

# Chip-scale terahertz frequency combs and multiheterodyne spectroscopy

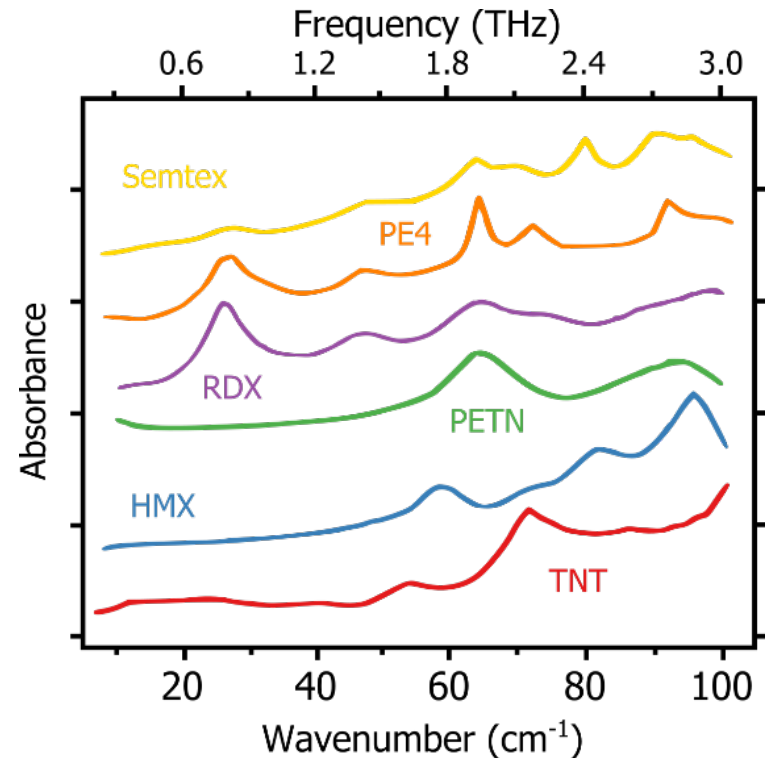
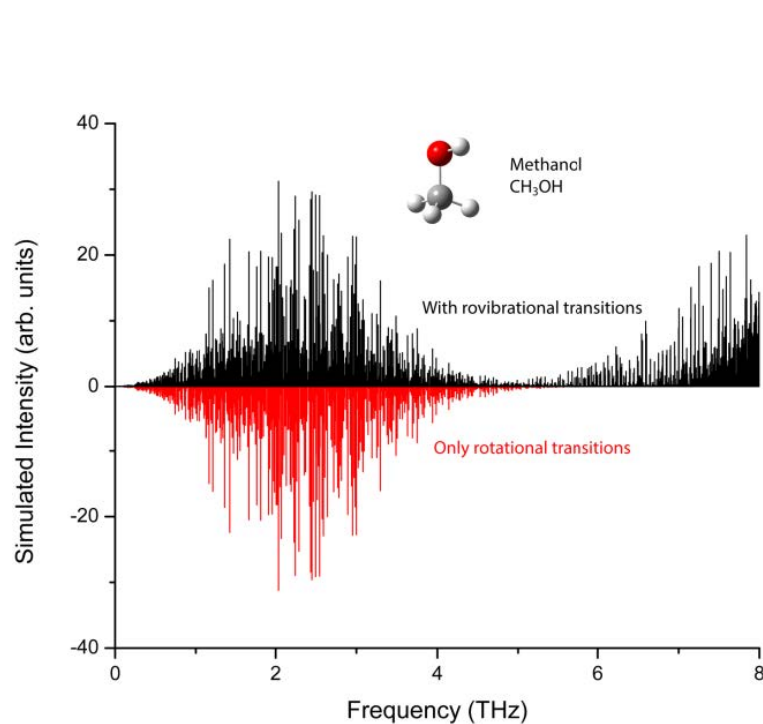
**David Burghoff**

OSA Laser Systems Technical Group

December 6, 2017

# Main motivation: broadband chip-scale spectroscopy

- Many molecules have distinctive spectral features at long wavelengths due to structure



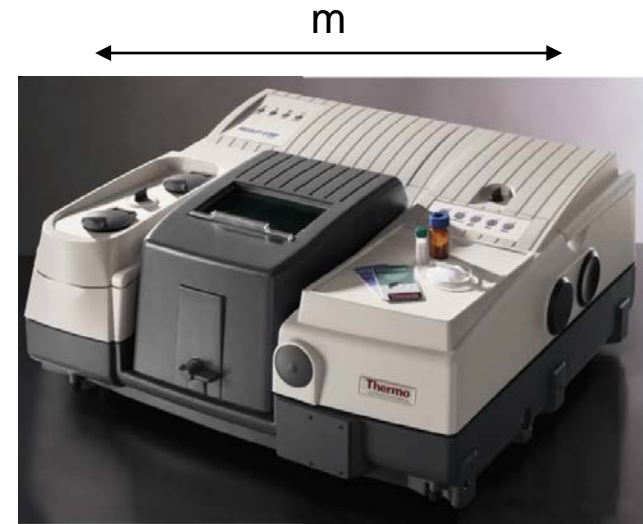
- Terahertz: 30-300  $\mu\text{m}$  (1-10 THz)
- Mid-infrared: 3-30  $\mu\text{m}$

# DARPA SCOUT program: Broadband chip-scale spectroscopy



Spectral Combs from **UV** to **THz**

Basic problem: highest sensitivity systems are large and have moving parts

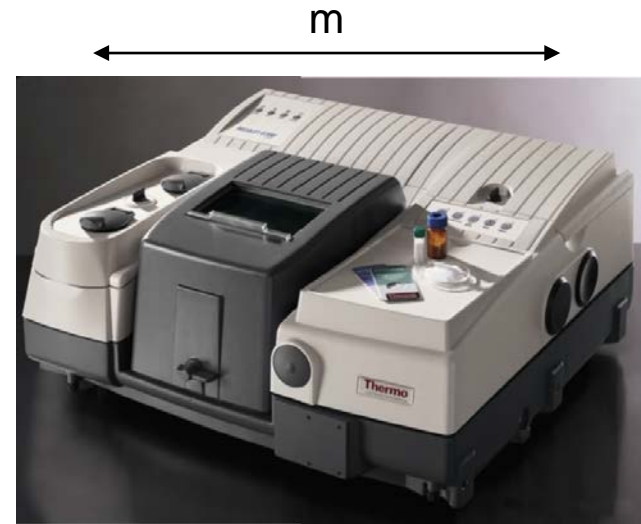


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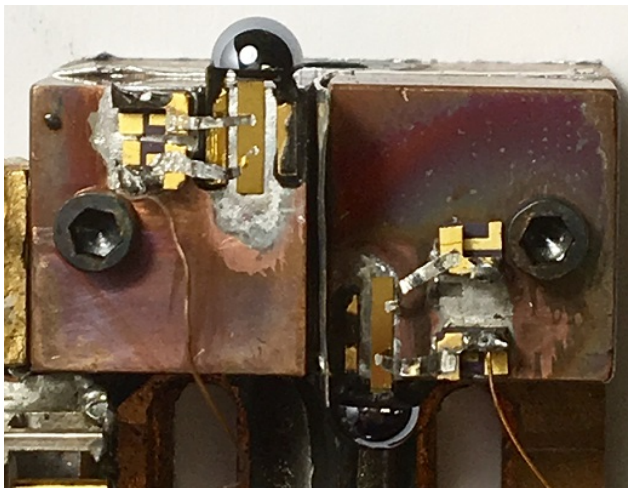


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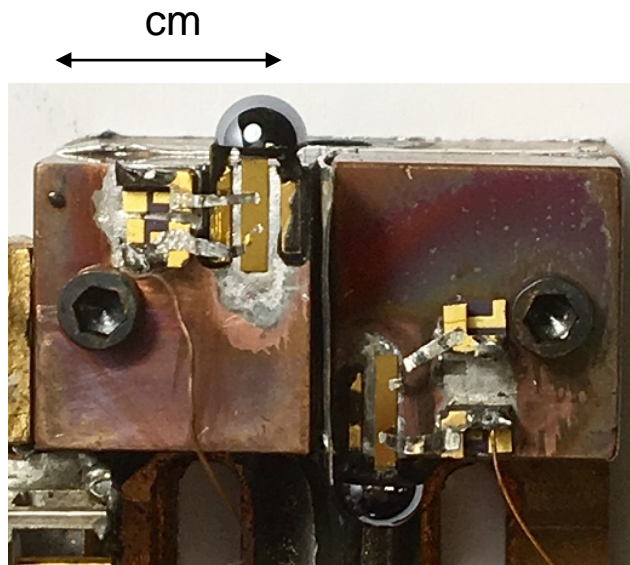
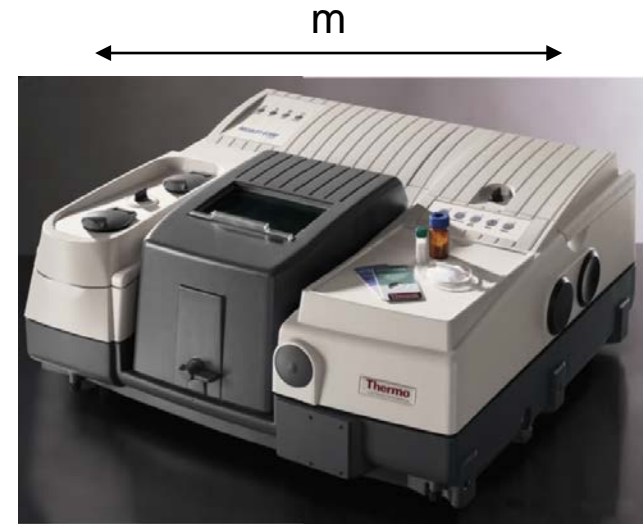
Semiconductor frequency combs can perform high-SNR spectroscopy without any moving parts!

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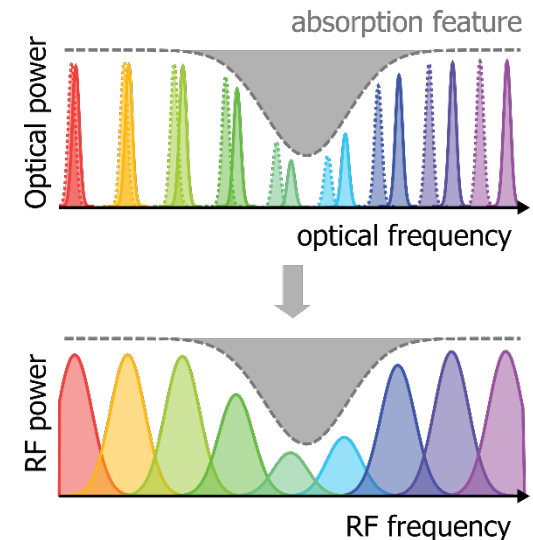


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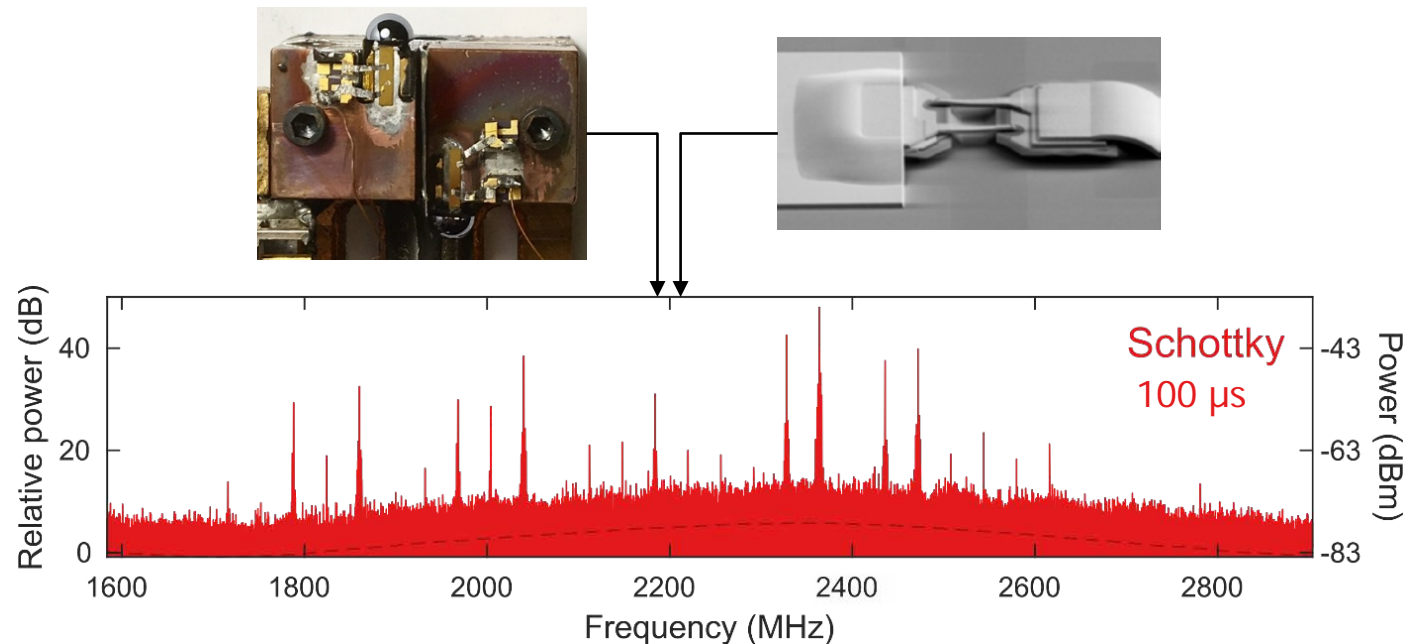
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Dual comb spectroscopy

# Terahertz QCL dual comb spectroscopy

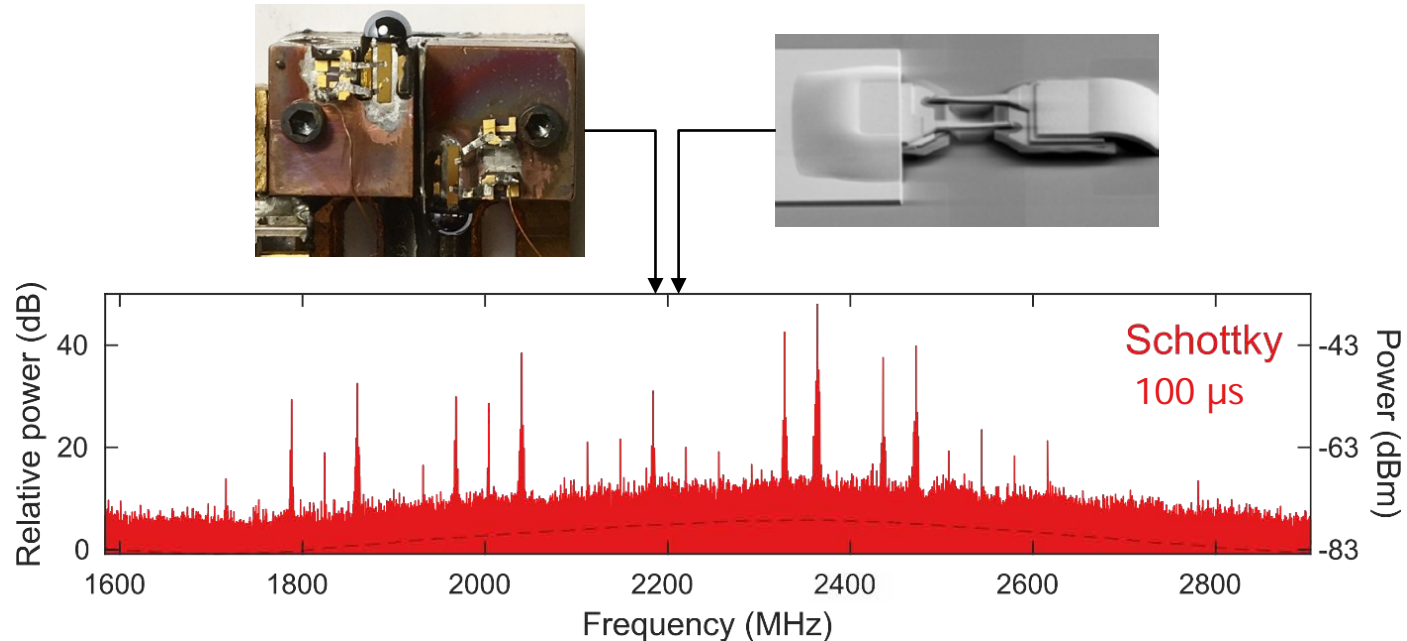
- With dual comb spectroscopy, can perform broadband spectroscopy using chip-scale components. No spectrometer and no moving parts!



Yang, Burghoff et al., "Terahertz multiheterodyne spectroscopy using laser frequency combs," *Optica* (2016).

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- Part I** : Quantum cascade laser (QCL) basics
- Part II** : Comb formation in QCLs
- Part III** : Dual comb spectroscopy based on THz QCLs

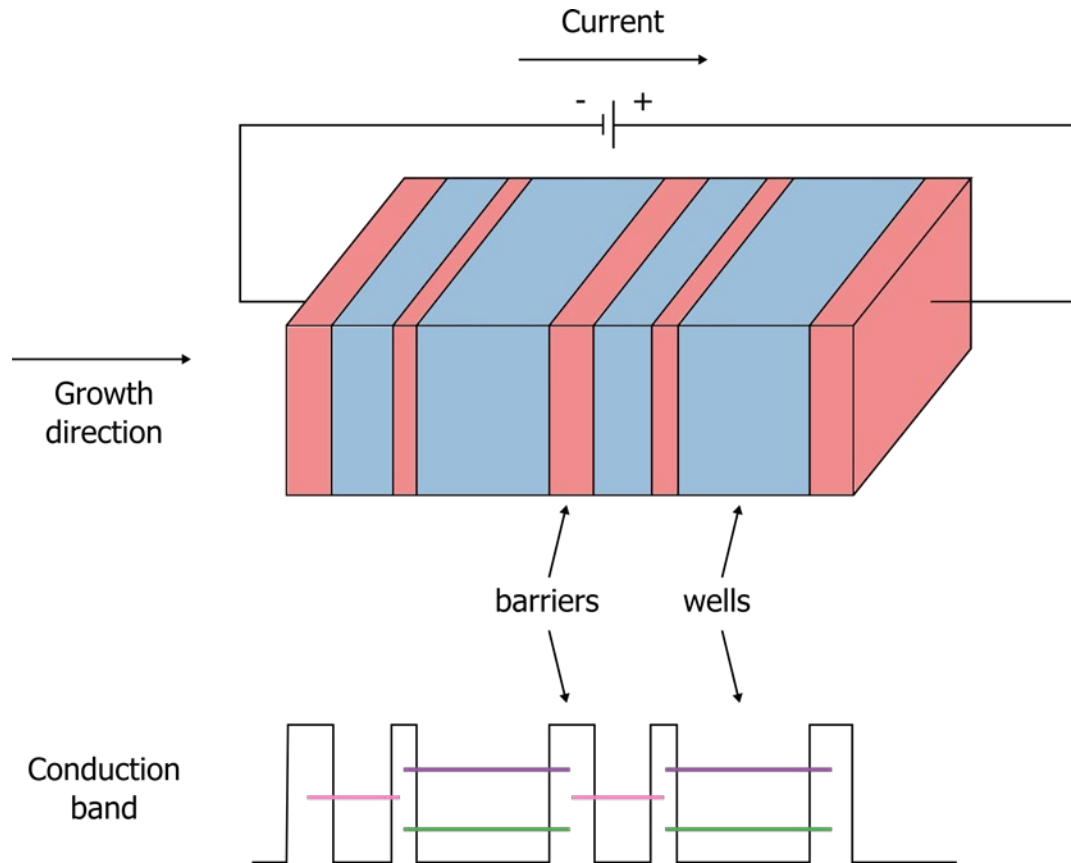
# Part I

## Quantum cascade laser basics



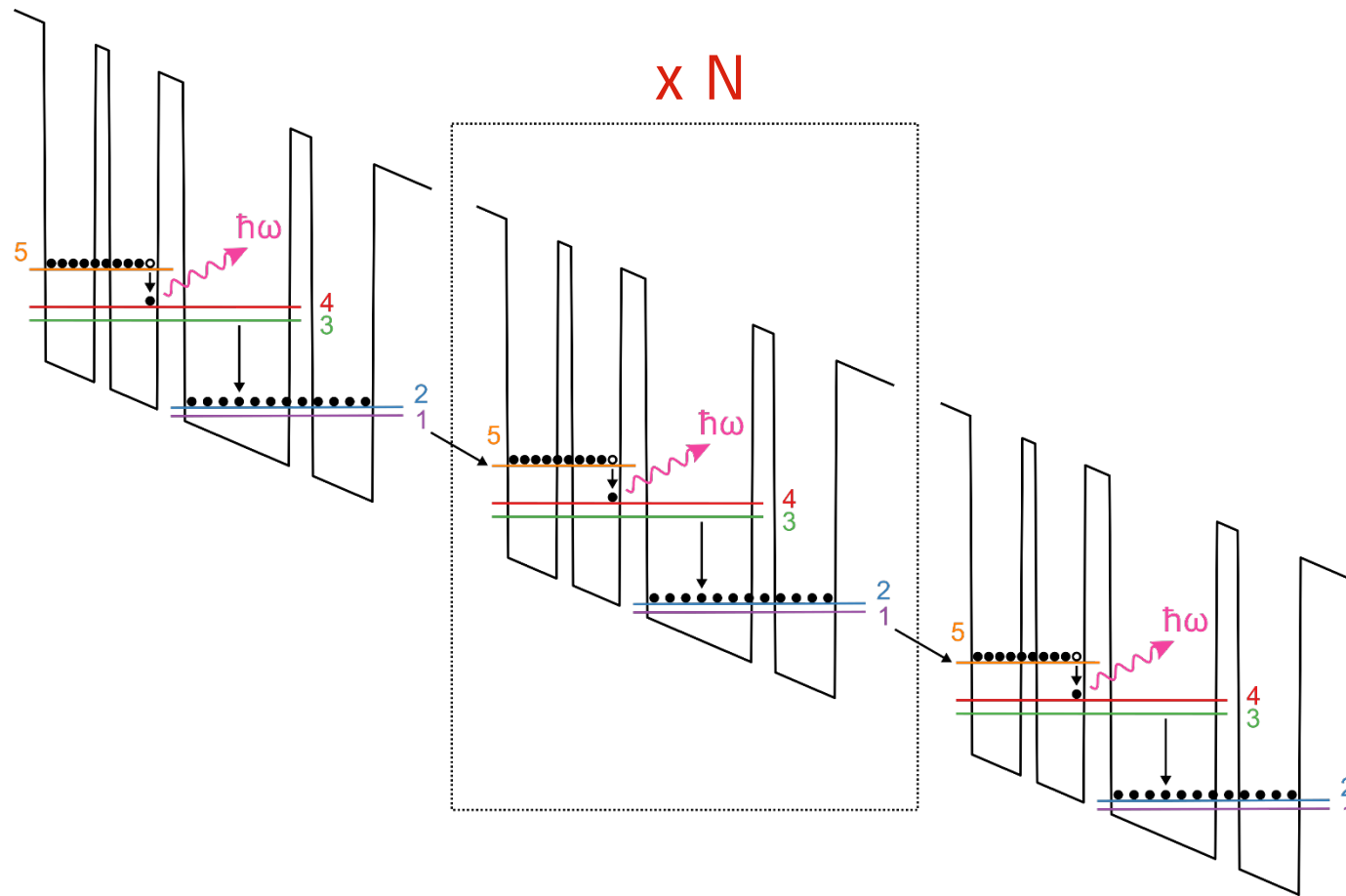
# Quantum cascade lasers: a triumph of band structure engineering

- Basic idea: grow a series of quantum wells and barriers on a semiconductor substrate



Can make  
"artificial atoms"

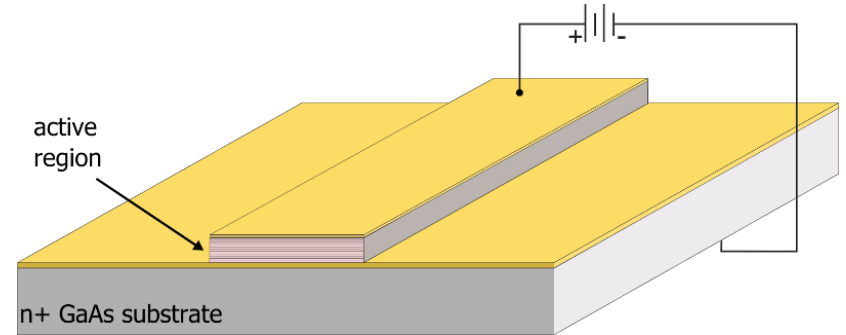
# Electrically-pumped intersubband lasers



- $\hbar\omega$  chosen by design—not nature
- No electron-hole recombination. One electron cascades down  $N$  identical modules, generating  $N$  photons.

