



▫ ***Chip-Based Frequency Combs***

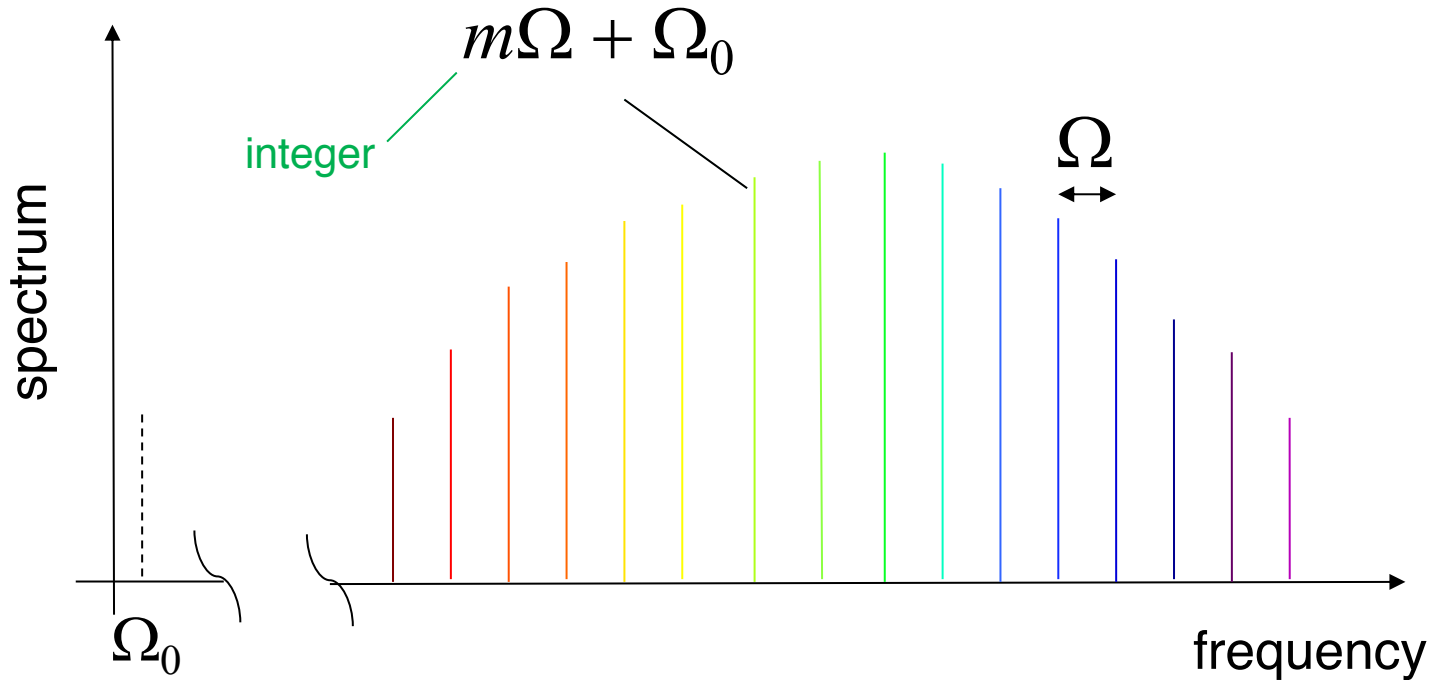
Alexander Gaeta

Department of Applied Physics and Applied Mathematics



COLUMBIA | ENGINEERING
The Fu Foundation School of Engineering and Applied Science

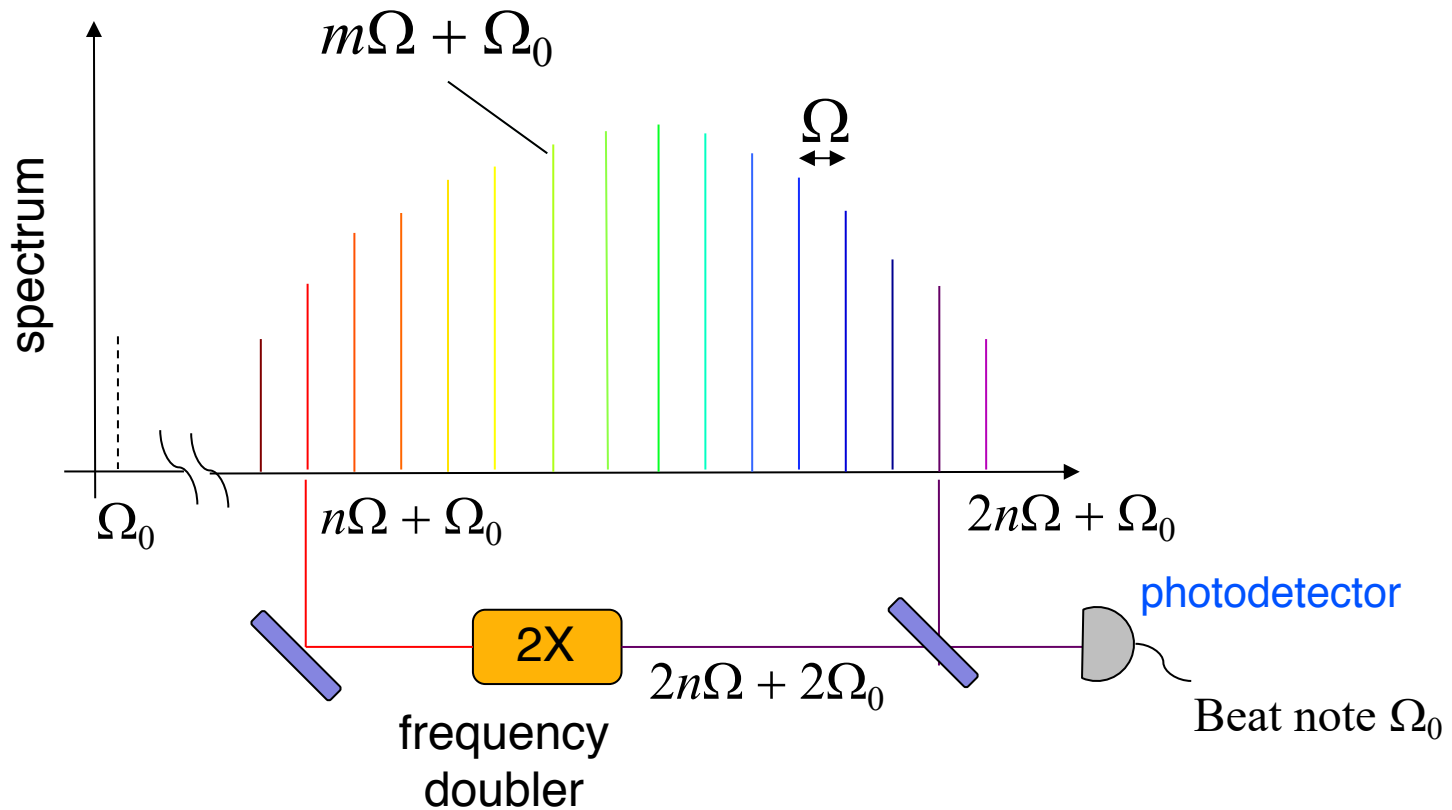
OSA Integrated Photonics Webinar
January 19, 2021



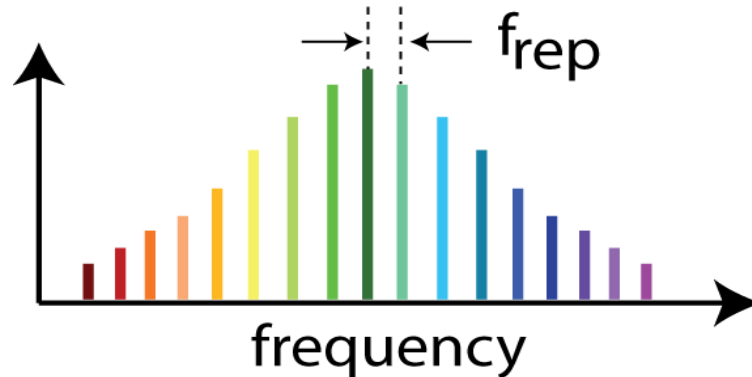
Carrier-envelope-offset
frequency

- **Direct link between optical and microwave frequencies.**

Why an Octave-Spanning Comb?



- Control of the position in the comb frequencies can be achieved.
- Link between microwave & optical frequencies.



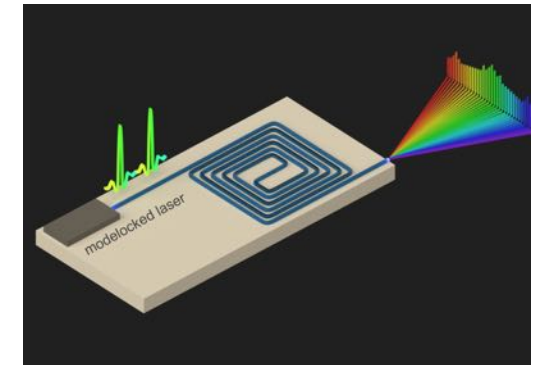
- Chemical/biological sensing
- Optical communications & interconnects
- Optical clockwork
- Astronomical spectral calibration
- Microwave generation
- Navigation (GPS) and distance ranging
- Tests of fundamental laws and constants (R , Lamb shift, fine-structure constant)
- Very-long baseline interferometry
- Arbitrary-waveform generation

Comb Generation with Ultralow Powers and in Highly Miniaturized Devices

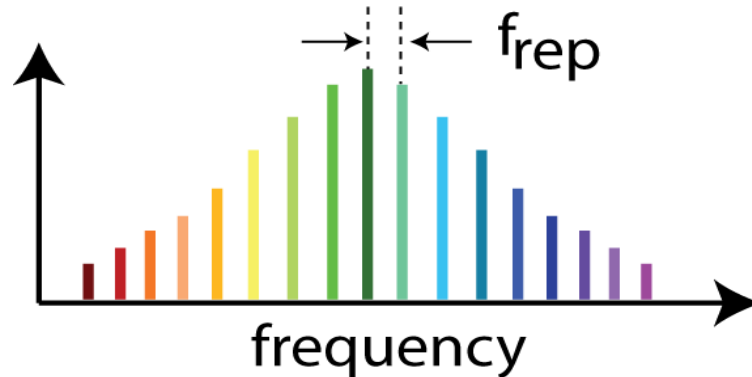


Menlo Systems

centimeter size, < 1 W



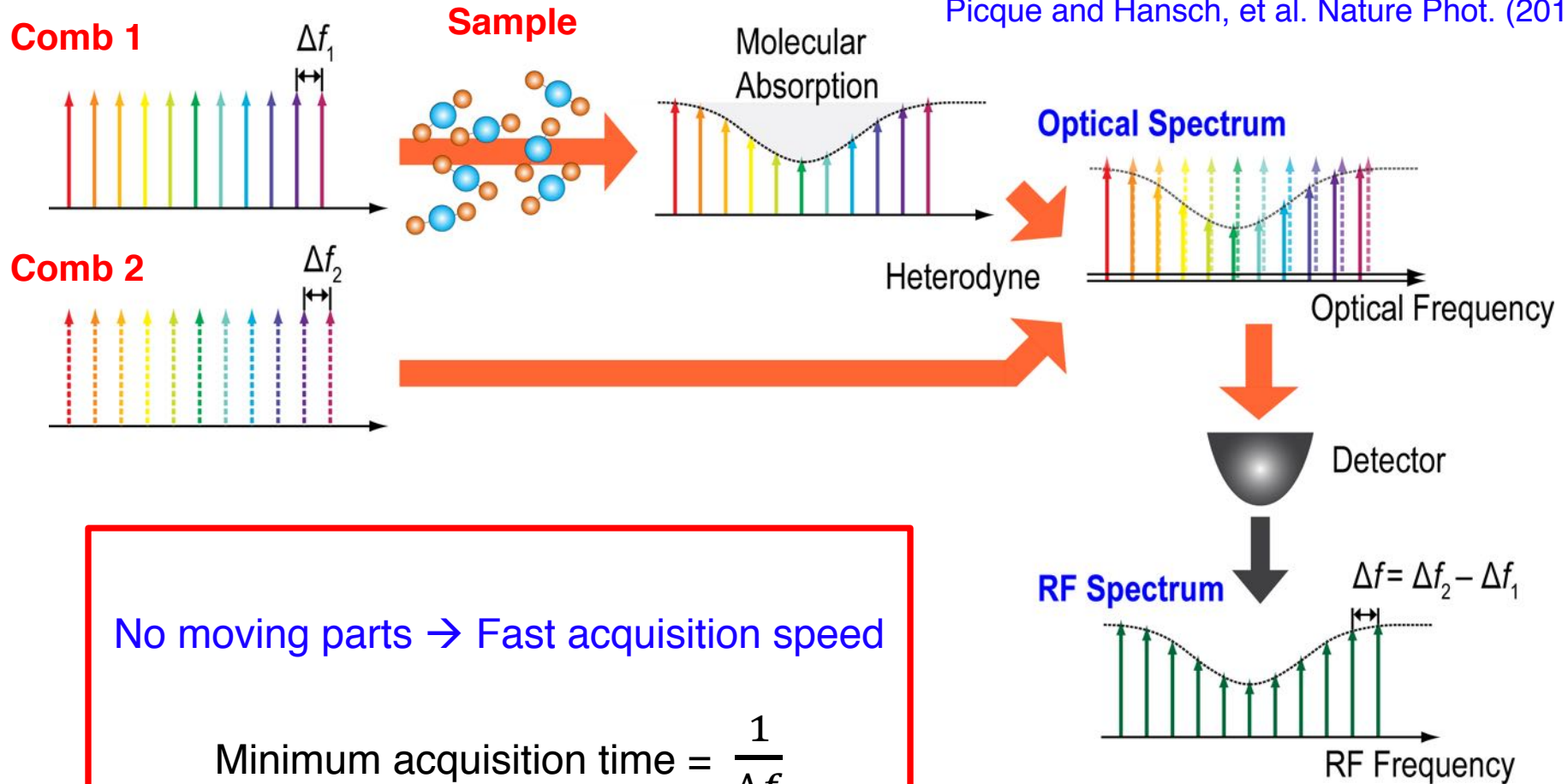
- Handheld devices
- WDM sources
- Satellite
- ...



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Reviews: Newbury, et al., *Optica* (2016)

Picque and Hansch, et al. *Nature Phot.* (2019)



No moving parts \rightarrow Fast acquisition speed

$$\text{Minimum acquisition time} = \frac{1}{\Delta f}$$

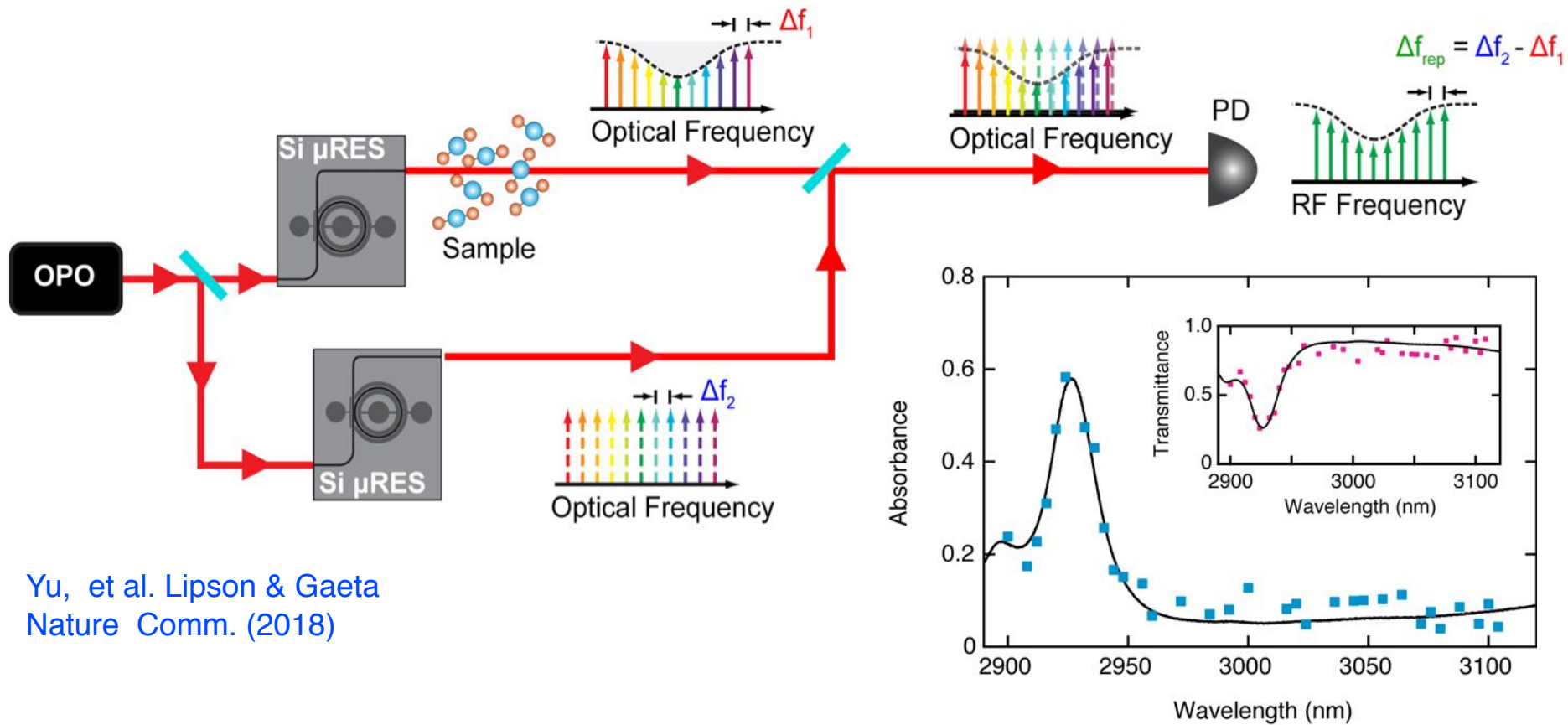
Requires only single detector.

Suh, et al. *Vahala*, *Science* (2016).

Dutt, et al. *Gaeta & Lipson*, *Science Adv.* (2018).

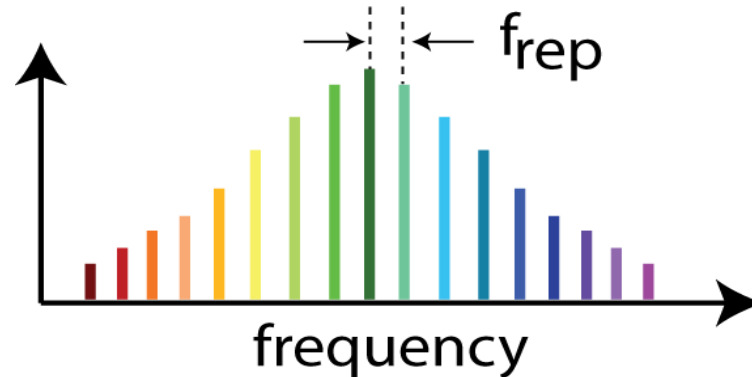
Yu, et al., *Lipson & Gaeta*, *Nature Comm.* (2018).

- Measurement of acetone absorption near 2925 nm in 1 μs

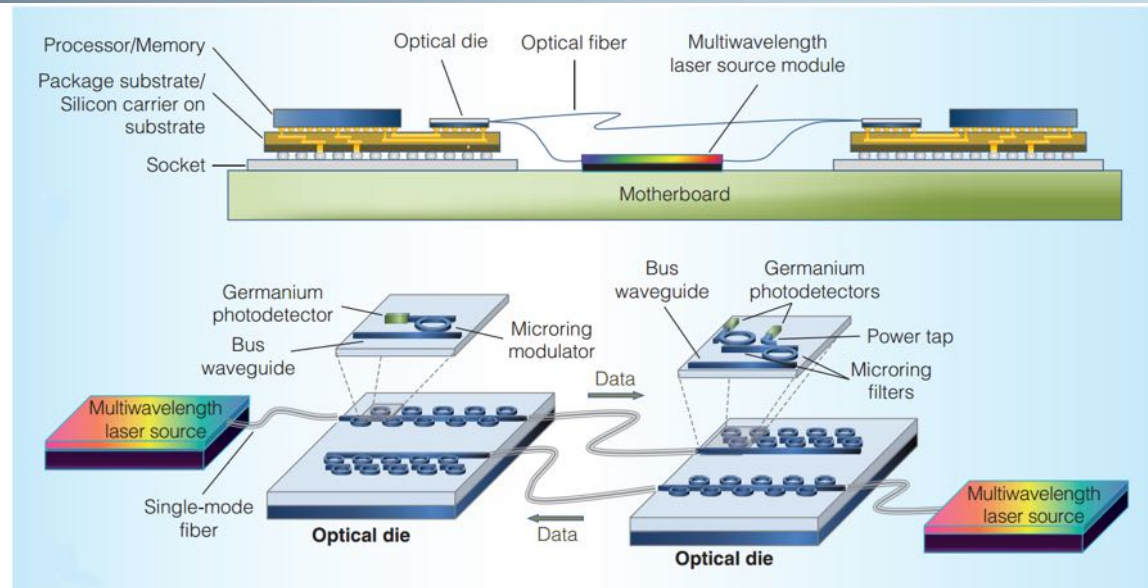


Yu, et al. Lipson & Gaeta
Nature Comm. (2018)

Real-time on-chip dual-comb spectrometer for liquid/condensed matter phase studies

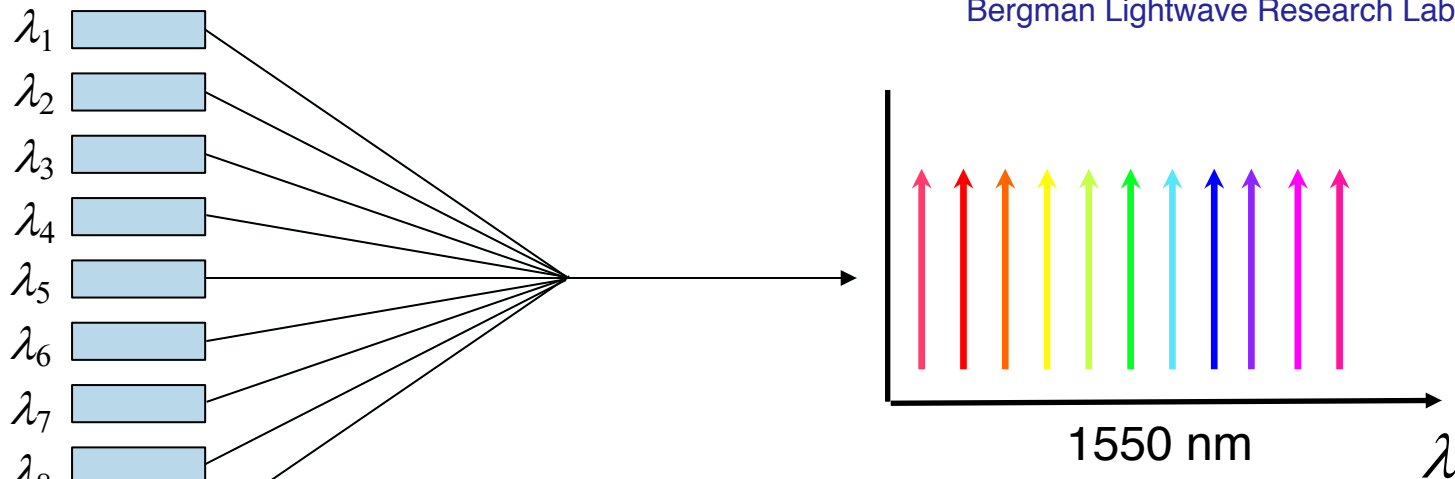


- Chemical/biological sensing
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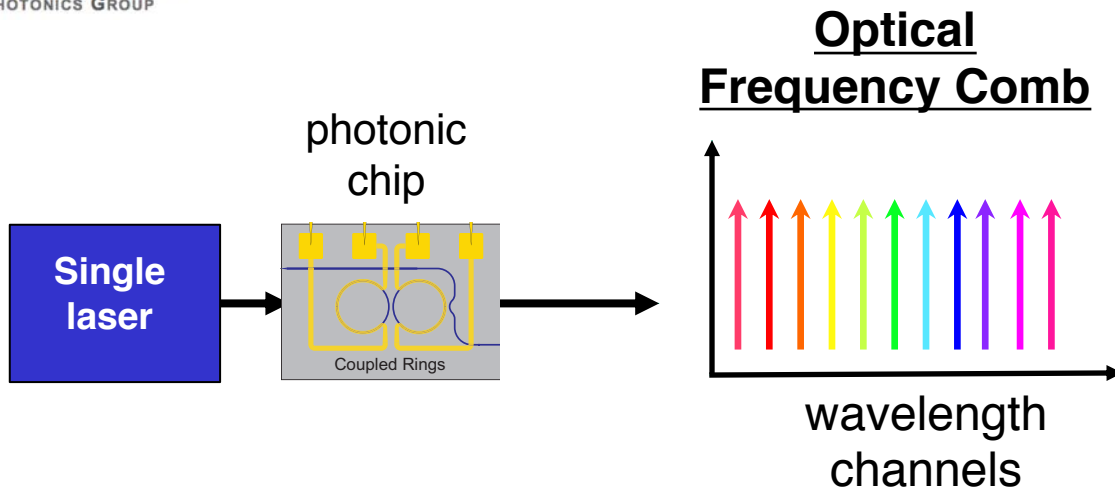


