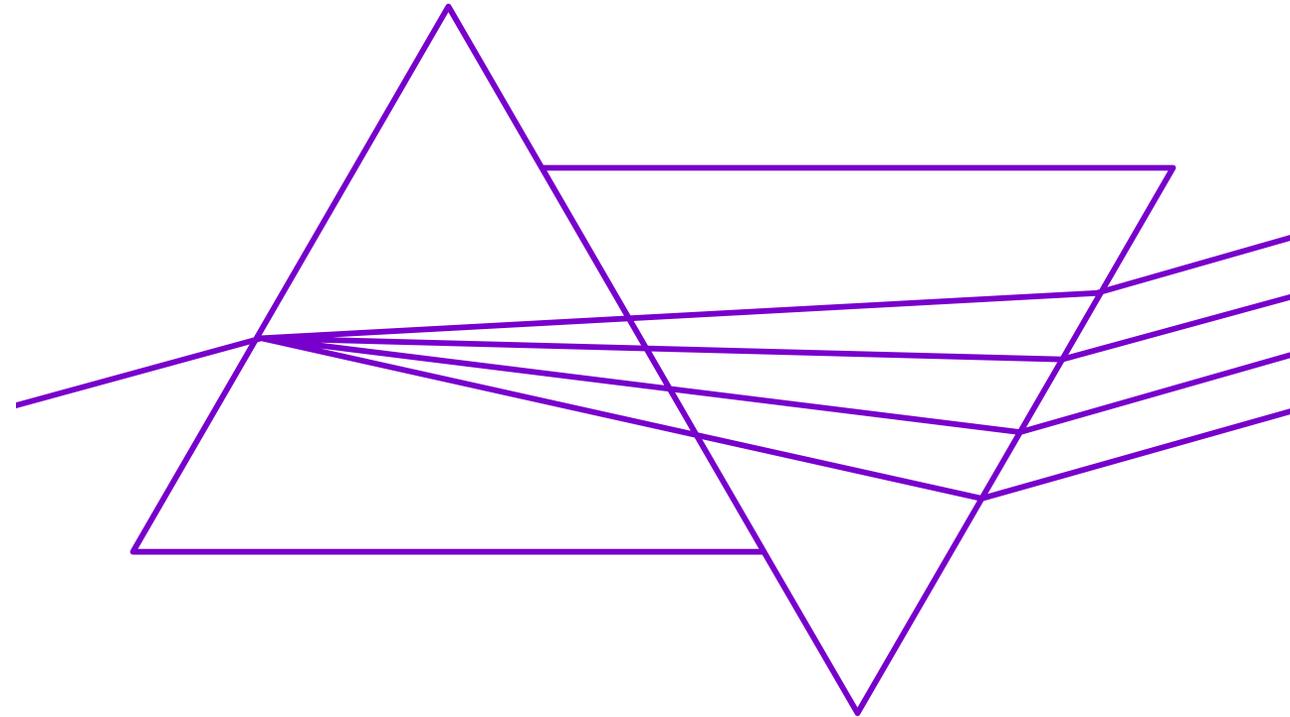


# Digital Holography with Single-Pixel Detection

Featuring Enrique Tajahuerce, Universitat Jaume I  
14 December 2021



# About Our Technical Group

Our technical group focuses on the design and implementation of holographic and diffractive-optic devices and systems for scientific, commercial, and other applications.

Our mission is to connect the 1000+ members of our community through technical events, webinars, networking events, and social media.

Our past activities have included:

- [Digital Holographic Microscopy Techniques for Applications in Cytometry and Histology](#)
- [Structured Light with Digital Holograms](#)
- [Metasurface Holograms](#)
- [Real-Time Hologram Rendering from Optically-Acquired Interferograms](#)

# Connect with our Technical Group

Join our online community to stay up to date on our group's activities. You also can share your ideas for technical group events or let us know if you're interested in presenting your research.