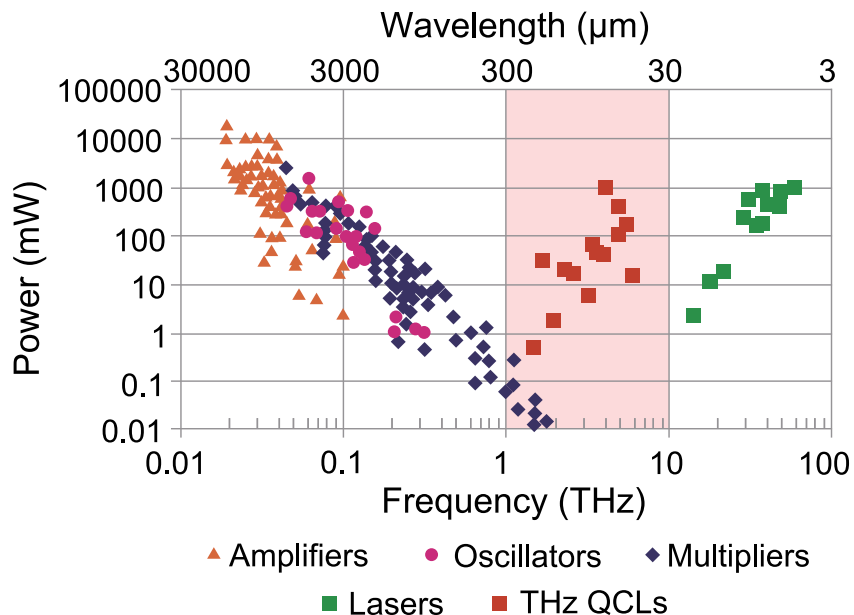
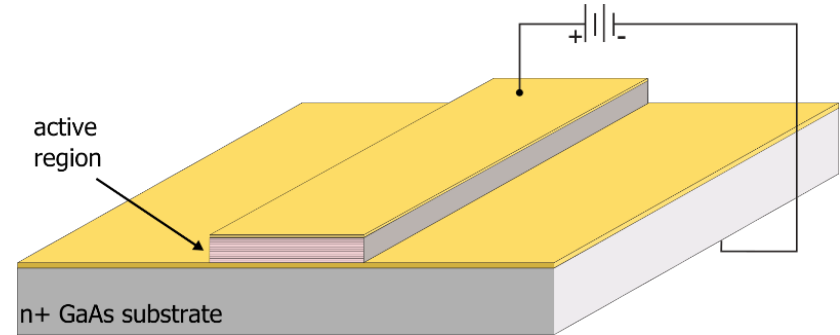
# Terahertz quantum cascade lasers (1-5 THz)

- Main focus of this talk: THz quantum cascade lasers (GaAs/AlGaAs)
  - Metal-metal waveguide: gain medium sandwiched between two gold layers



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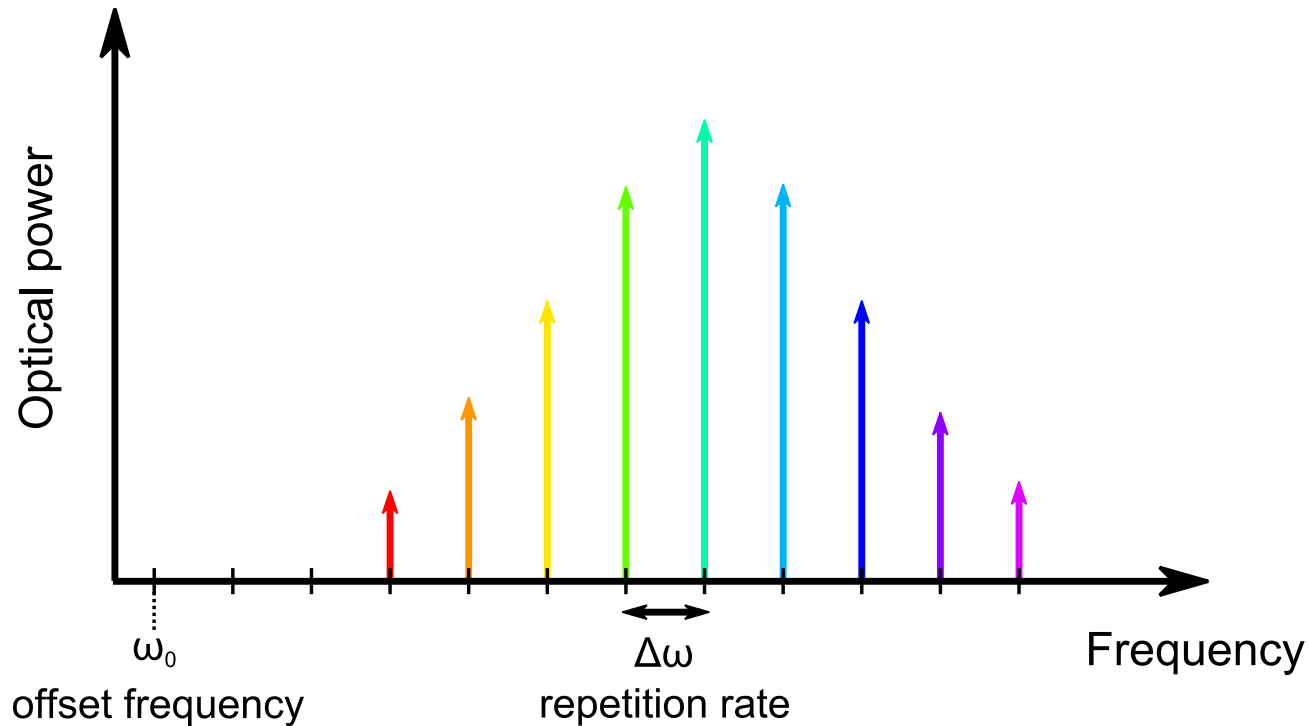
- Milliwatt power, low cost and size
- **Excellent platform for nonlinear optics**
  - large intersubband nonlinearity, intracavity power (W)

# Part II

## Comb formation in QCLs

# What is a frequency comb?

- **Frequency combs:** Light sources that consist of a large number of **evenly-spaced** laser lines



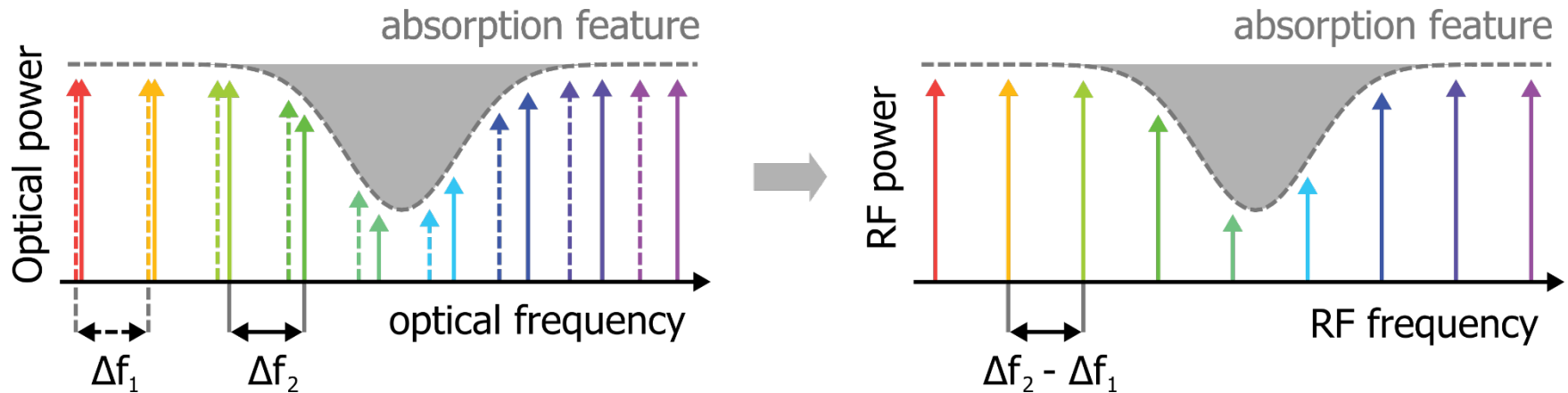
- First laser combs based on pulsed mode-locked lasers (e.g., Ti:Sapphire)

# Frequency combs for frequency discrimination

- How are combs relevant for spectroscopy?

## Dual comb spectroscopy (multi-heterodyne)

- Two combs, with slightly different spacings, shined on fast detector

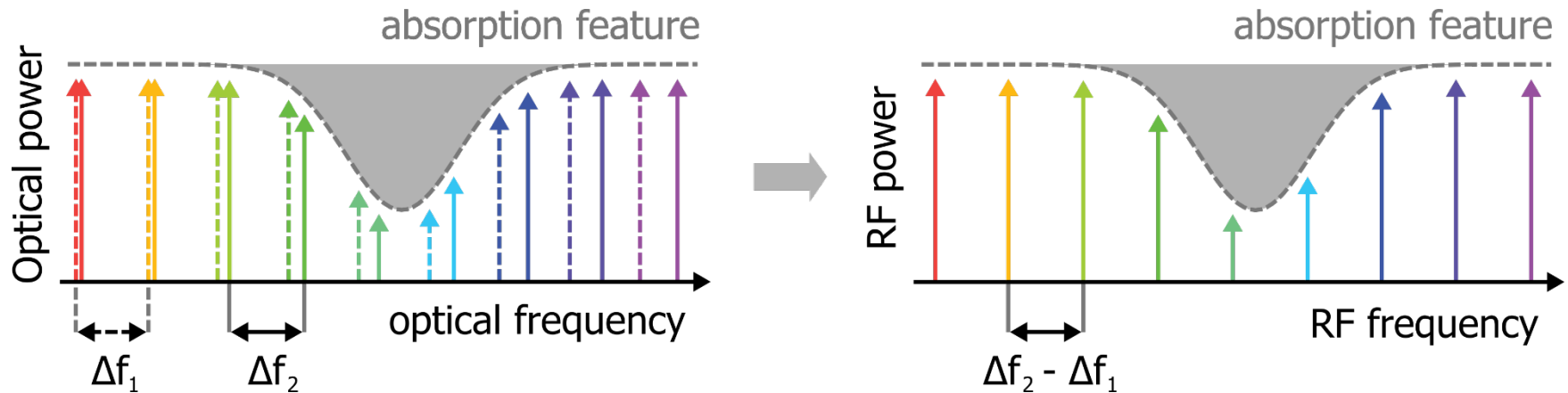


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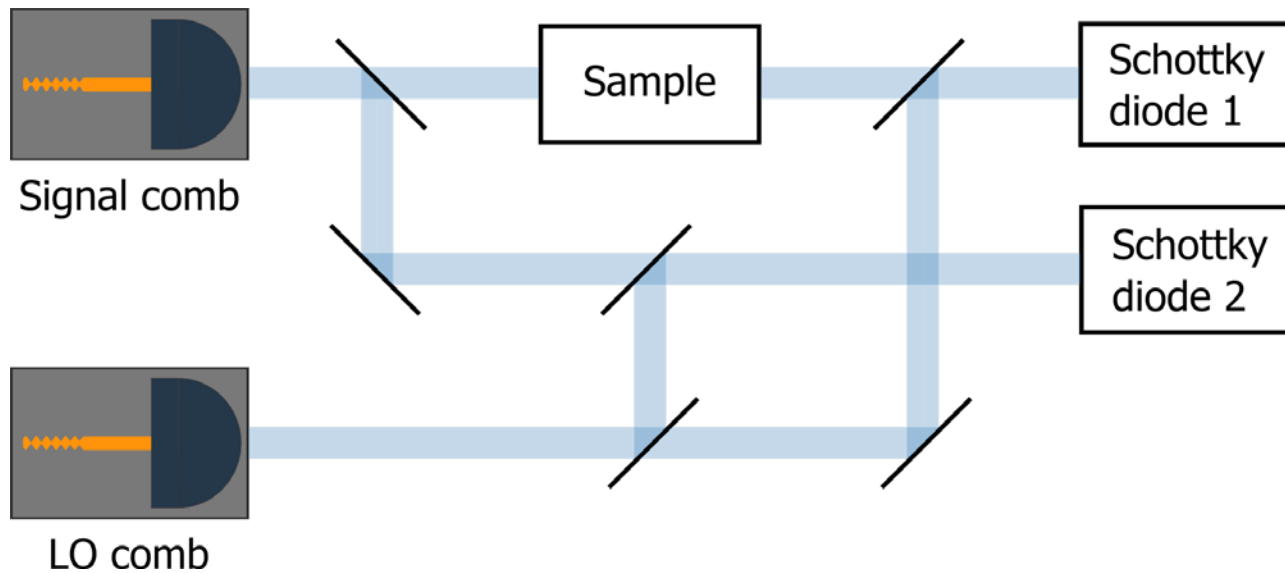
- Two combs, with slightly different spacings, shined on fast detector



- Optical** spectrum encoded onto **electrical** spectrum
- Can have broadband capabilities and high sensitivity, without moving parts!



# Dual comb spectroscopy can be very cheap and small

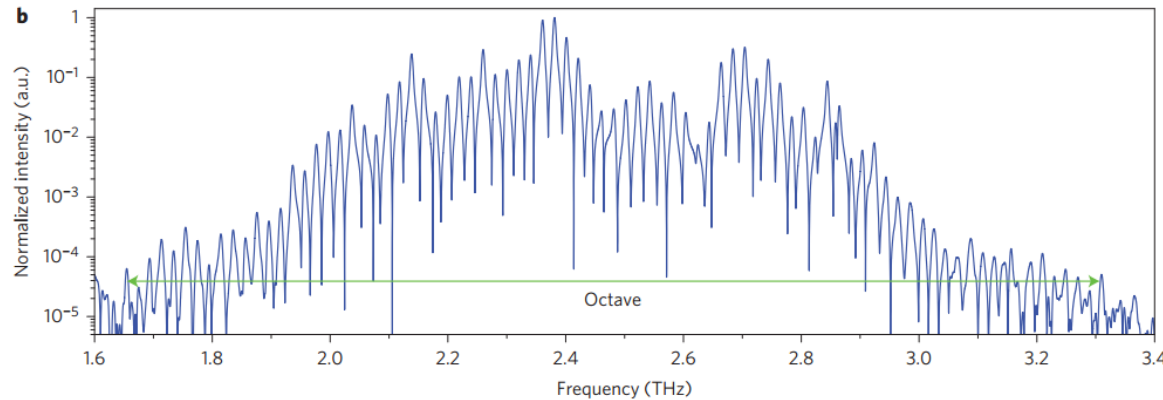


- Can make very compact THz spectrometers
  - Lasers: could be \$
  - Schottky diodes (Si): ¢
- Coherence requirements not that severe

**But how do you get a quantum  
cascade laser to form a comb?**

# QCLs are intrinsically broadband devices

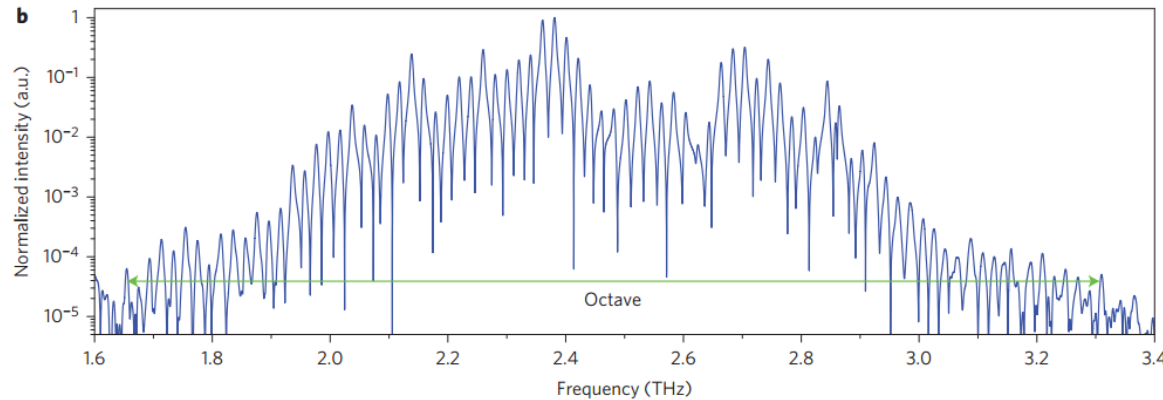
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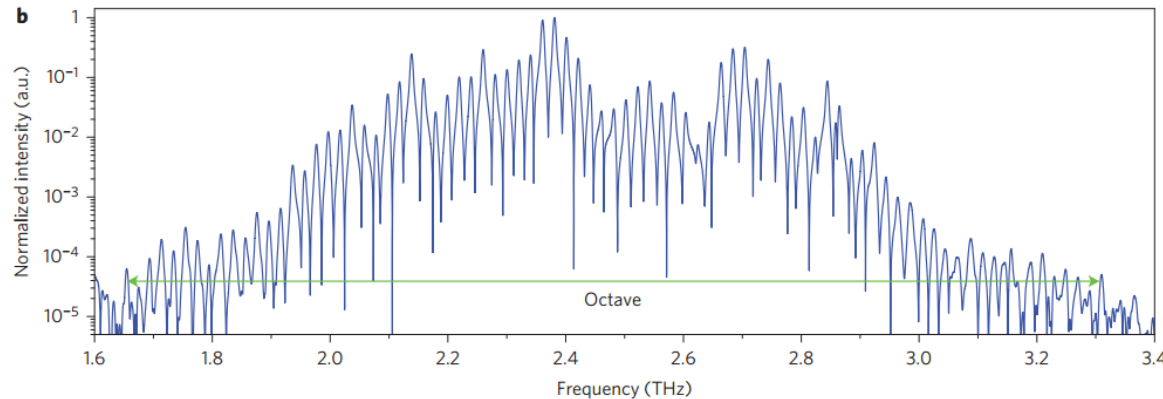


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- Broad doesn't mean comb, though! Prove using beatnote:

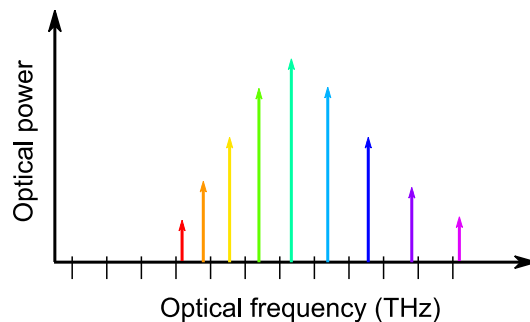
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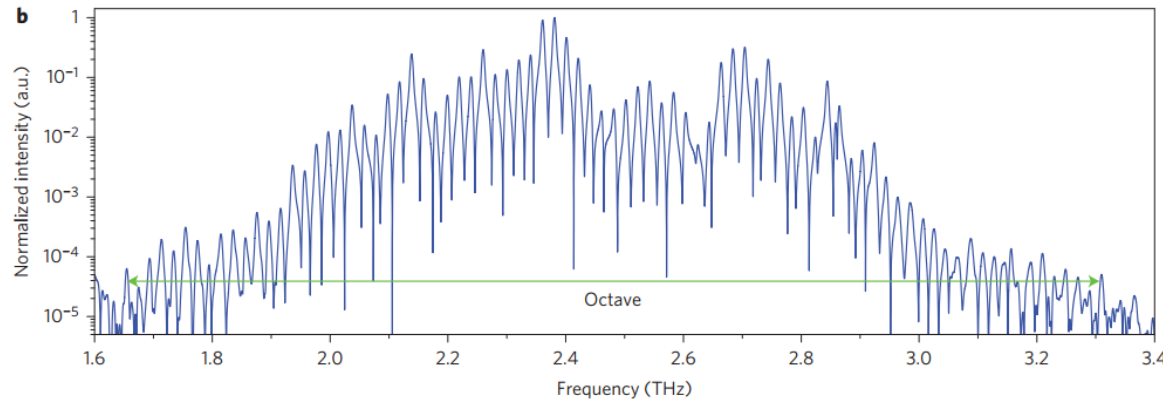
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non-comb

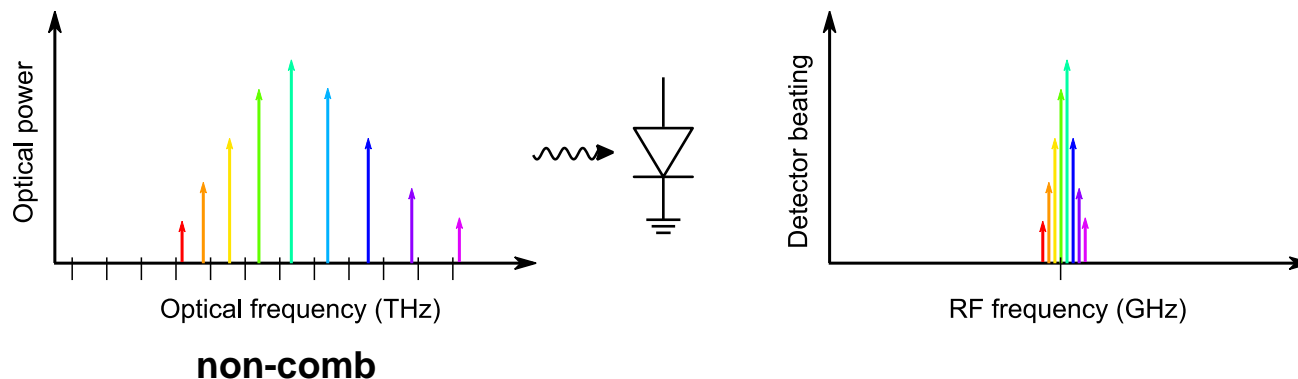
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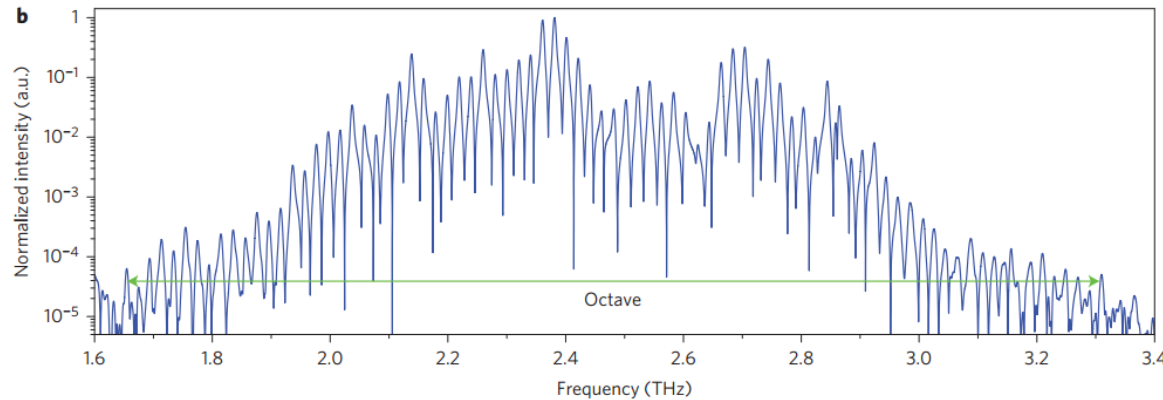
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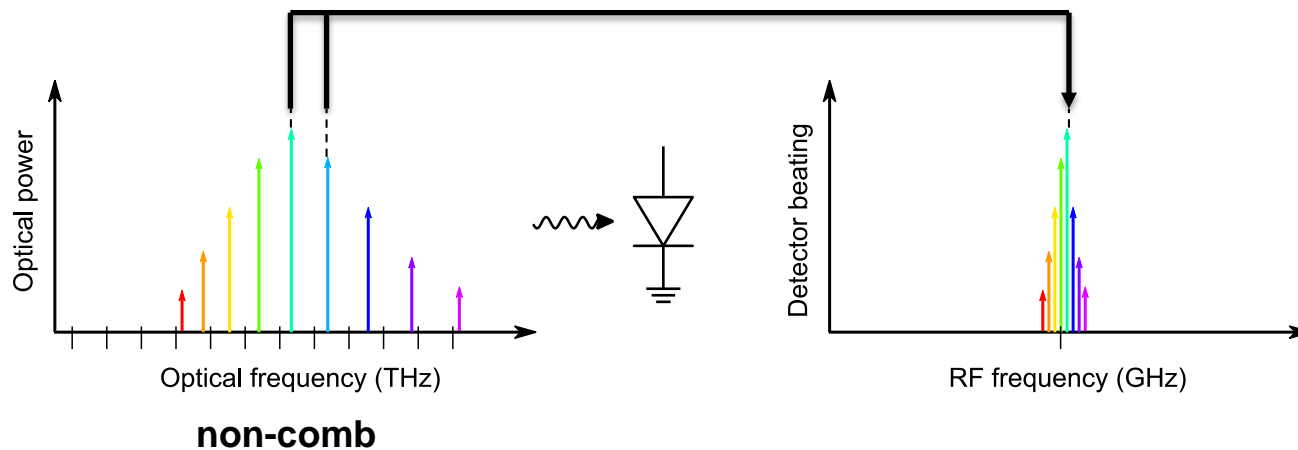
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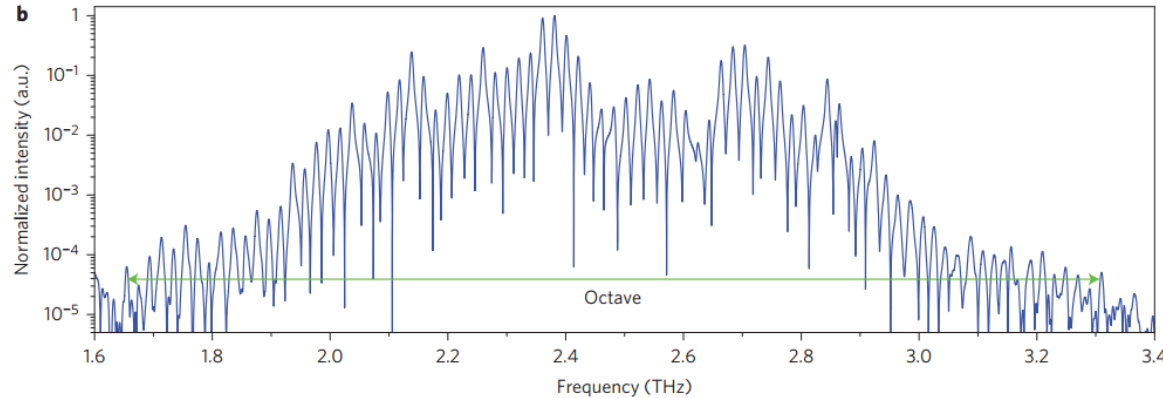
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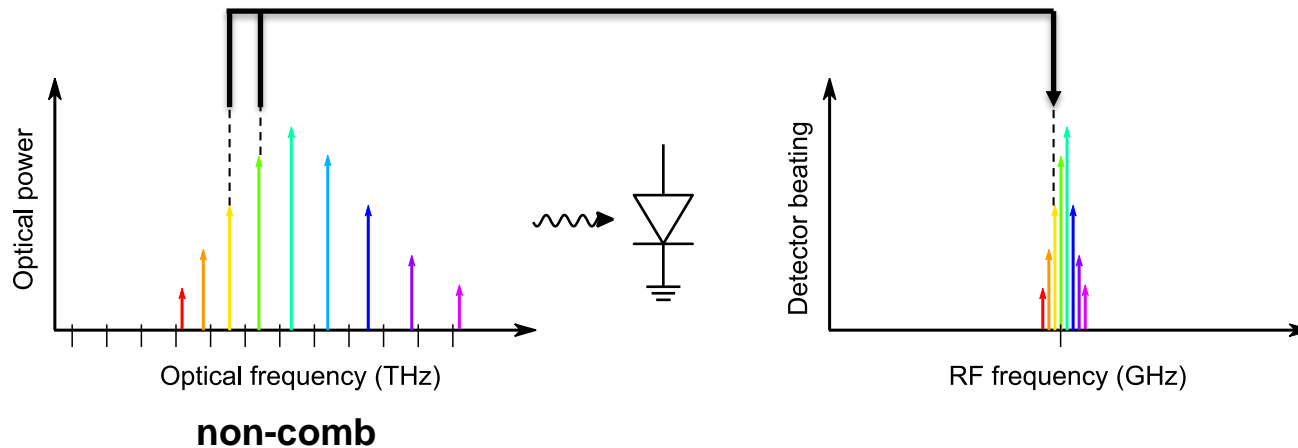
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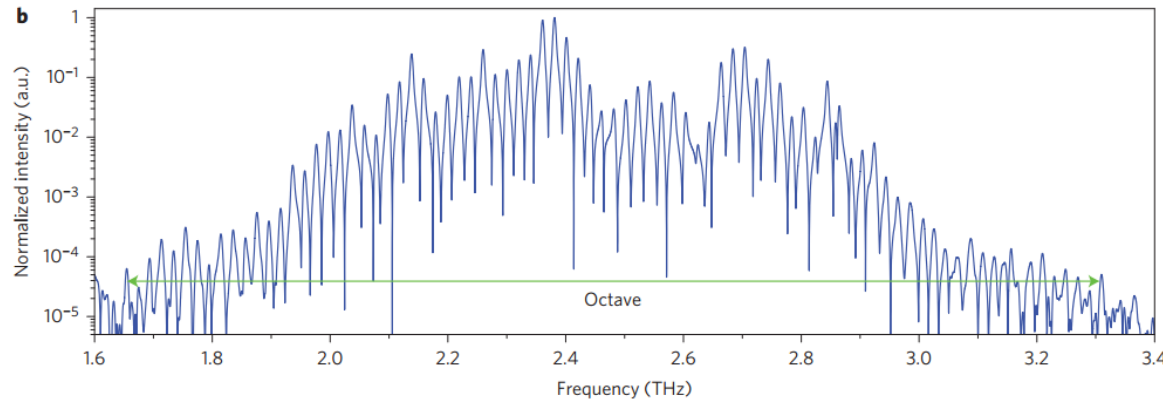
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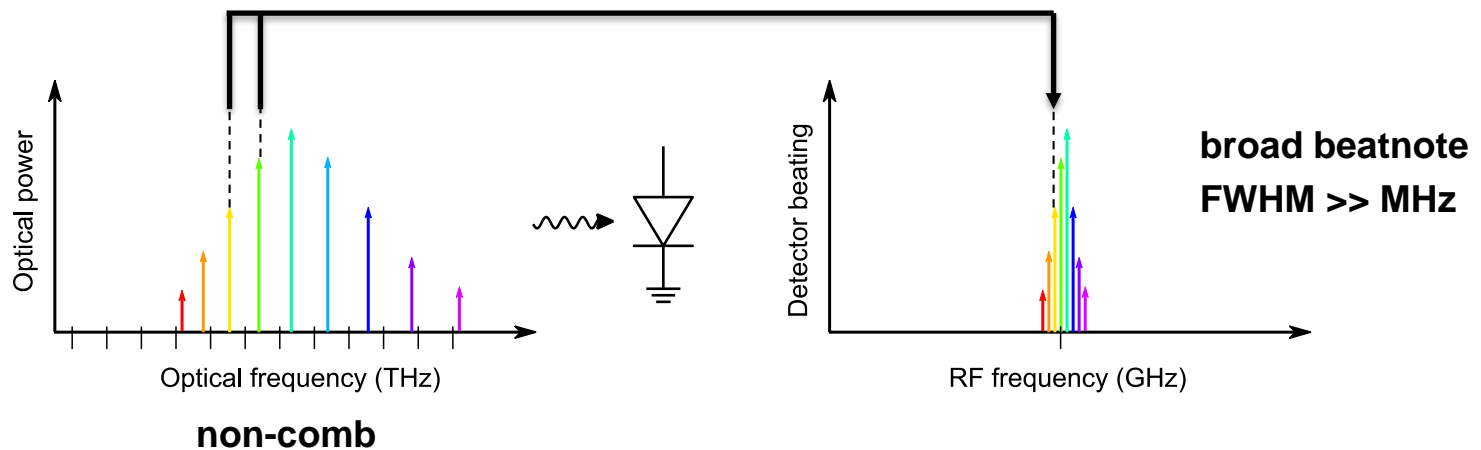
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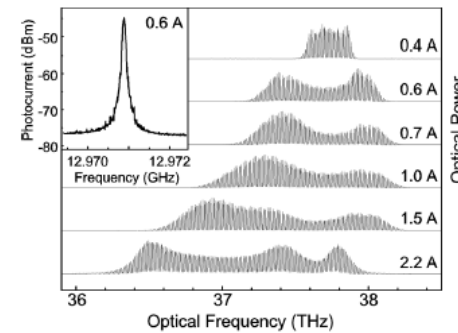