Bergman Lightwave Research Laboratory, Columbia

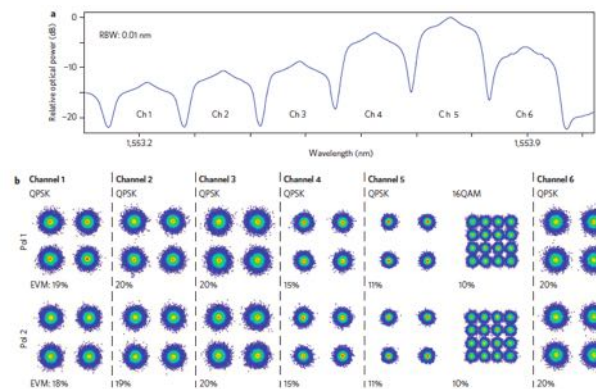
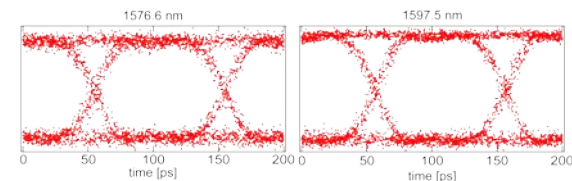
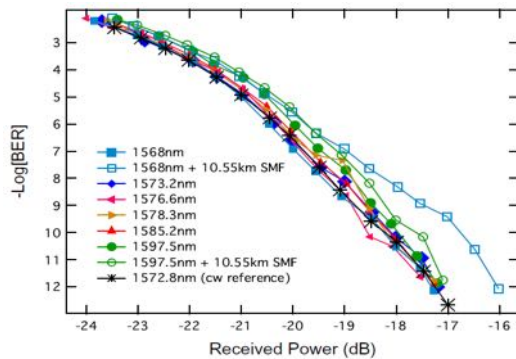
Multiple Lasers



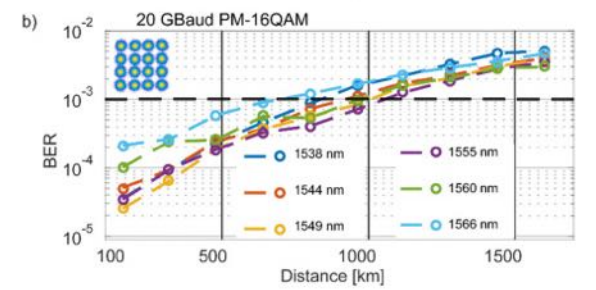
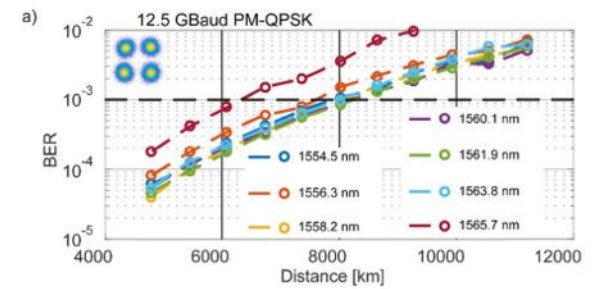
100 Tb/s => 10,000 lasers (10-GHz spacing)



- Advantages:**
- i) Cost
 - ii) Energy efficiency
 - iii) Scalability and flexibility
 - iv) Ease of integration

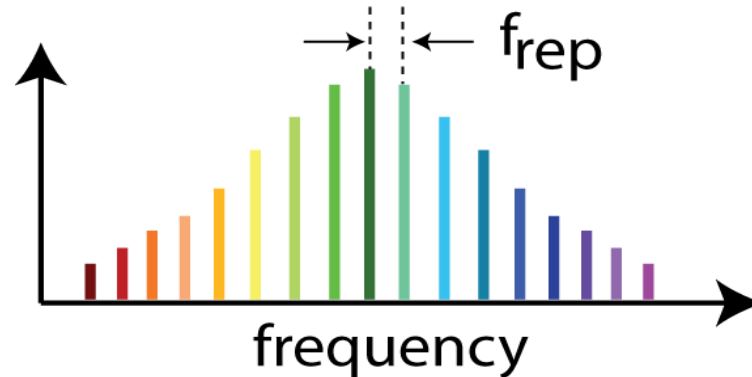


Pfeifle, *et al.*, Nature Photon. (2014).
Marin-Palombo, *et al.*, Nature (2017)



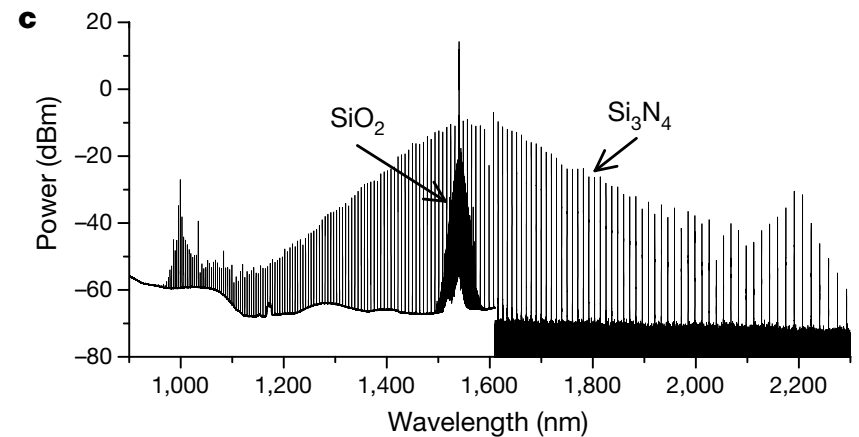
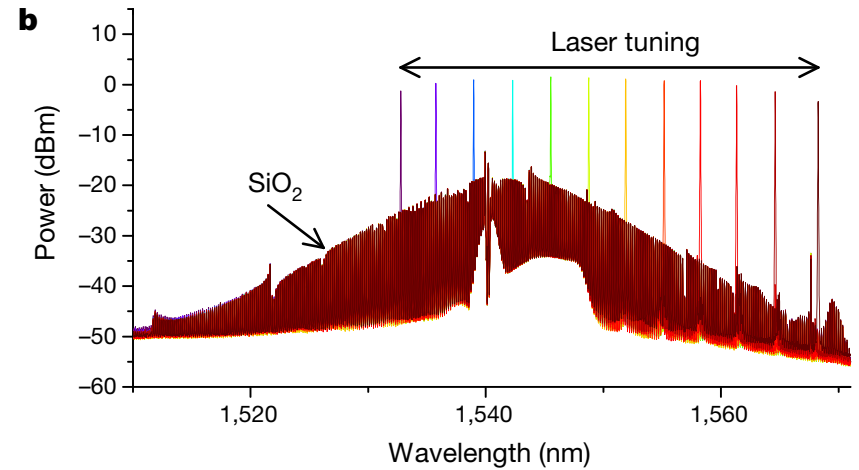
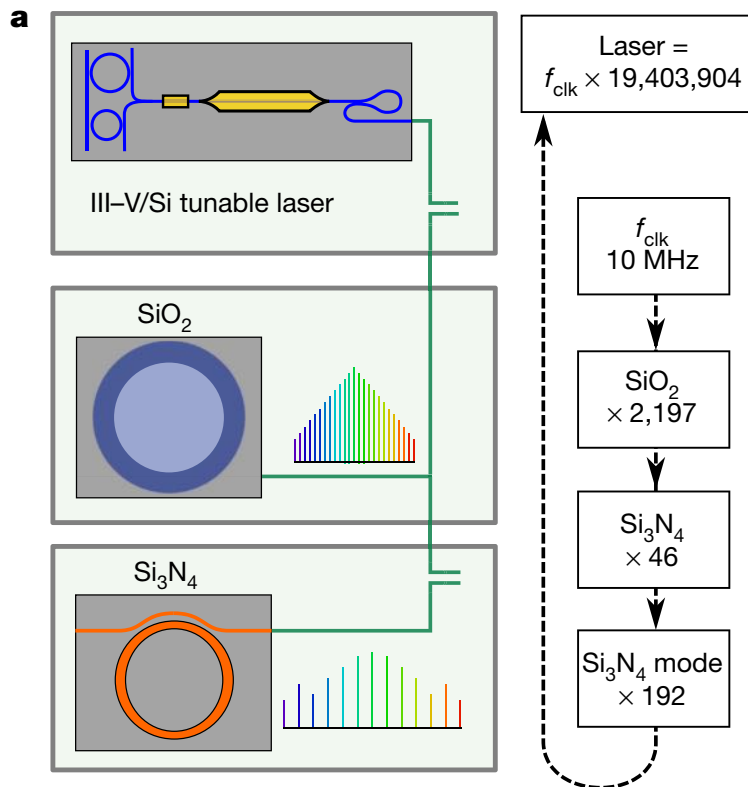
Levy, *et al.*, Gaeta & Lipson Nature Photon. (2010).
Levy, *et al.*, Gaeta & Lipson, PTL (2012).

Fülöp, *et al.*, Opt. Express (2017).
Fülöp, *et al.*, Nature Comm. (2018).

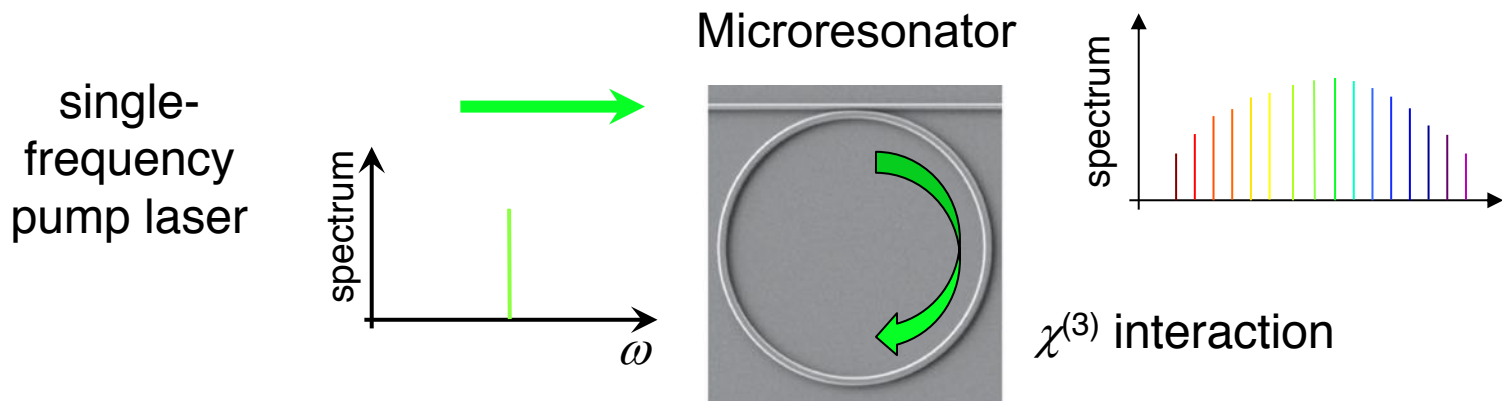
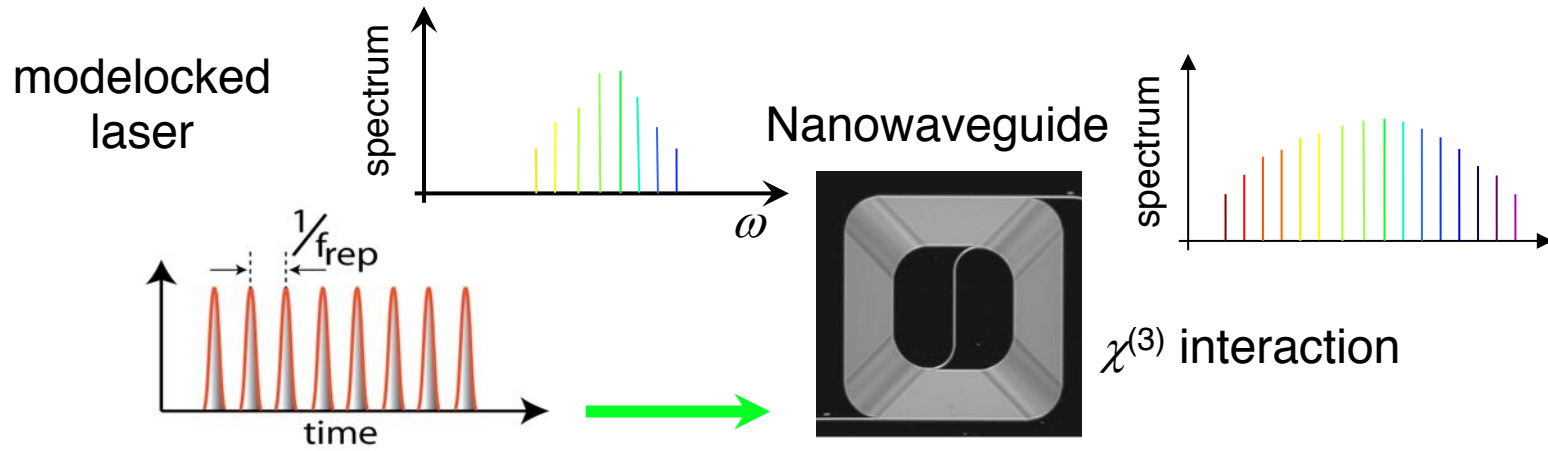


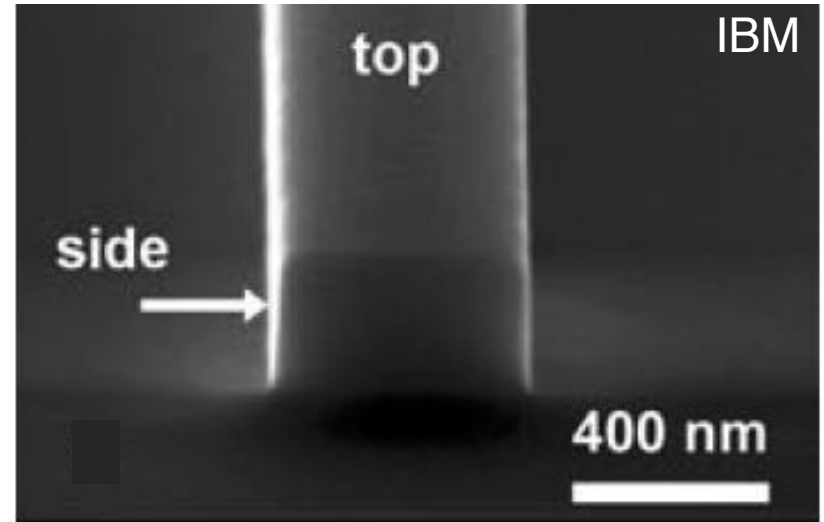
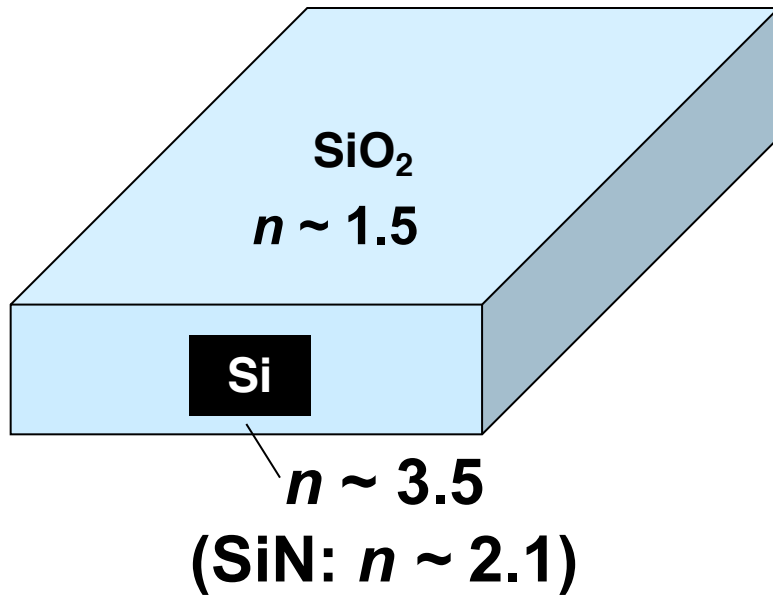
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UCSB / NIST / Caltech / EPFL / UVa / Aurrion



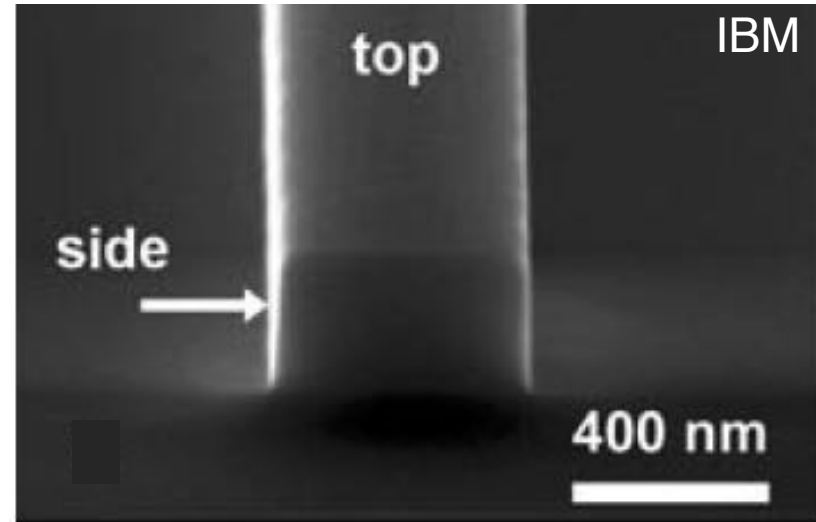
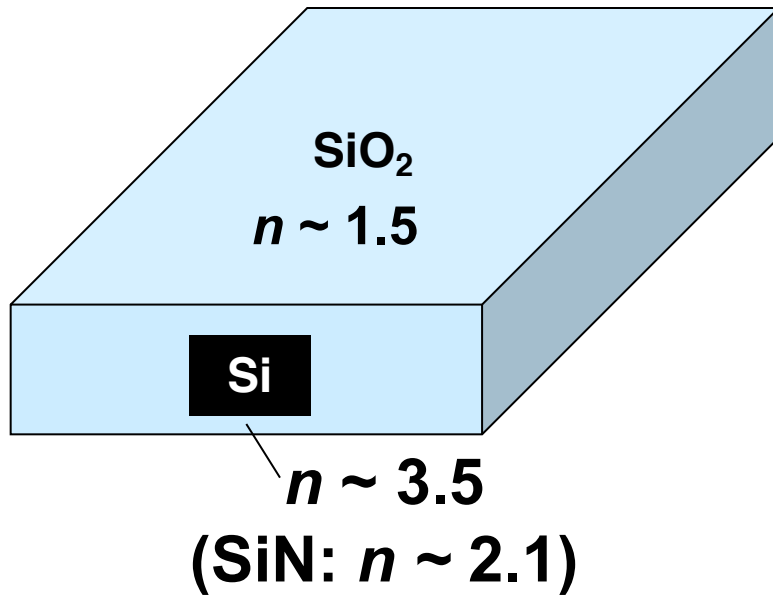
Chip-Based Comb Generation: Cavity Solitons





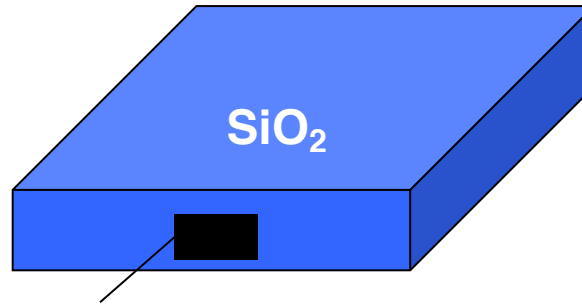
Absorption edge: Silicon $\Rightarrow \sim 1.1 \mu\text{m}$ Si₃N₄ $\Rightarrow \sim 400 \text{ nm}$

- Nonlinearity of Silicon 100X (Si₃N₄: 10X) silica
- Losses: Silicon – 1 dB/cm (Si₃N₄ – 0.01 dB/cm)
- Light confined to a region $<$ than a wavelength.