## Ways to connect with us:

- Our website at [www.optica.org/FH](http://www.optica.org/FH)
- On LinkedIn at [www.linkedin.com/groups/4826728](http://www.linkedin.com/groups/4826728)
- On Facebook at [www.facebook.com/groups/opticaholography](http://www.facebook.com/groups/opticaholography)
- Email us at [TGactivities@optica.org](mailto:TGactivities@optica.org)

# Today's Speaker



## Enrique Tajahuerce

*Universitat Jaume I*

Enrique Tajahuerce is an associate professor in the Department of Physics at Universitat Jaume I, Castelló, Spain. He has conducted his research at the Institute of New Imaging Technologies (INIT) there since 2010. He received his PhD in physics from Universidad de Valencia in 1998. He is co-author of more than 90 research papers and over 120 communications in international conference meetings. He has collaborated in the scientific committee and organization of international conferences sponsored by Optica, IEEE, and SPIE. In 2008, he received the IEEE Donald G. Fink Prize Paper Award. He is Fellow of Optica, Senior Member of SPIE and serves as topical editor for Optics Letters. Dr. Tajahuerce coordinates the Photonics Research Group (GROC·UJI) at University Jaume I. His research interests lie in the areas of diffractive optics, adaptive optics, optical security and encryption, digital holography, and computational imaging.

# Digital holography with single-pixel detection

Enrique Tajahuerce

*GROC-UJI, Institute of New Imaging Technologies (INIT), Universitat Jaume I, Castelló, Spain*



## Research group

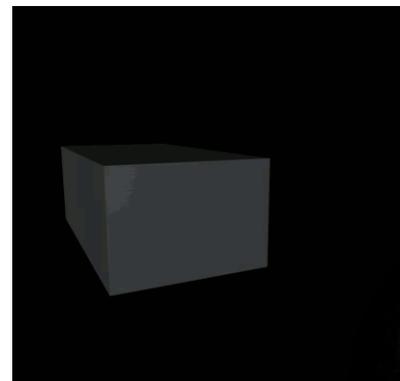
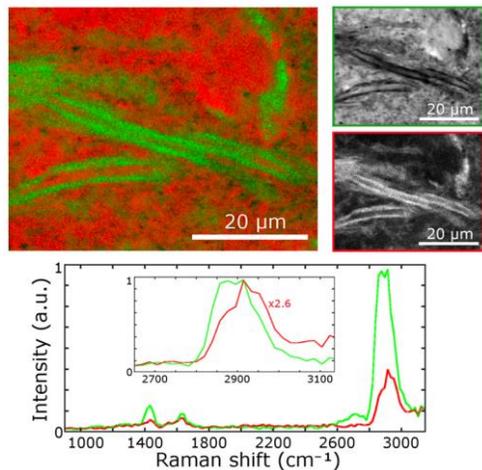
Jesús Lancis , Pedro Andrés, Vicent Climent, Enrique Tajahuerce, Gladys Mínguez-Vega, Lluís Martínez-León, Omel Mendoza, Pere Clemente, Dani Torrent, Vicente Durán, Armin Lenz, Marc Martí, Erick Ipus, Luis Ordóñez, Sergio Fernández, Francis Rey

<https://www.init.uji.es>

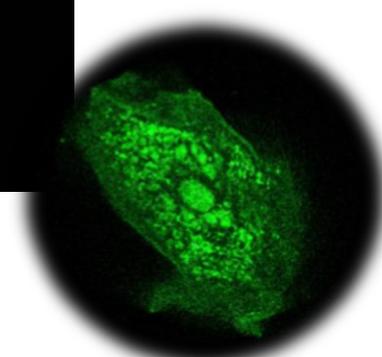
 @photonicsuji



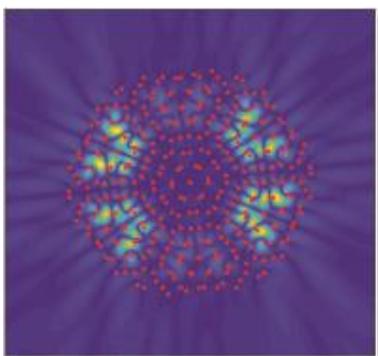
## Computational imaging and holography with structured illumination