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- Long been known that the beatnote can spontaneously narrow (100 MHz to 10 kHz)

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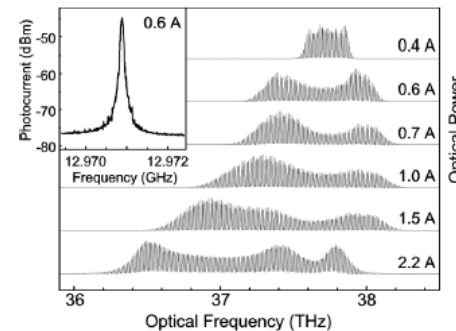
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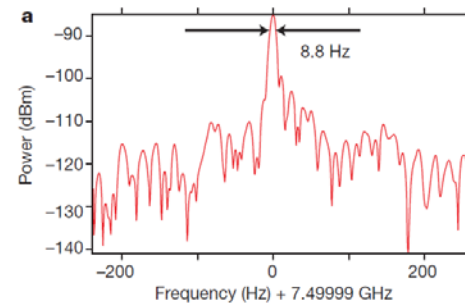
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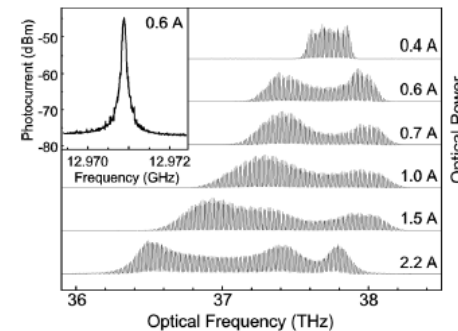
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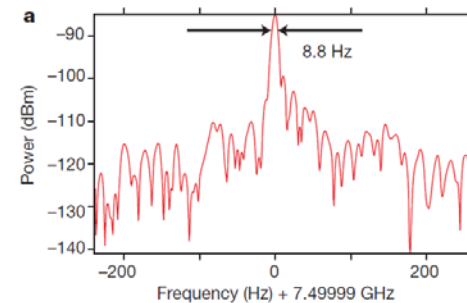
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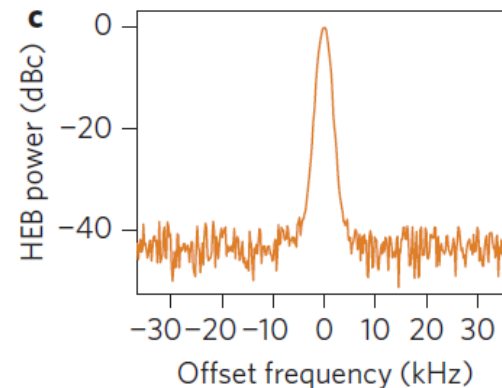
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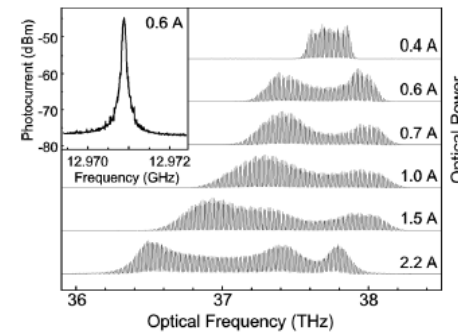


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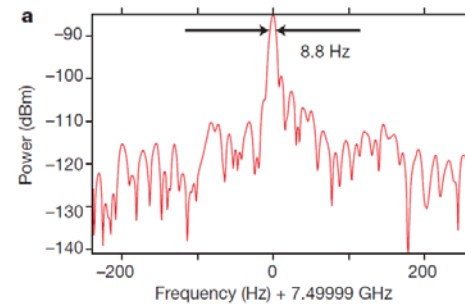
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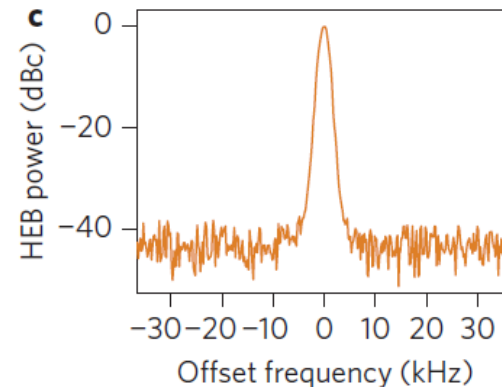
- Mid-IR
- THZ
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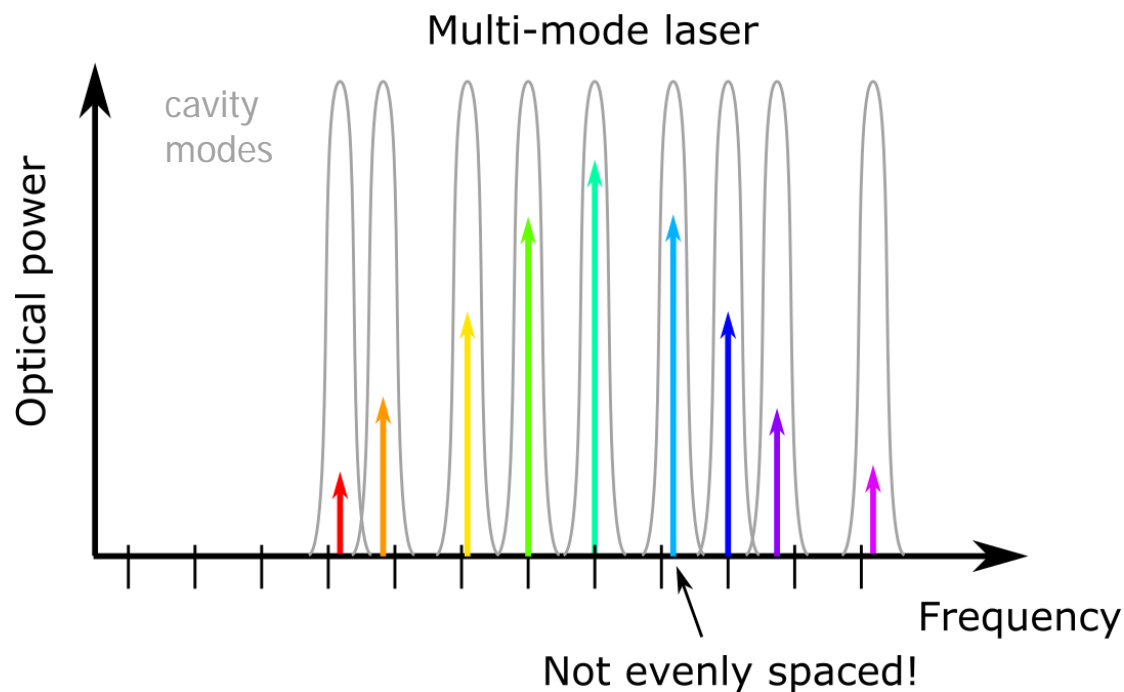
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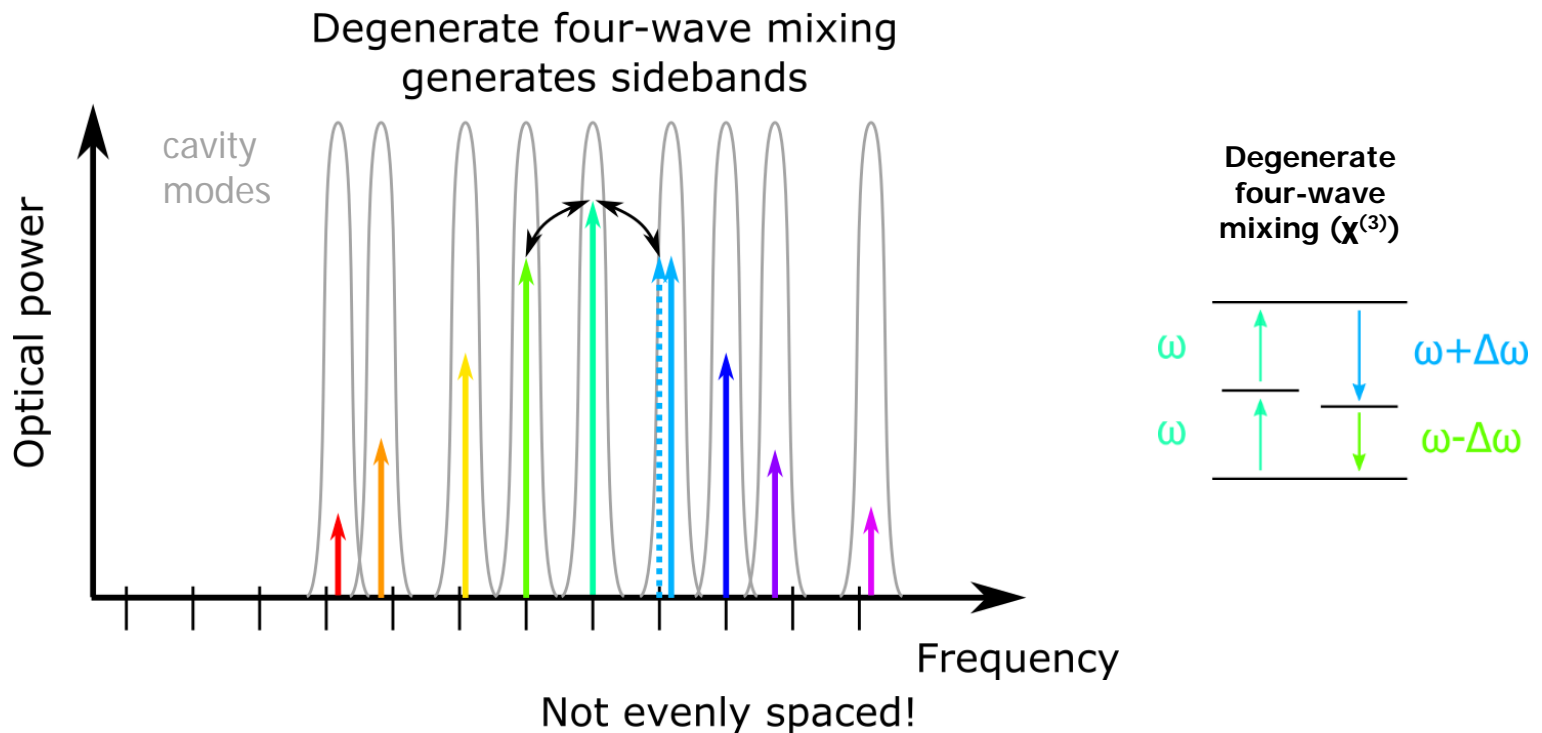
# Quantum cascade laser combs: basic principles

- QCL lasing is naturally broadband, but **uncorrelated**
- Four-wave mixing allows lines to **synchronize**, pull new lines into comb
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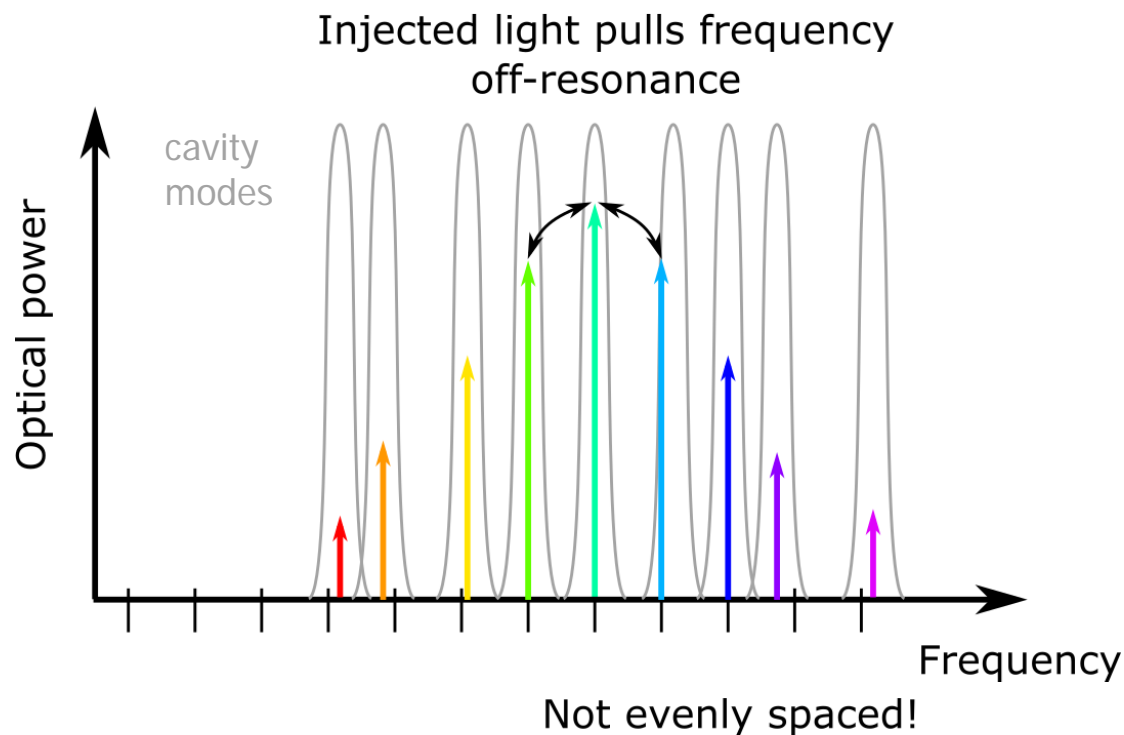
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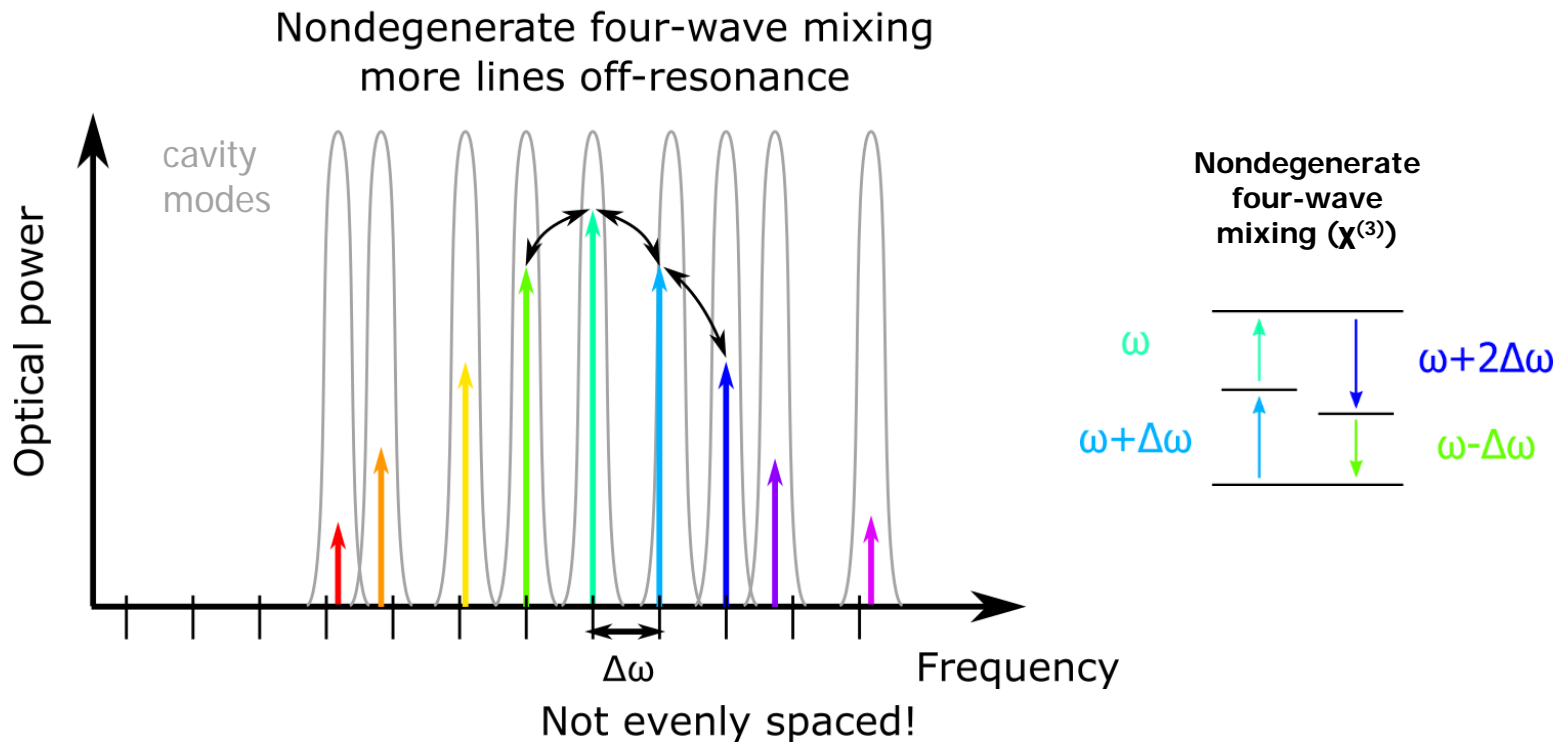
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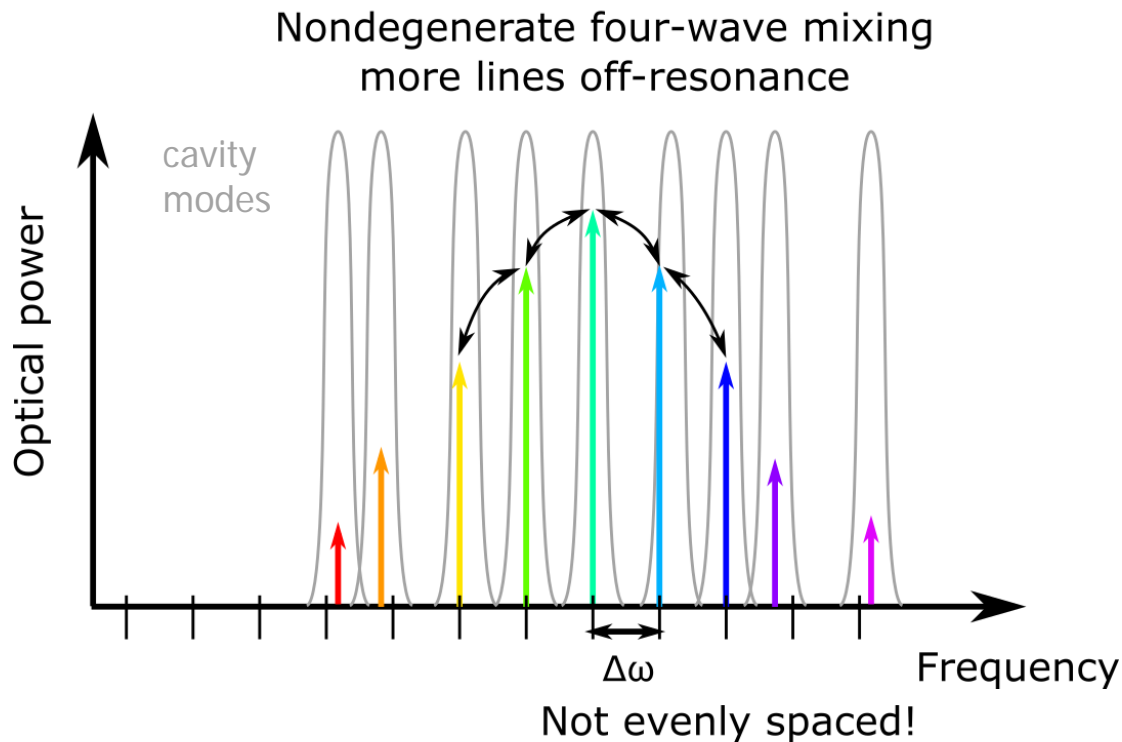
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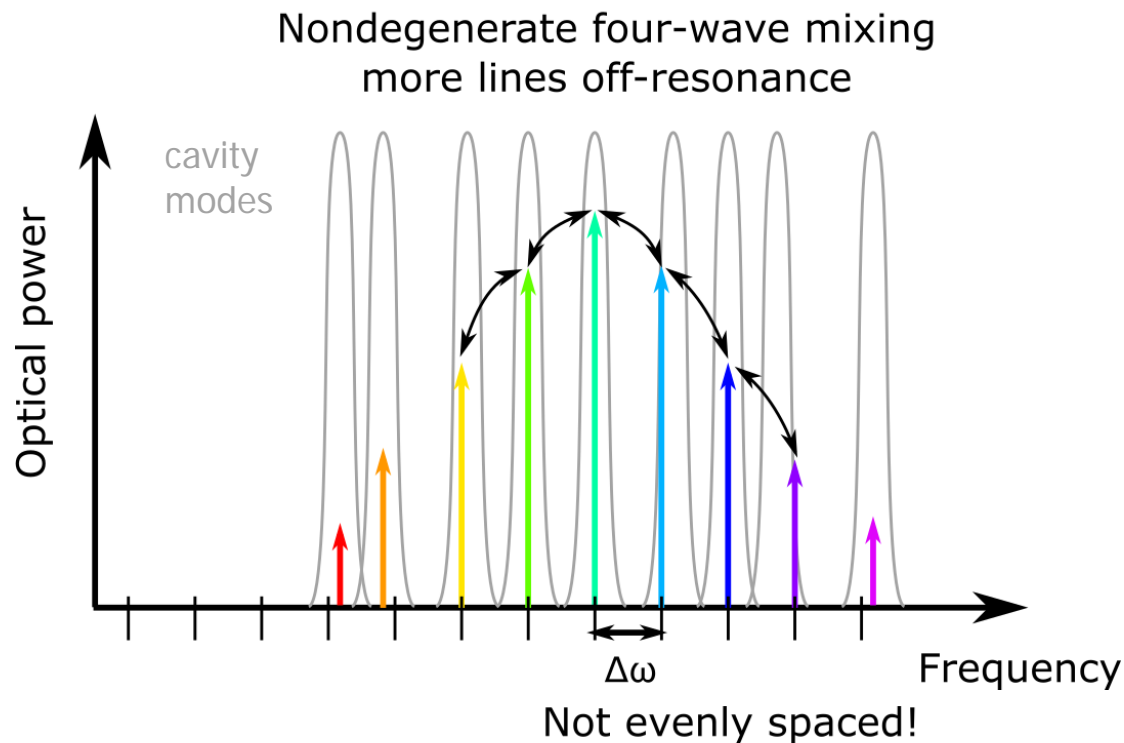
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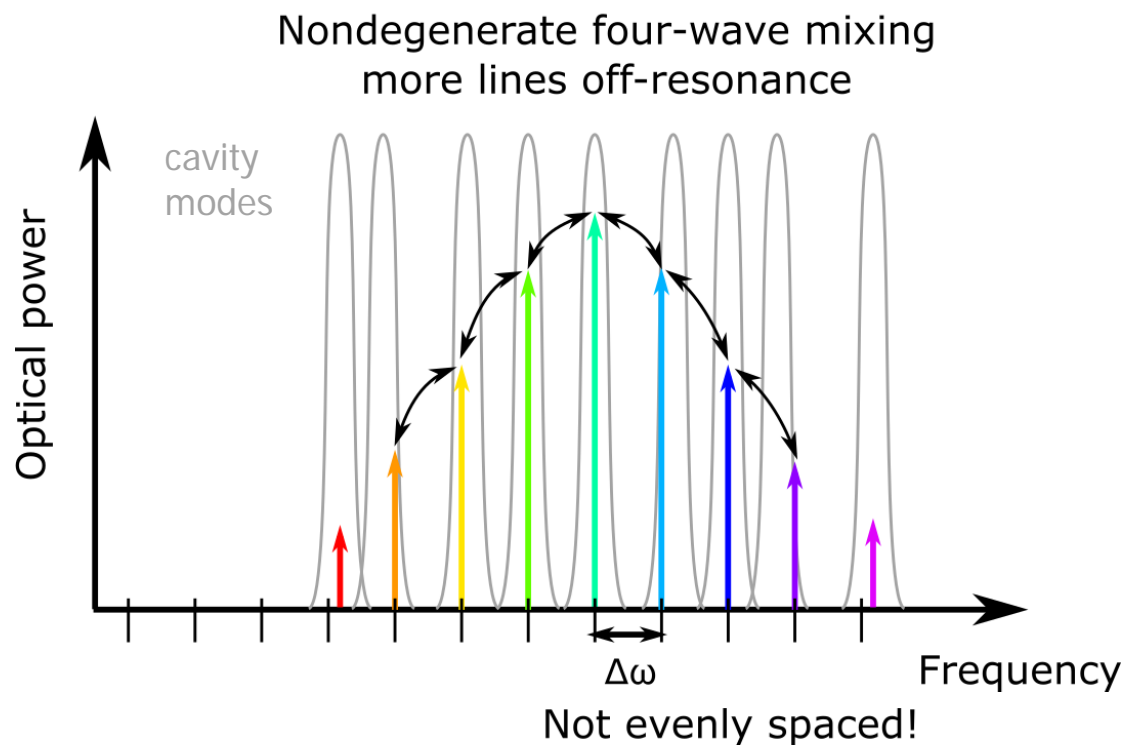
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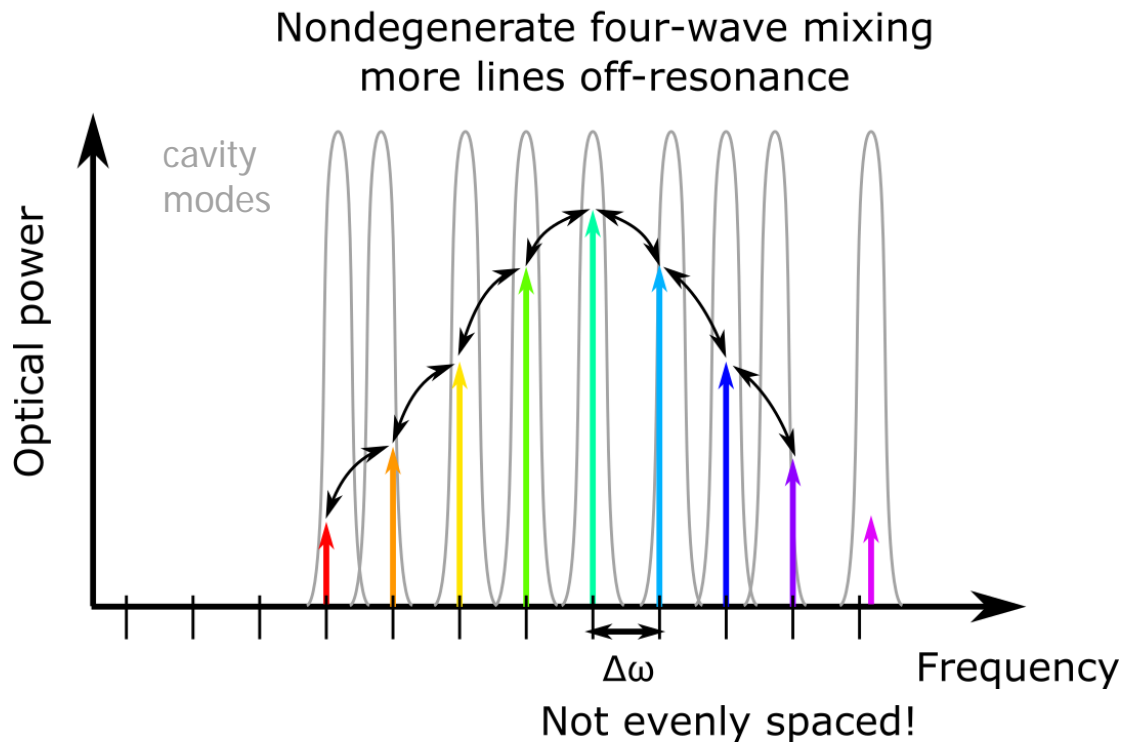
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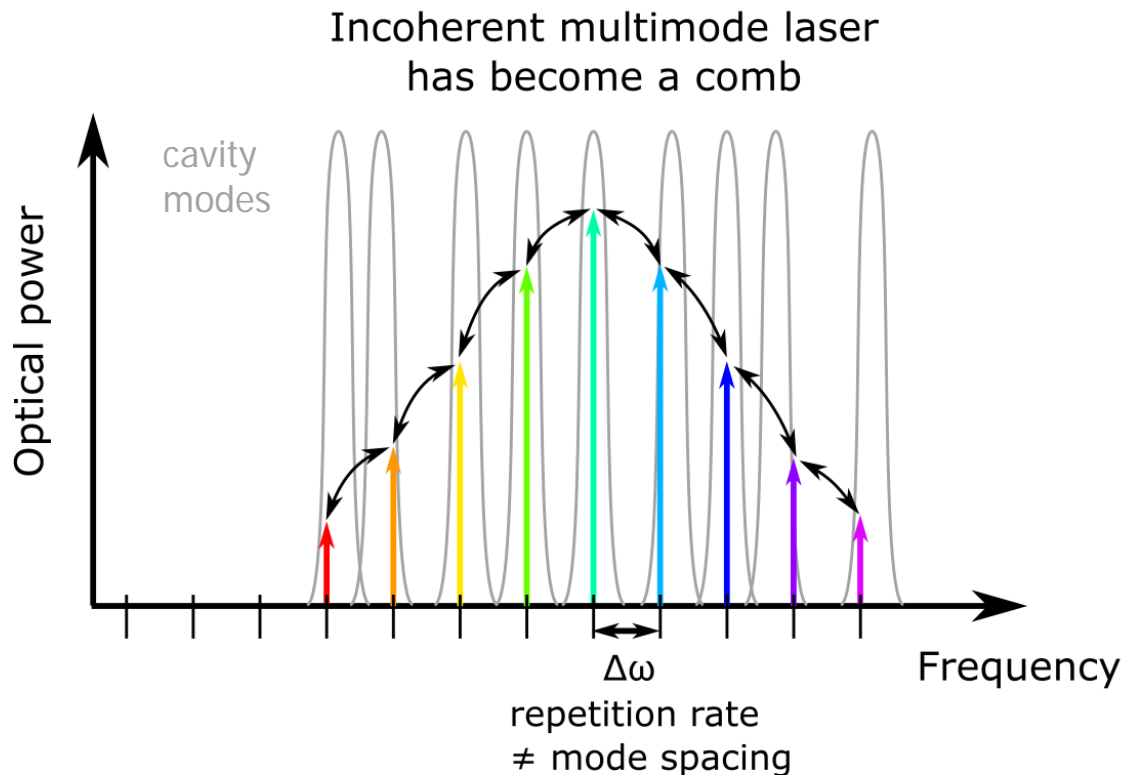
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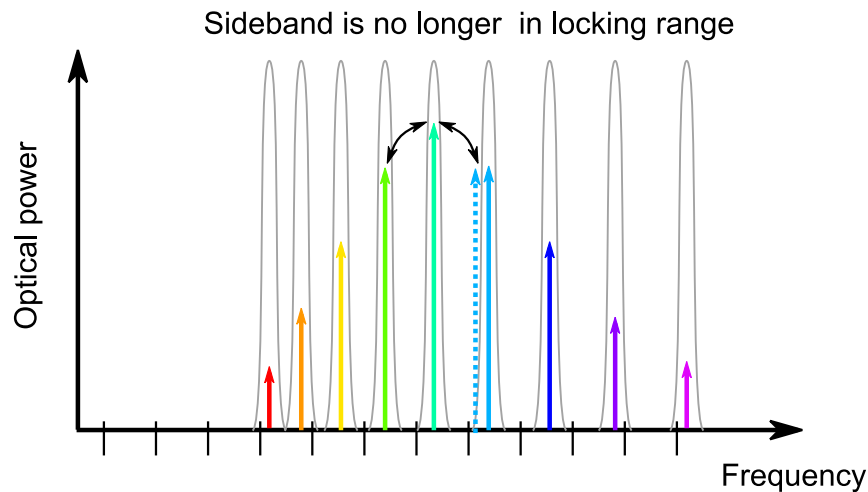
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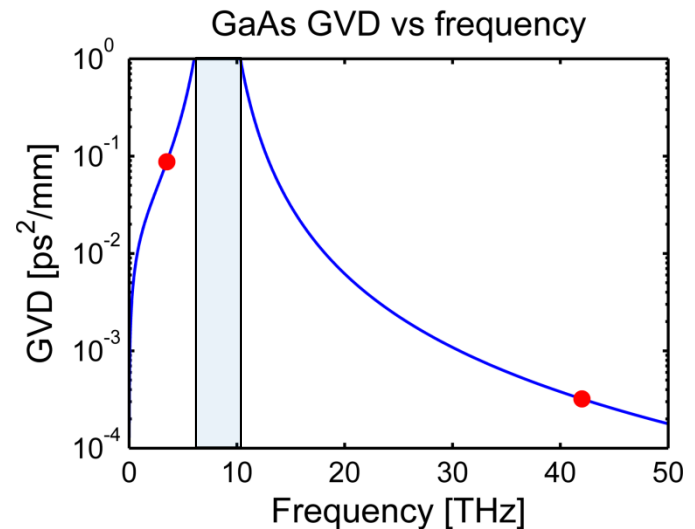
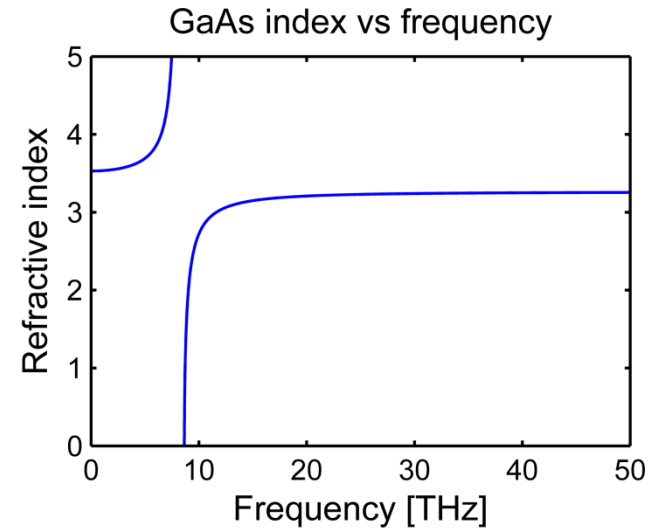
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- As group velocity dispersion (GVD) increases, modes are more and more non-uniform
- Four-wave mixing is too far off-resonance, injection locking cannot occur