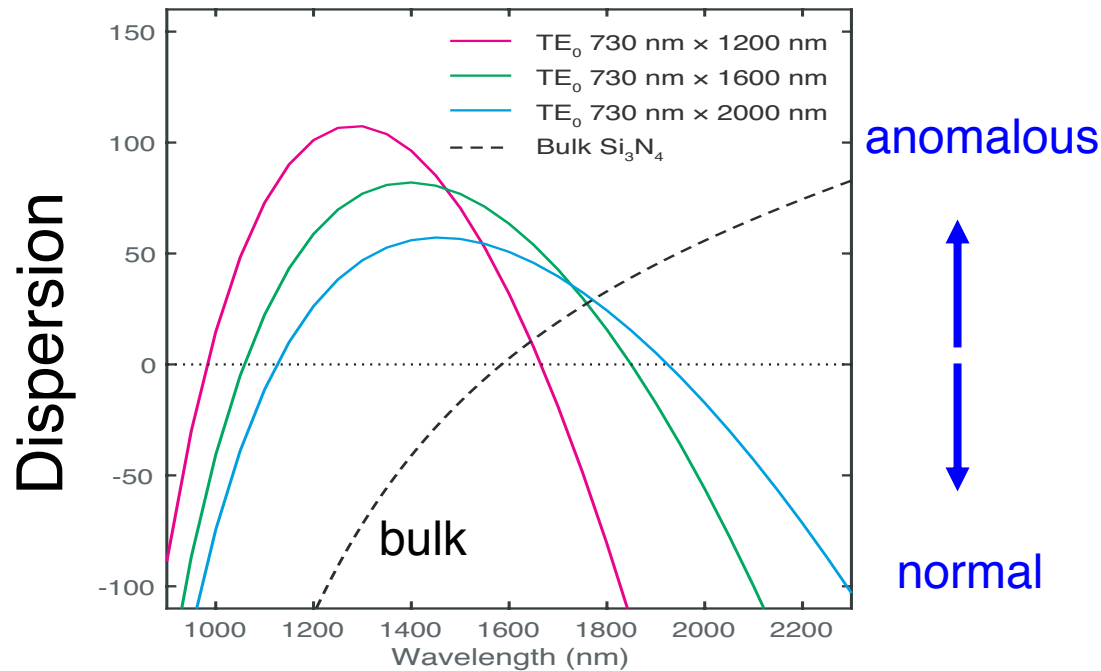


Absorption edge: Silicon $\Rightarrow \sim 1.1 \mu\text{m}$ $\text{Si}_3\text{N}_4 \Rightarrow \sim 400 \text{ nm}$

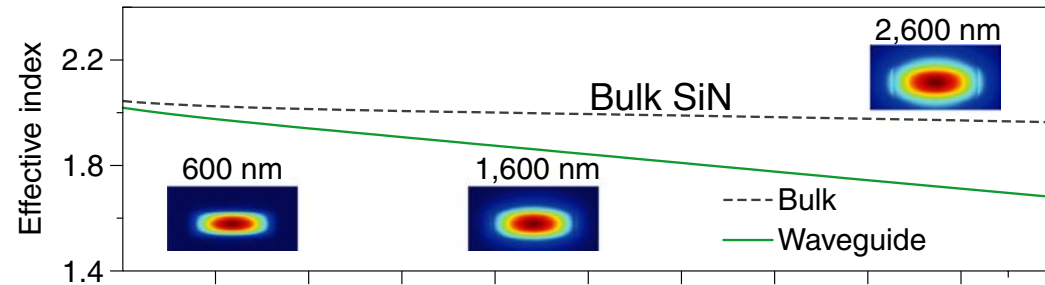
- Nonlinearity of Silicon 100X (Si_3N_4 : 10X) silica
- Losses: Silicon $\sim 1 \text{ dB/cm}$ ($\text{Si}_3\text{N}_4 - 0.01 \text{ dB/cm}$)
- Light confined to a region $<$ than a wavelength.
- **Dispersion can be engineered.**



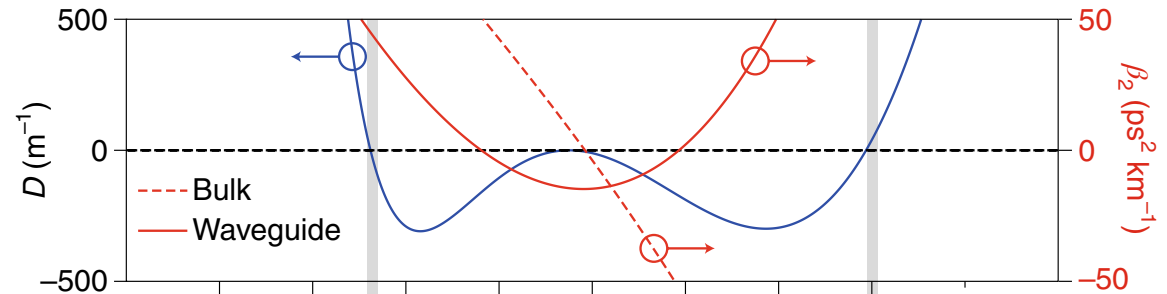
Si_3N_4



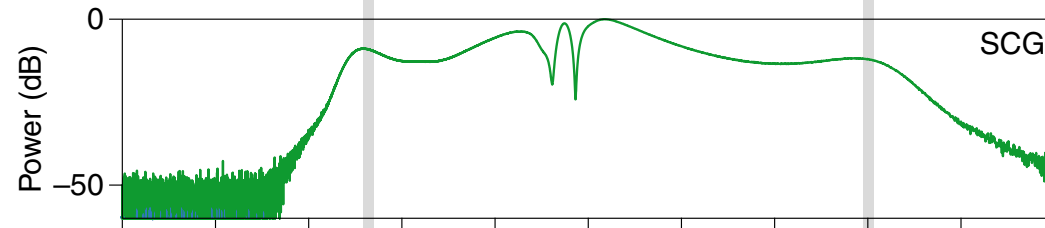
Effective
Index



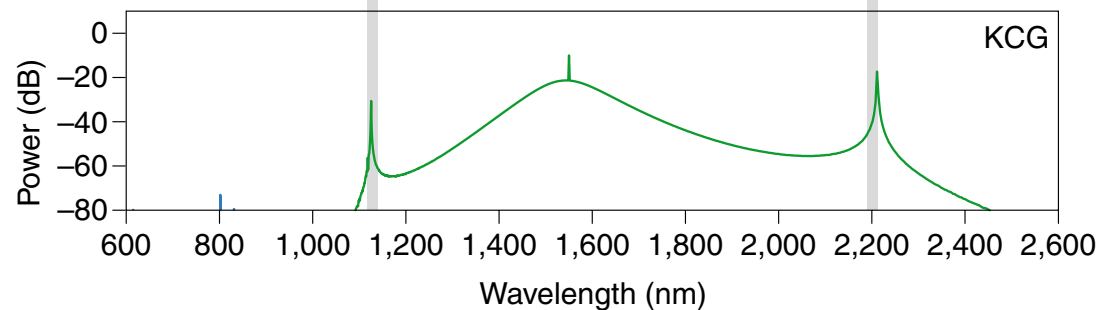
Dispersion



Supercontinuum



Kerr-Comb



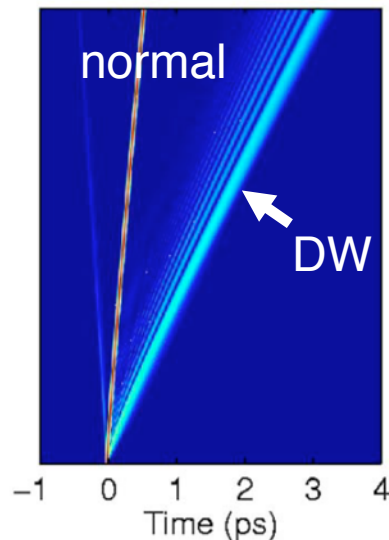
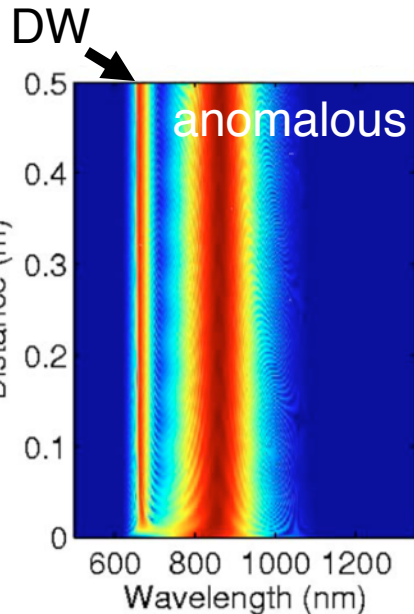
Dispersive Wave (DW) Formation

- Phase matched process that relies on higher-order dispersion
Dudley et al., Rev. Mod. Phys. (2006); Efimov, et al., PRL (2005).
- Position of DW's given by dispersion operator

$$\hat{D} = \sum_{n=2,3,\dots} \frac{\beta_n(\omega_0)}{n!} (\omega - \omega_0)^n = 0$$

dispersion

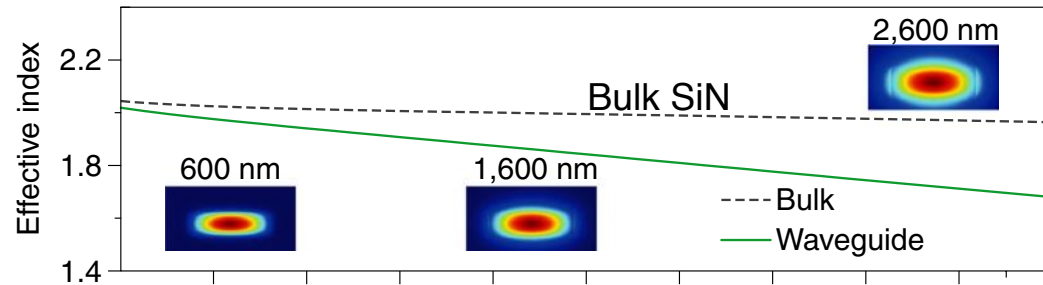
pump frequency



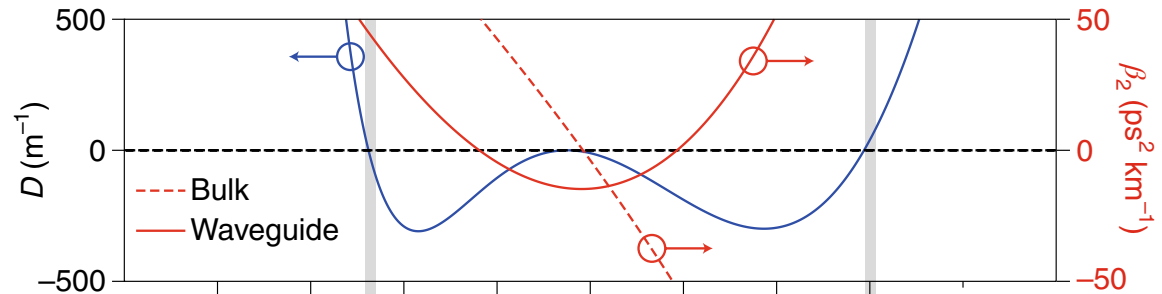
Energy transfer from soliton (anomalous GVD) to narrowband resonance (normal GVD)

Dispersive Wave Generation in Chip-Based Combs

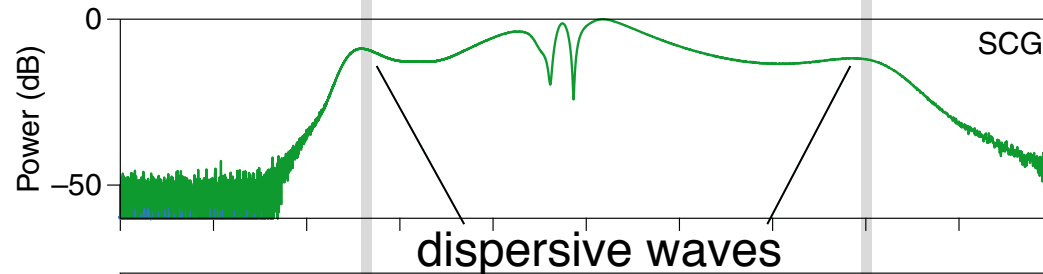
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Index



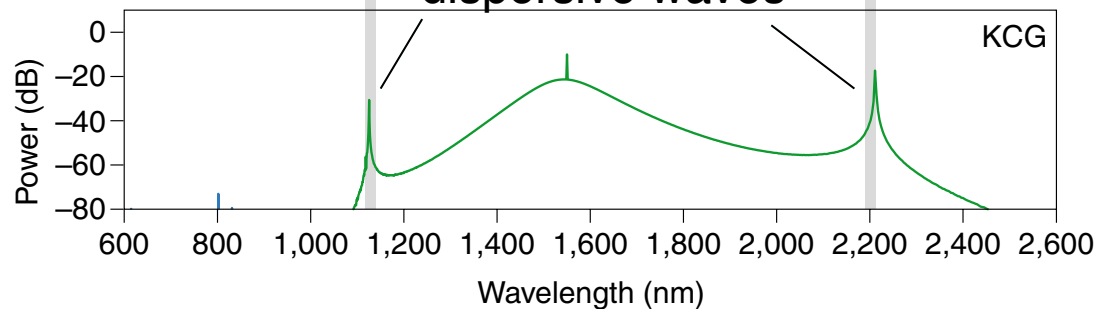
Dispersion



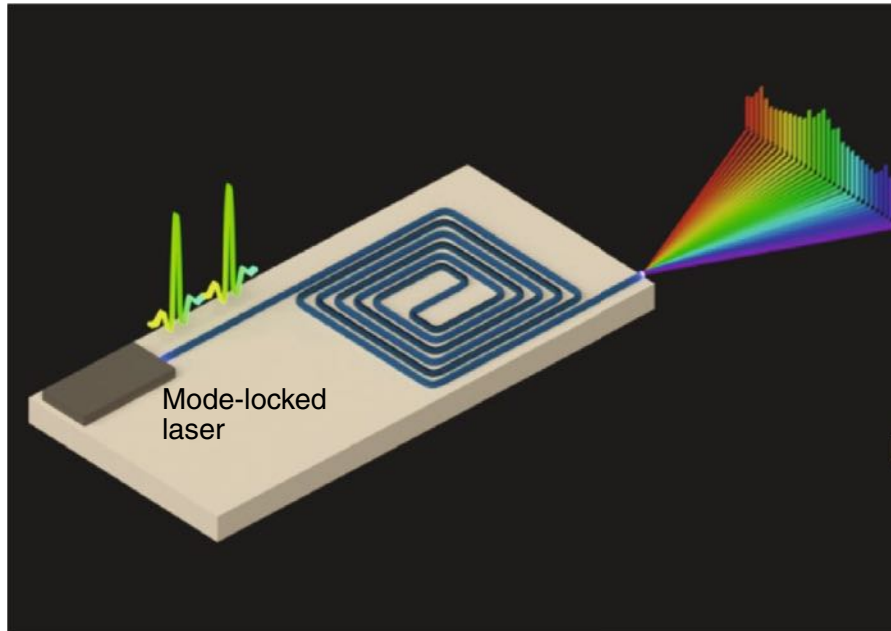
Supercontinuum



Kerr-Comb



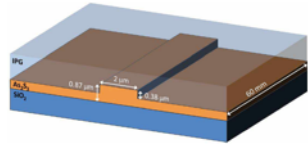
Supercontinuum Generation



Review Article: Gaeta, Lipson, and Kippenberg, Nature Phot. (2019)

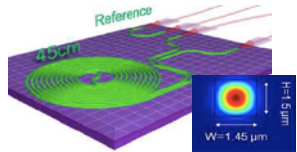


SCG in Integrated Photonic Waveguides



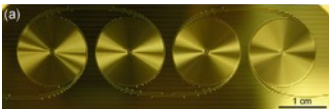
Chalcogenide

Lamont, *et al.*, Opt. Exp. (2008).
Lee, *et al.*, Opt. Lett. (2014).



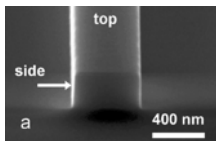
Hydex glass

Duchesne, *et al.*, Opt. Exp. (2010).



Silica

Oh, *et al.*, Opt. Lett. (2014).



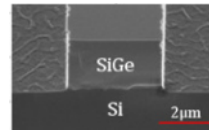
Silicon

Hsieh, *et al.*, Opt. Exp. (2007).
Lau, *et al.*, Opt. Lett. (2014).
F. Leo, *et al.*, Opt. Lett. (2015).
Kuyken, *et al.*, Opt. Exp. (2015).



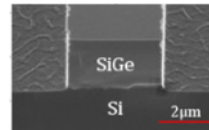
Amorphous silicon

Dave, *et al.*, Opt. Express (2013).
Safioui, *et al.*, Opt. Express (2014).
Leo, *et al.*, Opt. Express (2014).



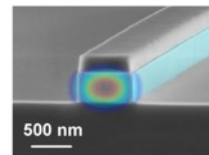
Diamond

Shams-Ansari, *et al.*, Opt. Lett. (2019).



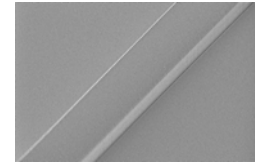
Silicon germanium

Sinobad, *et al.*, Optica (2018).



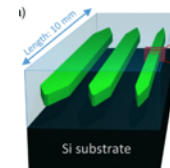
Aluminum gallium arsenide

Kuyken, *et al.*, Opt. Lett. (2020).



Silicon nitride

Halir, *et al.*, Opt. Lett. (2012).
Chavez Boggio, *et al.*, JOSA B (2014).
Wang, *et al.*, LPR (2015).
Liu, *et al.*, Opt. Lett. (2016).
Carlson, *et al.*, Opt. Lett. (2017).
Porcel, *et al.*, Opt. Exp. (2017).
Guo, *et al.*, Nature Photon. (2018).



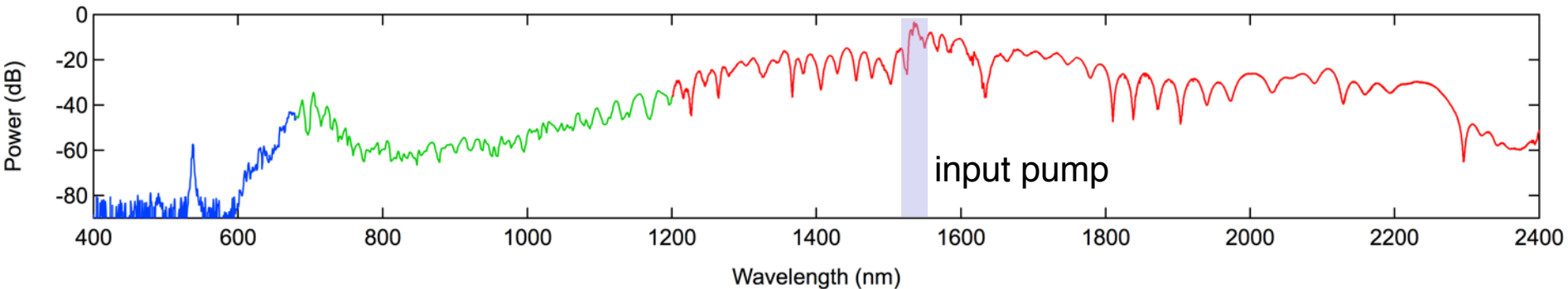
Aluminum nitride

Hickstein, *et al.*, P.R. Appl. (2017).



Lithium niobate

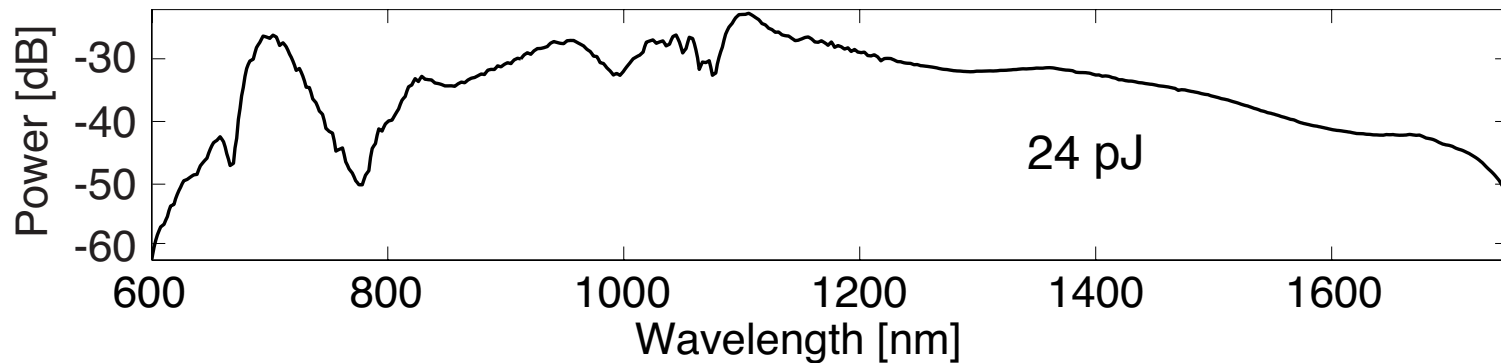
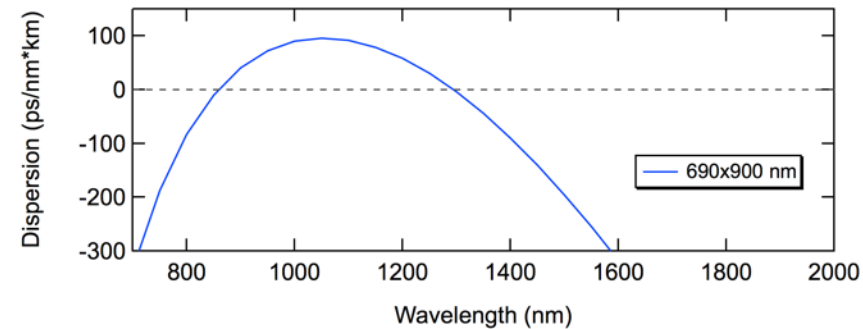
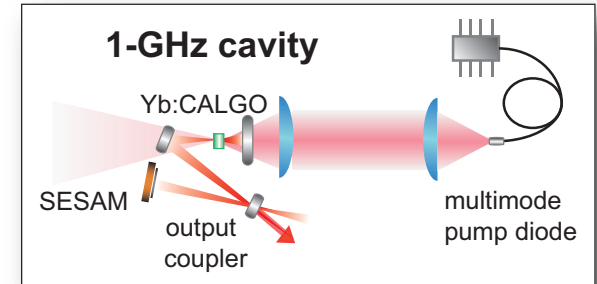
Yu, *et al.*, Opt. Lett. (2019).
Lu, *et al.*, Opt. Lett. (2019).
Jankowski, *et al.*, Optica (2020).



- 5-cm Si_3N_4 waveguide, 730×1500 nm cross section
- 1560 nm pump, 100-fs pulse duration, 10 mW coupled power (80 MHz)
- > 2 octave spanning comb
- Wide transparency (400 – 4600 nm) visible to mid-IR

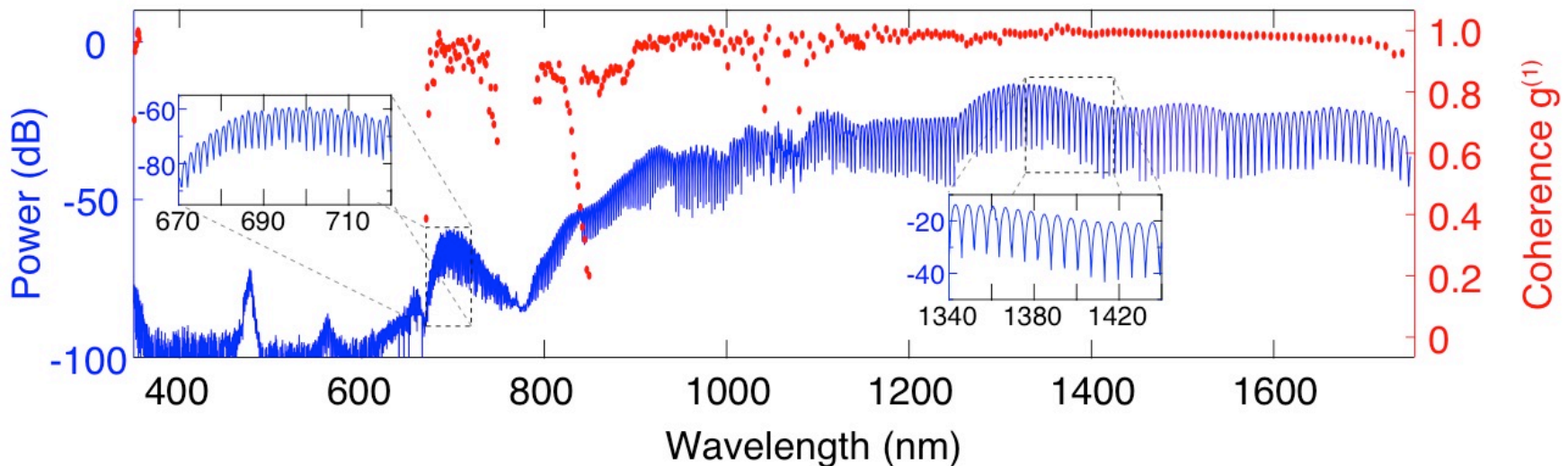
Coherence Characterization of Supercontinuum Spectrum (Experiment)

- Collaboration with **Keller Group** (ETH Zürich)
- Pump with 100-fs, 1-GHz repetition rate, 1055 nm
[A. Klenner *et al.*, *Opt. Express* (2014).]
- 7.5 mm Si₃N₄ waveguide, 690 × 900 nm



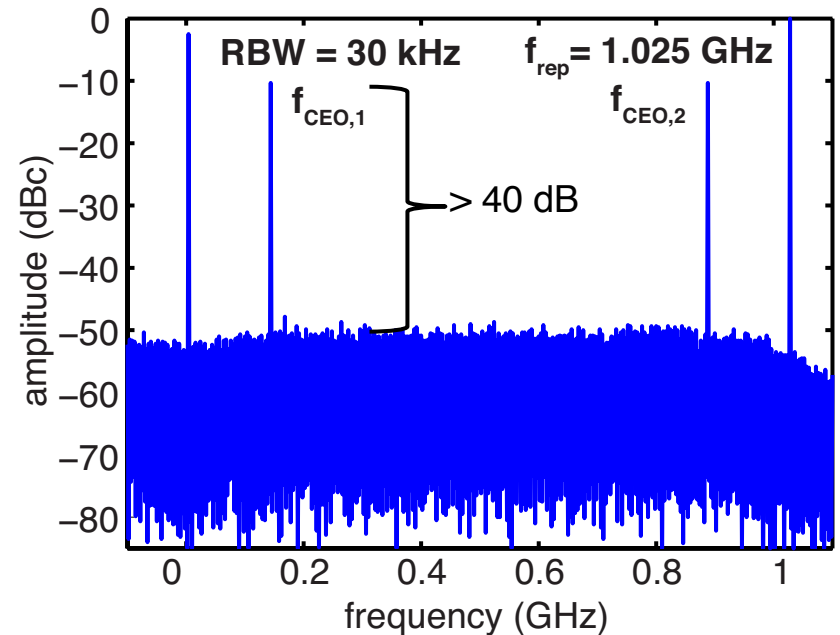
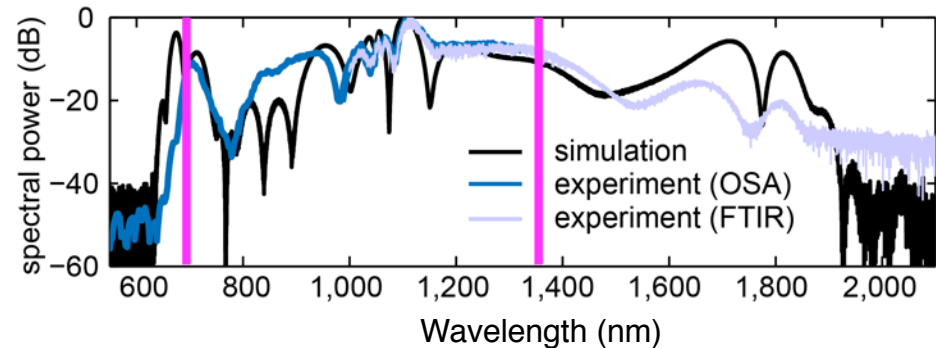
- Measure fringes in asymmetric Michelson interferometer
[F. Lu *et al.*, *Opt. Express* (2004).]
- Extract visibility and coherence
[J W. Nicholson *et al.*, *Opt. Express* (2004); X. Gu *et al.*, *Opt. Express* (2003)]

$$V(\lambda) = \frac{I_{\max}(\lambda) - I_{\min}(\lambda)}{I_{\max}(\lambda) + I_{\min}(\lambda)} \quad \left| g_{12}^{(1)}(\lambda) \right| = \frac{V(\lambda)[I_1(\lambda) + I_2(\lambda)]}{2[I_1(\lambda)I_2(\lambda)]^{1/2}}$$