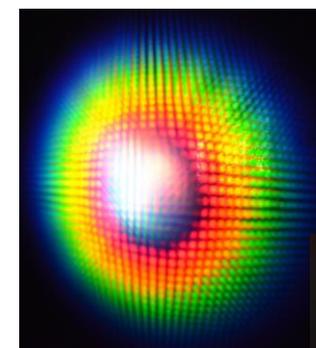
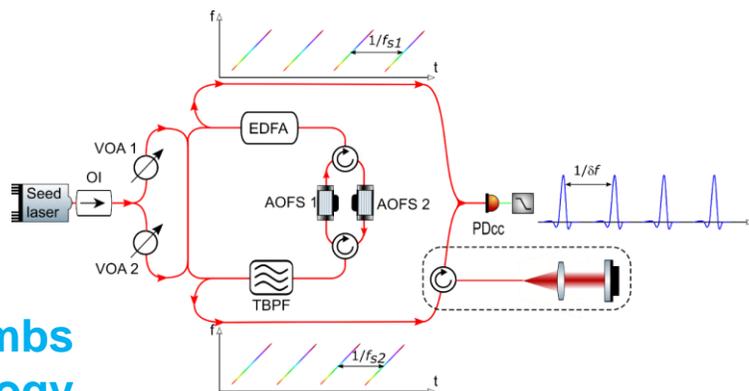
## Nanomaterial synthesized with ultrashort lasers and its applications



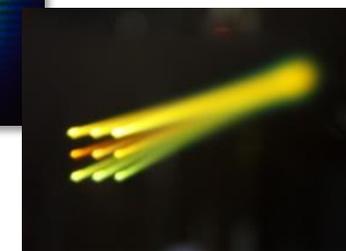
## Control of the vibrational energy localized in thin elastic plates



## Optical frequency combs for optical metrology applications



## Complex beam shaping with dynamic DOEs



Description of **computational imaging techniques based on single-pixel detection** with microstructured illumination and compressive sensing.

Application on **complex (amplitude and phase) imaging** with interferometric and non interferometric approaches.

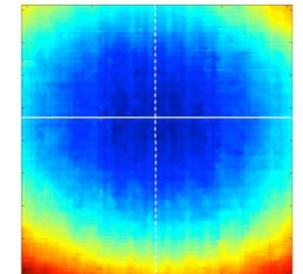
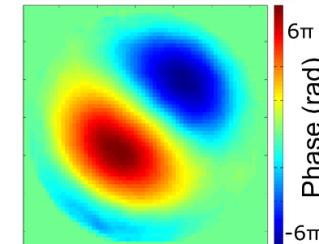
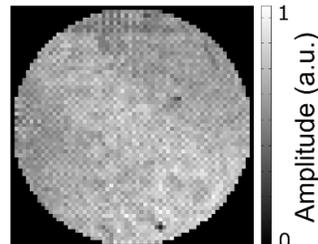
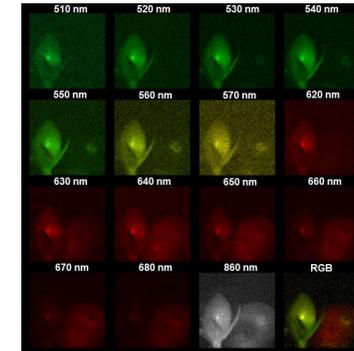
## 1. The single-pixel camera