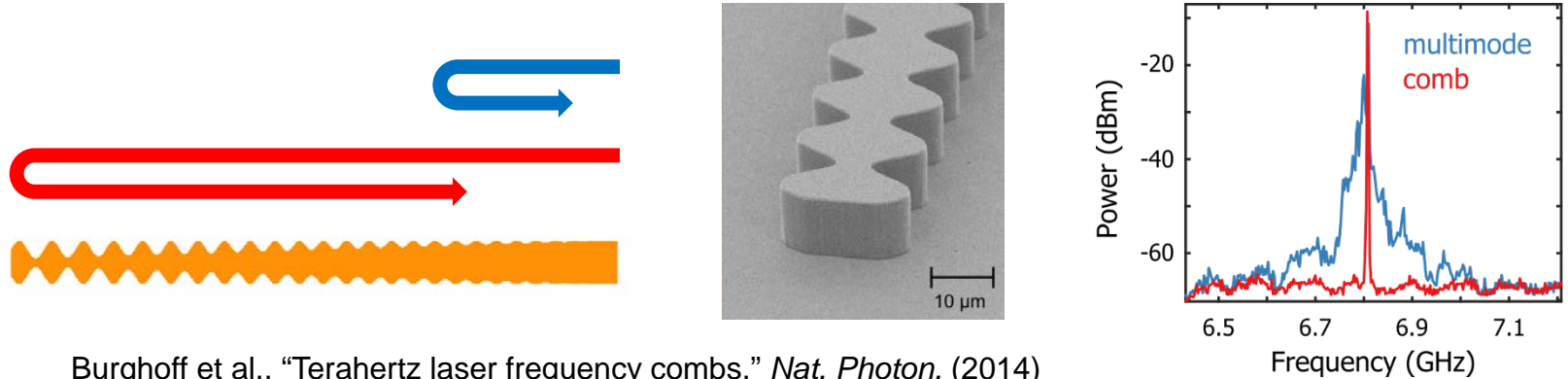
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- III-V materials are particularly dispersive in THz
  - GaAs at 3.5 THz: 87,400 fs<sup>2</sup>/mm
  - Frequencies separated by 1 THz will slip by  $\lambda/4$  after only 130  $\mu\text{m}$ !



# Combs enabled by dispersion engineering

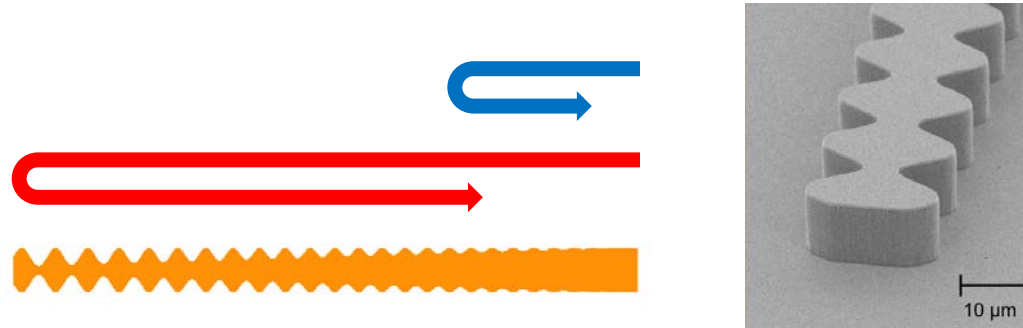
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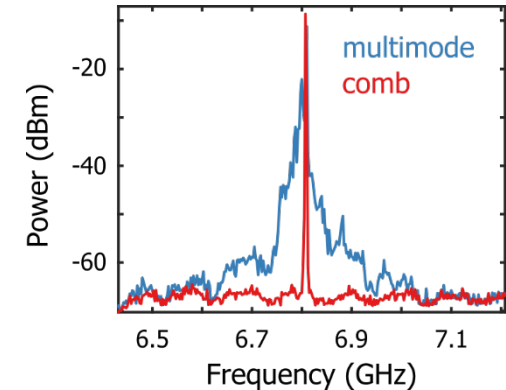
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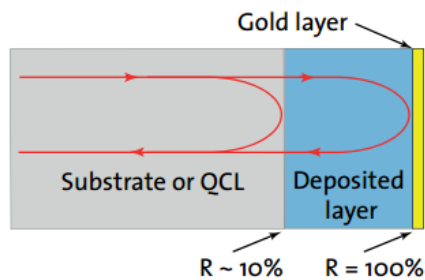
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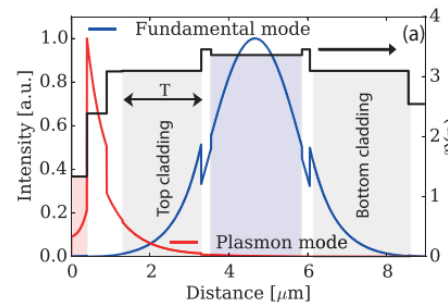
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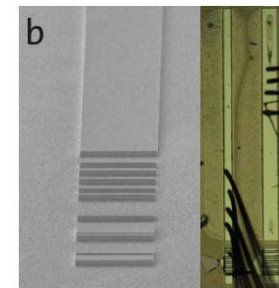
- Other GVD compensation schemes in QCLs:



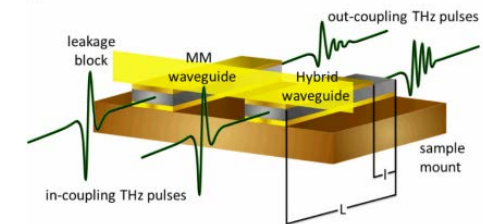
Villares et al., *Optica* (2016)



Bidaux et al., *Opt. Lett.* (2017)



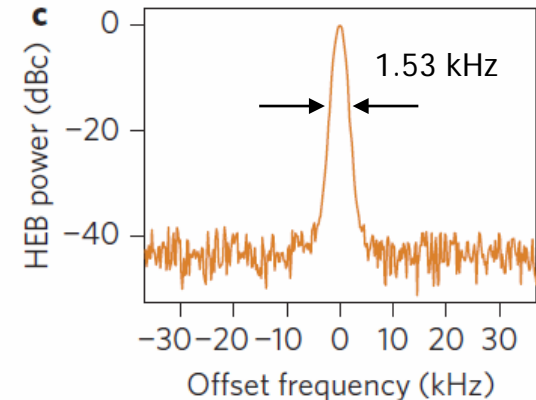
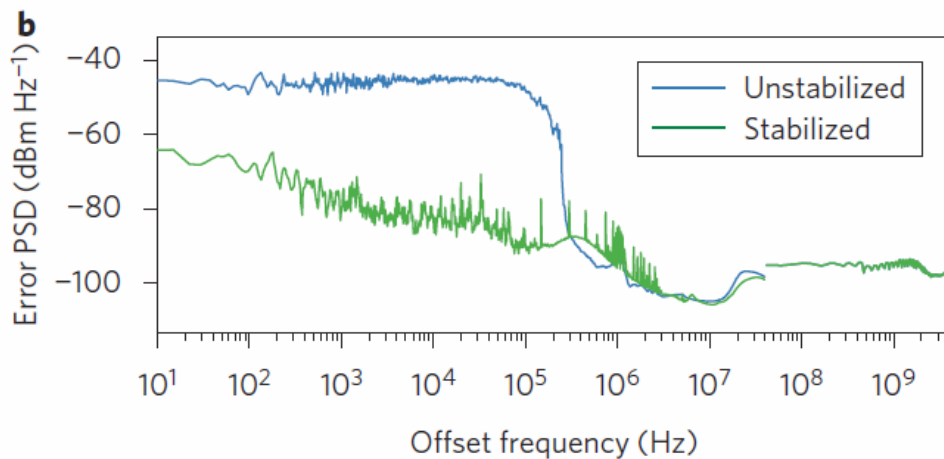
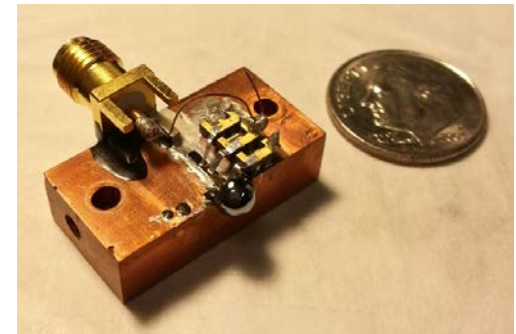
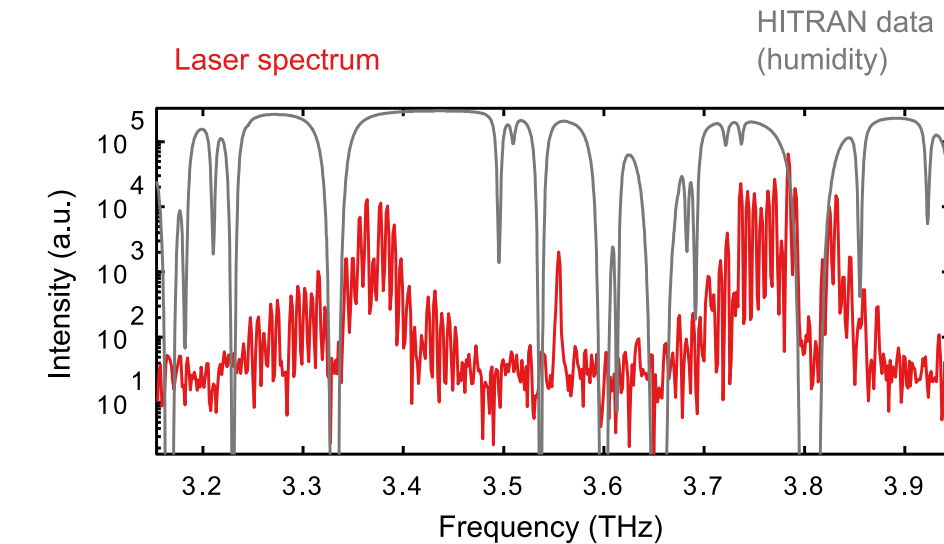
Faist et al., *Nanophotonics* (2015)



Fobbe et al., *Opt. Express* (2016)

# Basic results: spectra

- Properly-compensated laser generates broadband spectrum, narrow beatnote when CW-biased



Burghoff et al., *Nat. Photon.* (2014)

# Spectrally-resolved coherence measurement

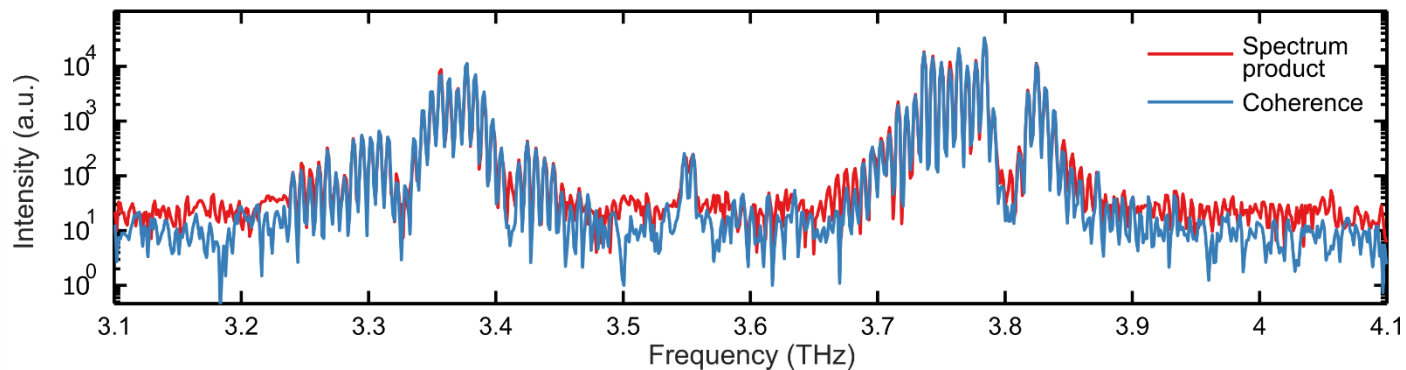
- Can use an interferometer to directly measure first-order coherence...

$$g_{\pm}(\omega) \equiv \frac{|\langle E^*(\omega)E(\omega \pm \Delta\omega) \rangle|}{\sqrt{\langle |E(\omega)|^2 \rangle \langle |E(\omega \pm \Delta\omega)|^2 \rangle}}$$

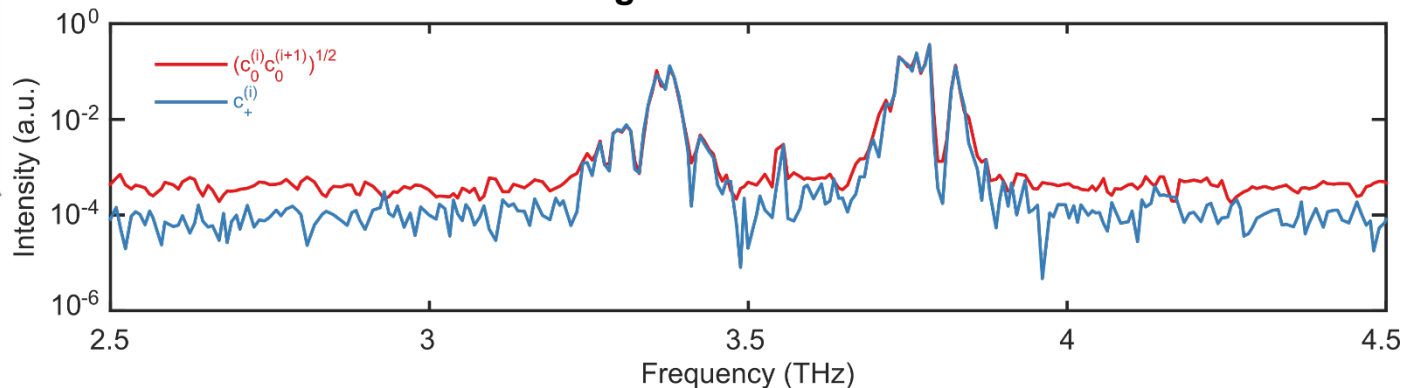
← coherence  
← spectrum

- Dispersion-compensated THz QCL comb

Raw data



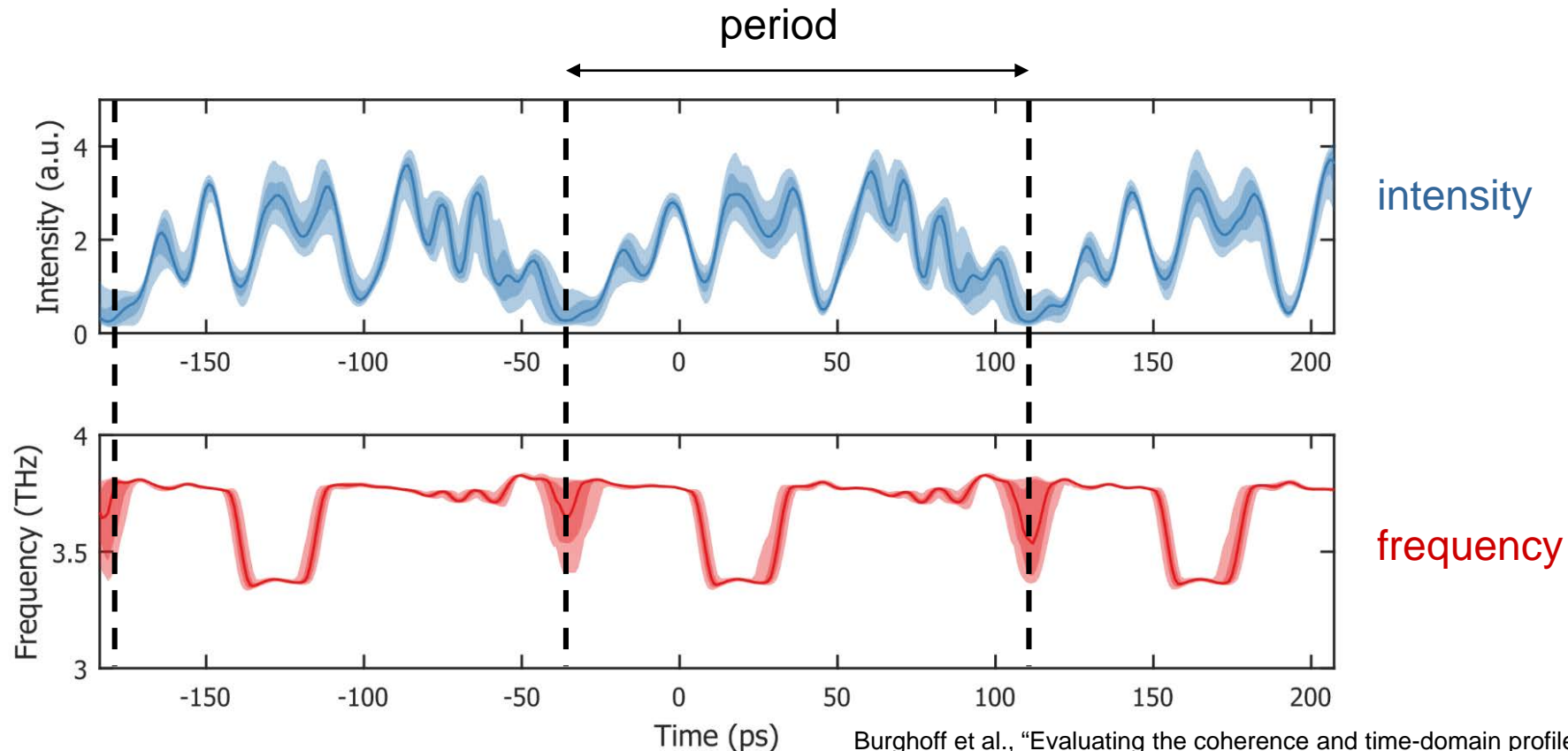
Degree of coherence



FTS deconvolution



# Temporal properties of QCL combs

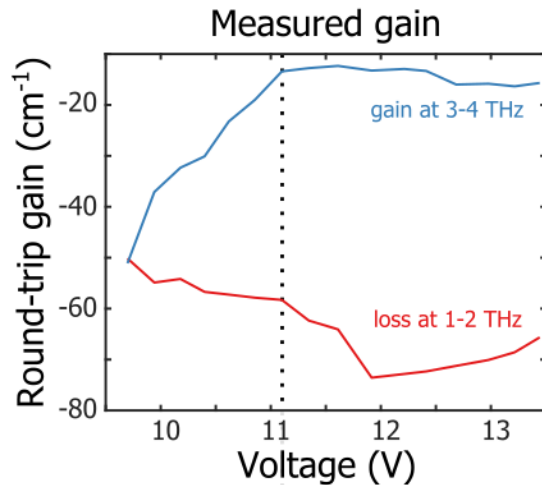


- Instantaneous intensity and frequency are **periodic**, but not a pulse
- Simultaneous AM and FM, not conventional mode-locking
  - QCL dynamics preclude mode-locking (see Khurgin et al, APL (2014))

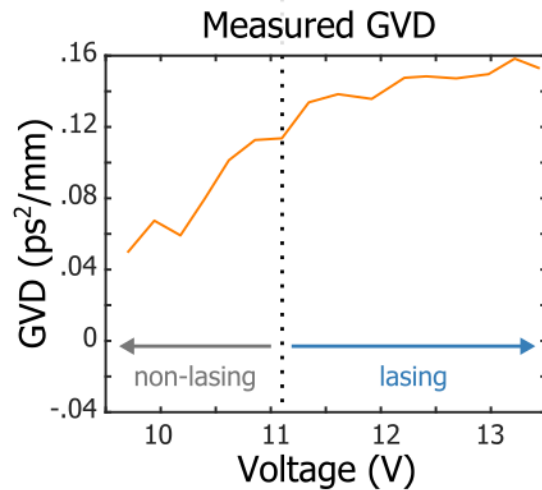
Theory:

Tzenov, Jirauschek et al., *Opt. Express* (2016)  
Tzenov, Jirauschek et al., *IEEE THz* (2017)  
Henry, Khurgin et al., *Opt. Eng.* (2017)

# Bias dependence of dispersion above threshold



**Gain:** clamps to constant value above threshold



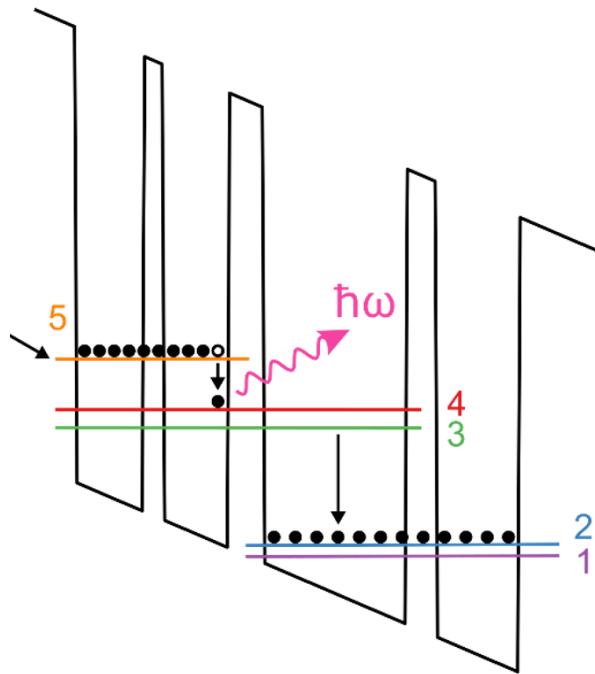
**Dispersion:** does *not* clamp above threshold in QCLs  
**Lineshape changes with bias, changing dispersion**

Limits the dynamic range of comb formation



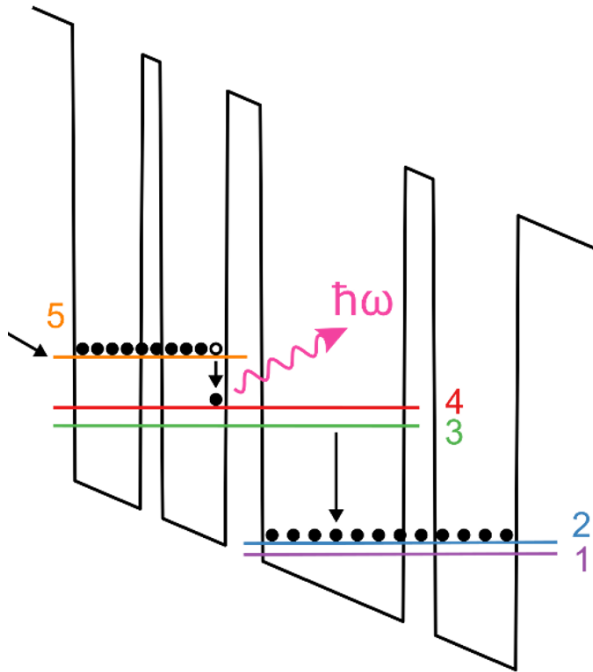
# Intracavity detection

- QCLs can act as detectors as well as lasers
  - Current through QCL changes due to stimulated emission