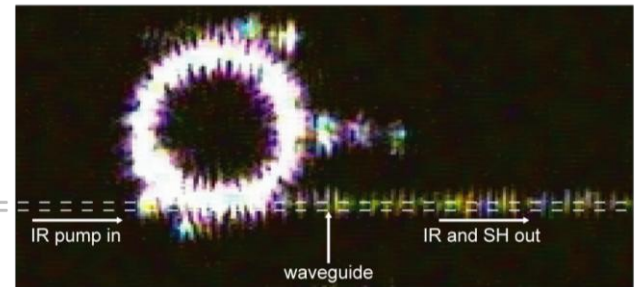
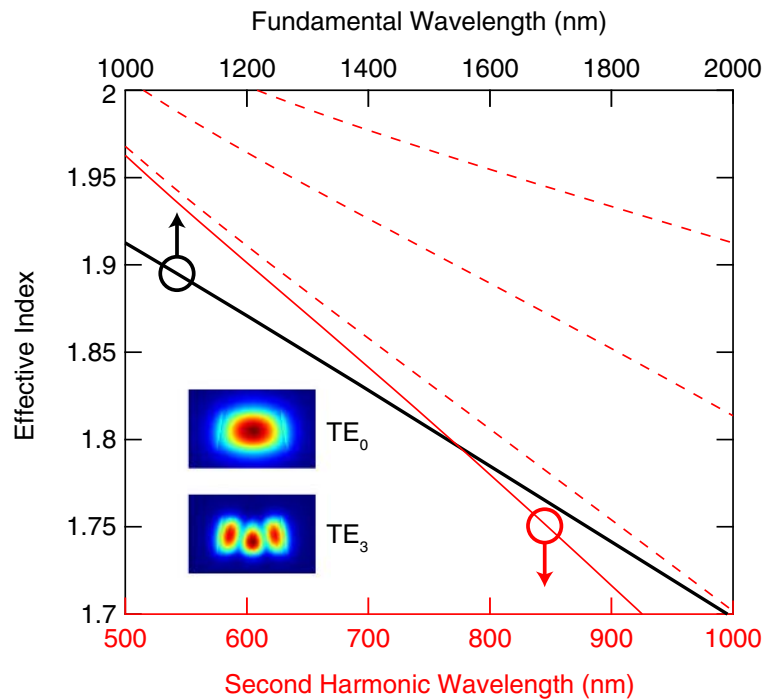


Comb-Offset Detection and Stabilization Using SCG in Si_3N_4

- Carrier envelop offset frequency (f_{ceo}) beatnote from f -to- $2f$ interferometry
- Coupled pulse energy = 36 pJ
Peak power = 0.34 kW
- f_{ceo} signal-to-noise ratio 40 dB



Simultaneous SHG and SCG with Si_3N_4

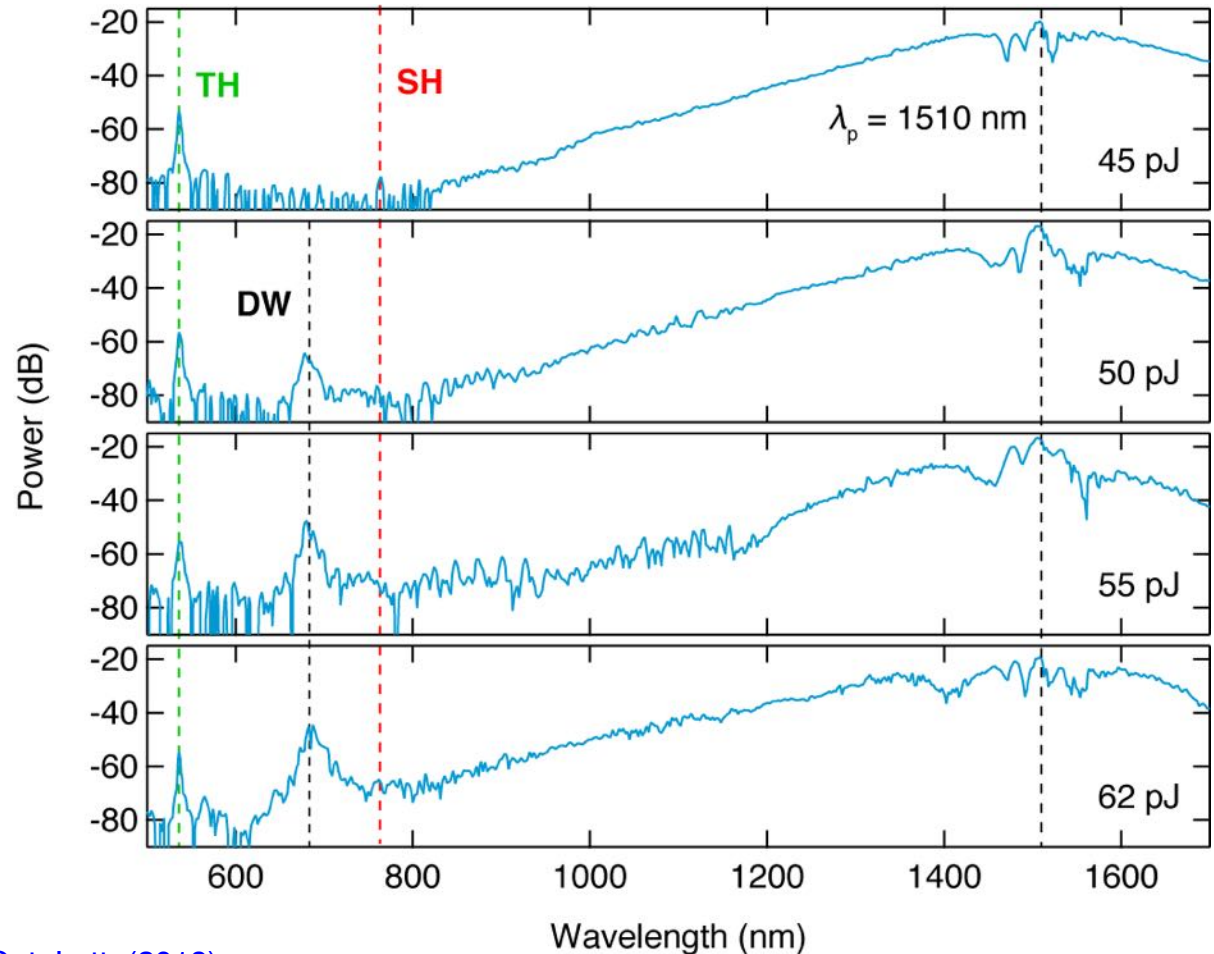
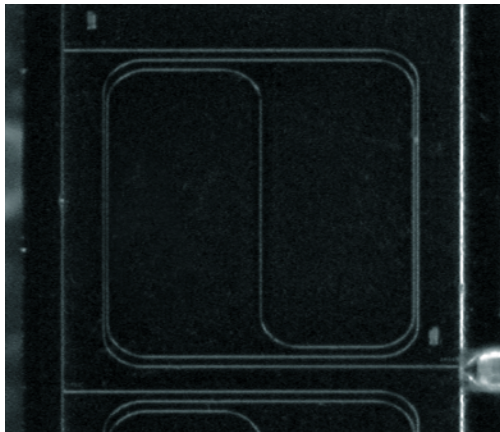


Levy, et al. Gaeta & Lipson, *Opt. Express* (2011).

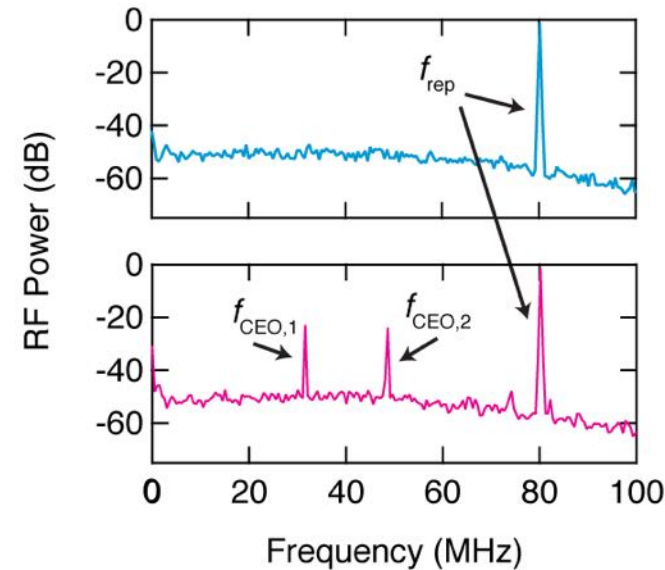
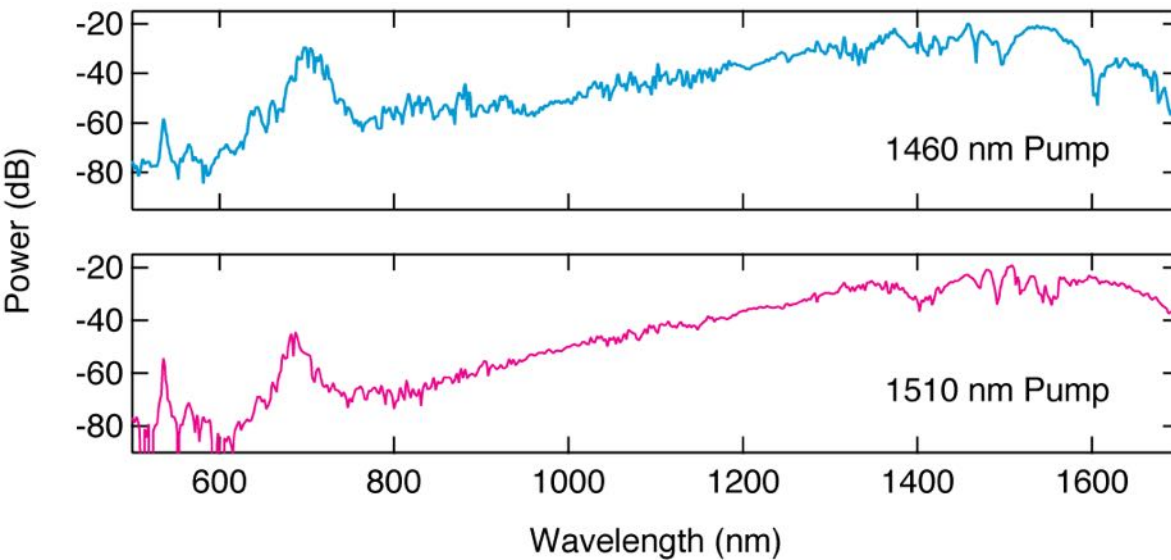
- Si_3N_4 can exhibit $\chi^{(2)}$ response due to symmetry breaking at waveguide interface, high film stress, or electromigration

Lettieri, et al. (2002); Levy, et al. (2011); Khurgin, et al. (2015); Billat et al. (2017).

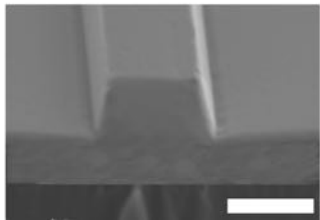
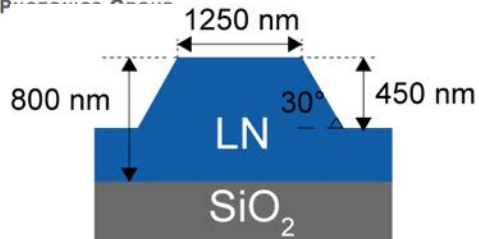
- 2-cm-long Si_3N_4 waveguide
- 200-fs pulse



f_{CEO} Detection via Simultaneous SCG and SHG

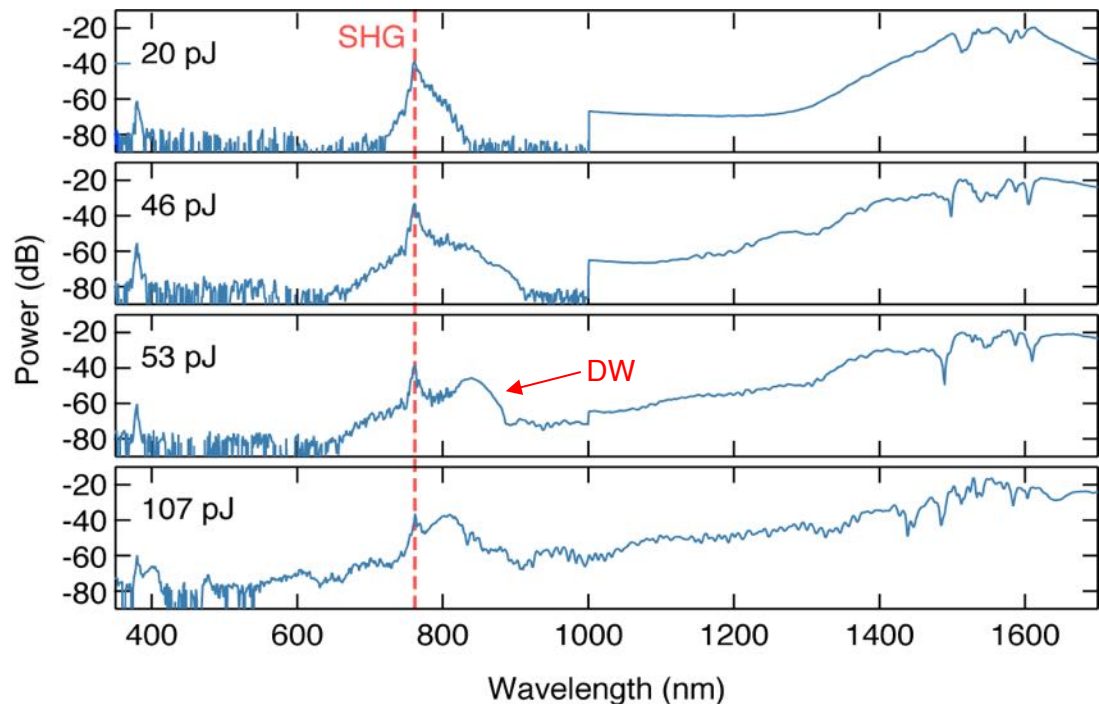


- Measured f_{CEO} beatnote with 27 dB signal-to-noise ratio.
- Carrier envelope offset frequency detection in a single device!

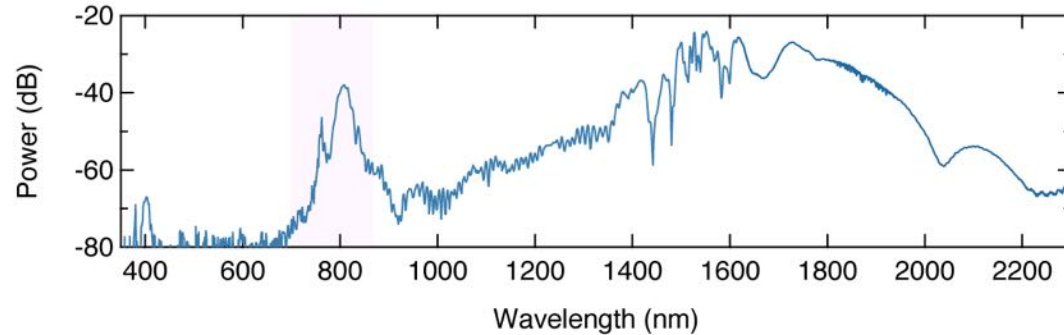


Devices fabricated
by Loncar Group

- Modelocked 90-fs pulses at 1560 nm
- 5-mm-long LN waveguide
- TE mode to access largest $\chi^{(2)}$ nonlinear tensor component

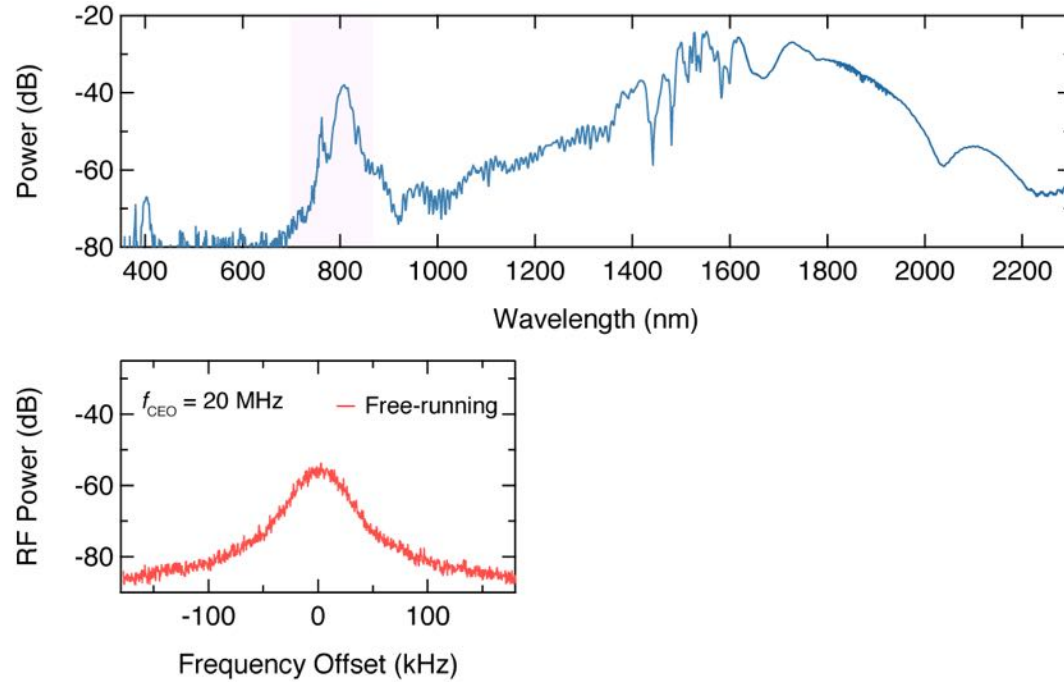


On-Chip f - $2f$ Interferometry for f_{CEO} Stabilization



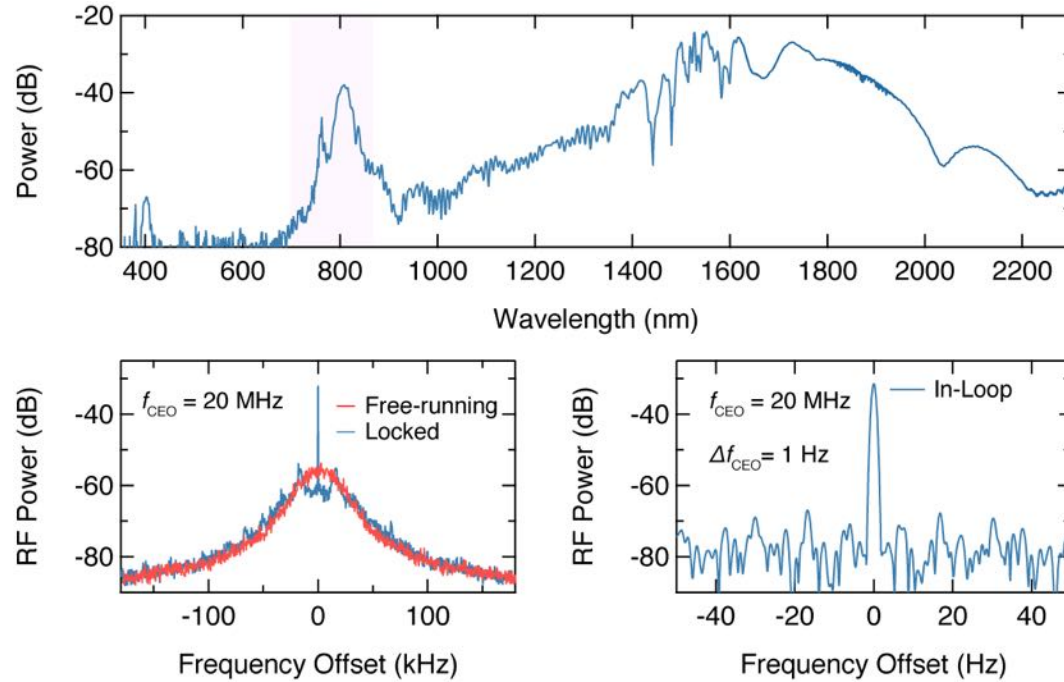
- Octave-spanning spectrum (700 – 2200 nm) with 107 pJ pulse energy
- Direct detection of f_{CEO} with silicon avalanche photodiode (400 – 1000 nm wavelength range)

On-Chip f - $2f$ Interferometry for f_{CEO} Stabilization



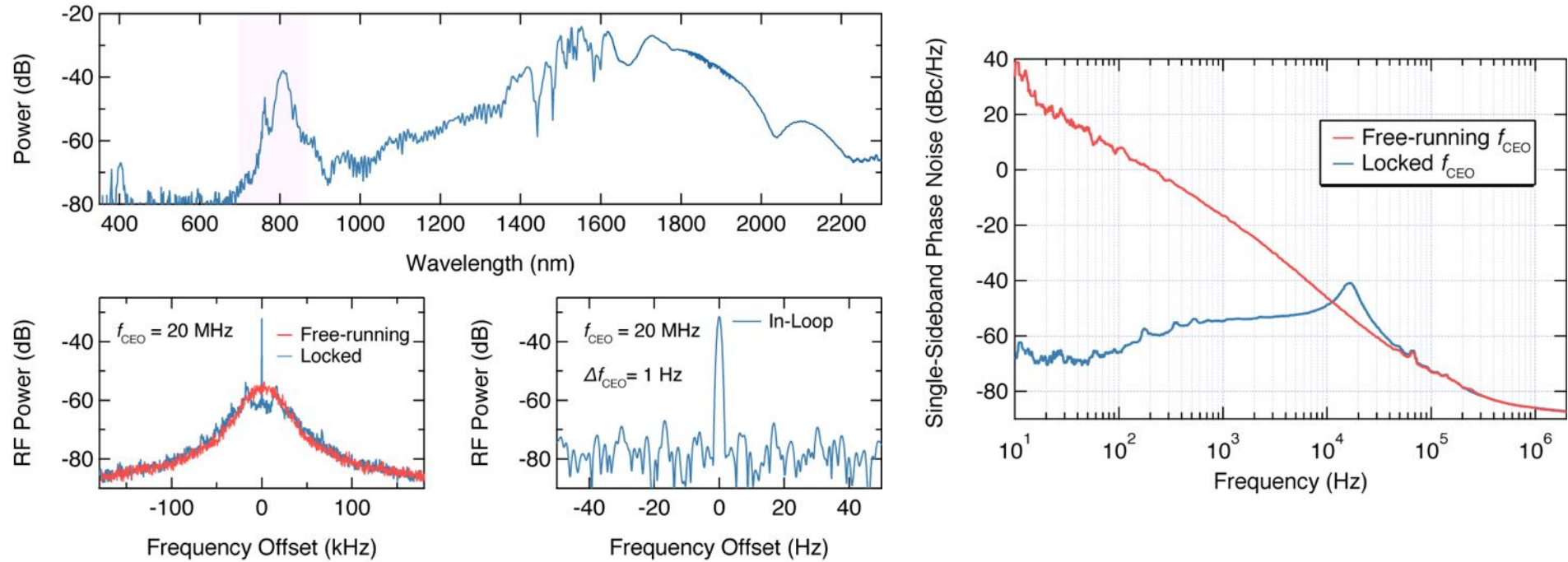
- f_{CEO} phase locked to rubidium frequency standard
- Feedback loop with phase detector and PID controller