## 2. Multispectral imaging

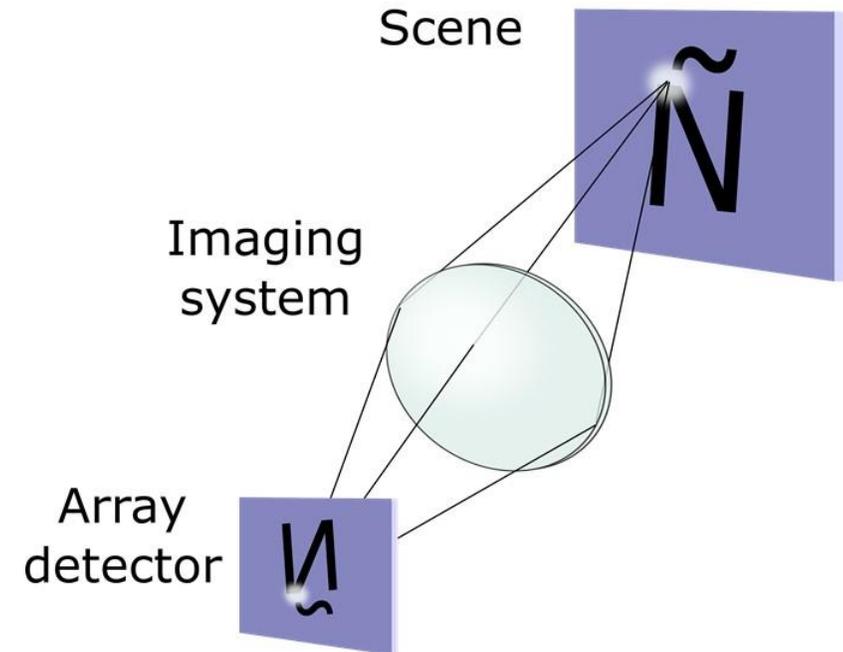
## 3. Complex amplitude imaging

Non-interferometric setups

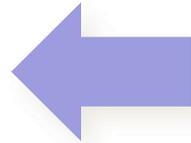
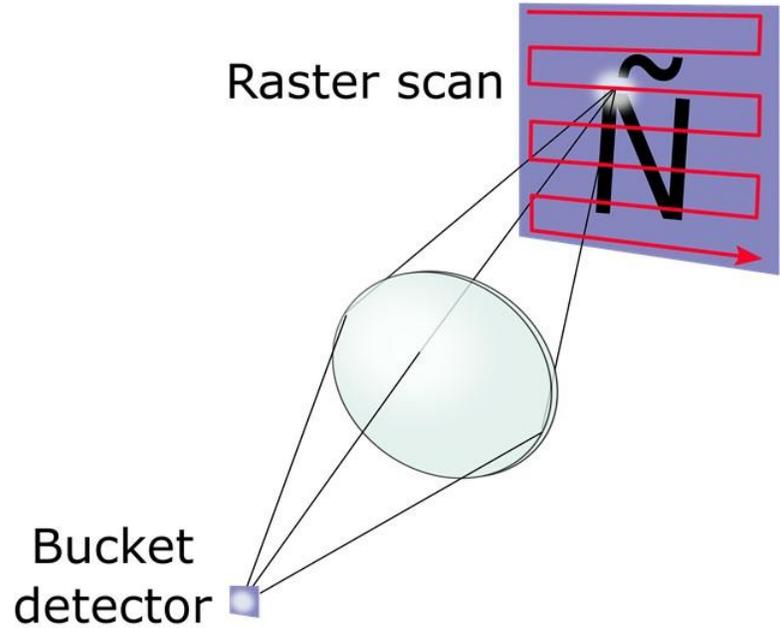
Interferometric setups