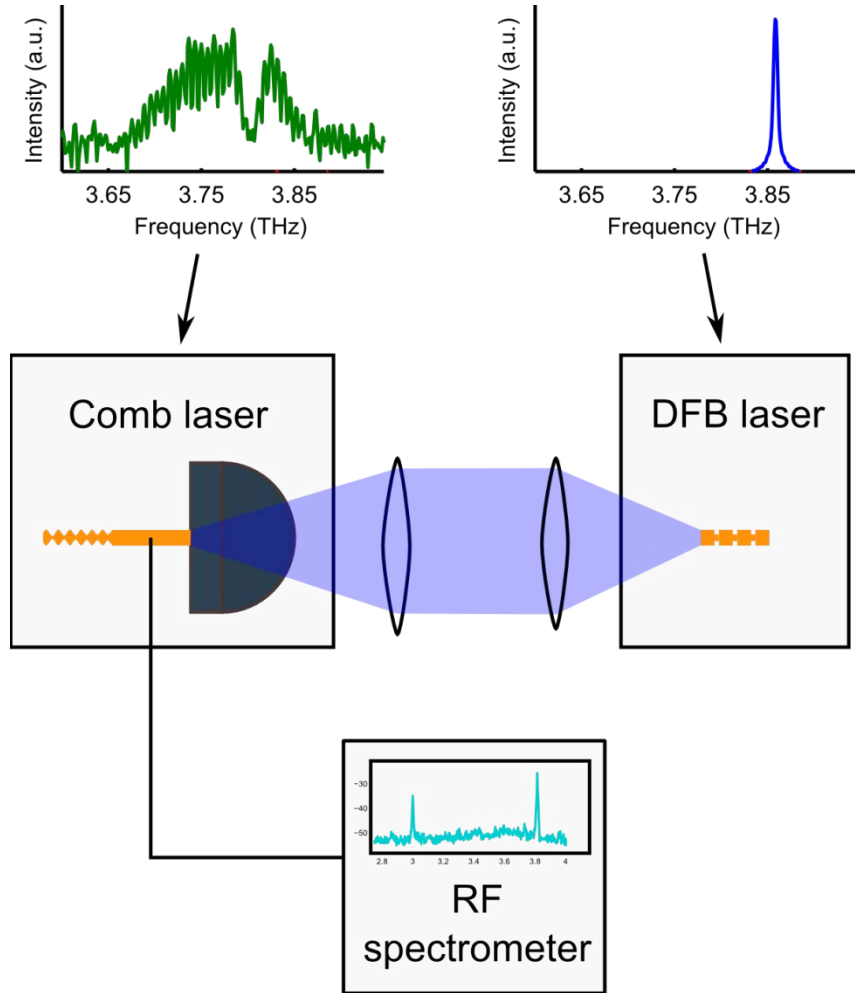


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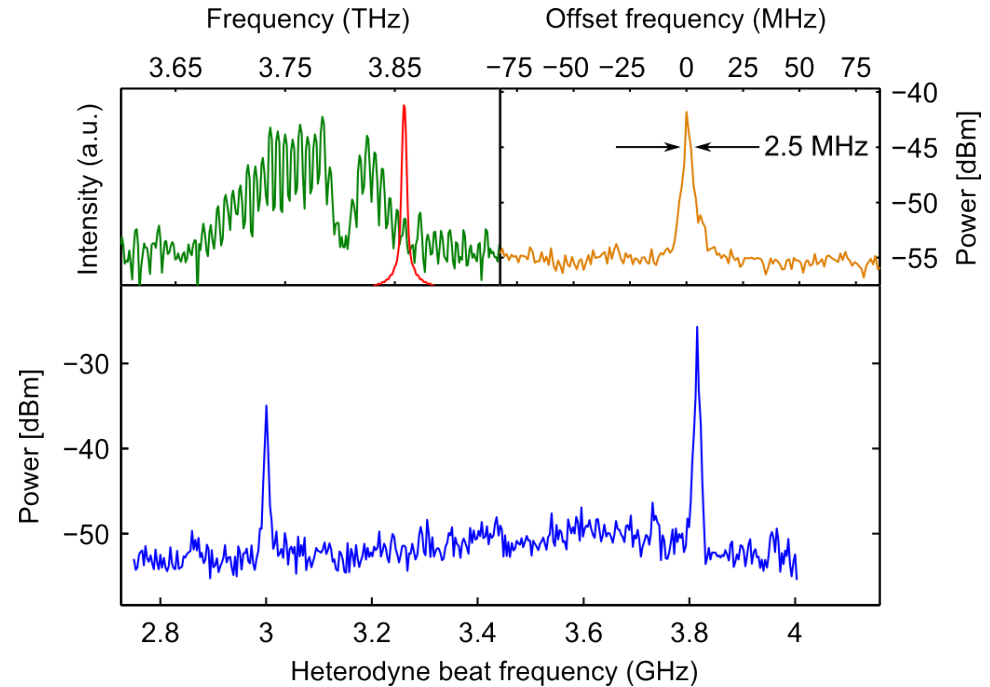


- Injecting another laser allows the difference frequency to be detected



# Intracavity detection (2)

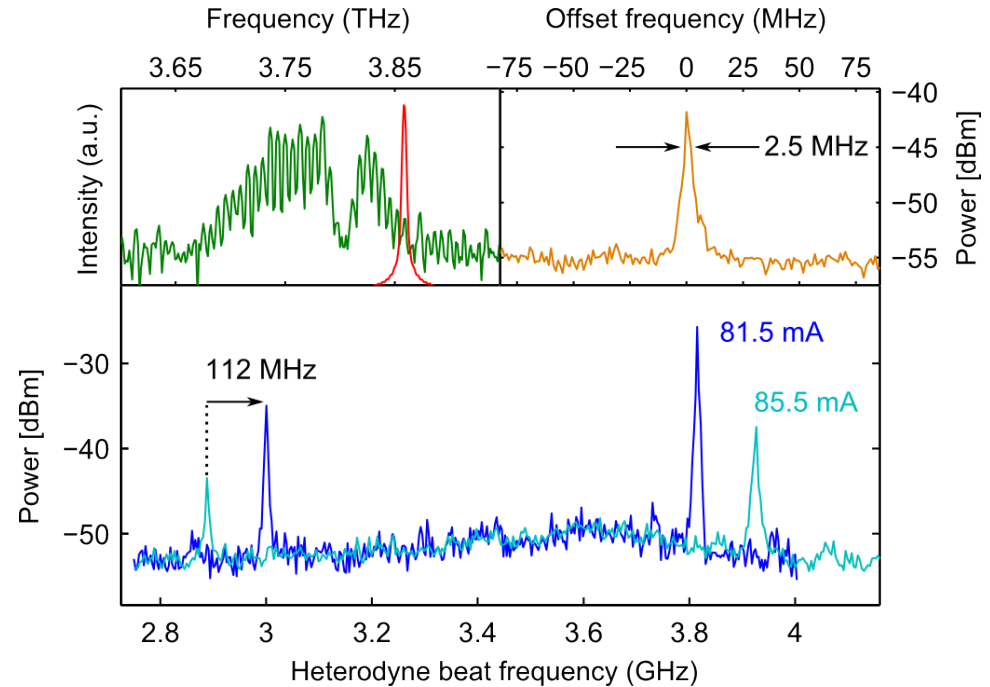
- Inject light from a narrowband (DFB) laser into comb cavity and measure intracavity beating between them
- Two beatnotes sum to the repetition rate, tune with DFB
- SNR limited by shot noise of QCL
  - NEP  $\sim nW/\sqrt{Hz}$  (similar to pyroelectric detection)
  - Equivalent joint power here  $\sim 10 \mu W$



Burghoff et al., "Terahertz laser frequency combs," *Nat. Photon.* (2014)

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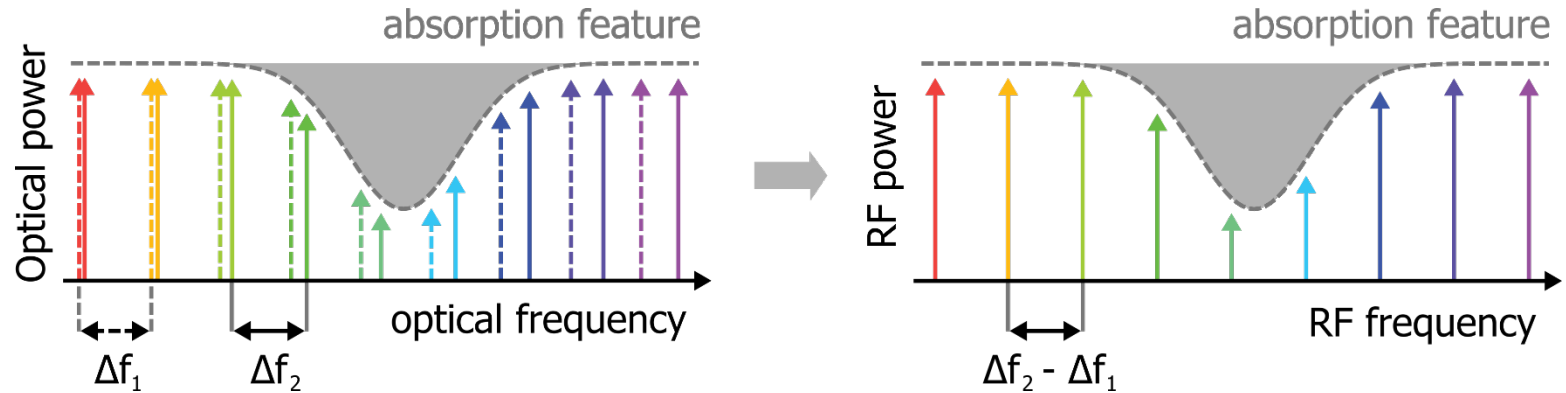
Burghoff et al., "Terahertz laser frequency combs," *Nat. Photon.* (2014)

## Part III

# Multiheterodyne spectroscopy based on terahertz QCLs

# Dual comb spectroscopy reminder

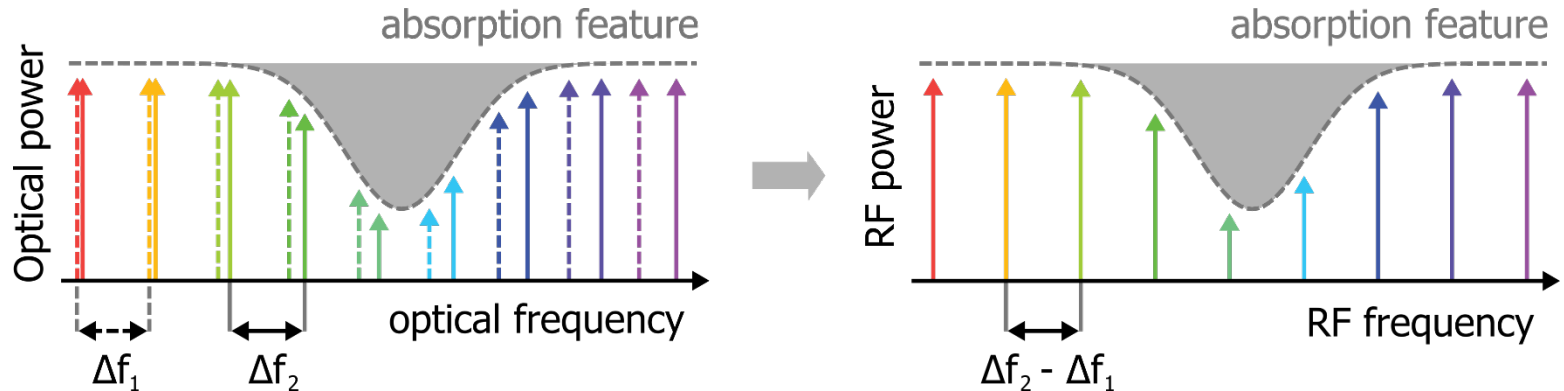
- Two combs, with slightly different spacings, shined on a detector.  
**Electrical** spectrum encodes **optical** spectrum:



- Two optical combs beat together to produce a comb at radio frequencies (MHz)
  - Typically,  $\Delta f_i \sim 10$  GHz and  $\Delta f_1 - \Delta f_2 \sim 10$  MHz

# Dual comb spectroscopy reminder

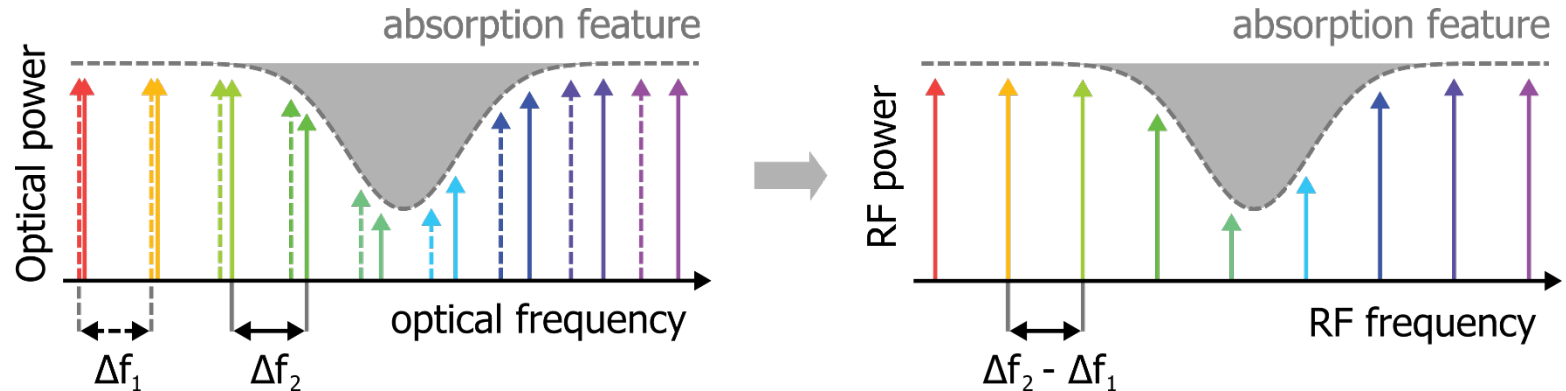
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  - van der Weide, Murakowski, Keilmann, *IEEE TMTT* (2000)

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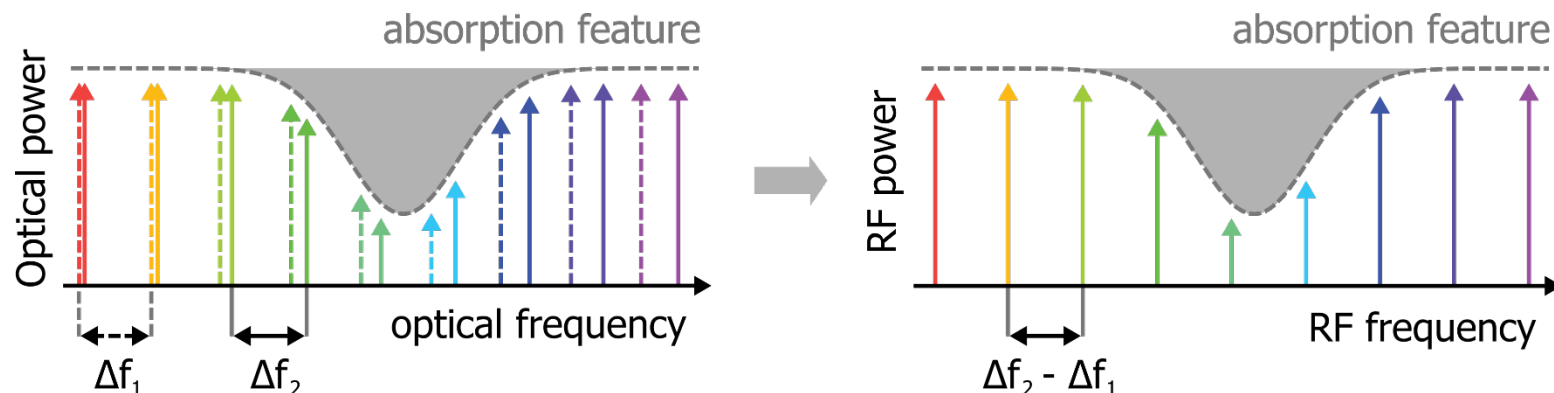


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- Most work at NIR with mode-locked lasers
  - Review from NIST: Coddington et al., *Optica* (2016)



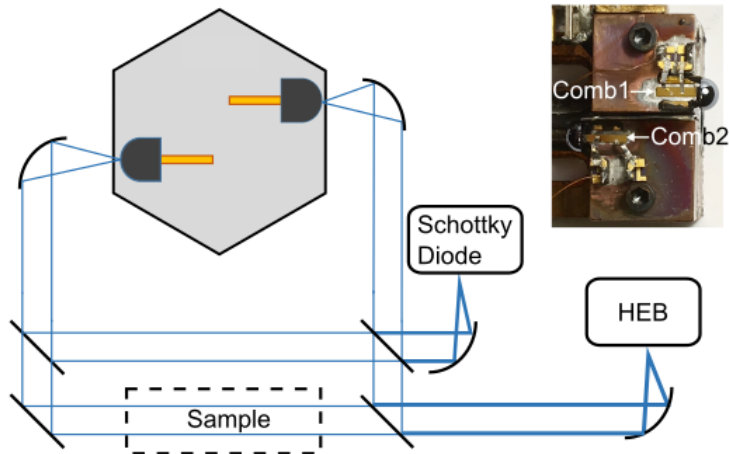
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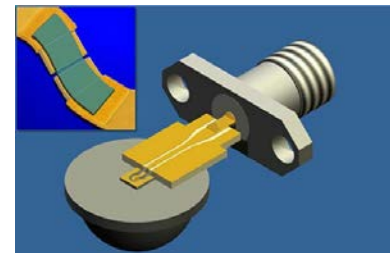


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- Most work at NIR with mode-locked lasers
  - Review from NIST: Coddington et al., *Optica* (2016)
- Mid-IR QCLs:
  - Wang, Wysocki, et al., *APL* (2014)
  - Villares, Faist, et al., *Nat. Comm.* (2014)

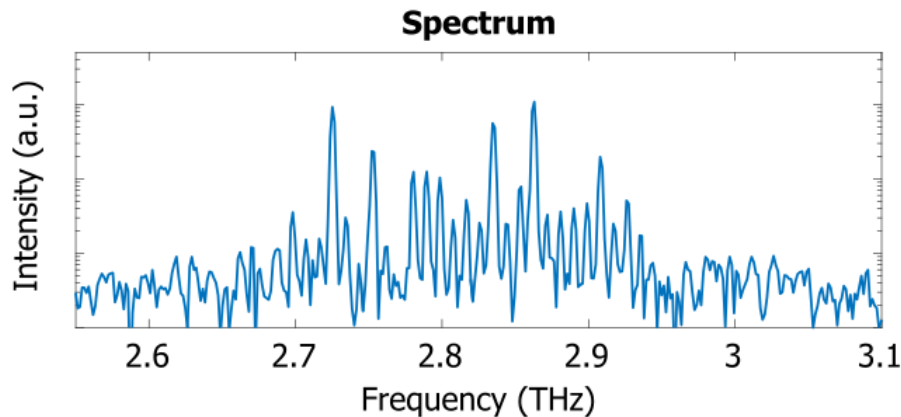
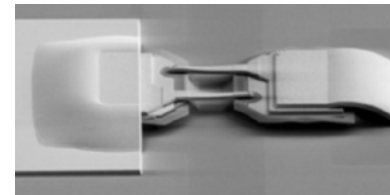
# THz QCL dual comb spectroscopy



**Detector 1:** HEB  
(superconducting  
bolometer)

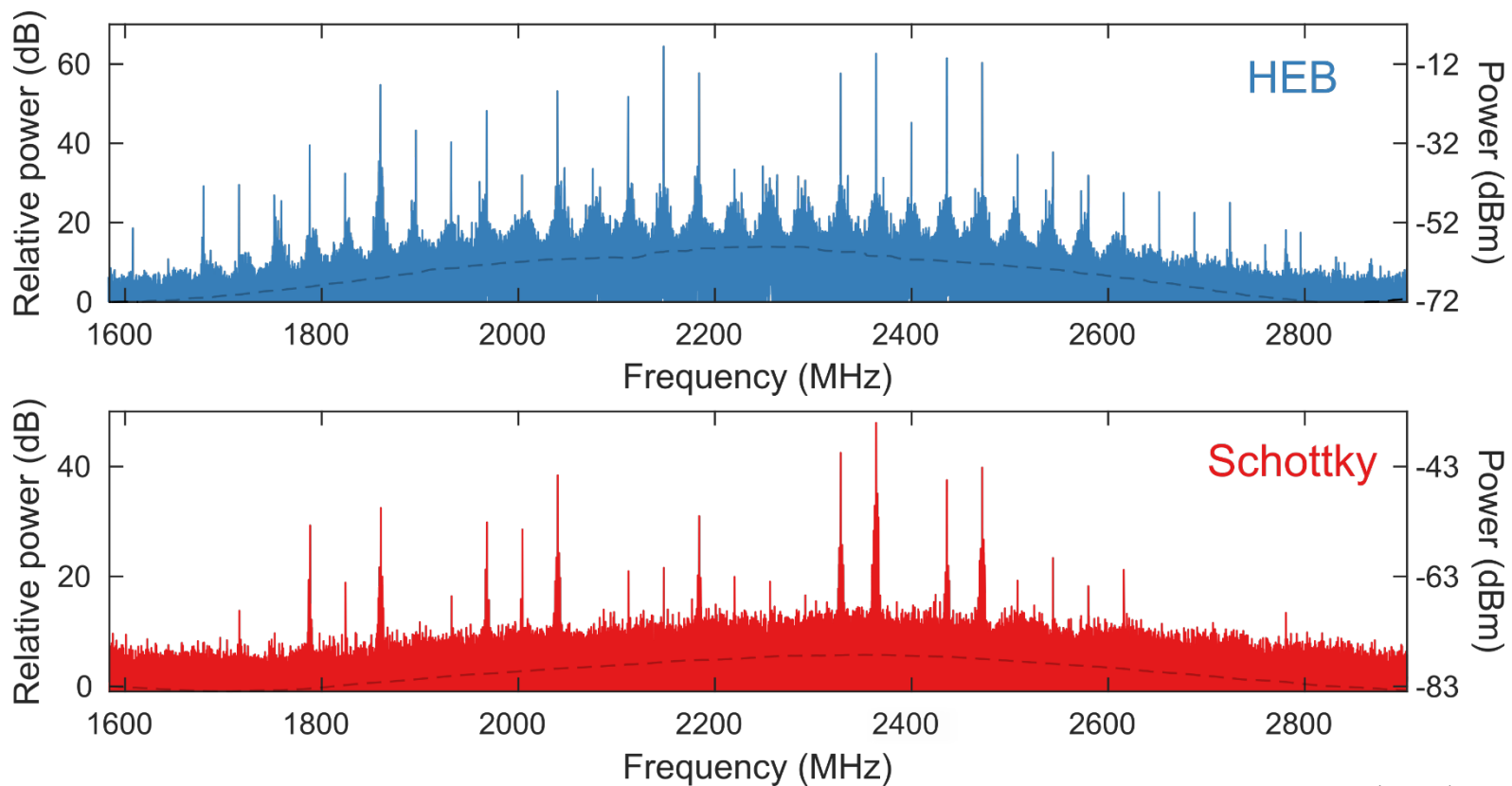


**Detector 2:** Schottky  
mixer (room-temperature)



Yang, Burghoff et al., "Terahertz multiheterodyne spectroscopy using laser frequency combs," *Optica* (2016)

# Example dual comb signals, 100 $\mu$ s integration

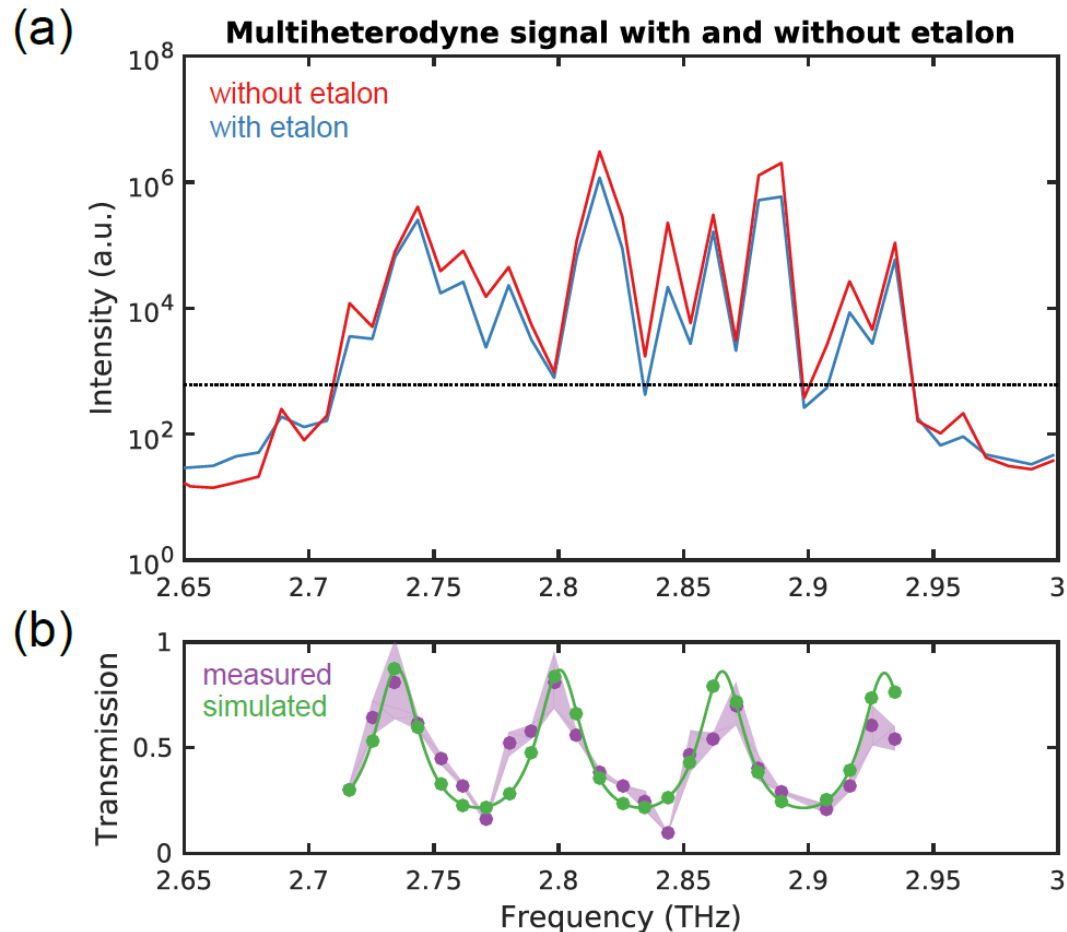


Yang, Burghoff et al., *Optica* (2016)

- HEB: Hot electron bolometer from J.R. Gao
  - Zhang, Gao, et al, "Quantum noise in a terahertz hot electron bolometer mixer," APL (2010)
- Schottky mixer: Virginia Diodes WR-0.34HM