On-Chip f - $2f$ Interferometry for f_{CEO} Stabilization



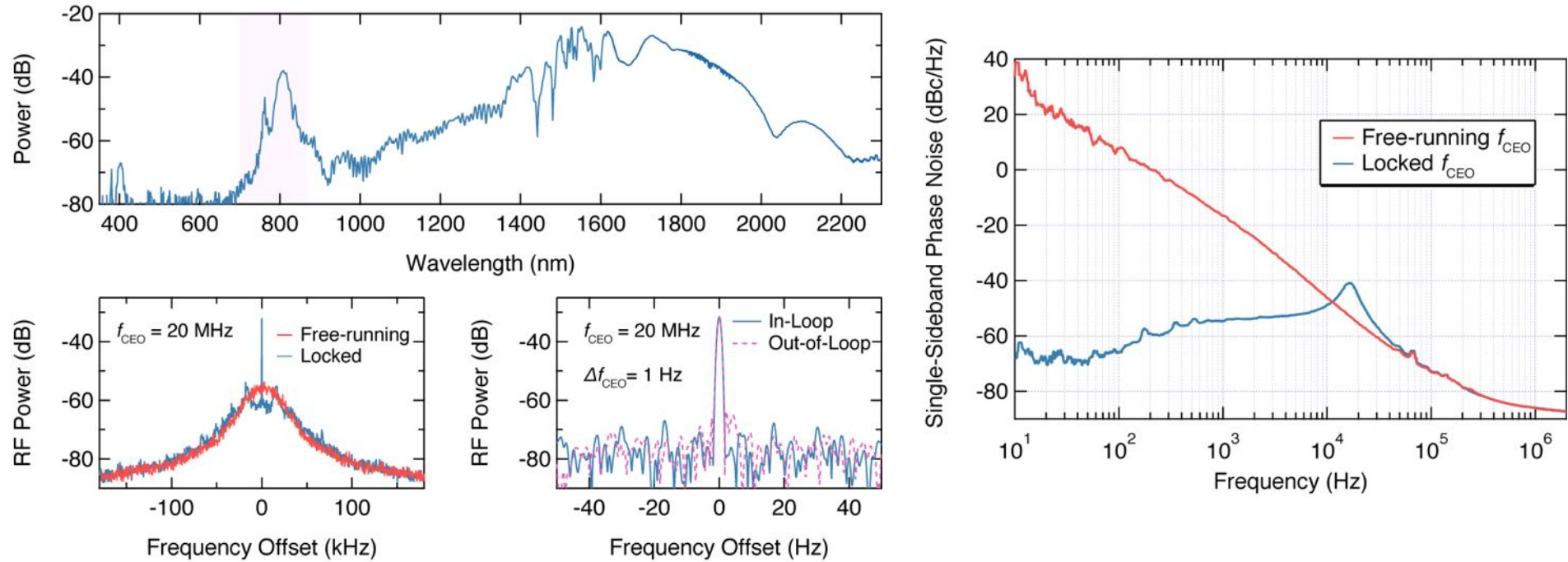
- f_{CEO} has 3-dB bandwidth of 1 Hz (resolution limited)

On-Chip f - $2f$ Interferometry for f_{CEO} Stabilization



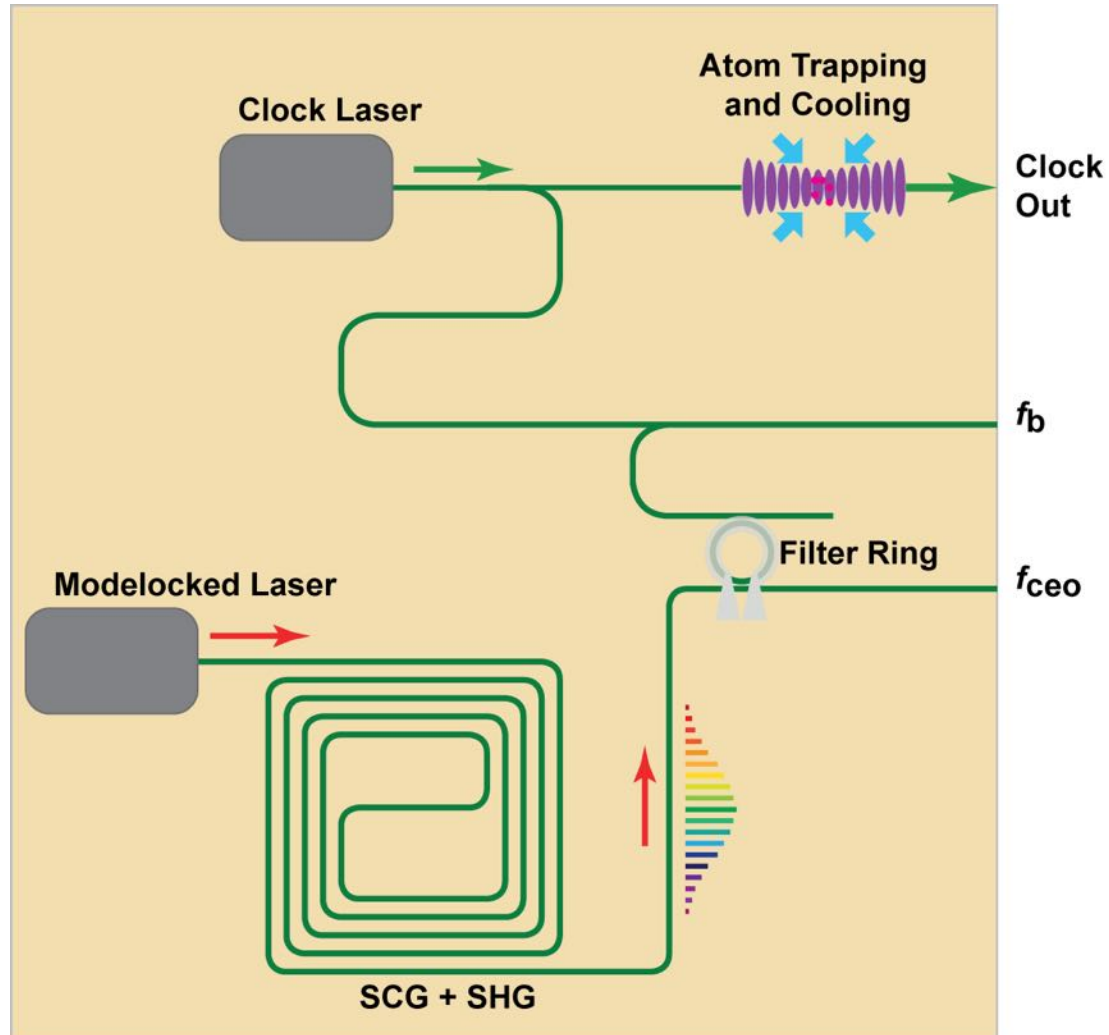
- f_{CEO} has 3-dB bandwidth of 1 Hz (resolution limited)
- >100 dB/Hz reduction of phase noise at 10 Hz

On-Chip f - $2f$ Interferometry for f_{CEO} Stabilization

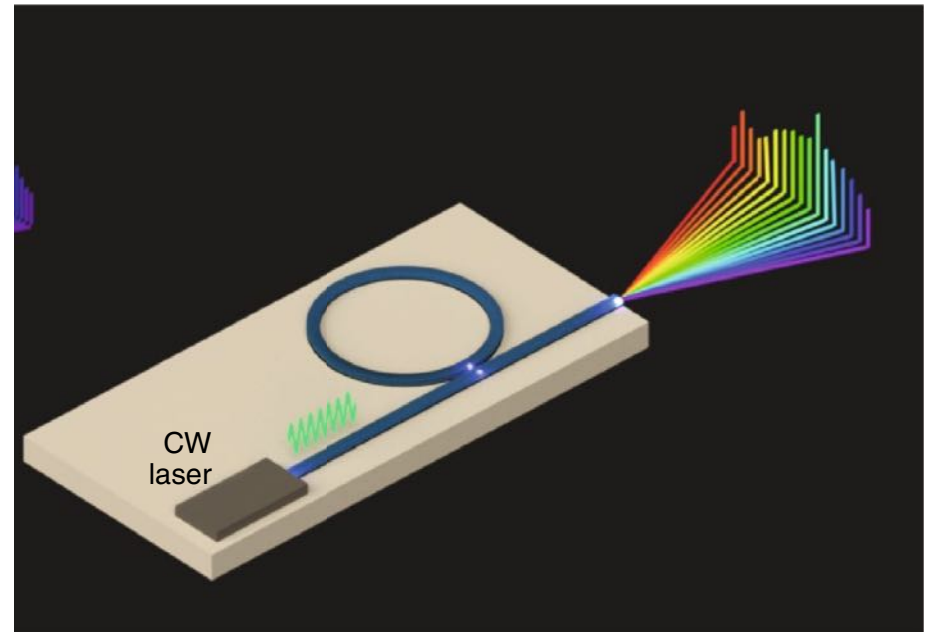


- f_{CEO} has 3-dB bandwidth of 1 Hz (resolution limited)
- >100 dB/Hz reduction of phase noise at 10 Hz
- Out-of-loop f_{CEO} measurement using conventional f - $2f$ interferometer

All-Optical Clock

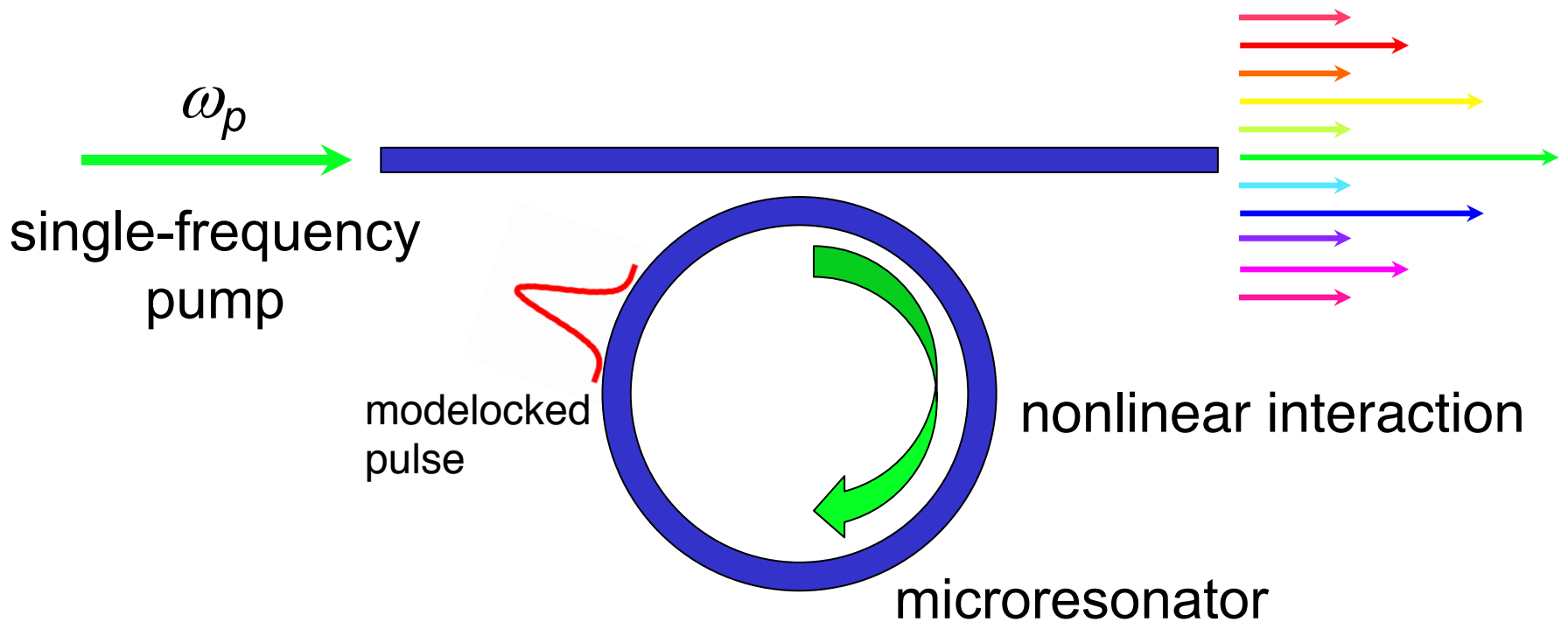
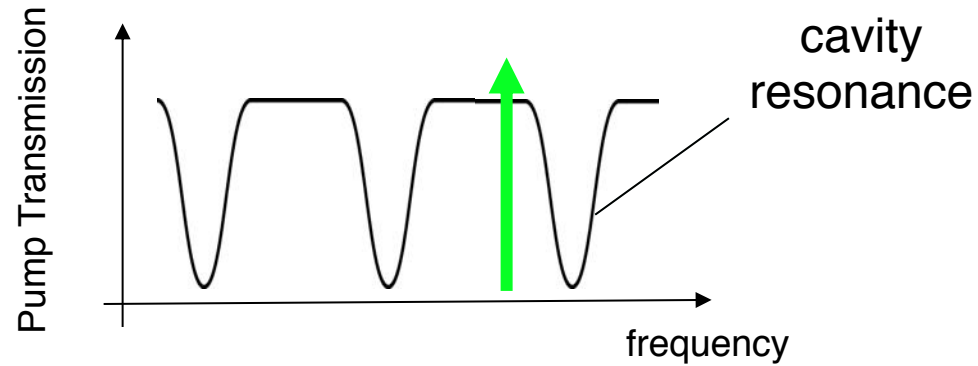


Kerr-Comb Generation

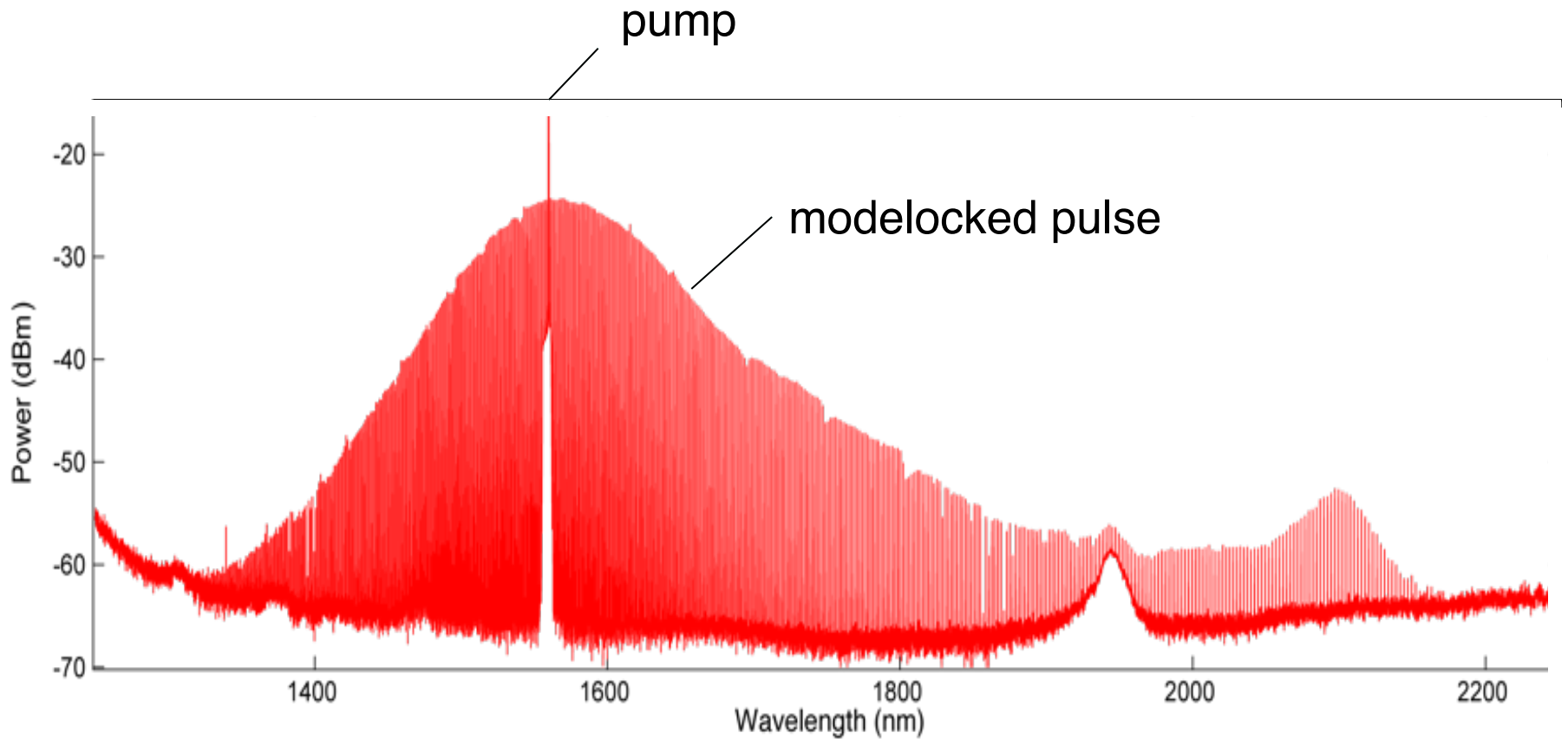


Review Article: Gaeta, Lipson, and Kippenberg, Nature Phot. (2019)

Comb Generation in Microresonators



Comb Generation in Microresonators



- Lugiato-Lefever model: NLSE with ring-resonator B.C.

Lugiato and Lefever, (1987); Haelterman, et al.(1992); Leo, et al. (2010); Matsko, et al.(2011); **Coen, et al. (2013)**
Chembo and Menyuk (2013); Lamont, Okawachi, & Gaeta (2013).

$$\frac{\partial}{\partial t} A = -(\alpha + i\delta) A - i \frac{L}{L_{DS}} \frac{\partial^2 A}{\partial \tau^2} + i \frac{L}{L_{NL}} |A|^2 A + \eta E_{in}$$

Cavity loss
& detuning

Dispersion

Nonlinearity

Pump

Dissipative soliton solutions exist

$$A(\tau) \sim C_1 + C_2 \sum_{j=1}^N \operatorname{sech} \left[(\tau - \tau_j) / \tau_0 \right]$$

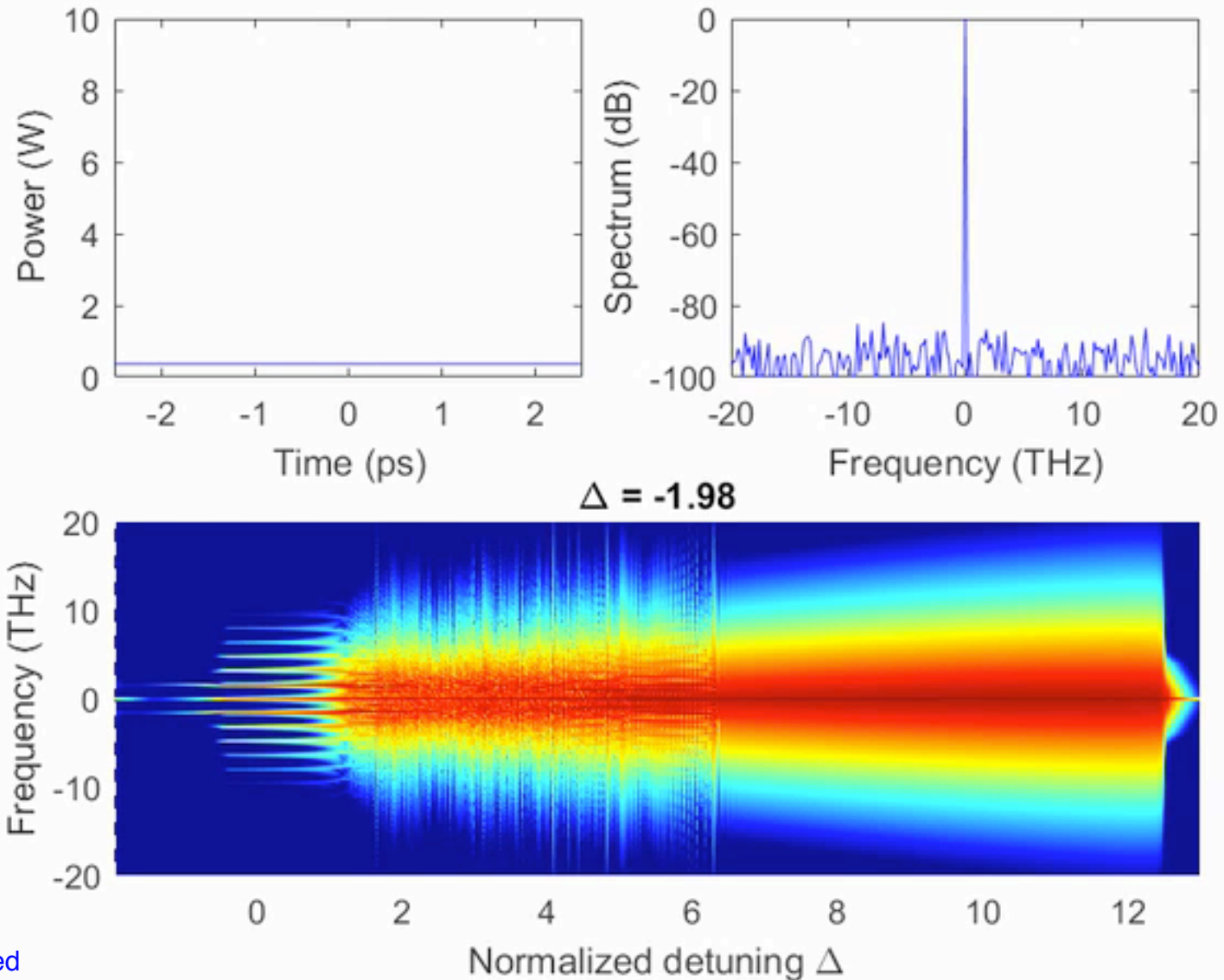
Haelterman, Trillo, and Wabnitz, *Opt. Commun.* (1992).

Wabnitz, *Electron. Lett.* (1993).

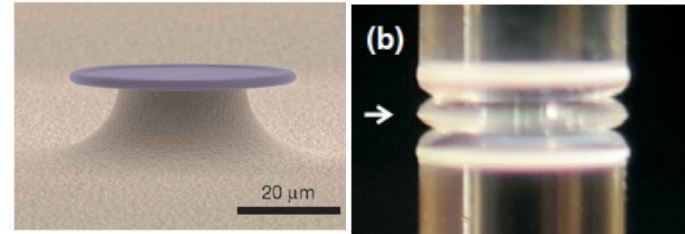
Nakazawa, et al. (1988).

Herr, et al., Kippenberg, *Nature Phot.* (2014).

Simulations: Dynamics versus Detuning



Microresonator-Based Frequency Combs



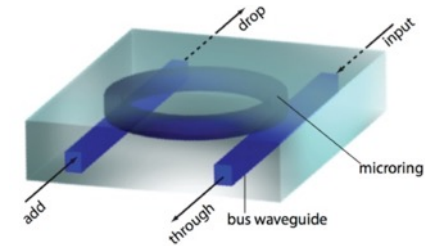
silica

Del' Haye, et al., Nature (2007)
Agha, et al., Opt. Express (2009)
Li, et al., PRL (2012)
Papp, et al., PRX (2013)



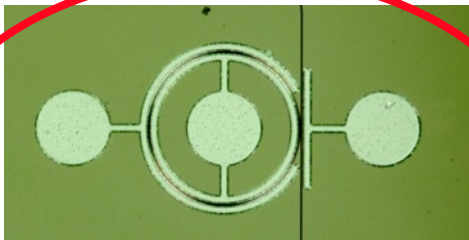
CaF₂, MgF₂, & quartz

Savchenkov, et al., PRL (2008)
Liang, et al., Opt. Lett. (2011)
Papp & Diddams, PRA (2011)
Herr, et al., Nature Photon. (2012)



high-index glass

Razzari, et al., Nature Photon. (2010).
Pasquazi, et al., Opt. Express (2013).