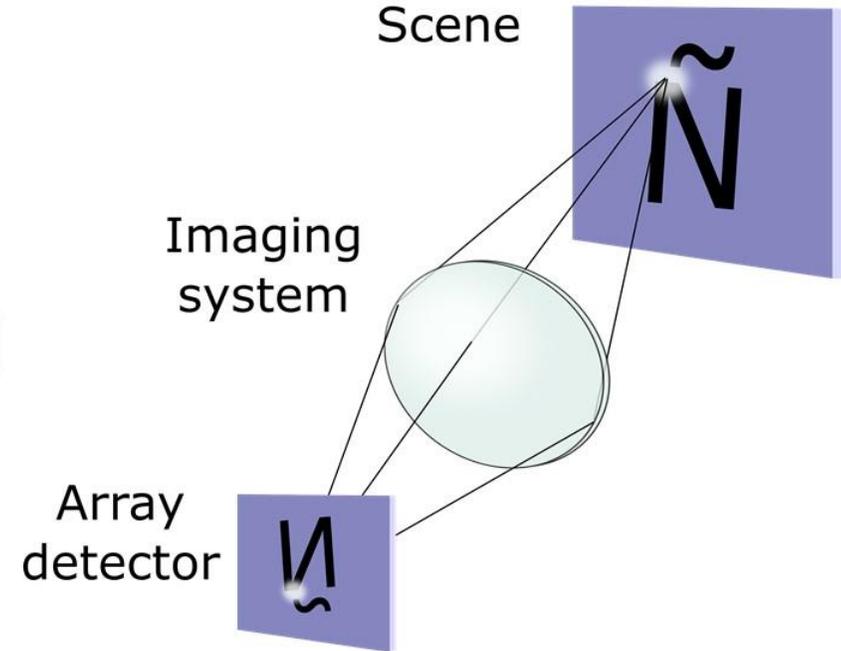
## Conventional imaging



## Raster scanning approach

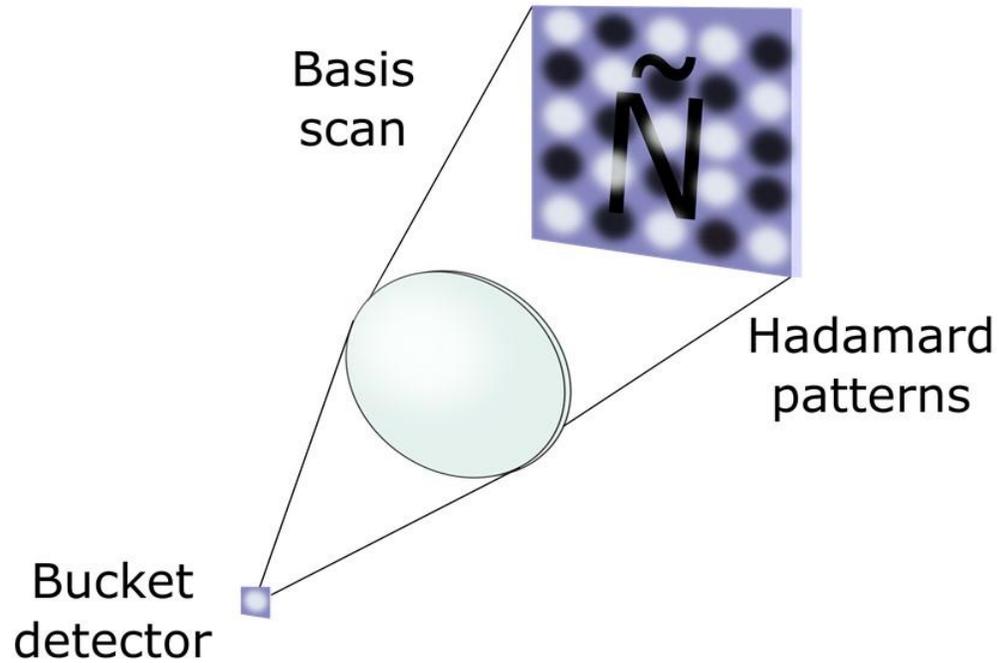


## Conventional imaging



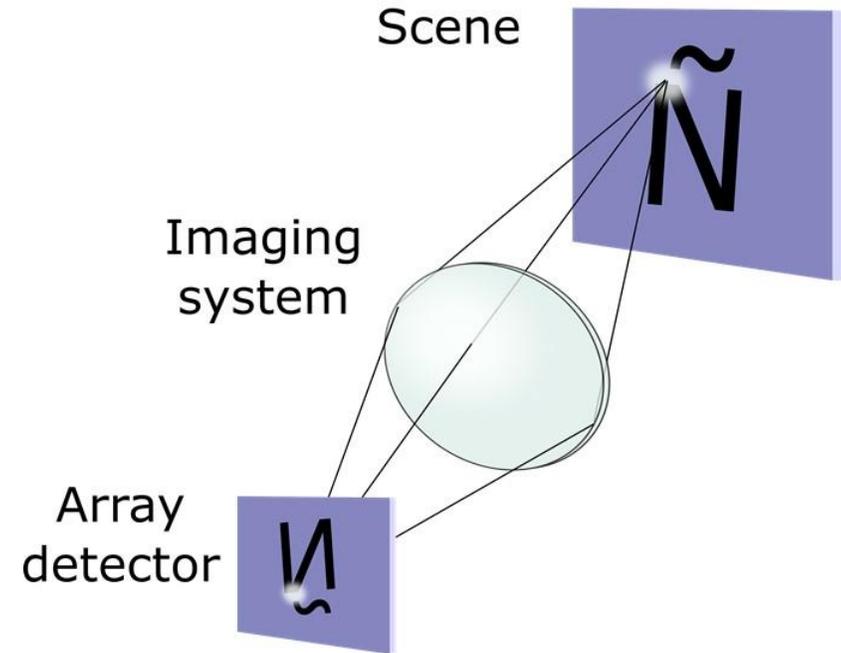