# Broadband etalon sample

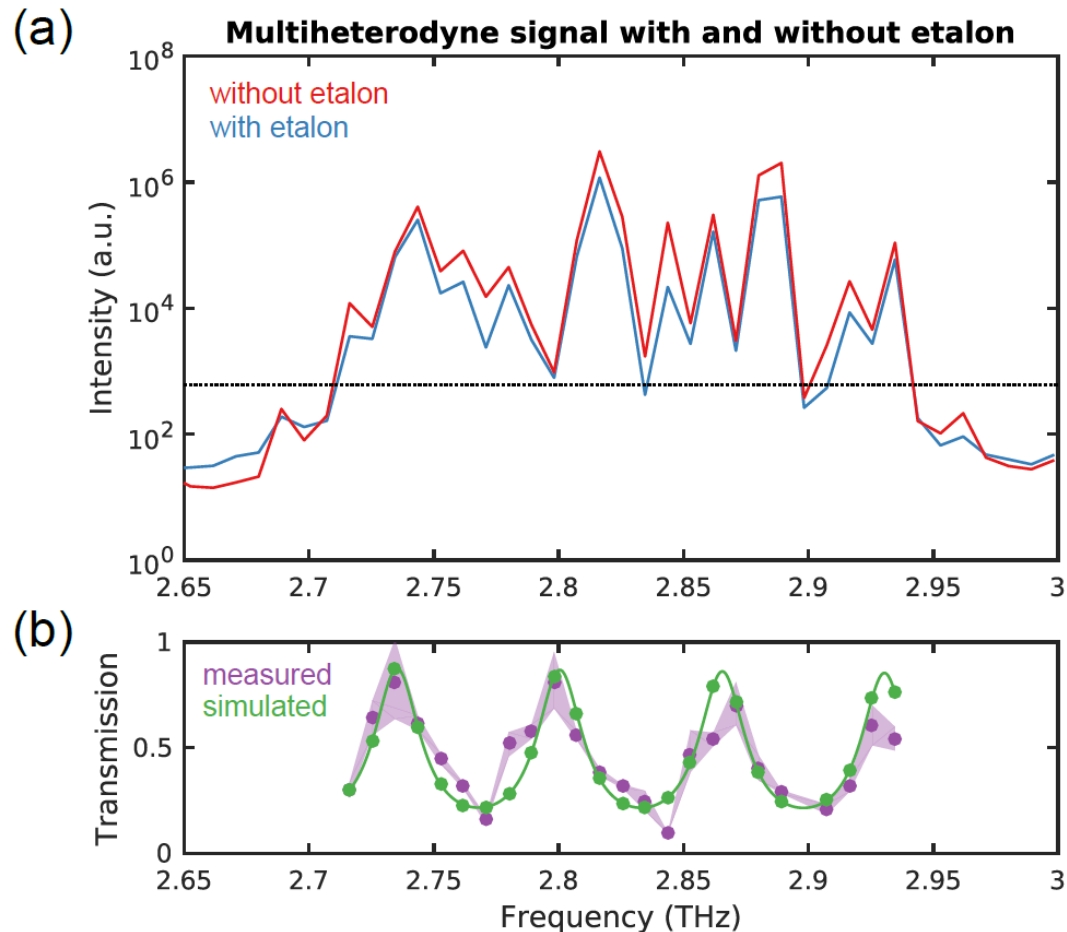
- Etalon transmission measurement
  - 625  $\mu\text{m}$  thick undoped GaAs etalon



Yang, Burghoff et al., *Optica* (2016)

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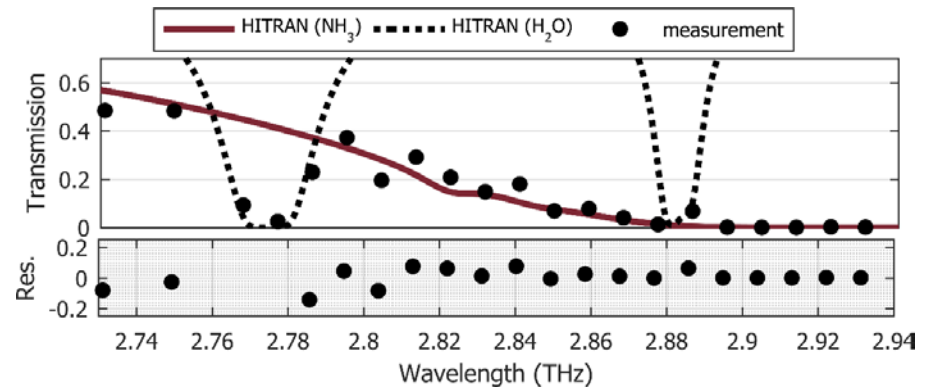
Current limitations:  
non-uniformity of comb  
+ detector nonlinearity

Yang, Burghoff et al., *Optica* (2016)

# Gas spectroscopy

- Collaboration with Gerard Wysocki's group at Princeton (Jonas Westberg and Lukasz Sterczewski)

- Ammonia
- 460 Torr
- 500  $\mu$ s acquisition time
- 220 GHz of coverage at 2.84 THz
- Water absorption highlighted



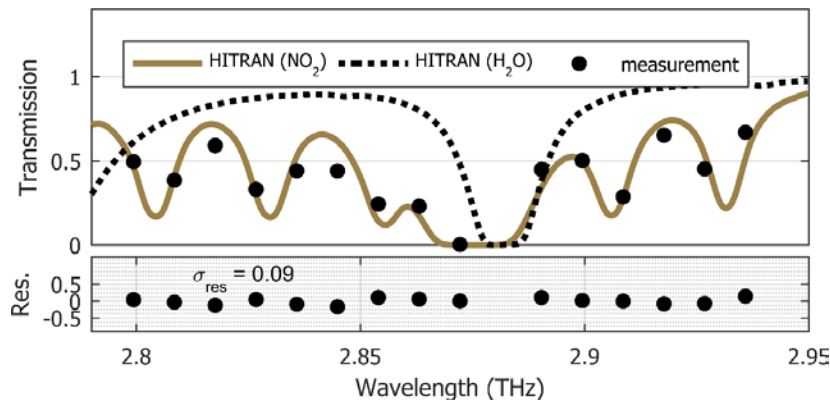
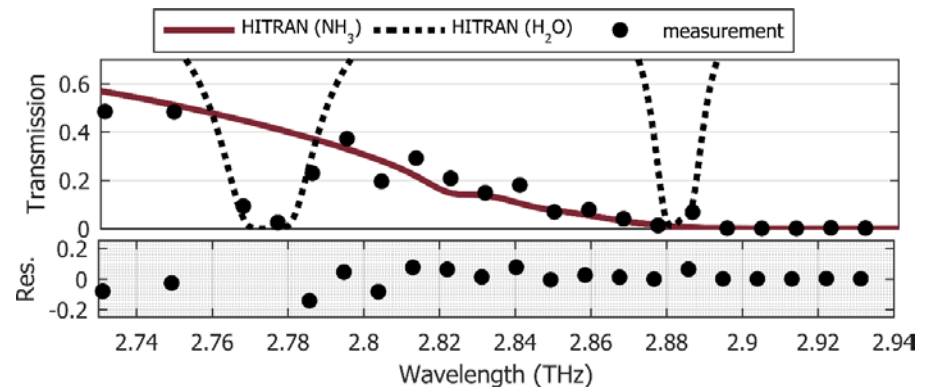
Sterczewski, Wysocki *et al.*, "Terahertz multiheterodyne spectroscopy with quantum cascade lasers – a feasibility study," in *International Conference on Infrared, Millimeter and Terahertz Waves* (2017).

Westberg, Wysocki, et al., "Broadband mid-infrared and THz chemical detection with quantum cascade laser multi-heterodyne spectrometers" in Proc. SPIE 10210, Next-Generation Spectroscopic Technologies (2017).

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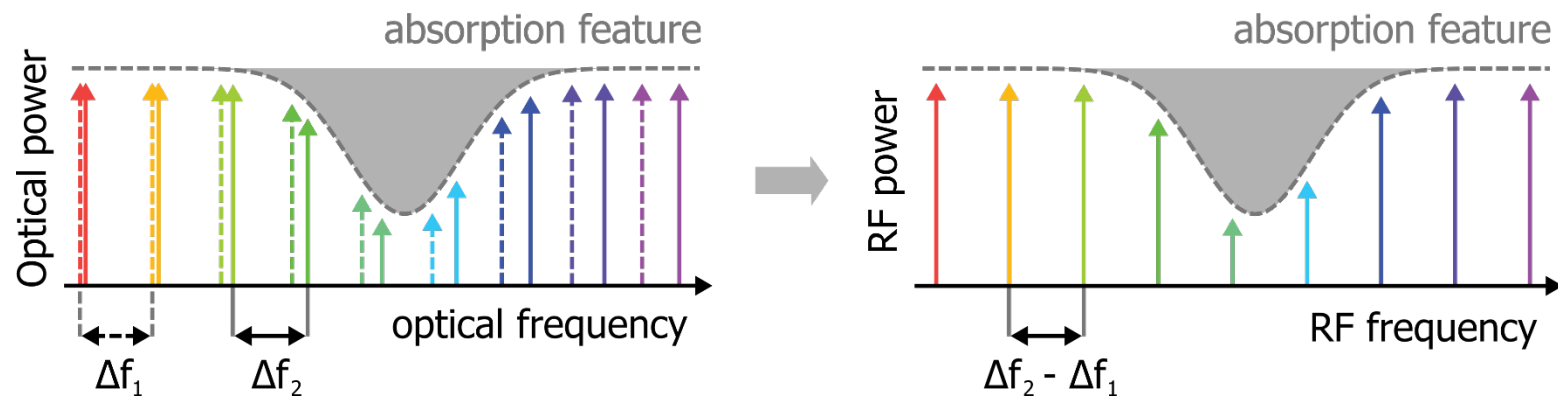
- Nitrogen dioxide (NO<sub>2</sub>)
- 840 Torr
- 500  $\mu$ s acquisition time

Sterczewski, Wysocki *et al.*, "Terahertz multiheterodyne spectroscopy with quantum cascade lasers – a feasibility study," in *International Conference on Infrared, Millimeter and Terahertz Waves* (2017).

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# Influence of phase noise on dual comb measurement

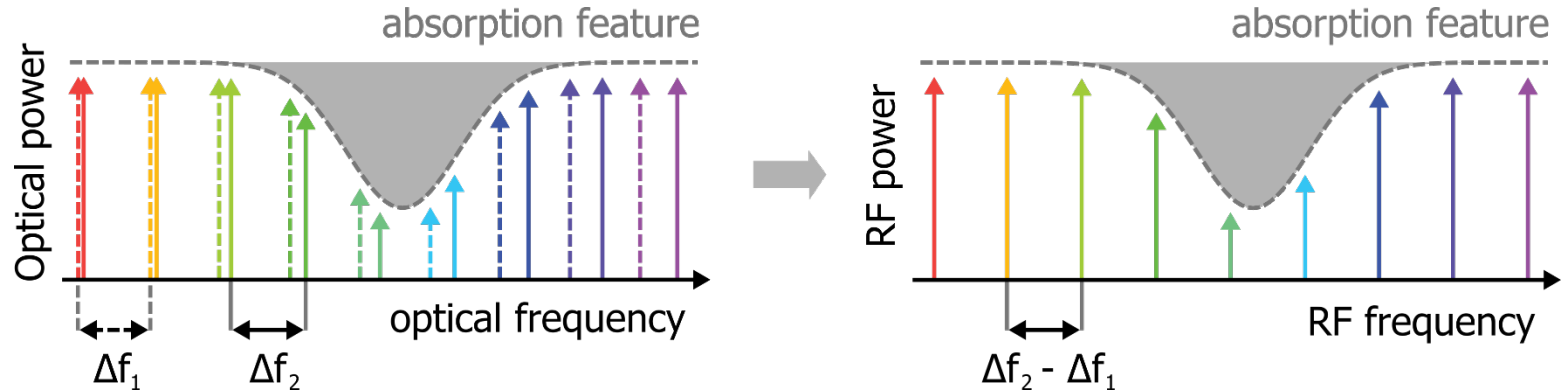
- Cartoon picture of dual comb spectroscopy:



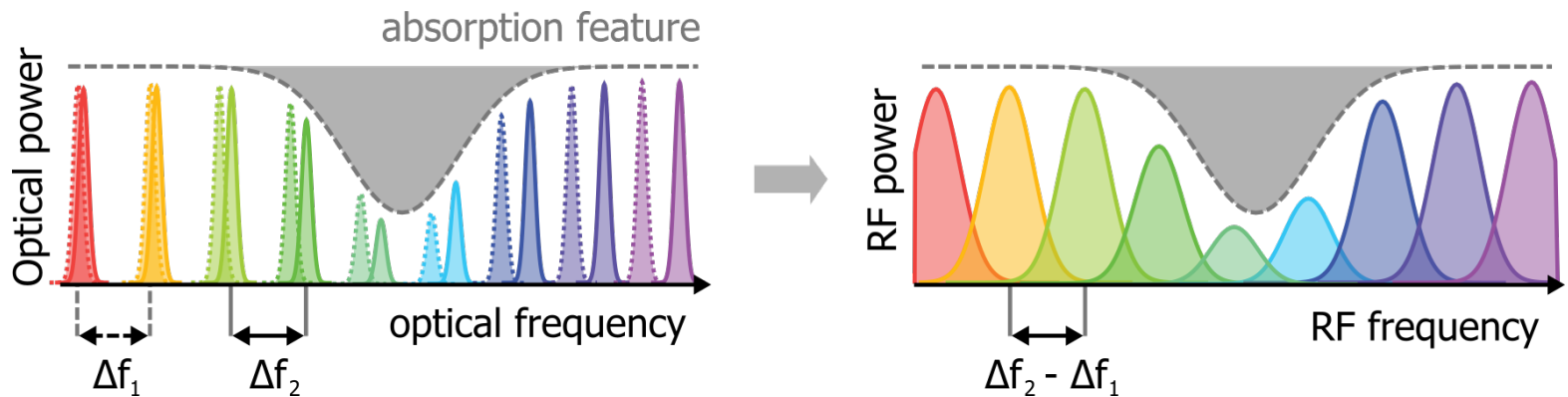


# Influence of phase noise on dual comb spectroscopy

- Cartoon picture of dual comb spectroscopy:

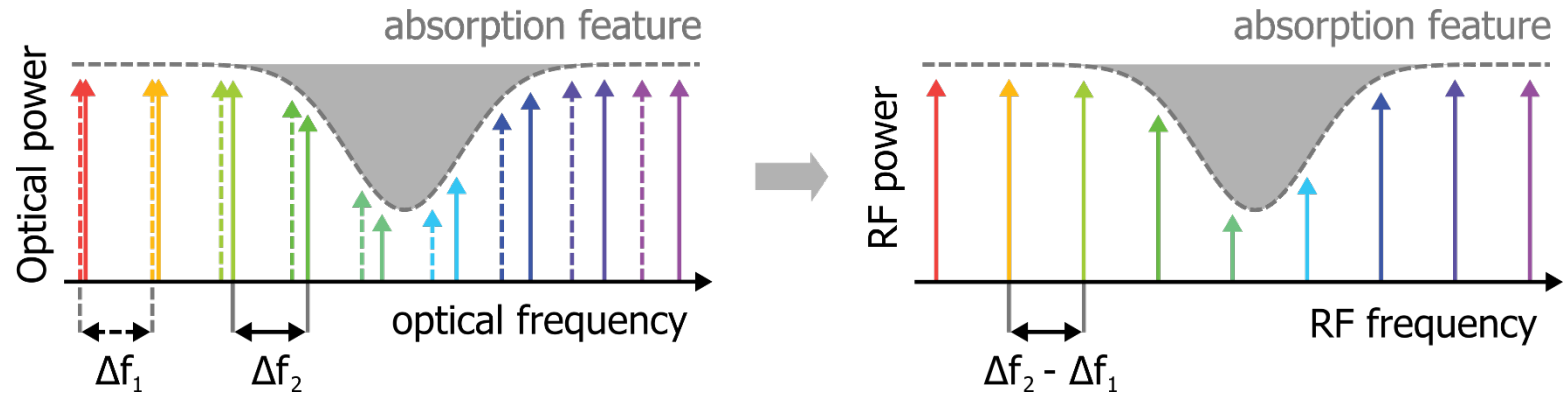


- Real life: some phase noise (feedback, environmental fluctuations, etc.)

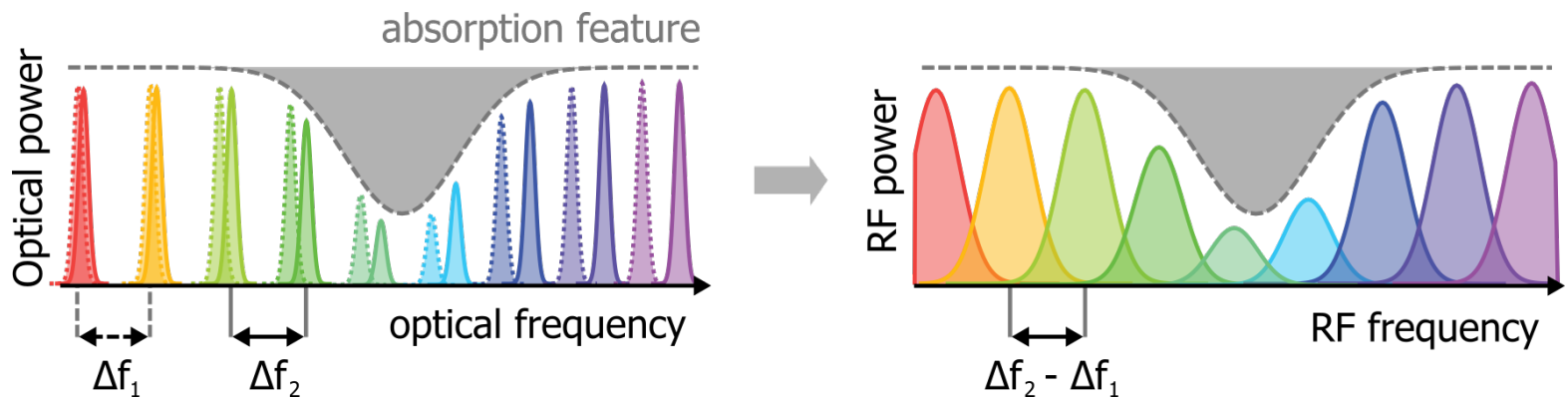


# Influence of phase noise on dual comb spectroscopy

- Cartoon picture of dual comb spectroscopy:



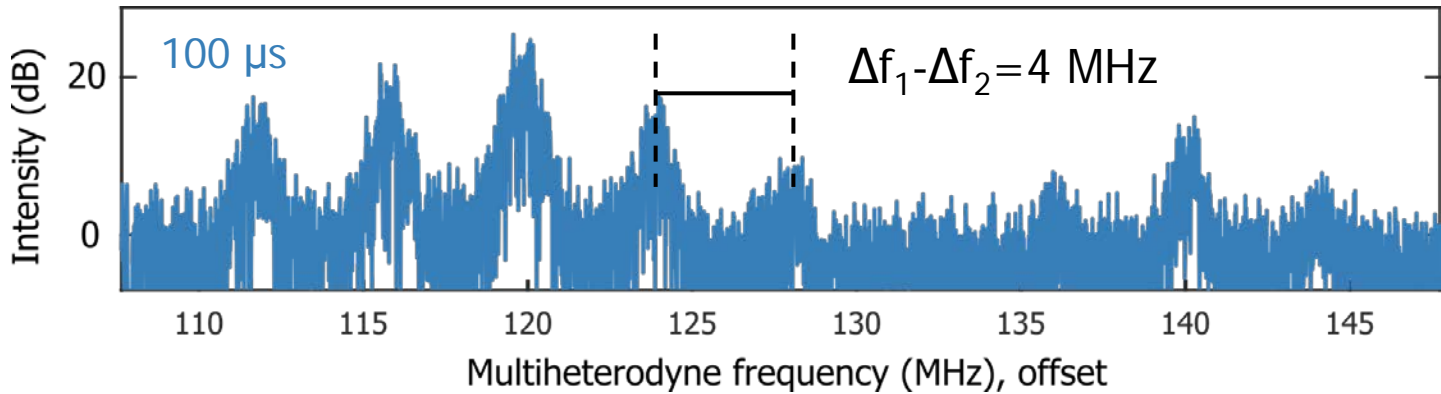
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What happens when there is too much noise?

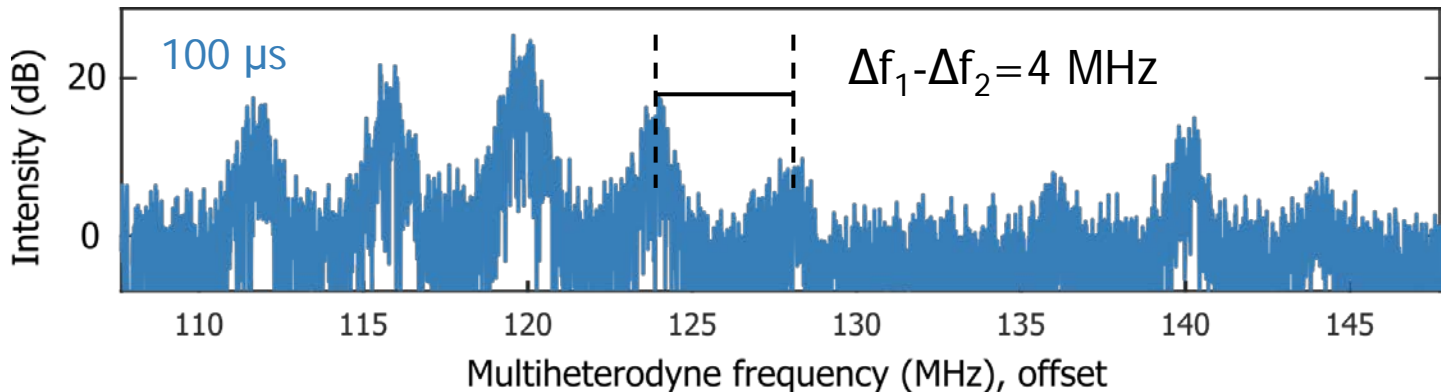
# Effect of phase noise

- Low noise state

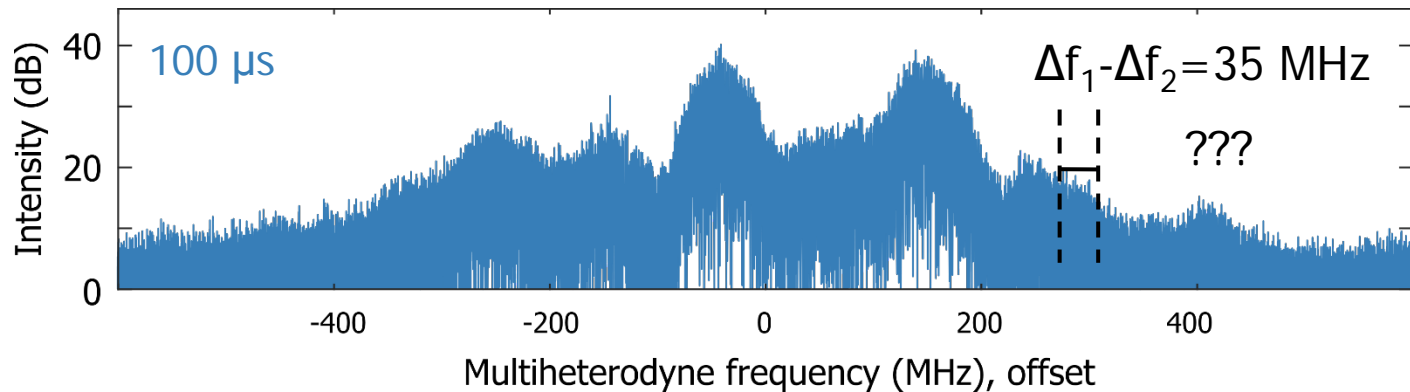


# Effect of phase noise

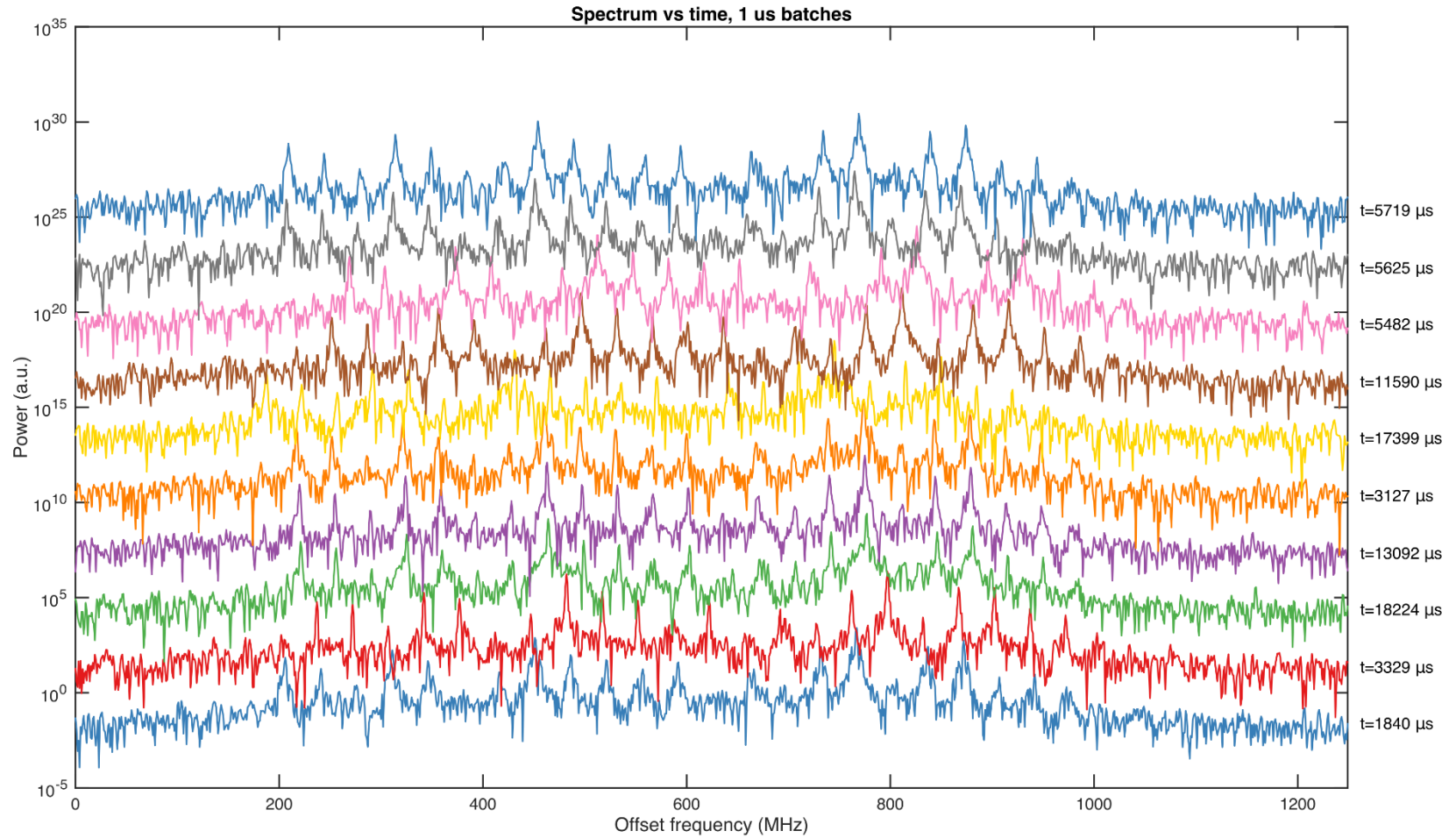
- Low noise state



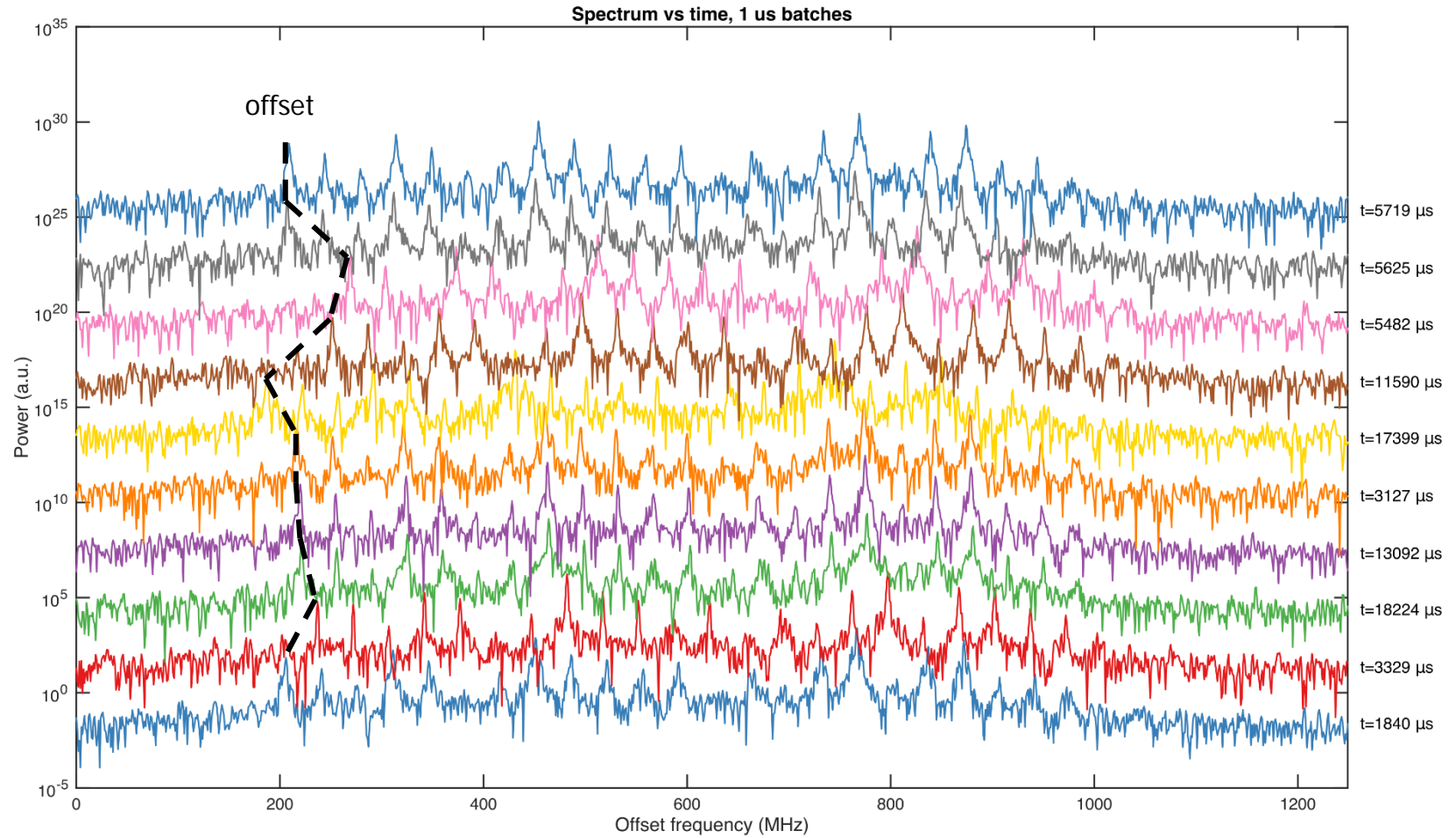
- High noise state (but still comb!)