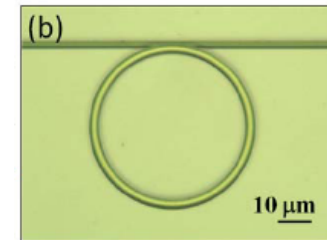
silicon

Griffith, et al., Nature Comm. (2014)
Yu, et al., Optica (2016)



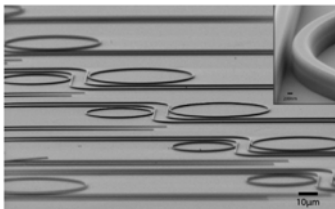
silicon nitride

Levy, et al., Nature Photon. (2010)
Ferdous, et al., Nature Photon. (2011)
Herr, et al., Nature Photon. (2012)



Al nitride

Jung, et al., Opt. Lett. (2013)



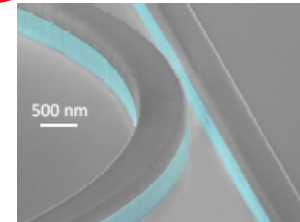
diamond

Hausmann, et al., Nature Phot. (2013)



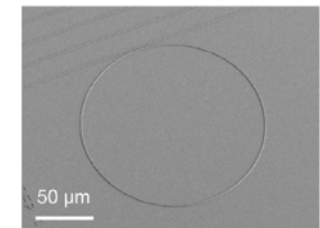
GaP

Wilson, et al., Nature Phot. (2018)



AlGaAs

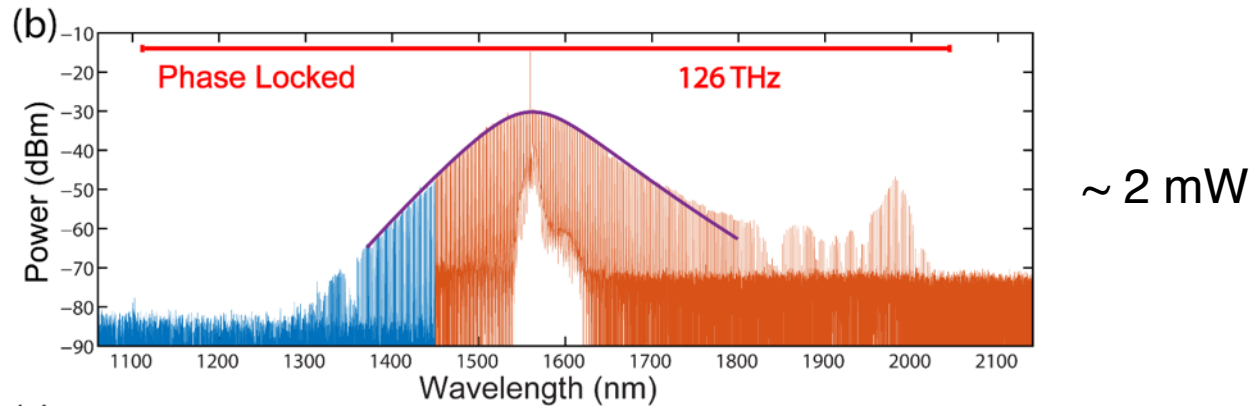
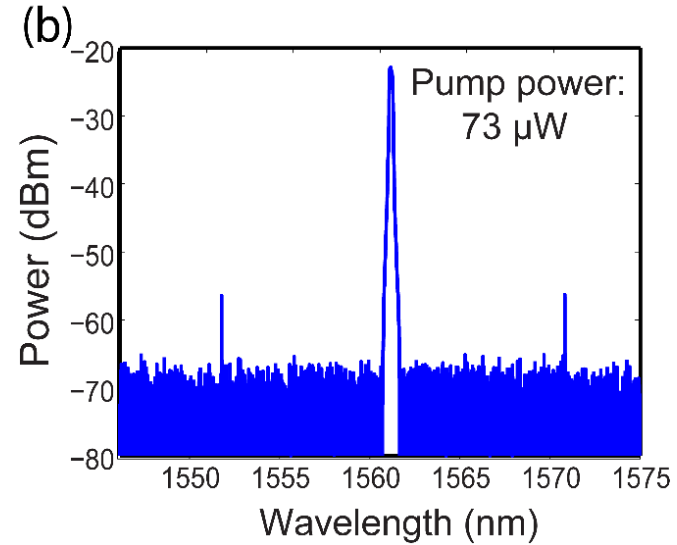
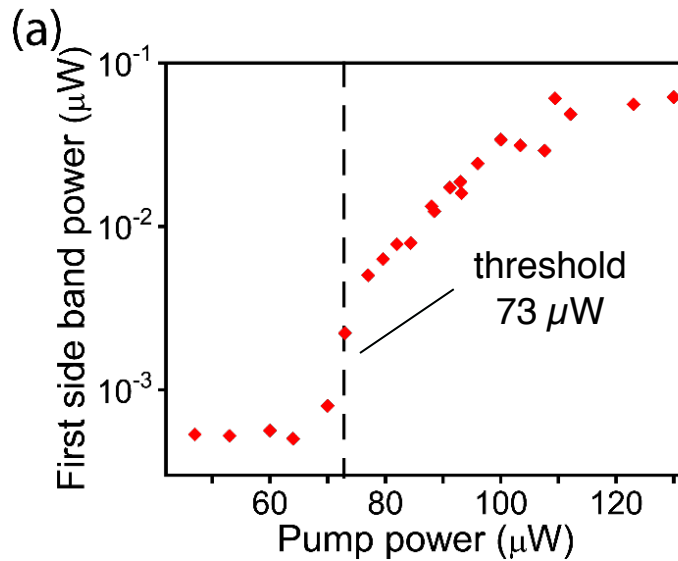
Pu, et al., Optica (2016)



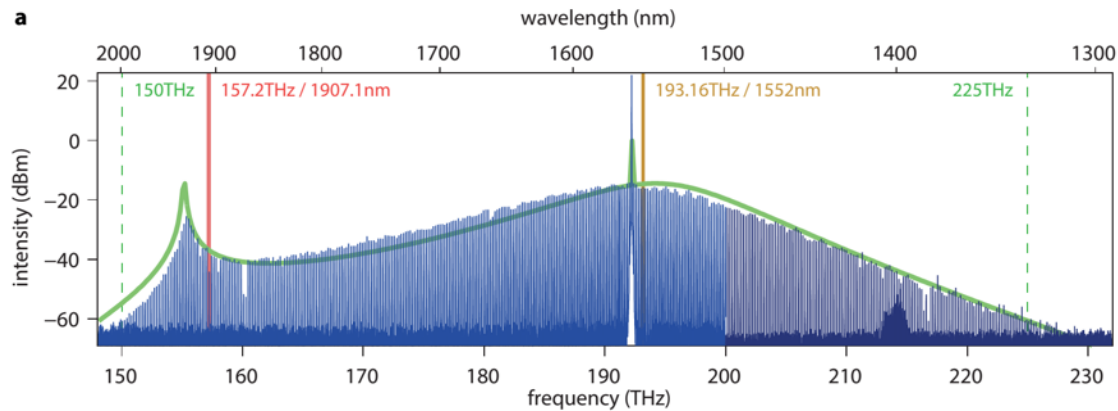
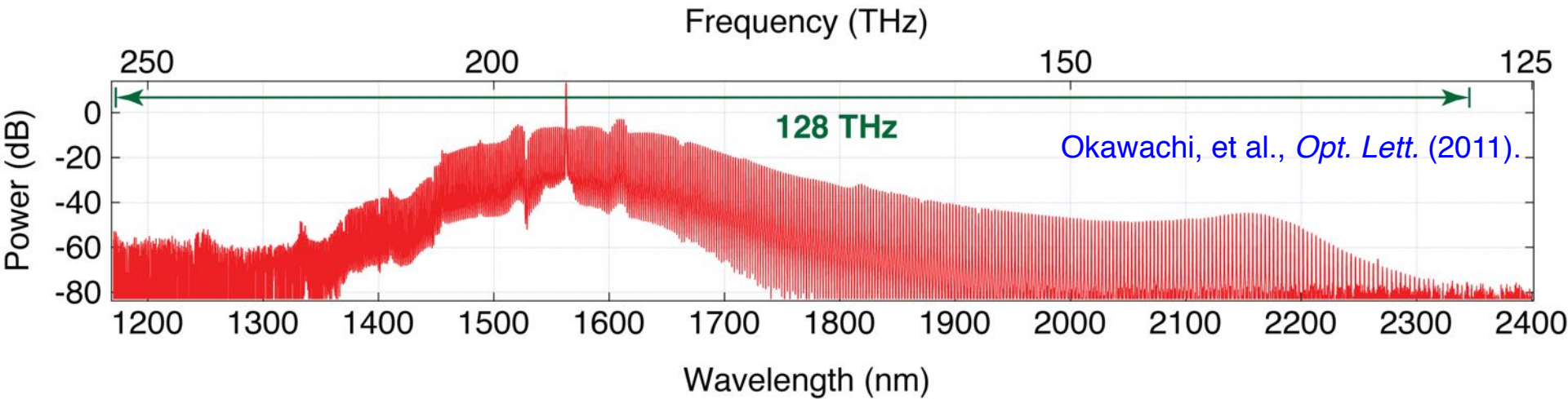
lithium niobate

Wang, et al., Opt. Lett. (2018)
He, et al., Optica (2019)
Yu, et al., Light (2020)

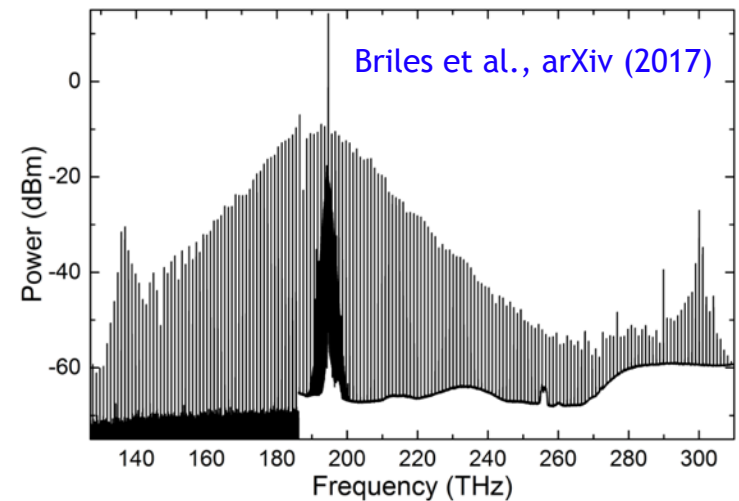
Ultrahigh-Q SiN Microresonators



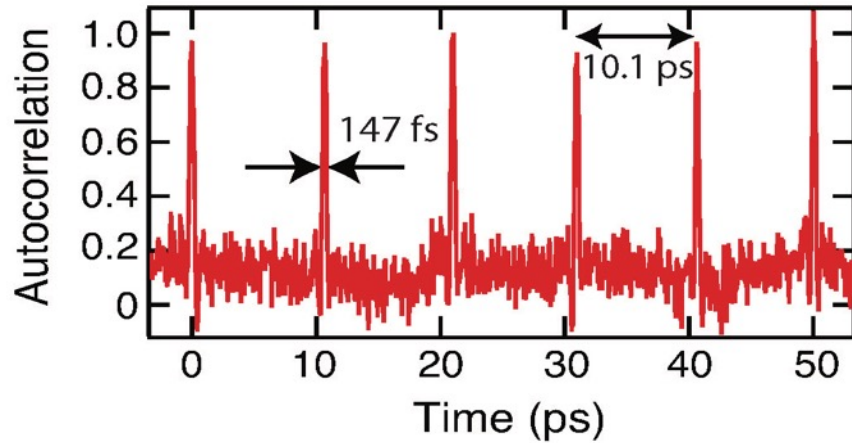
Octave-Spanning Comb in Si_3N_4 Microresonators



Brasch et al., *Science* (2016)



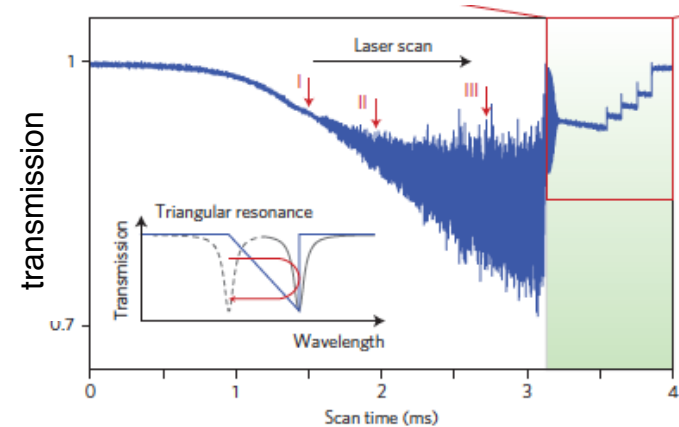
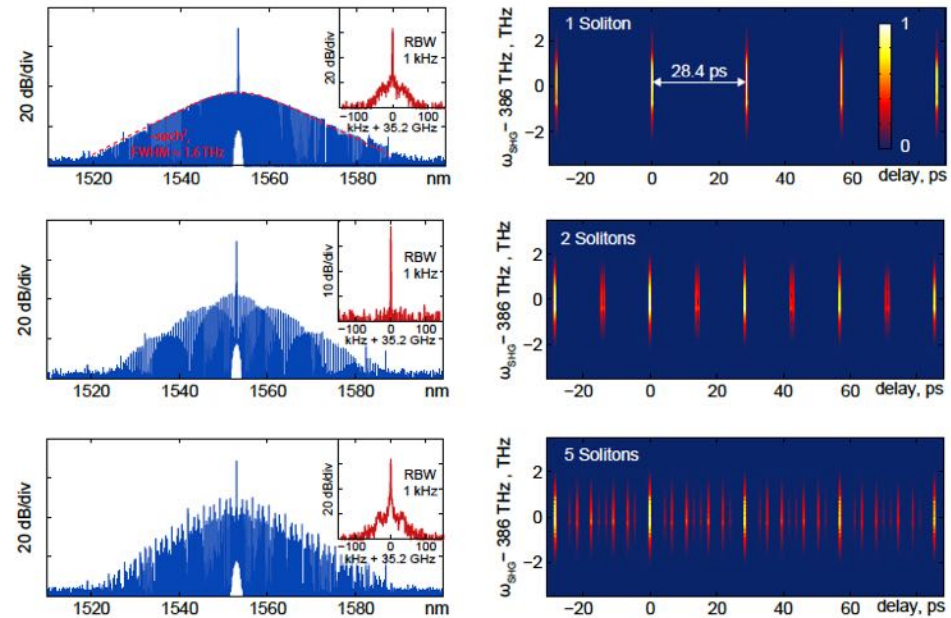
Modelocking & Dissipative Solitons in Microresonators



Saha et al, Opt. Express (2013).

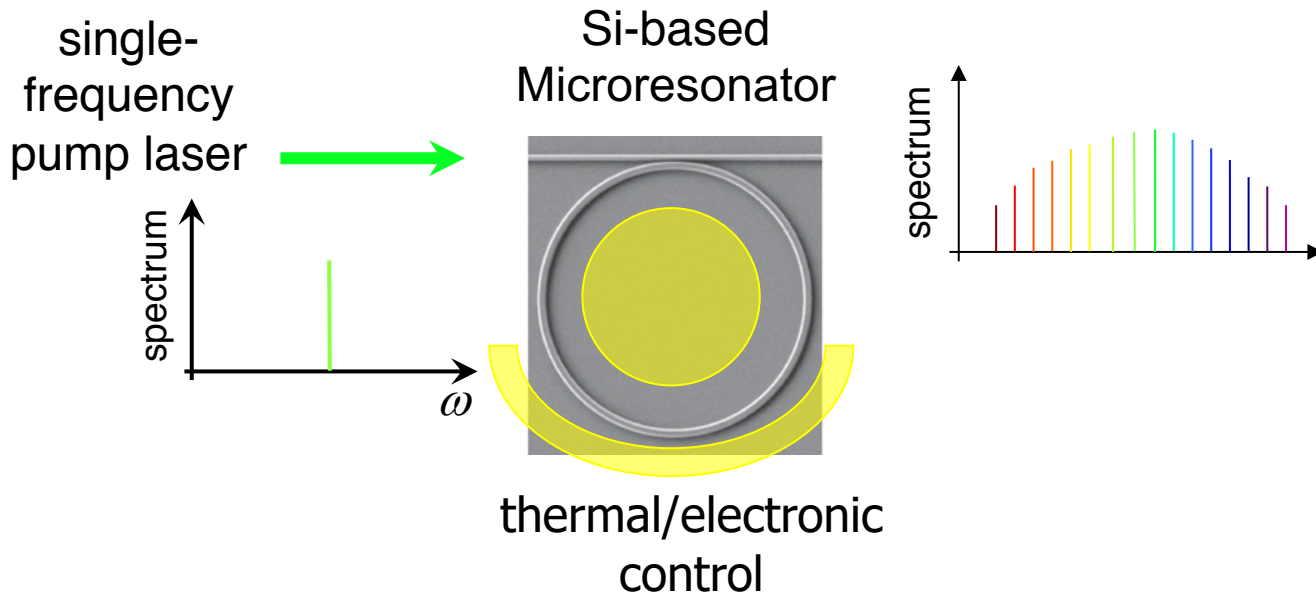
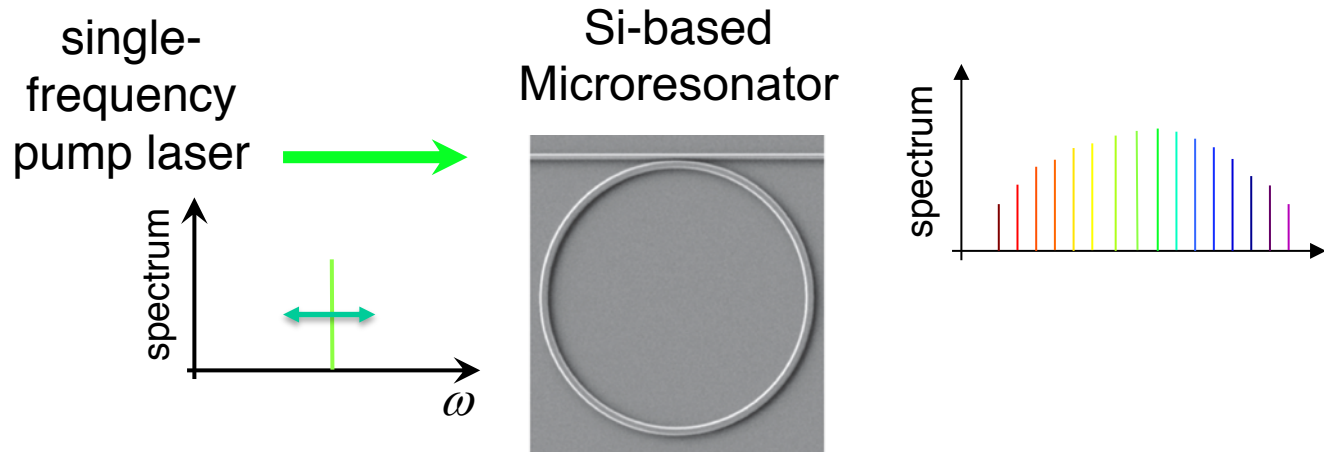
Review:

Kippenberg, Gaeta, Lipson, Gorodetsky
Science (2018).

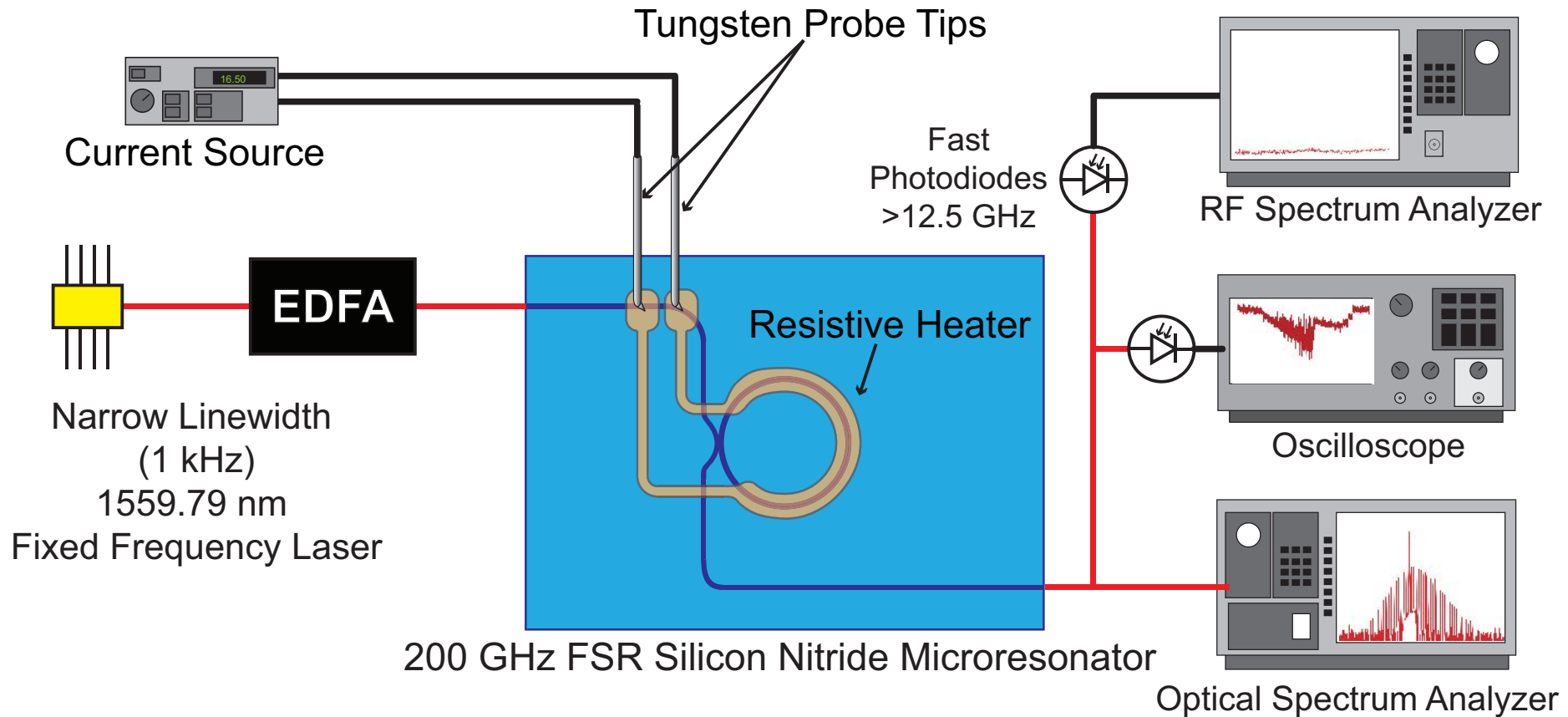


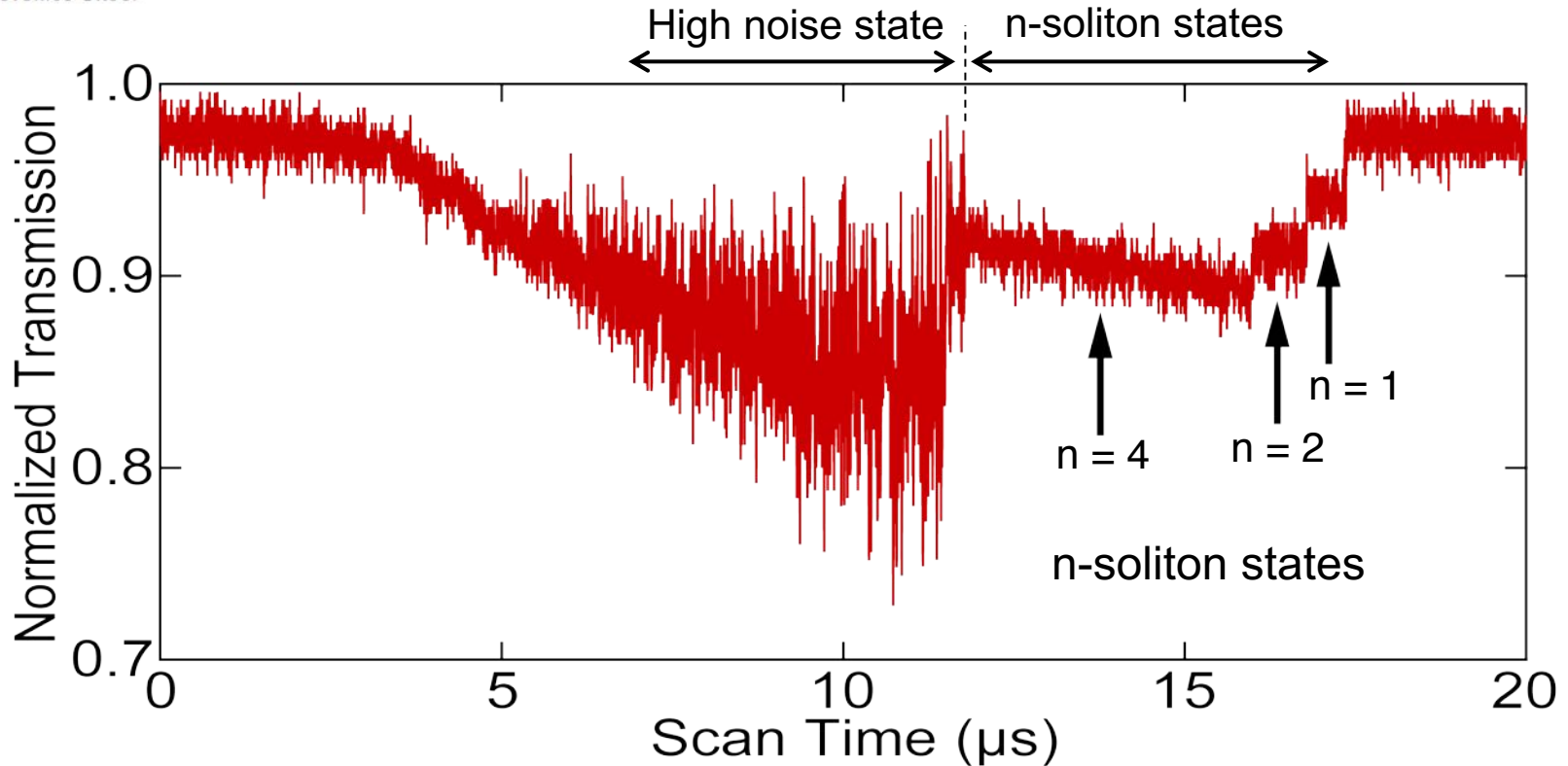
Herr, et al., Kippenberg, *Nature Phot.* (2014)