# The single pixel camera

## Single-pixel imaging

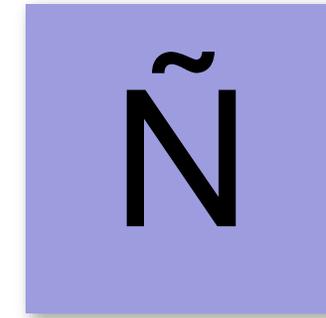
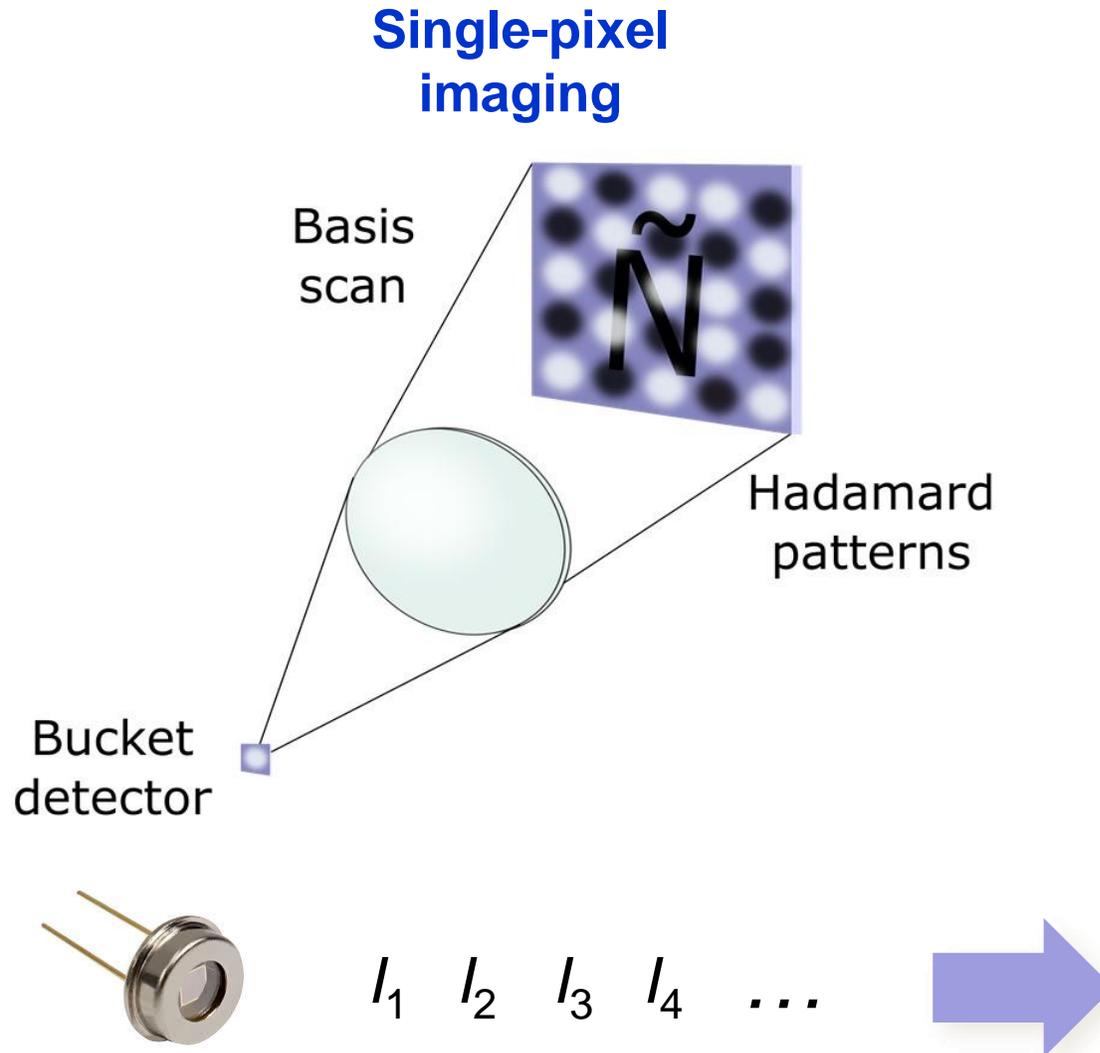


$I_1$   $I_2$   $I_3$   $I_4$  ...