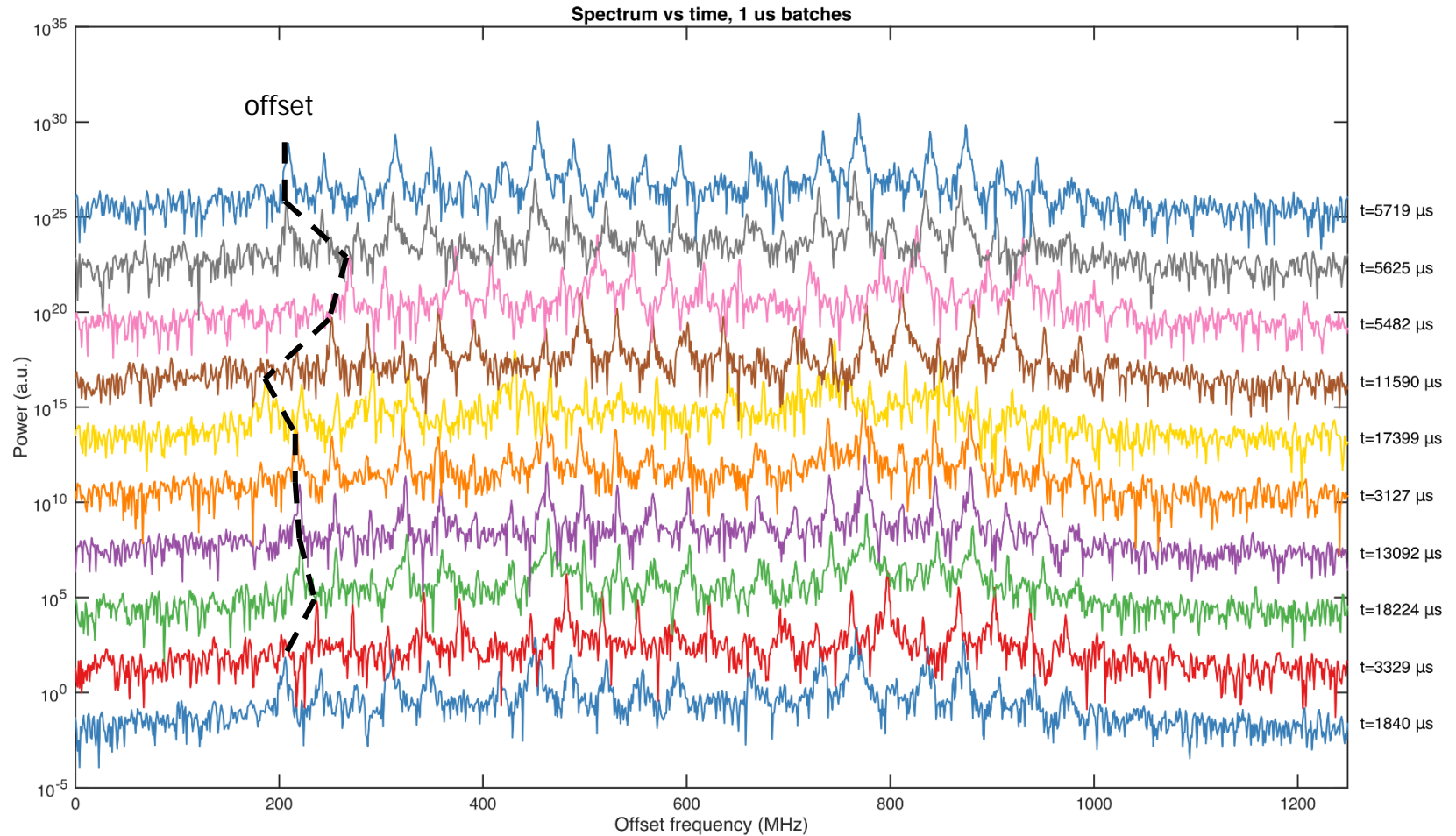
# High noise short timescale spectra



# High noise short timescale spectra

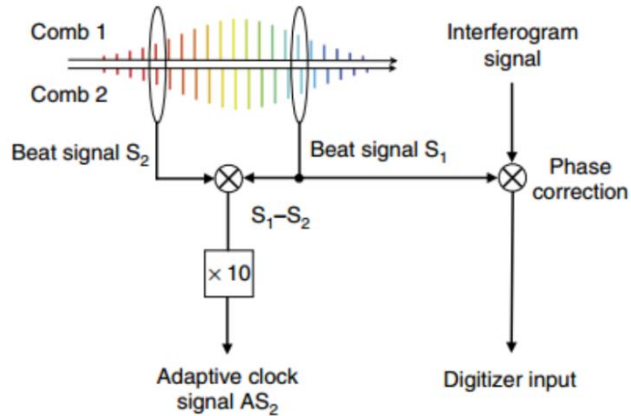


# High noise short timescale spectra

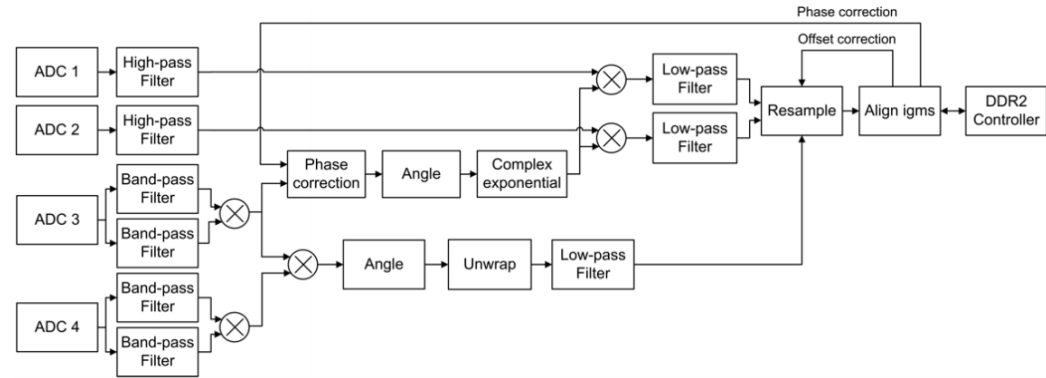


Offset fluctuations  $\sim 3 \cdot$  rep rate spacing

# Adaptive sampling approaches



Ideguchi et al., *Nat. Comm.*, (2014)

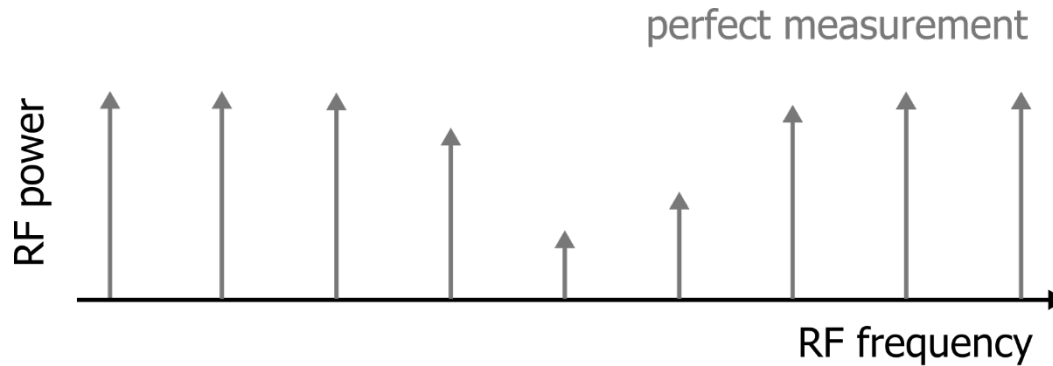


Roy et al., *Opt. Express*, (2012)

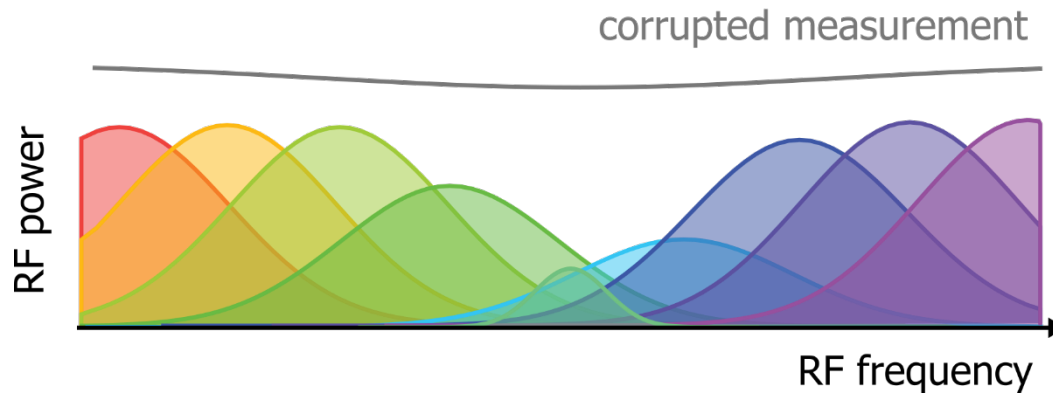
- Mode-locked laser community has done a lot of work on adaptive sampling techniques that correct these effects, but they're challenging at long-wavelengths:
  - Usually detector-noise limited, so no optical power to spare
  - Would like to avoid extra lasers, other optical components



# Can corruption of signal be inverted digitally?

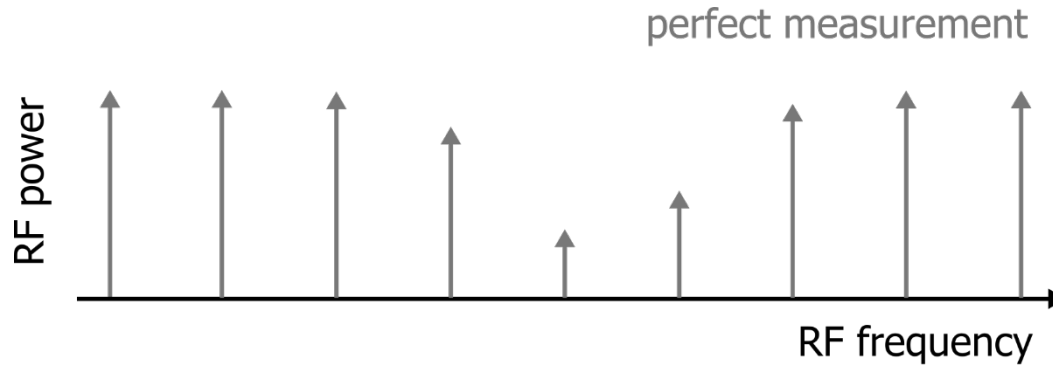


No or low  
phase noise

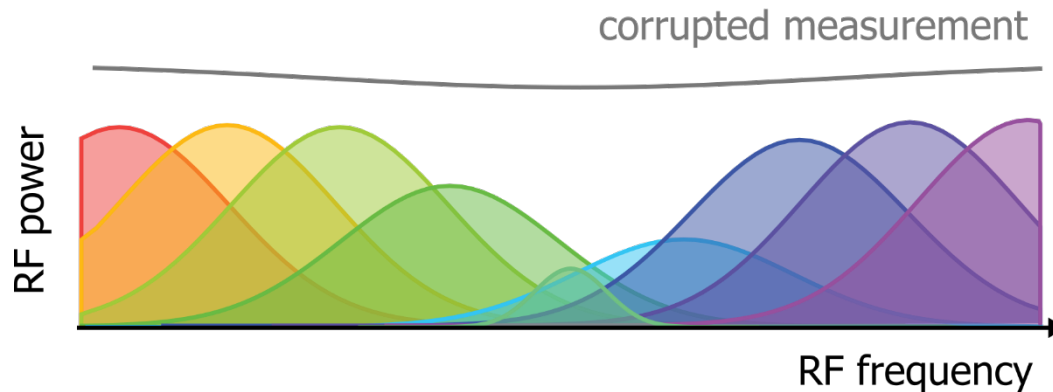


Phase noise large,  
but still **correlated**

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No or low  
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Phase noise large,  
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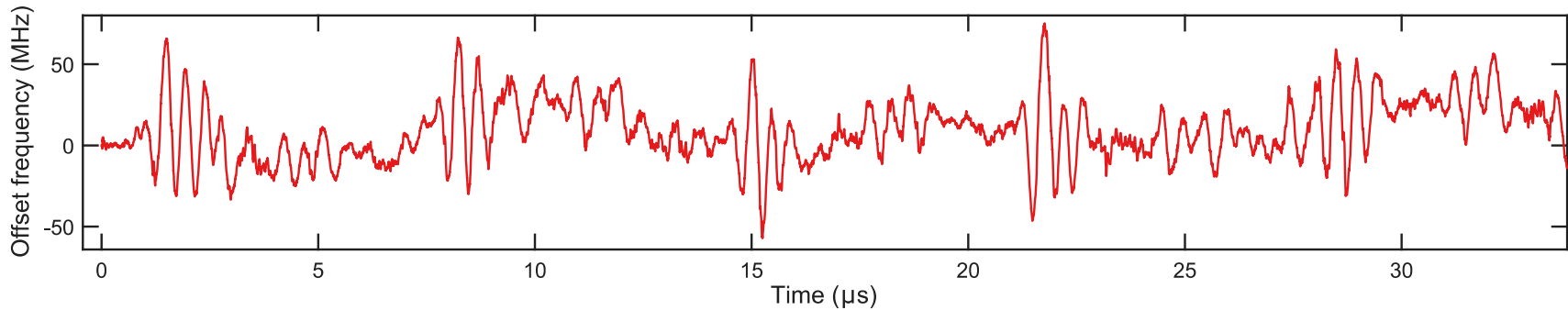
Can this corruption be extracted digitally, without any optical components?

# Extended Kalman filter frequency tracking

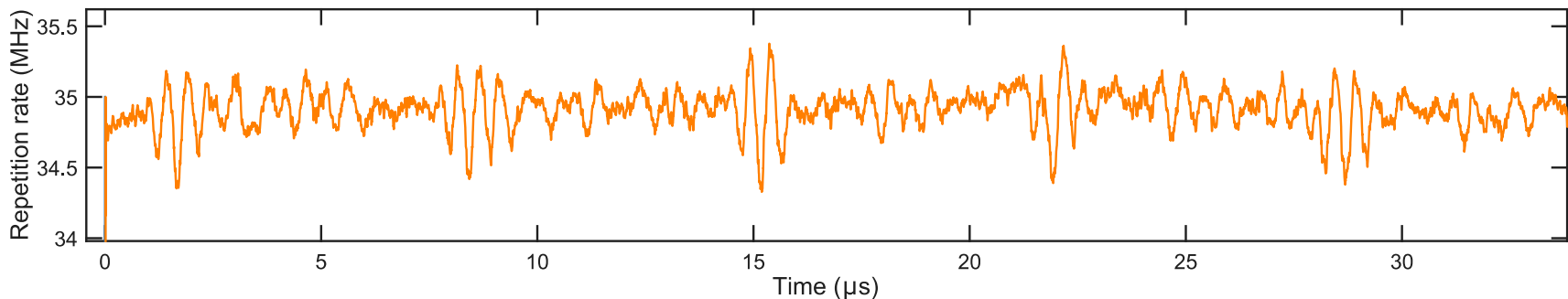
Use Kalman filters to track frequencies (solve a regularized fitting problem):

$$J(\phi_0, \Delta\phi) = \int dt \frac{1}{\sigma^2} \left| y(t) - \sum_n A_n e^{i(\phi_0(t) + n\Delta\phi(t))} \right|^2 + \frac{1}{Q_0} \left( \frac{d\phi_0}{dt} \right)^2 + \frac{1}{Q_\Delta} \left( \frac{d\Delta\phi}{dt} \right)^2$$

## Offset frequency



## Repetition rate



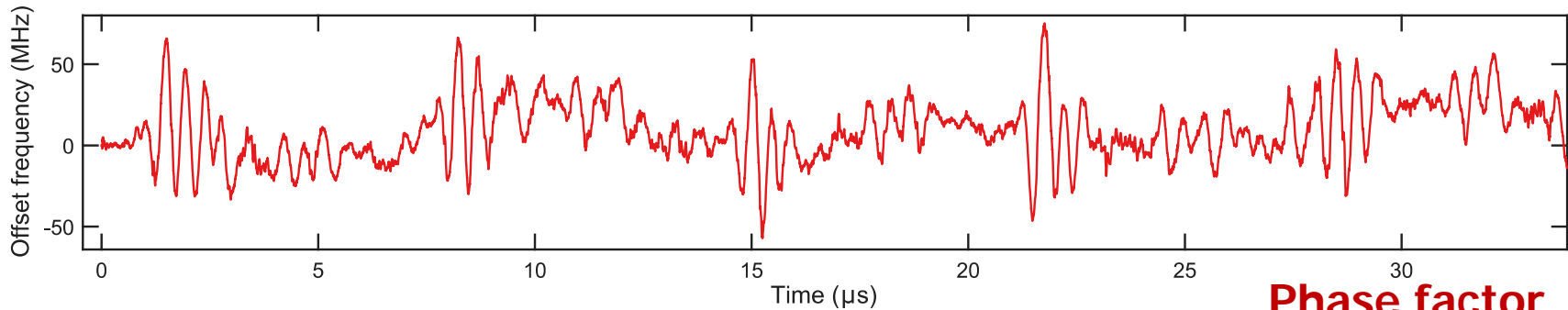
Burghoff, Yang, et al., "Computational multiheterodyne spectroscopy," *Science Advances* (2016)

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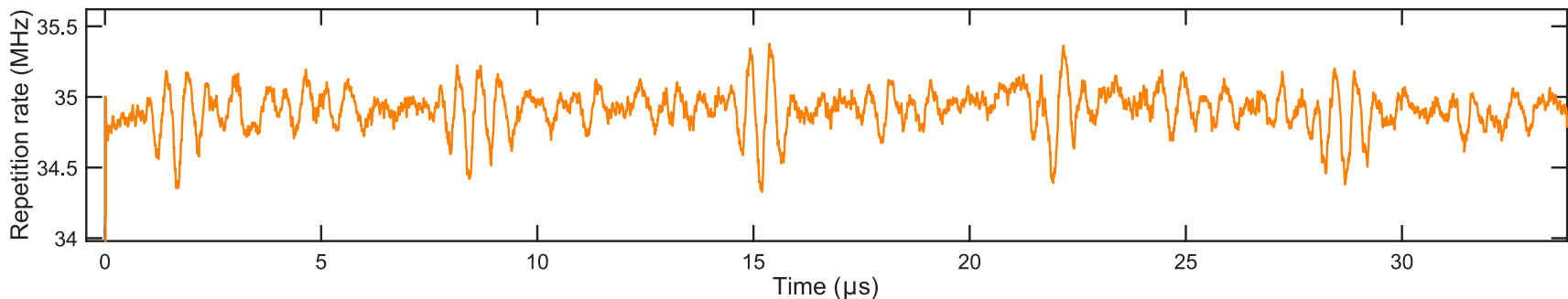
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## Offset frequency



## Phase factor

## Repetition rate



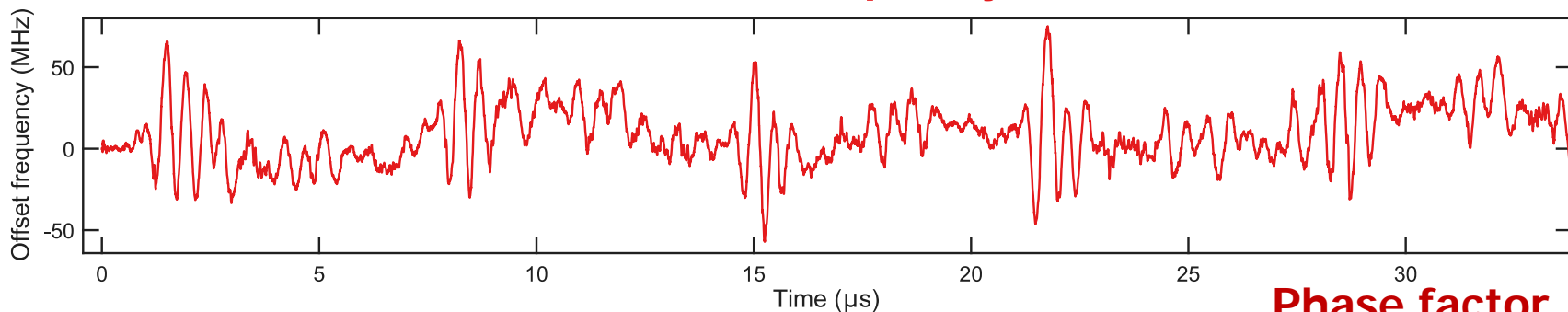
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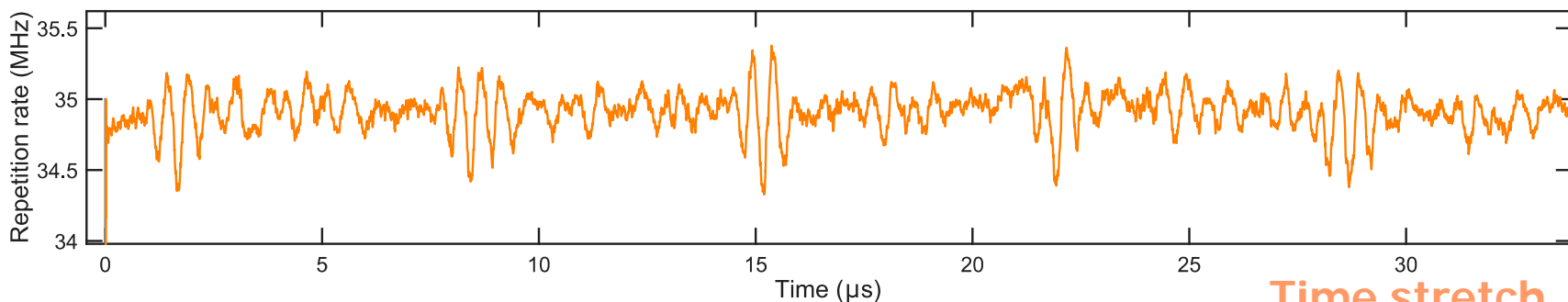
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**Offset frequency**



**Phase factor**

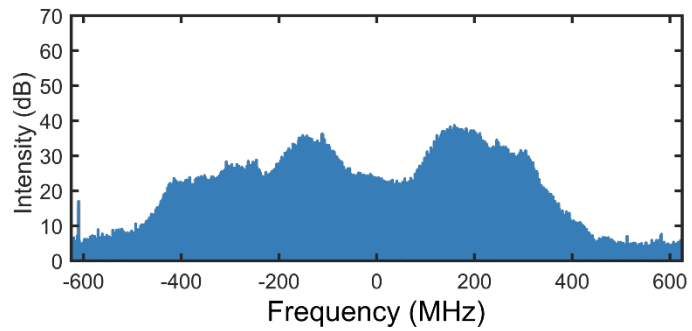
**Repetition rate**



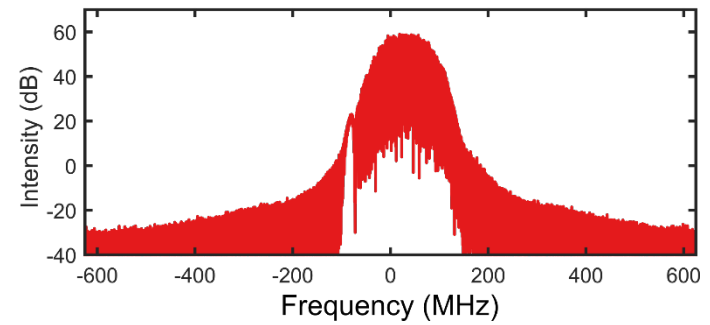
**Time stretch**

Burghoff, Yang, et al., "Computational multiheterodyne spectroscopy," *Science Advances* (2016)