Pump Detuning Control in Microresonators



Experimental Setup



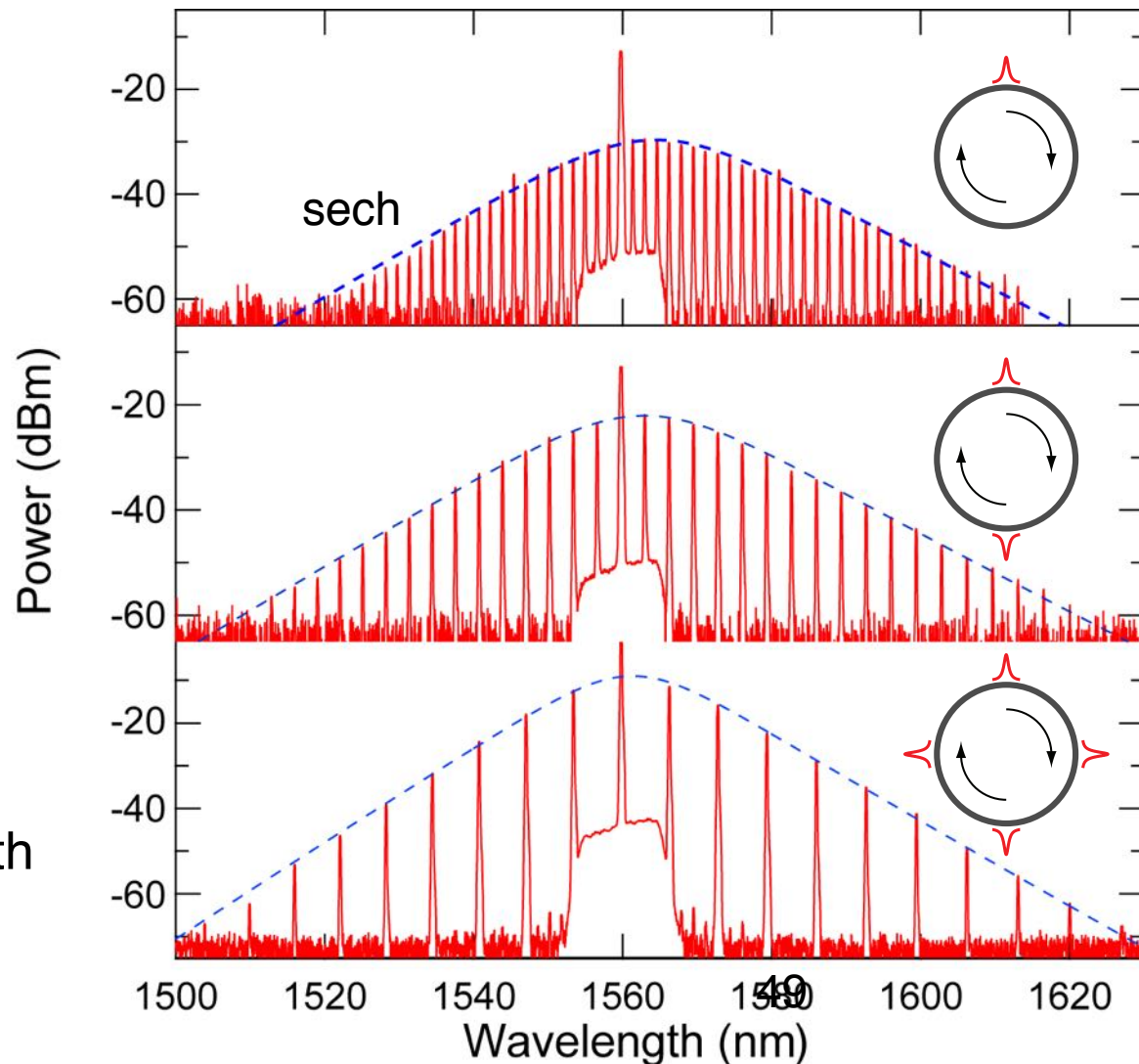


Joshi, et al., Lipson, Gaeta, *Opt. Lett.* (2016)

- Step-like features characteristic of soliton modelocking, similar to pump tuning [Herr, et al. Nature Photon. \(2014\)](#)

Spectral modulations due to relative positions of solitons

- Single Soliton – 1 FSR
- Two Soliton – 2 FSR
- Four Soliton – 4 FSR
- Show good agreement with sech^2 envelope





Microresonator Comb Spectral Coverage



Visible

Near-Infrared

Mid-Infrared

Si [6] 4500 nm

Si₃N₄ [5]

MgF₂ [4] 2550 nm

Si₃N₄ [3] 2350 nm

SiO₂ [2] 2170 nm

Si₃N₄ [1] 1540 nm

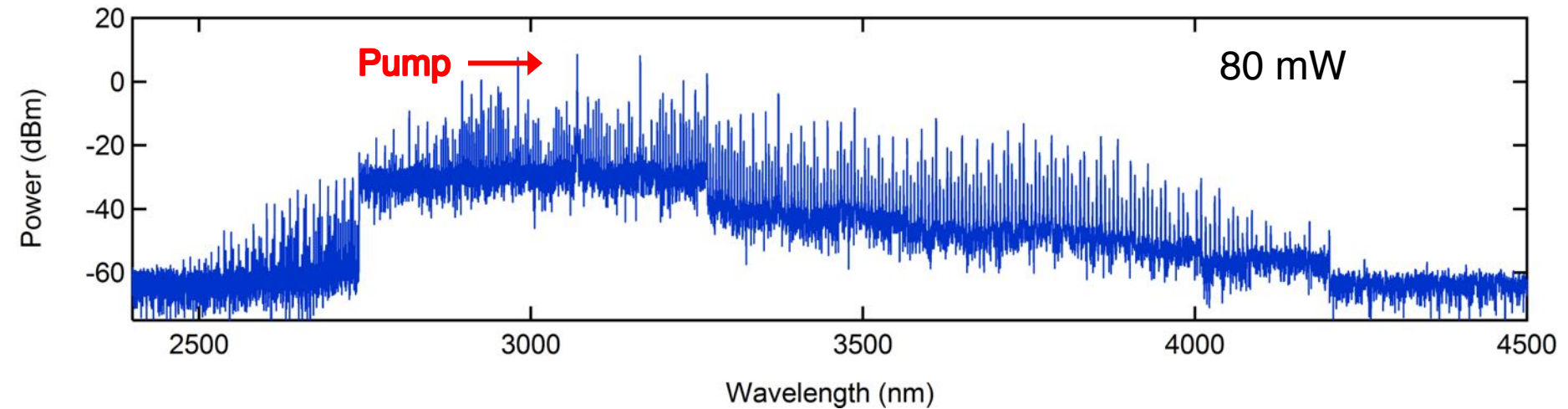
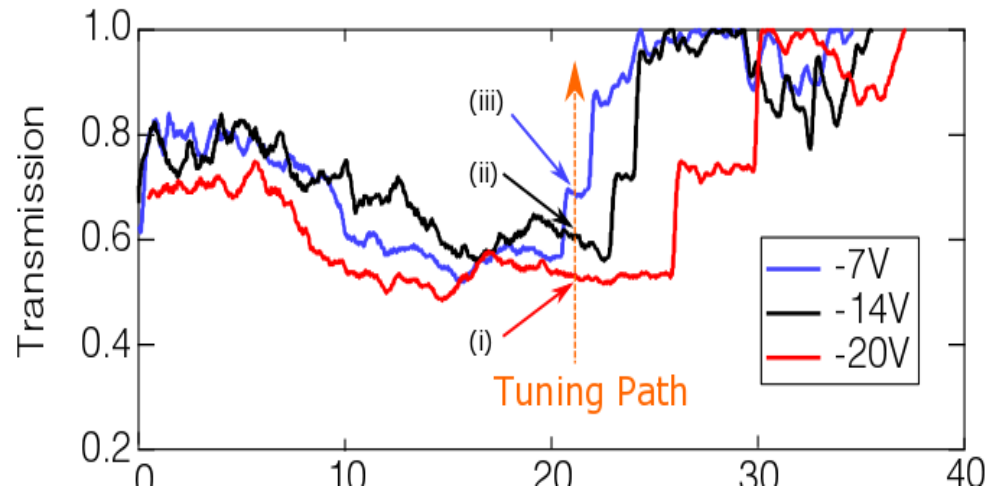
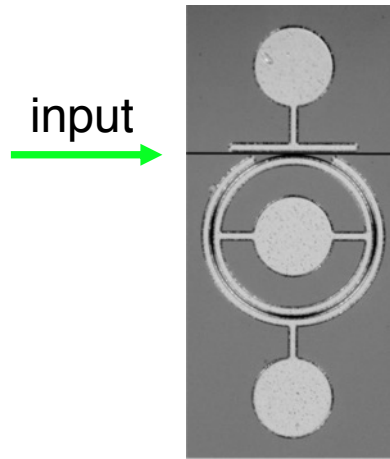
Si₃N₄ [7] 780nm

SiO₂ [8] 778nm

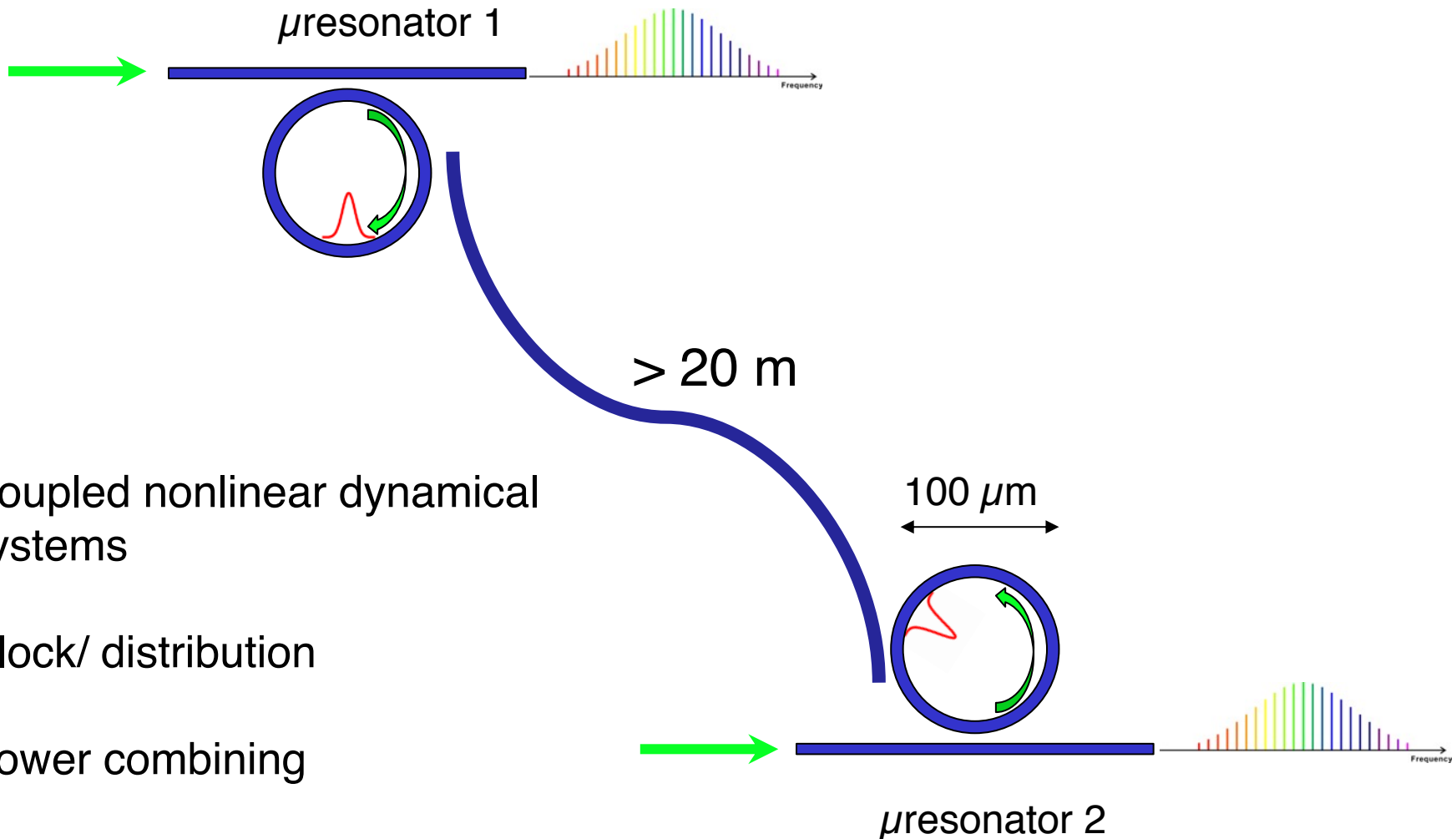
CaF₂ [9] 794 nm



[1] Saha, et al., Lipson & Gaeta OE (2013); Luke, et al., Gaeta & Lipson, OE (2016).
 [2] Del'Haye, et al., and Kippenberg, Phys. Rev. Lett. (2011).
 [3] Okawachi, et al., Lipson & Gaeta, Opt. Lett. (2011); Okawachi, et al., Lipson & Gaeta, Opt. Lett. (2013).
 [4] Wang, et al., and Kippenberg, Nature Comm. (2012).
 [5] Luke, et al., Gaeta and Lipson, Opt. Lett. (2015).
 [6] Griffiths, et al., Gaeta & Lipson, Nat. Comm. (2015); Yu, et al., Lipson & Gaeta, Optica (2016).
 [7] Donvalkar et al., Gaeta and Lipson, CLEO (2017).
 [8] Lee, et al. Vahala, arXiv (2017)
 [8] Savchenkov, et al., Nat. Phot. (2011).

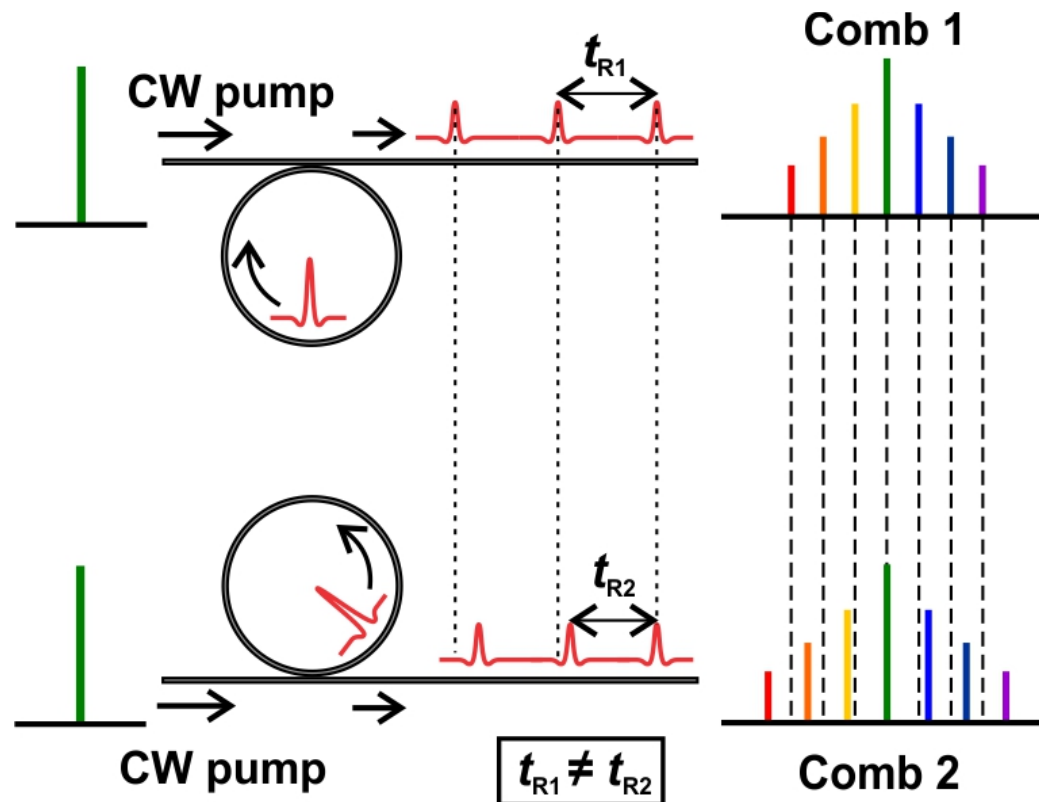


- High pump-to-comb conversion efficiency (40%)

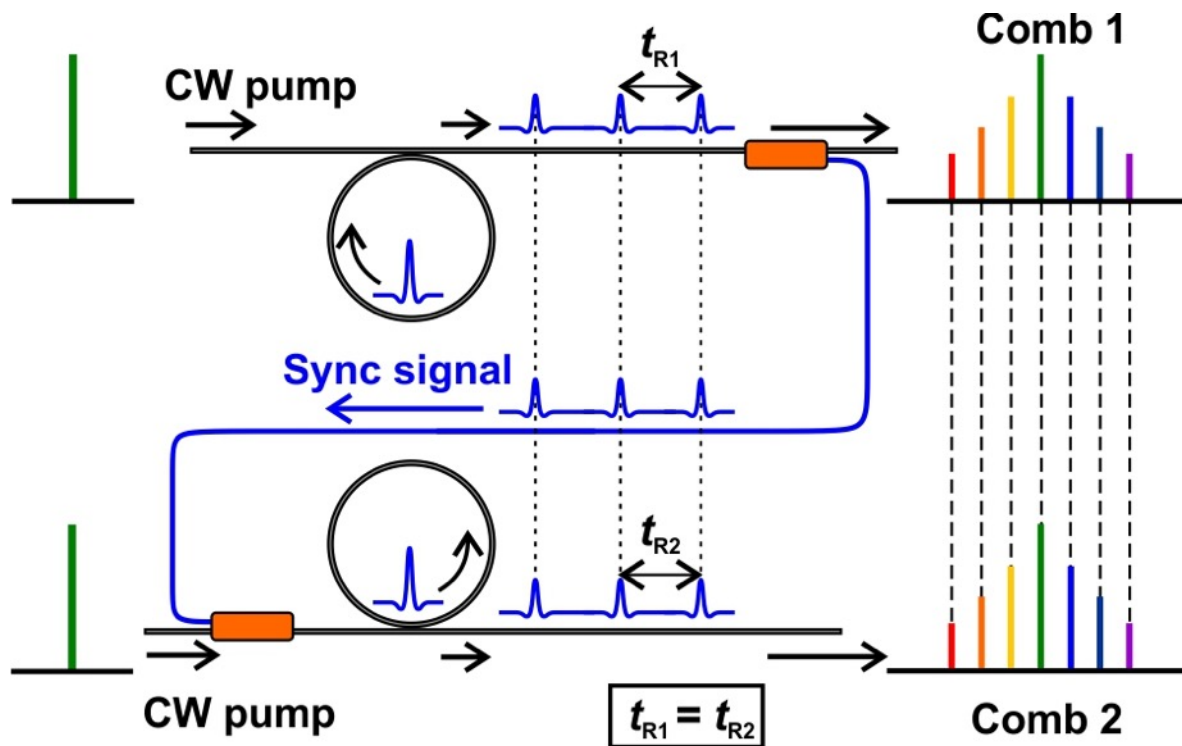


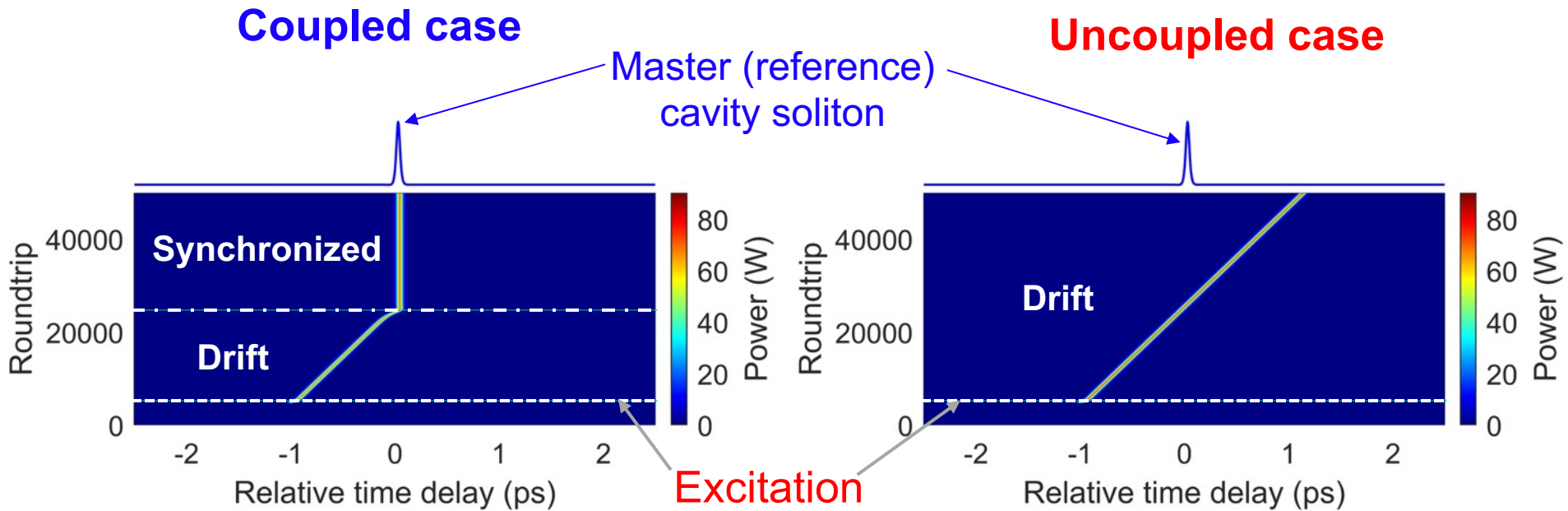
- Coupled nonlinear dynamical systems
- Clock/ distribution
- Power combining
- Microwave mixing applications

- **Comb spacing mismatched**
 - 1) Fabrication uncertainty
 - 2) Environmental fluctuations

