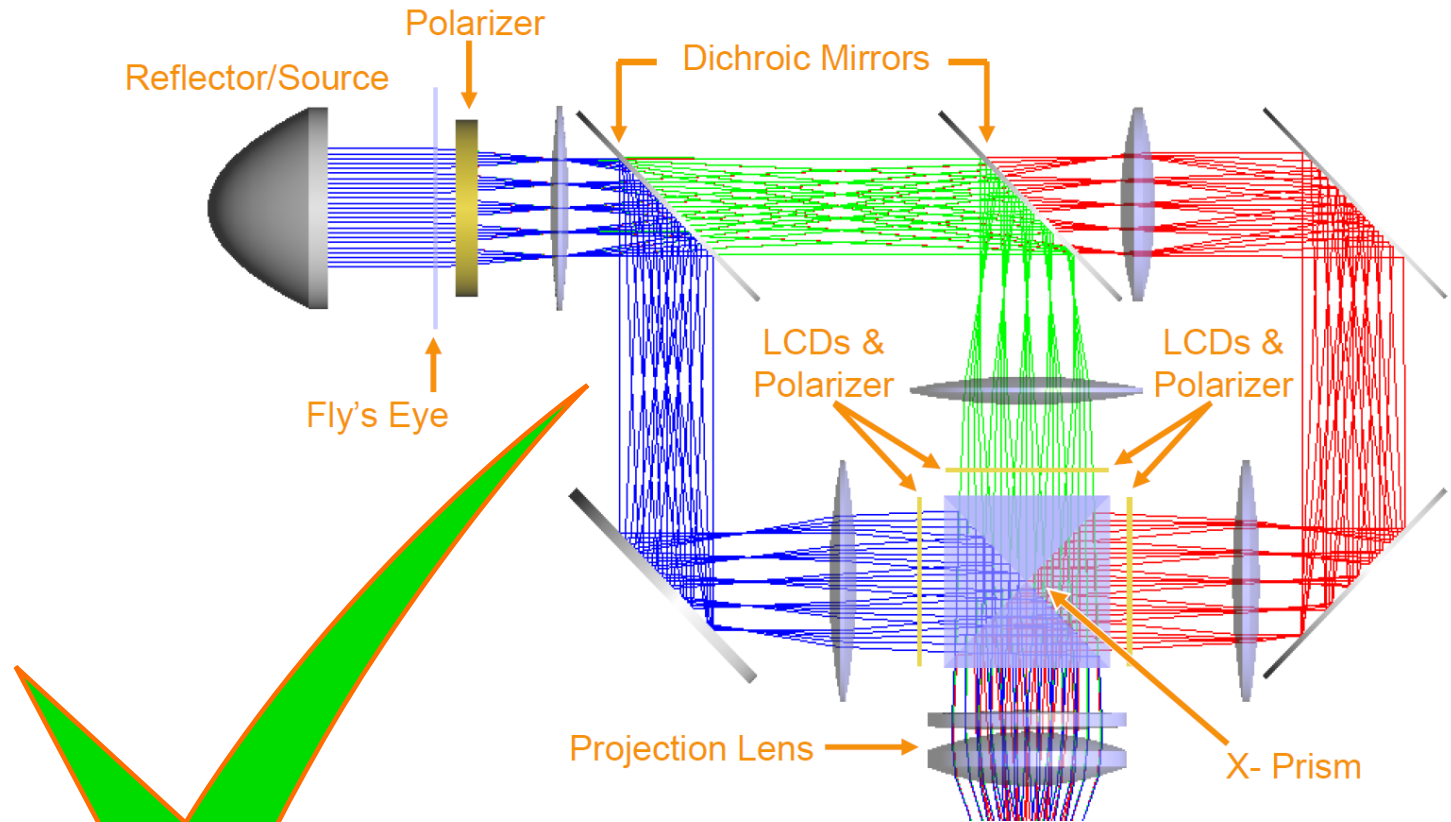
No violation of Second Law



Solving riddle # 3

At X-Prism:
Three sides input (R,G,B)
One side output (white)

Light with **different** wavelength combined into same phase space
No increase of **spectral** radiance
No violation of Second Law



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Étendue conservation spelled out

Consider a ray bundle passing through an optical system with

- refraction/reflection at smooth surfaces and free propagation only
- no scattering, no splitting of rays (consider one of the two splitted rays lost)
- no active components
- partial absorption allowed.

Place screens anywhere into the ray path, with exactly one intersection per ray

Determine étendues of ray bundle at each screen.

Étendue conservation: All these étendues are the same

When in doubt, ask yourself: Could I increase spectral radiance?

Using étendue

- Étendue conservation applicable to many optical systems
- Now you know when, and when not
- If applicable, then étendue conservation is supremely useful
- Compute hard, fundamental laws of nature based limits on aperture sizes, beam angles, source sizes, efficiencies...
in just a few lines of Matlab, Excel, or in your head
- If you'd like to learn more
(like about luminance, illuminance, intensity, design patterns, color):
 - Read the books, read my papers,
 - attend one of my courses (dates, locations and more on my LinkedIn profile)
 - just ask me

Thank you for your attention