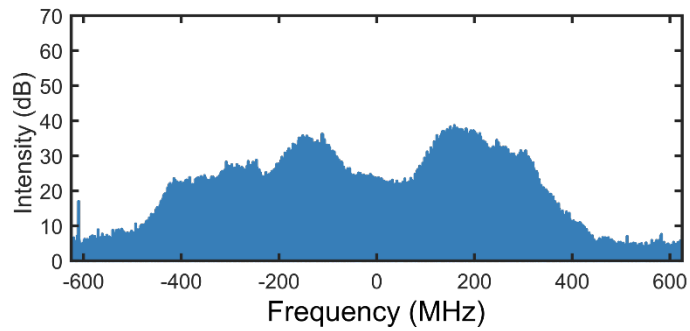
### Raw multiheterodyne data



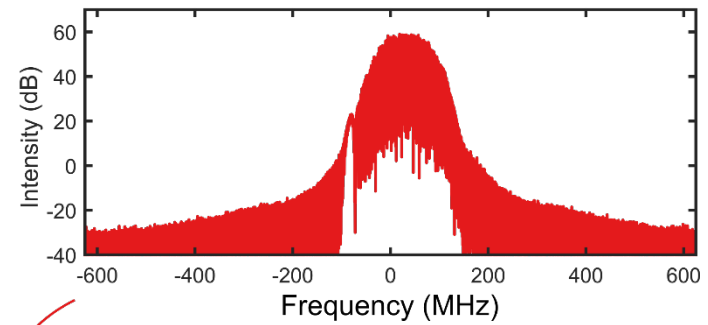
### Offset fluctuations



## Raw multiheterodyne data

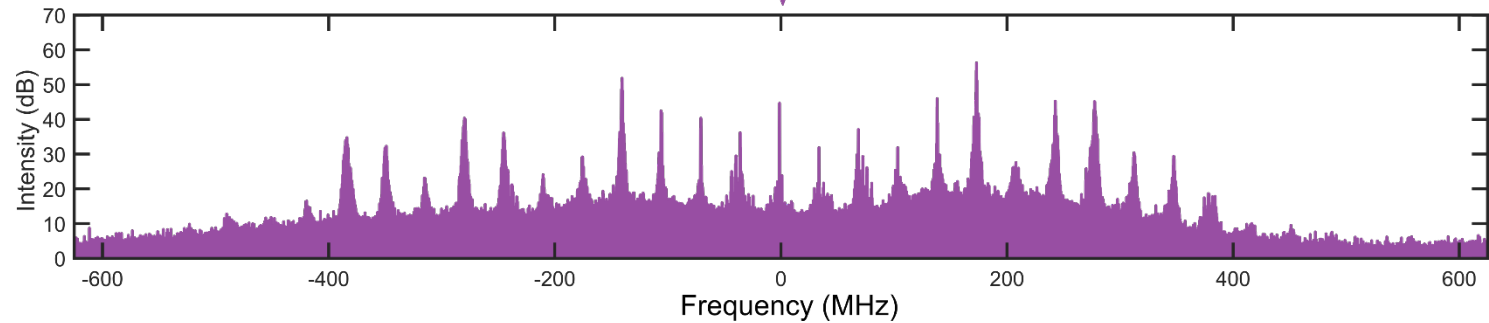


## Offset fluctuations

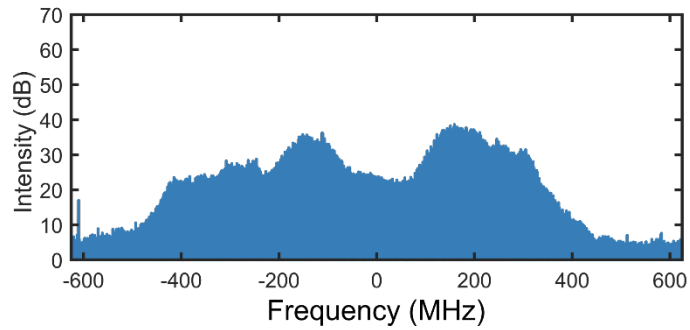


convolution

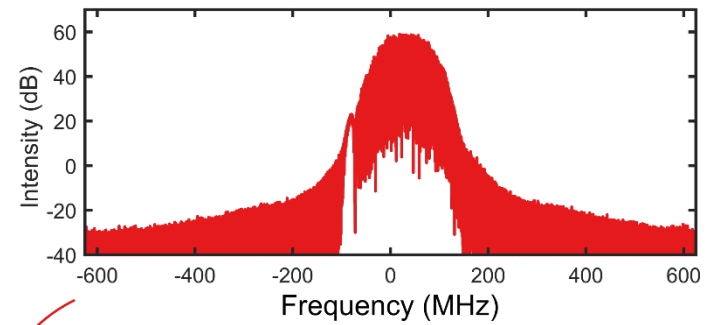
## Offset fluctuations corrected



## Raw multiheterodyne data

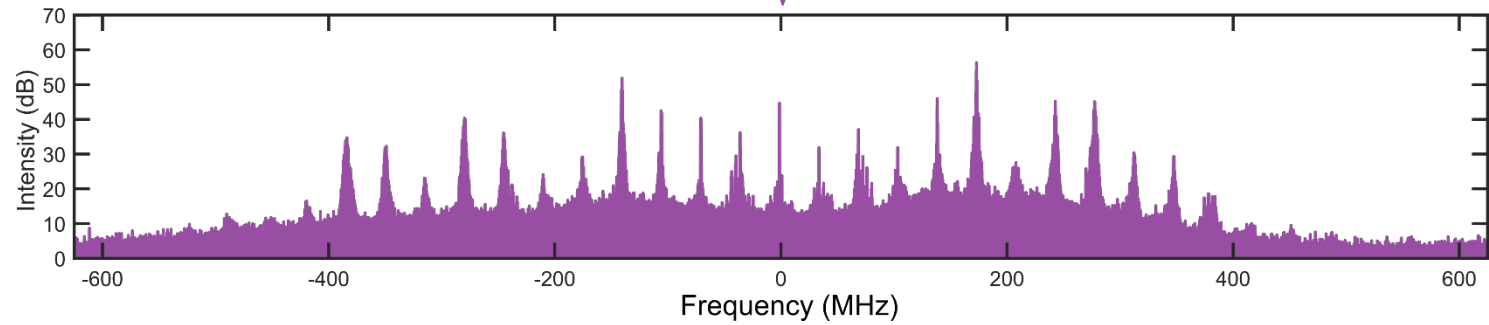


## Offset fluctuations

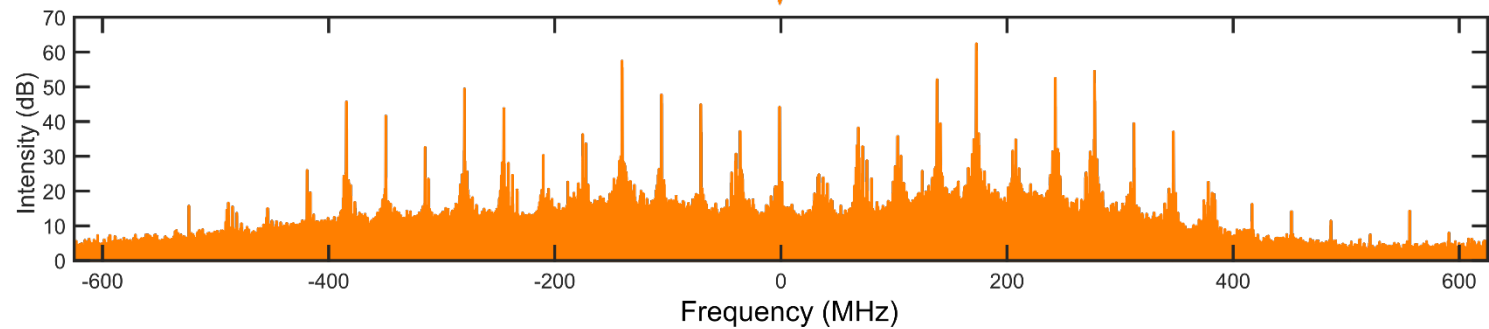


convolution

## Offset fluctuations corrected

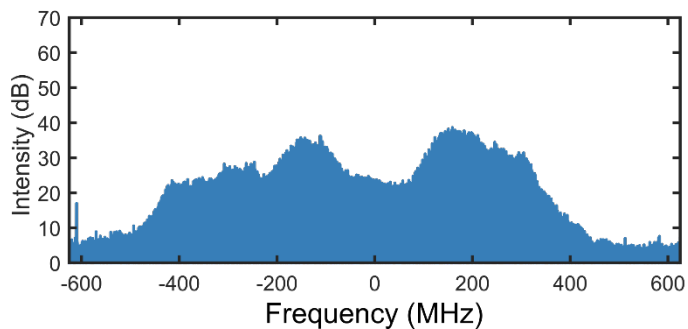


## Timing fluctuations corrected

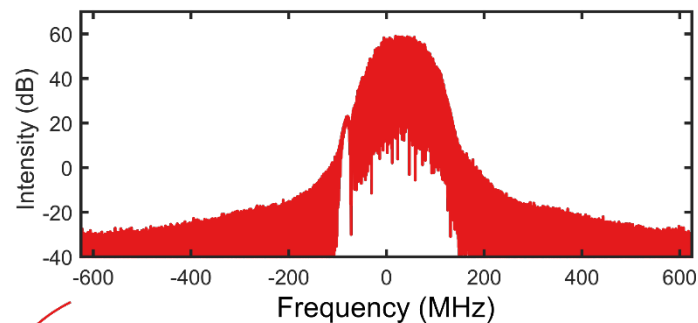




## Raw multiheterodyne data

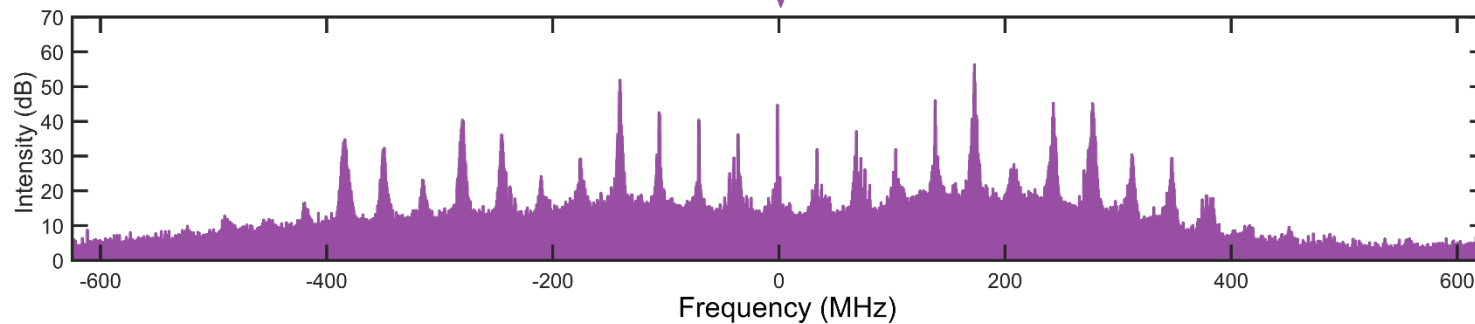


## Offset fluctuations

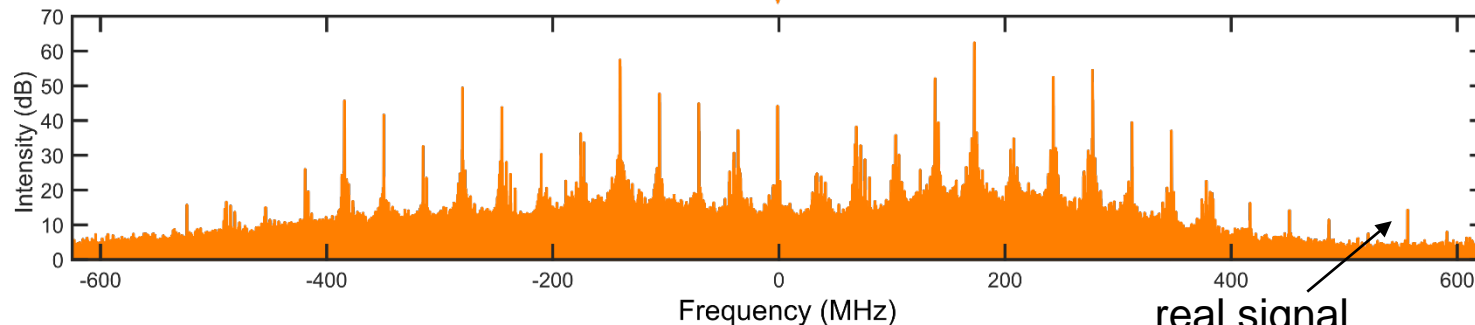


convolution

## Offset fluctuations corrected



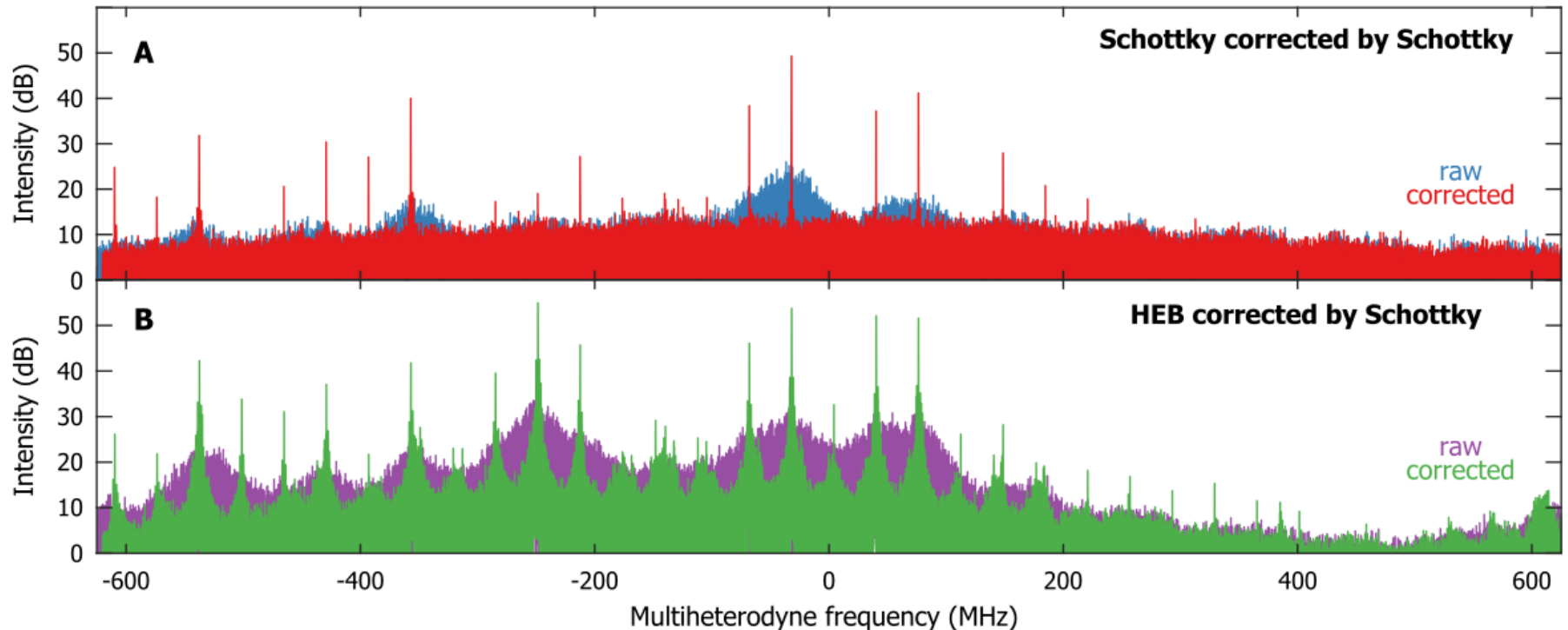
## Timing fluctuations corrected



real signal  
recovered from the  
noise floor

# Cross-correcting different spectroscopic channels

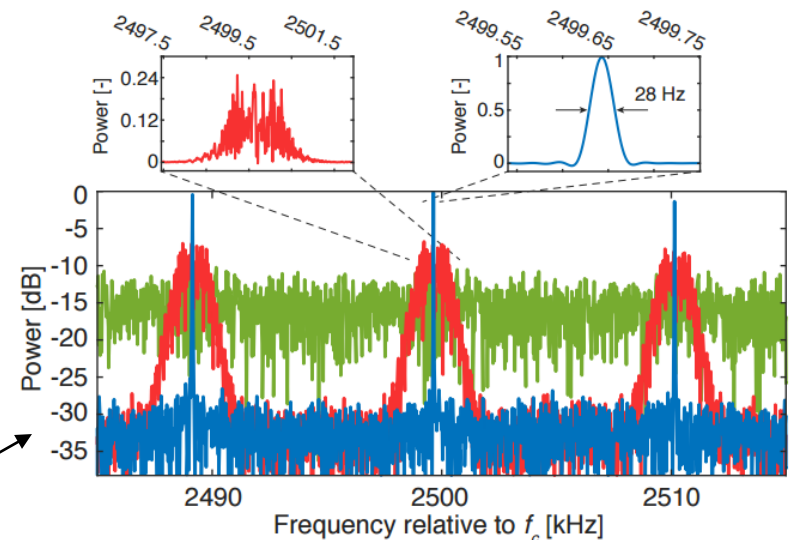
- Can use dual-comb signal from one detector to correct dual-comb signal of another



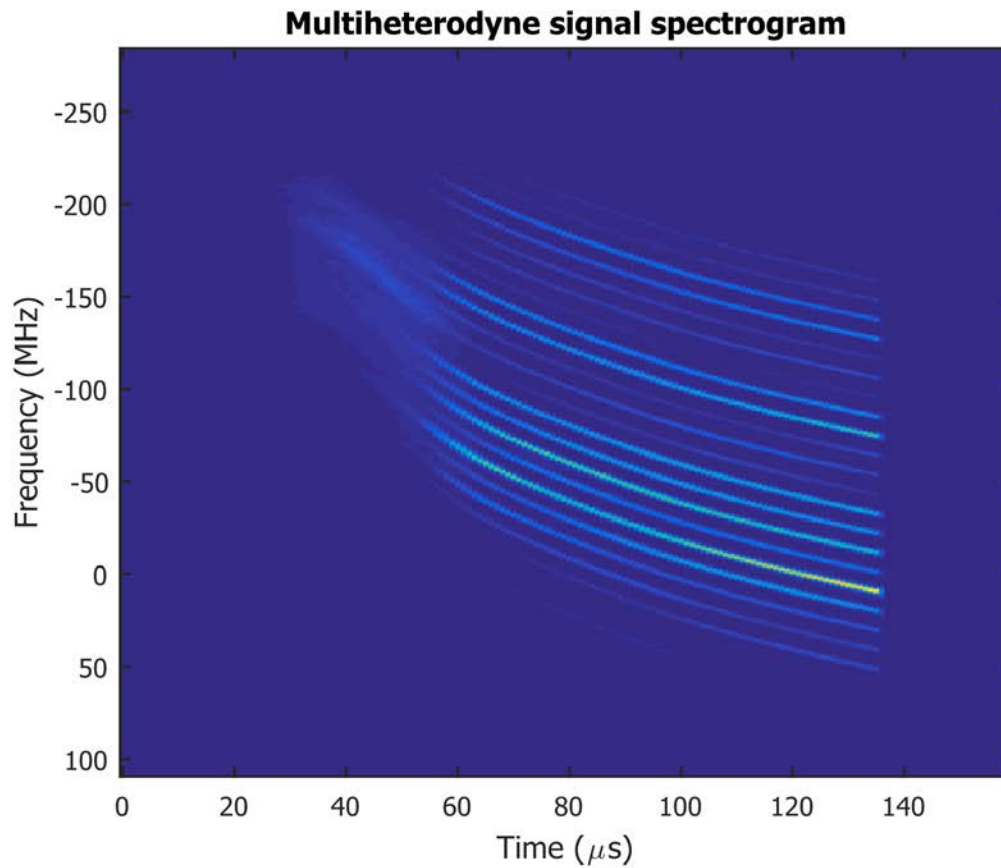
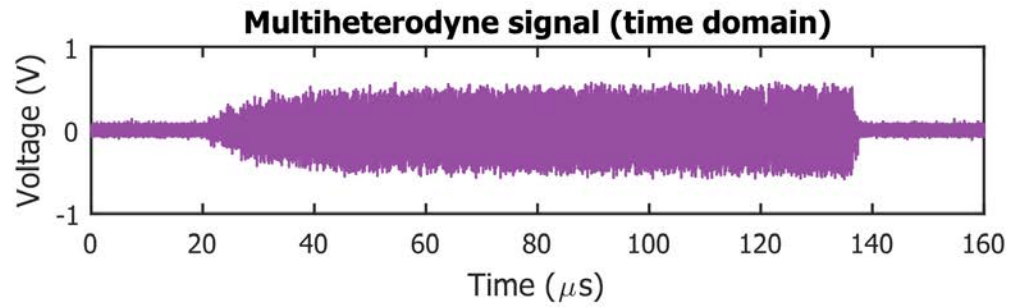
Burghoff, Yang, et al., "Computational multiheterodyne spectroscopy," *Science Advances* (2016)

# Advantages of computational correction

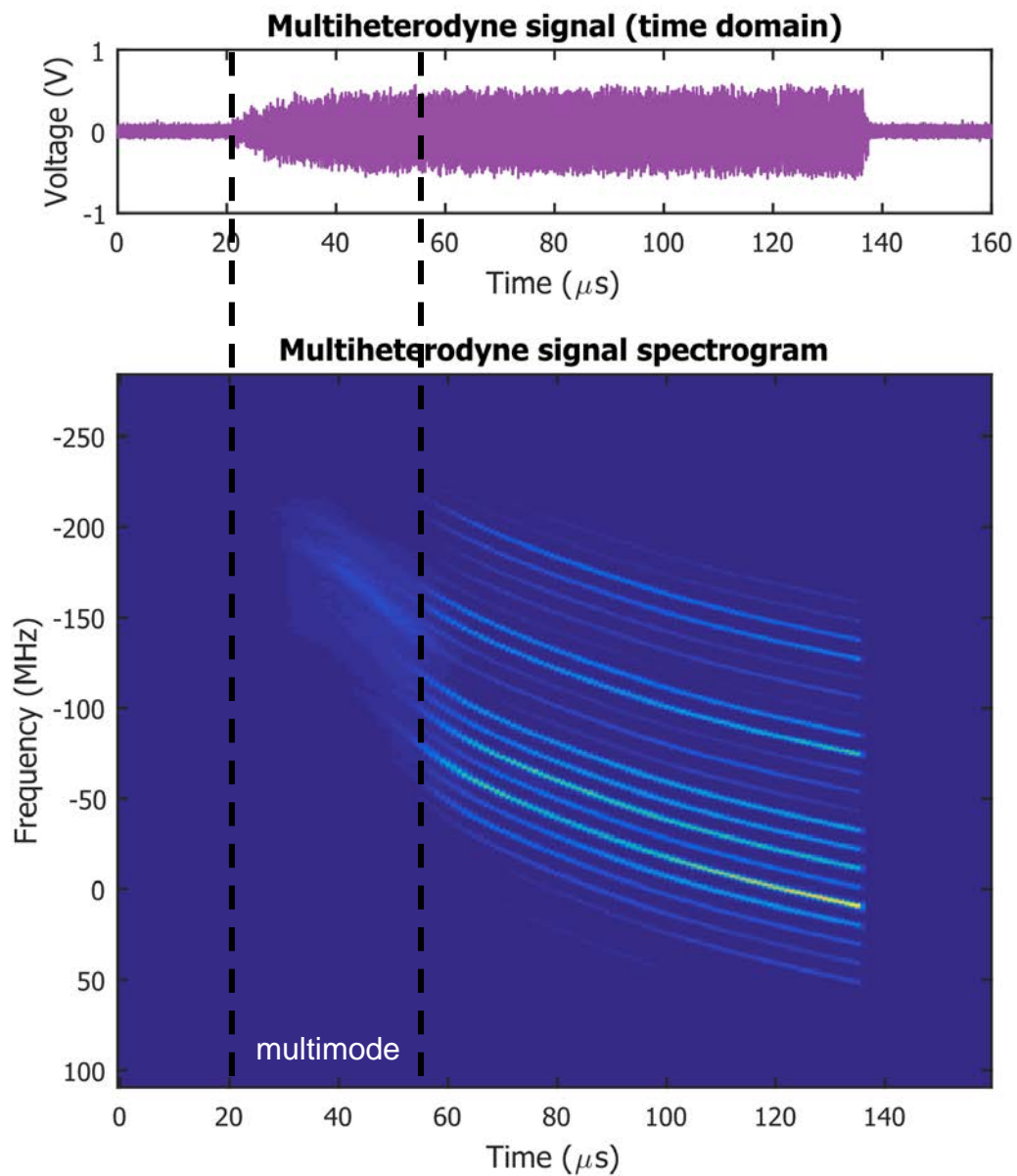
- Removes the need for temperature stabilization, bias stabilization, etc.
- Enables **pulsed mode dual comb spectroscopy**, which greatly reduces laser power consumption and makes portable sensing more viable.
- Computational approach viable for mode-locked lasers, interband cascade lasers:
  - Interband Cascade Lasers: Sterczewski, Westberg, Wysocki, et al., Opt. Eng (2017)
  - Mode-locked lasers: Hebert, Genest, et al., Optics Express (2017)



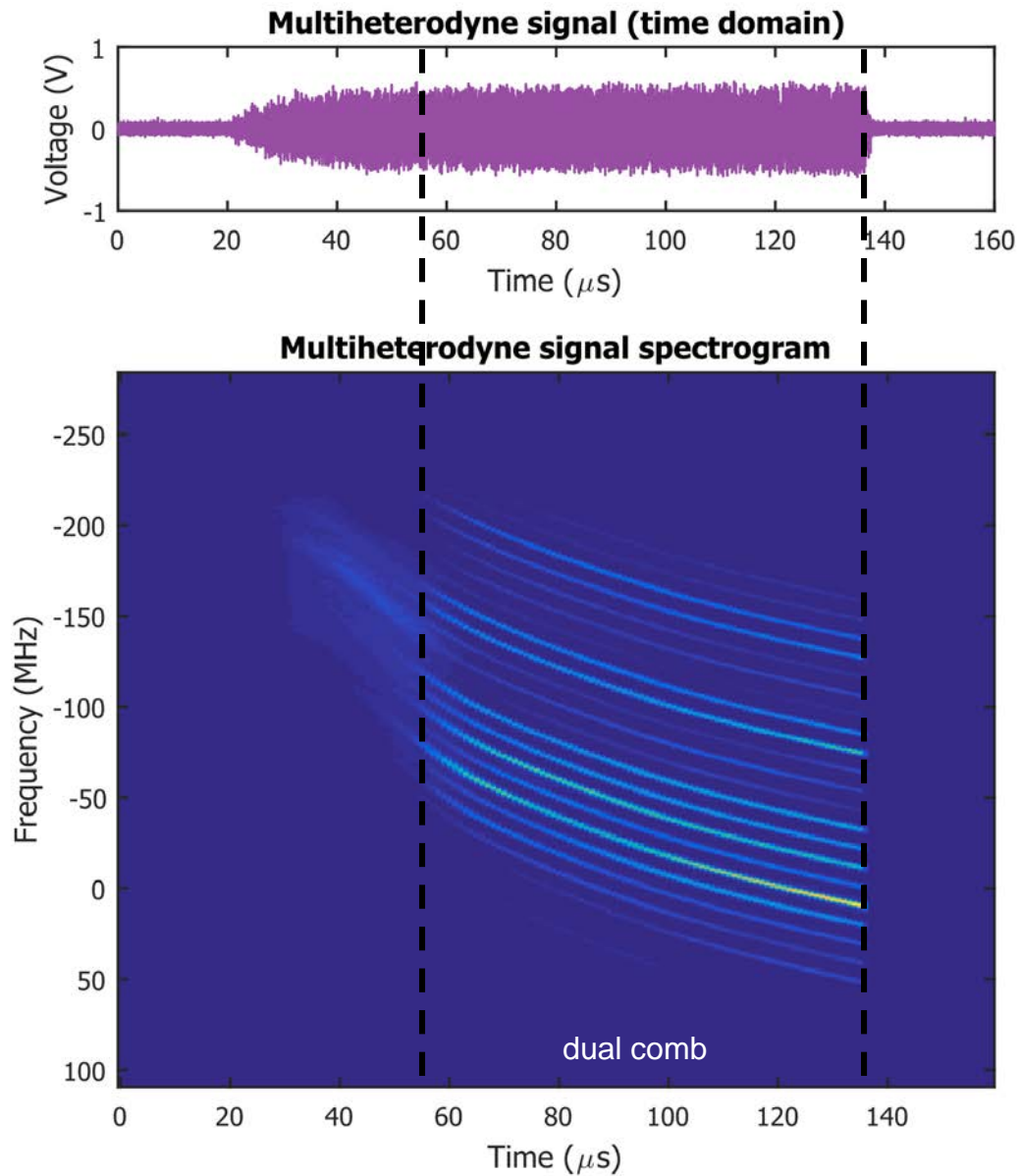
# Dual comb signal in pulsed mode



# Dual comb signal in pulsed mode



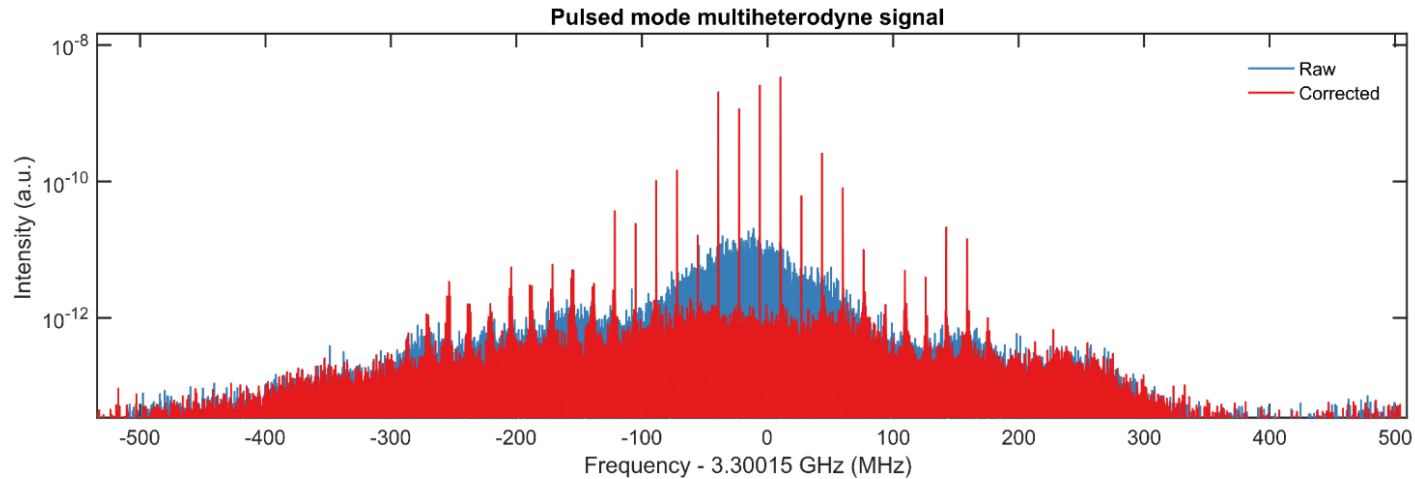
# Dual comb signal in pulsed mode



signal is chirped  
due to laser  
heating

# Pulsed mode dual comb spectroscopy

Spectrum from a single 120 us electrical pulse



- Computational phase correction allows for chirp to be measured and continuously corrected
- Reduces cooling requirements on QCLs ( $\sim 10$  W in continuous wave mode)



K561 Integral Stirling  
170 mW @ 80 K

# Conclusions

- Showed how by using dispersion engineering, terahertz quantum cascade lasers can be forced to operate in a comb regime
- Showed that dual comb (multiheterodyne) spectroscopy was possible in both pulsed and continuous-wave mode
- Showed that signal processing could be used to digitally reverse phase and timing corruption inherent to many dual comb systems, making systems more practical