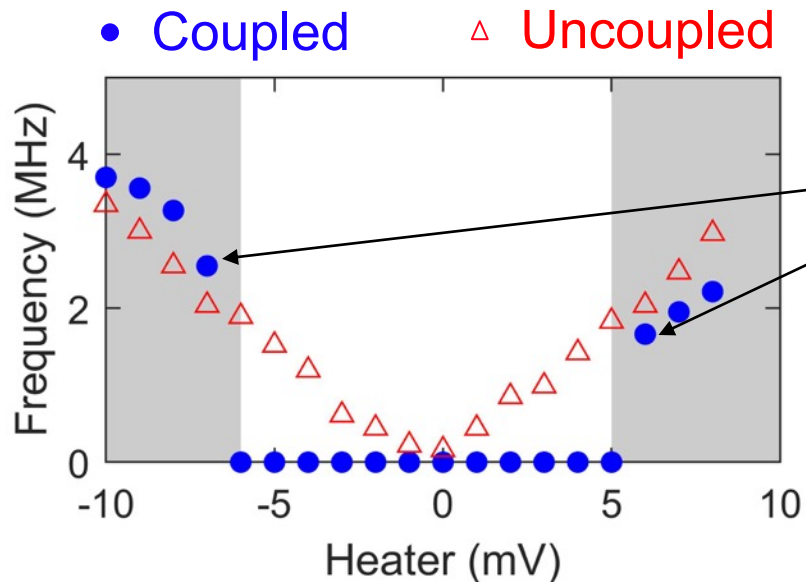
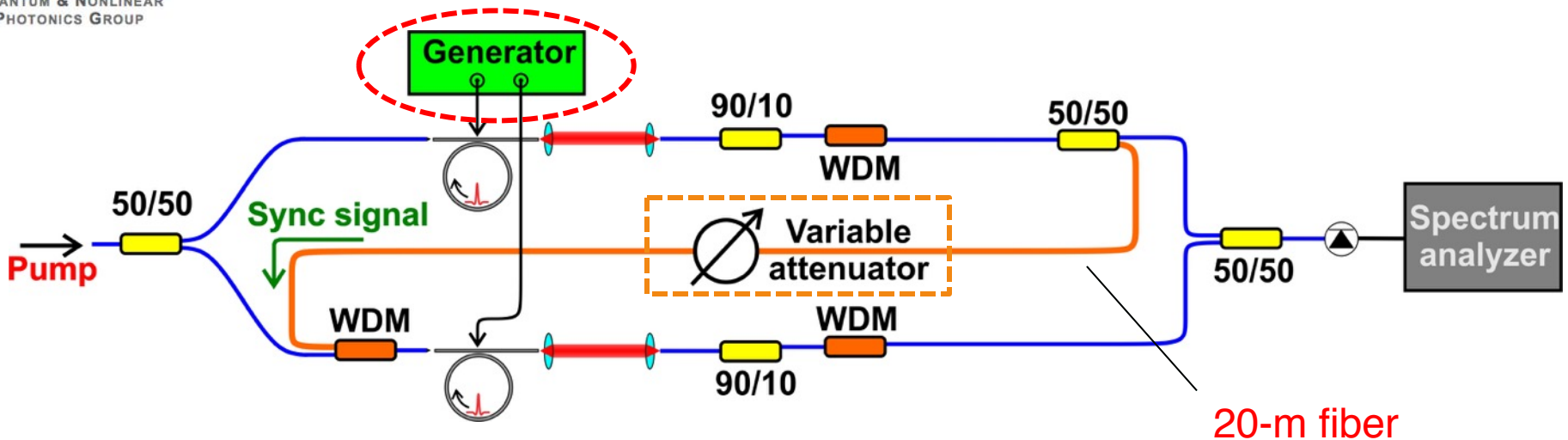


- Couple $<1\%$ of output from one microresonator to other
- Timing of cavity solitons become synchronized

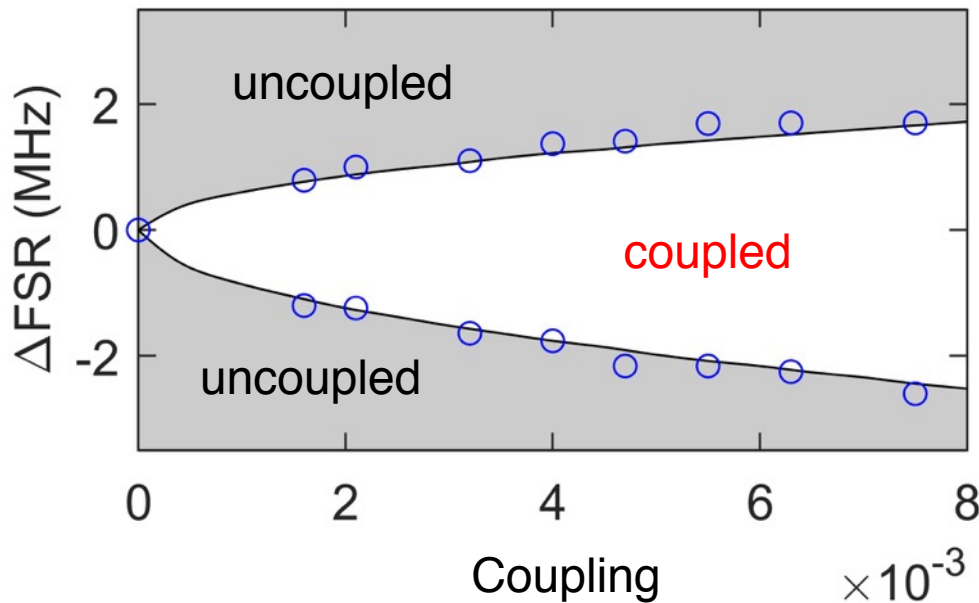
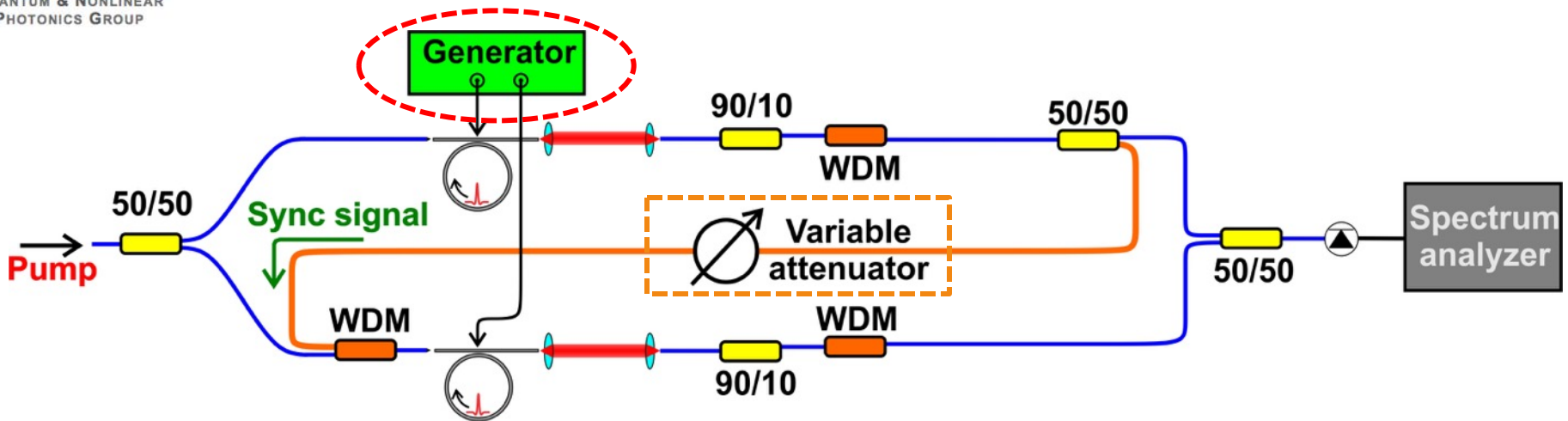




- Natural drift rate is 2 MHz for both cases.



- Allowed mismatch: 2.6 MHz and 1.7 MHz
- Numerical predictions: 2.5 MHz and 1.5 MHz



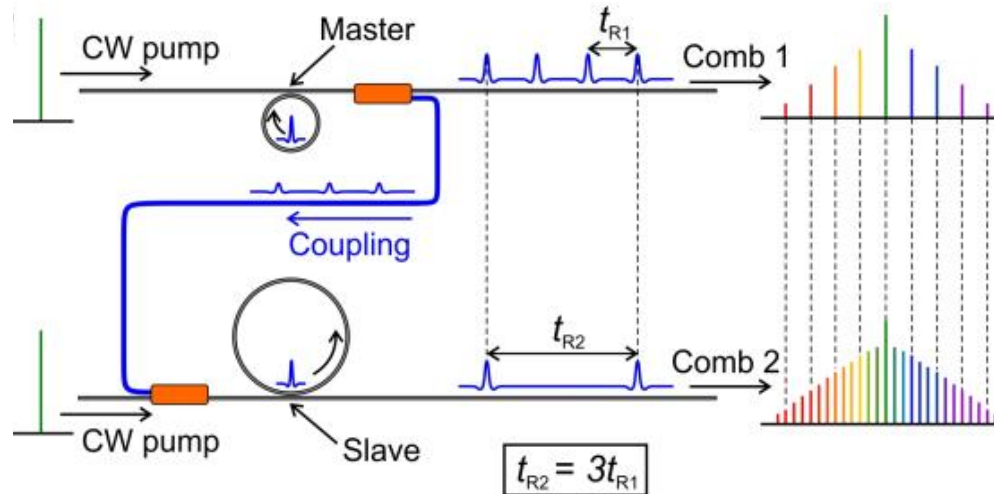
- Allowed mismatches for varying transmission

○ **Experimental**

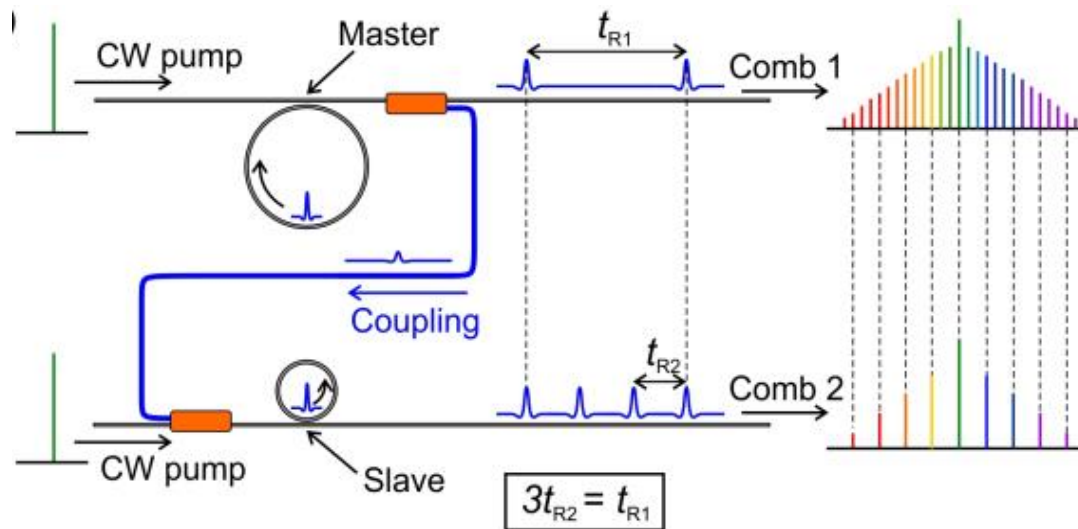
— **Numerical**

Harmonic & Sub-Harmonic Synchronization

Sub-Harmonic Synchronization

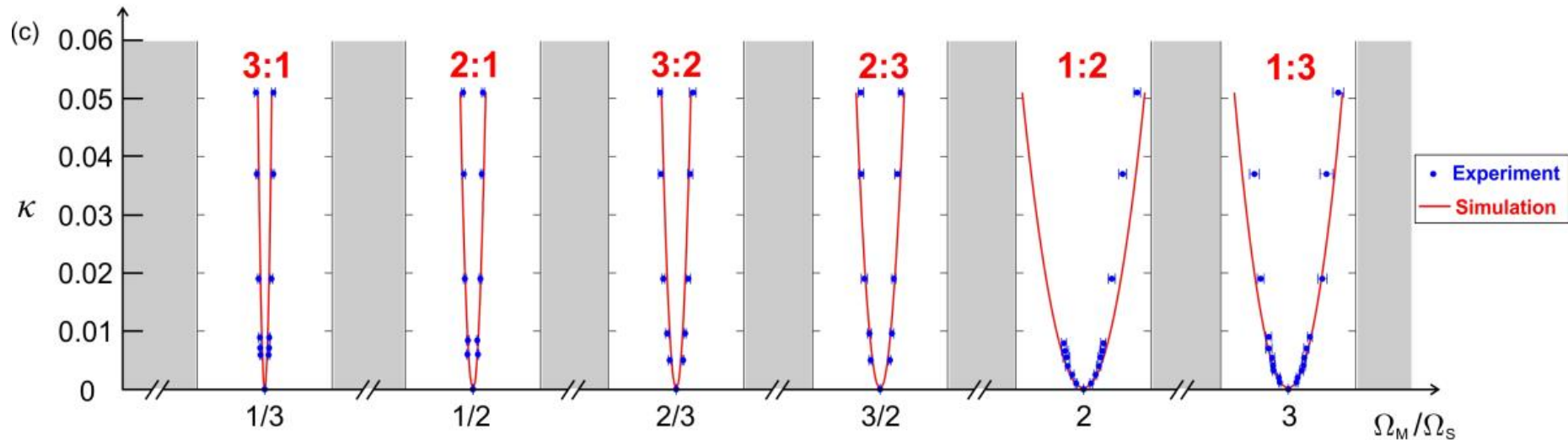


Harmonic Synchronization

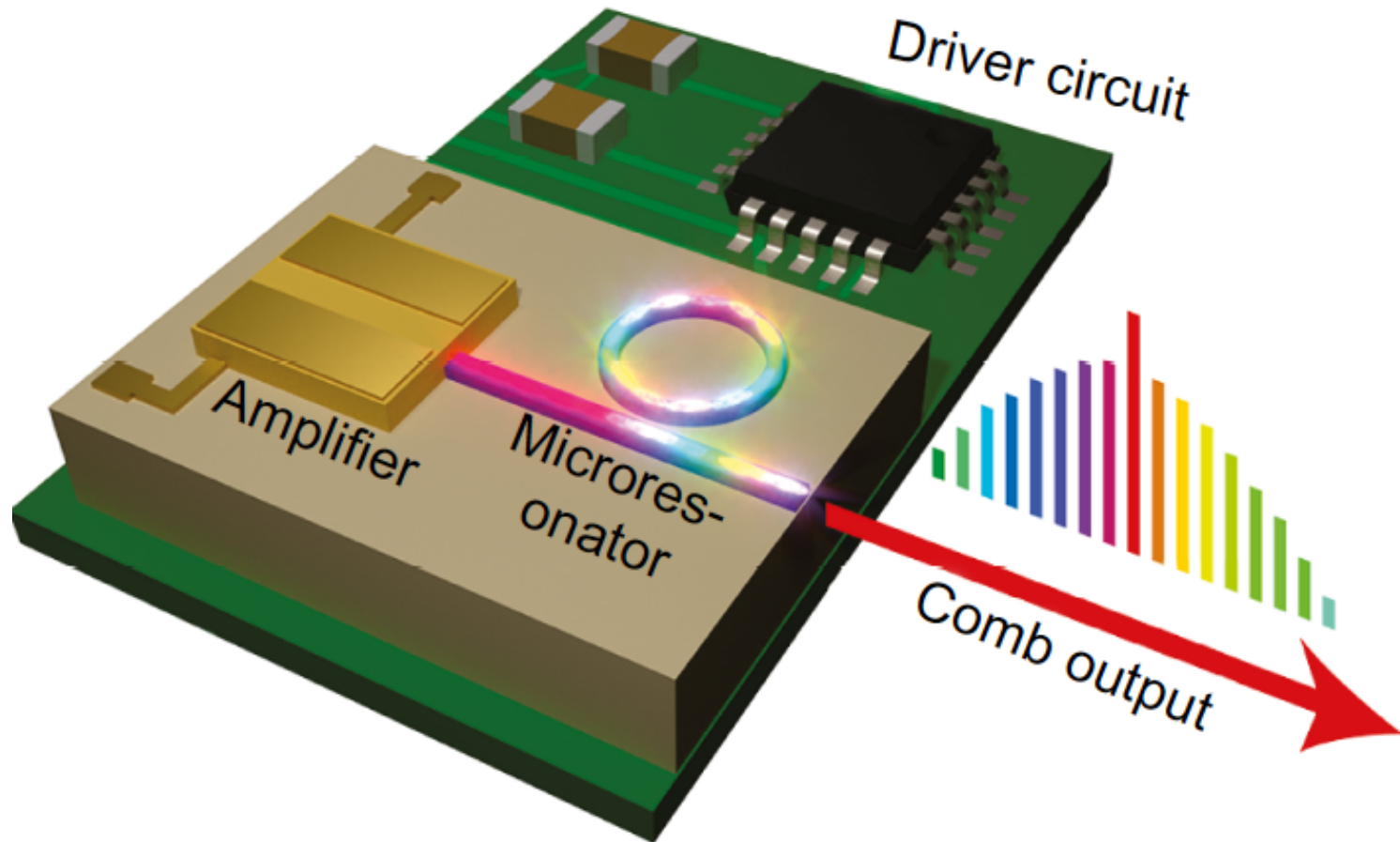


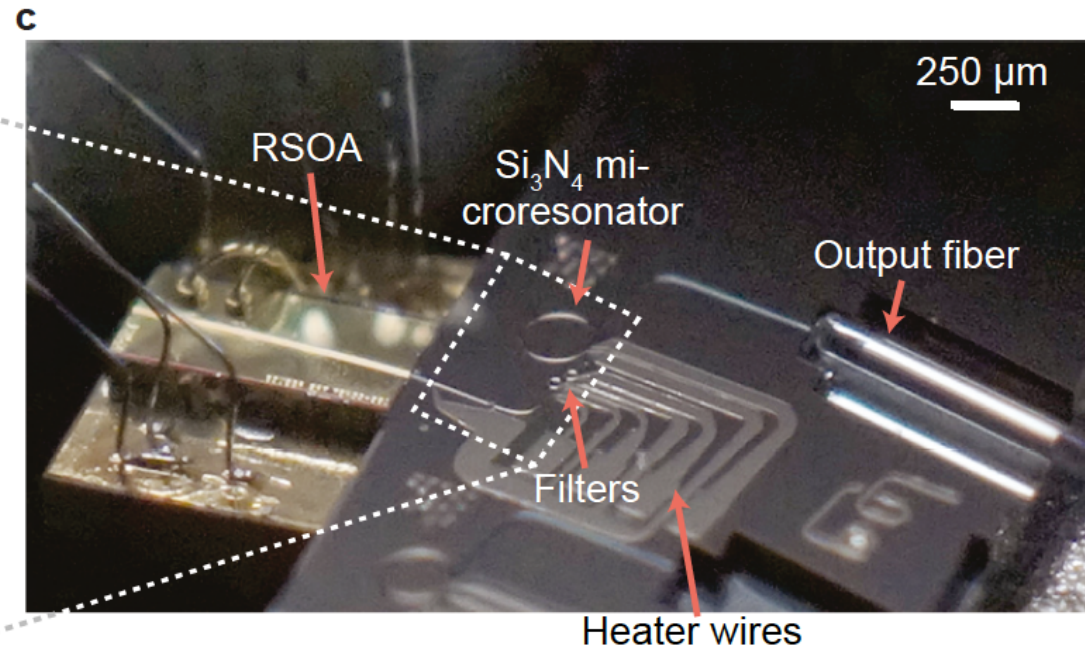
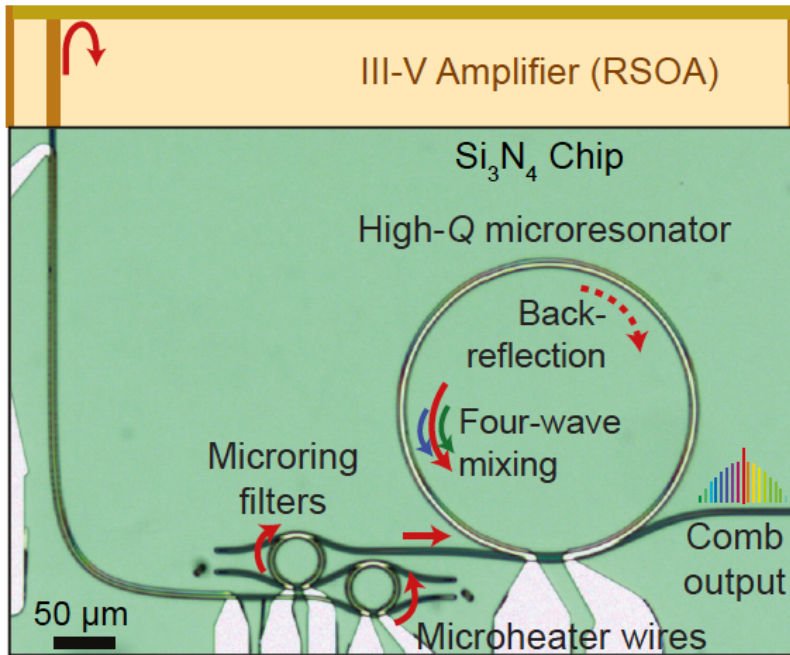
Sub-Harmonic Synchronization

Harmonic Synchronization



Vision for Integrated Kerr Comb Source



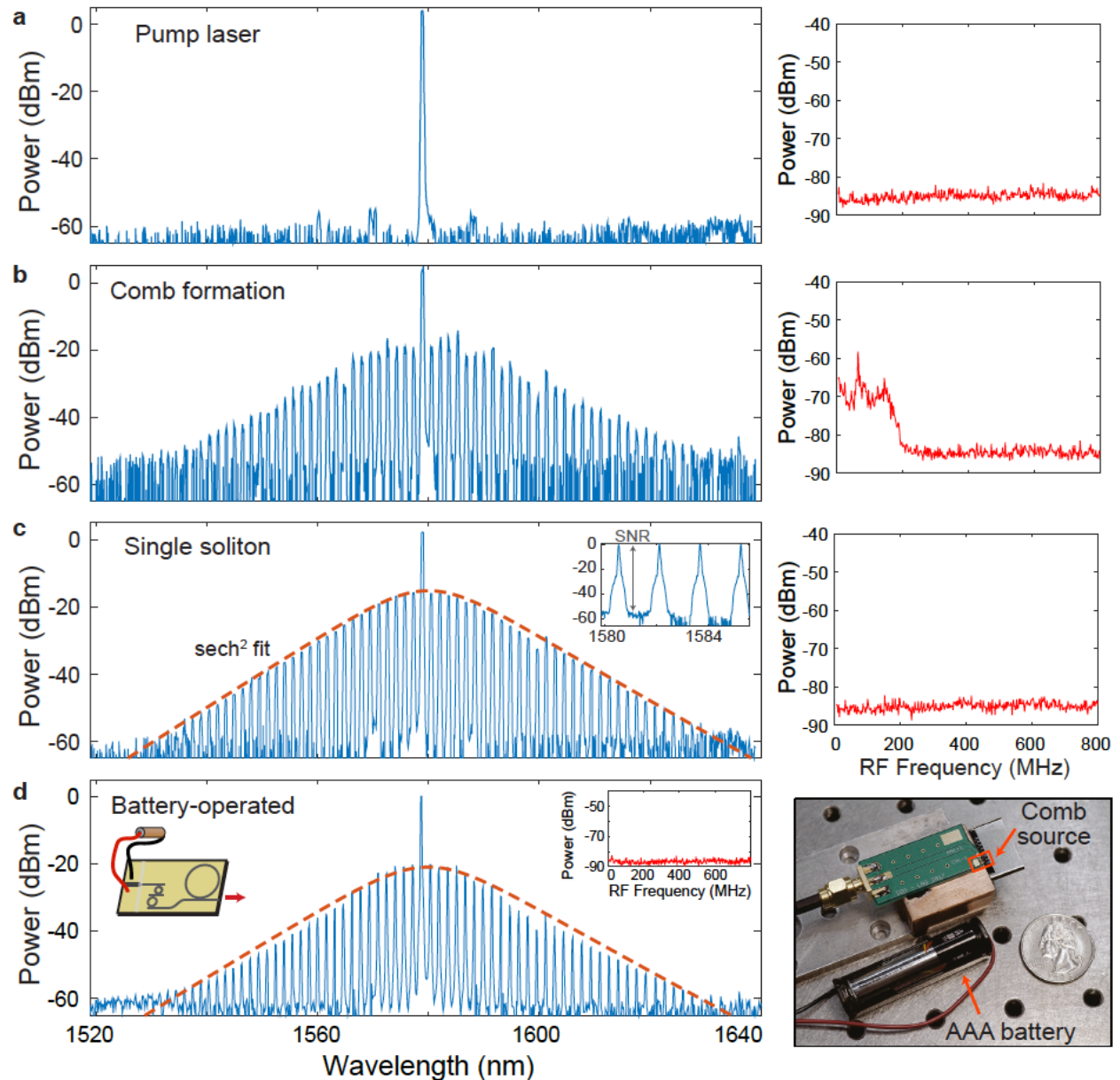


Stern, et al. Gaeta & Lipson, Nature (2018)

Recent work: Shen et al., Kippenberg, Vahala, & Bowers, Nature (2020)

Fully Integrated Comb Generator

98 mW
electrical power



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