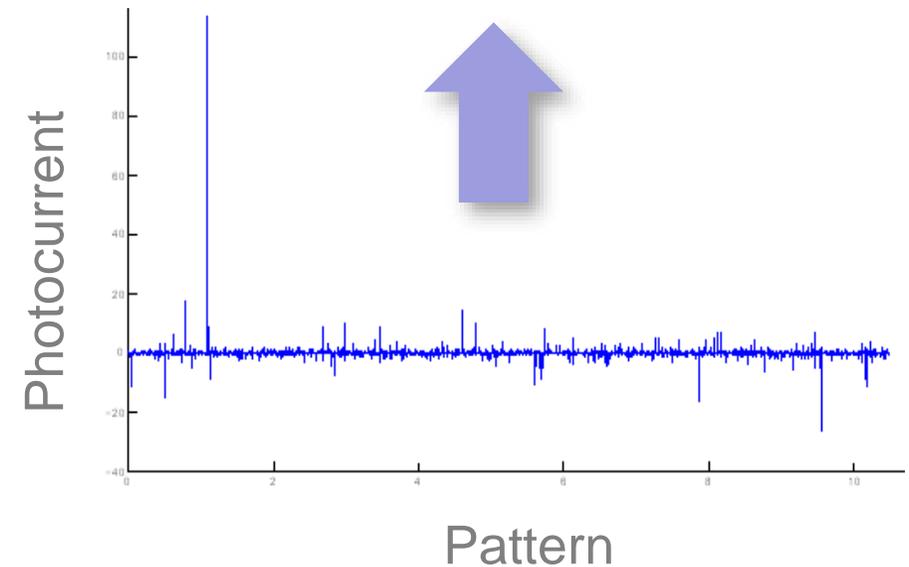
## Conventional imaging



# The single pixel camera



$$O(x, y) = \sum_{p=1}^M I_p \cdot H_p(x, y)$$



## Sensing patterns

### Random patterns

Binary or gray-level random patterns



Similar to  
**ghost imaging**

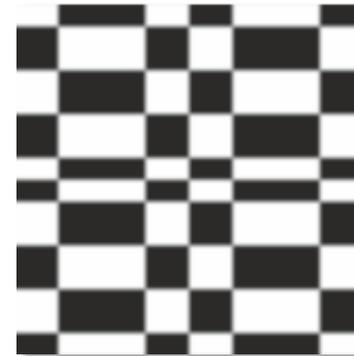
### Deterministic patterns

Complete basis of functions such as:

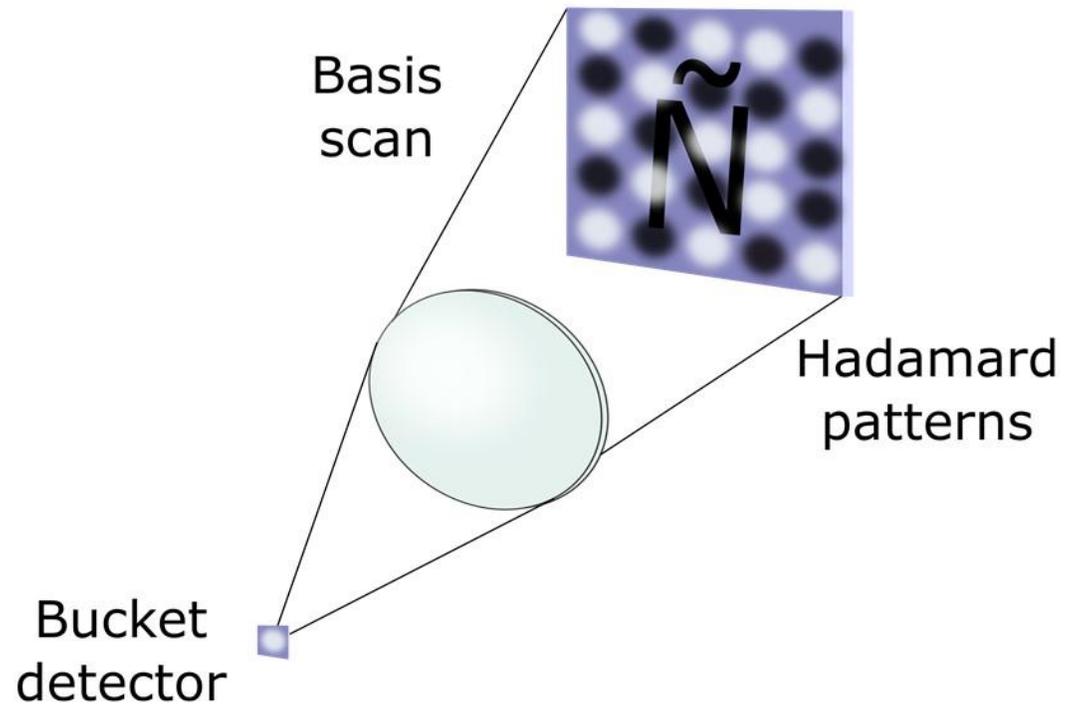
Discrete Fourier

Discrete Cosine

Walsh-Hadamard

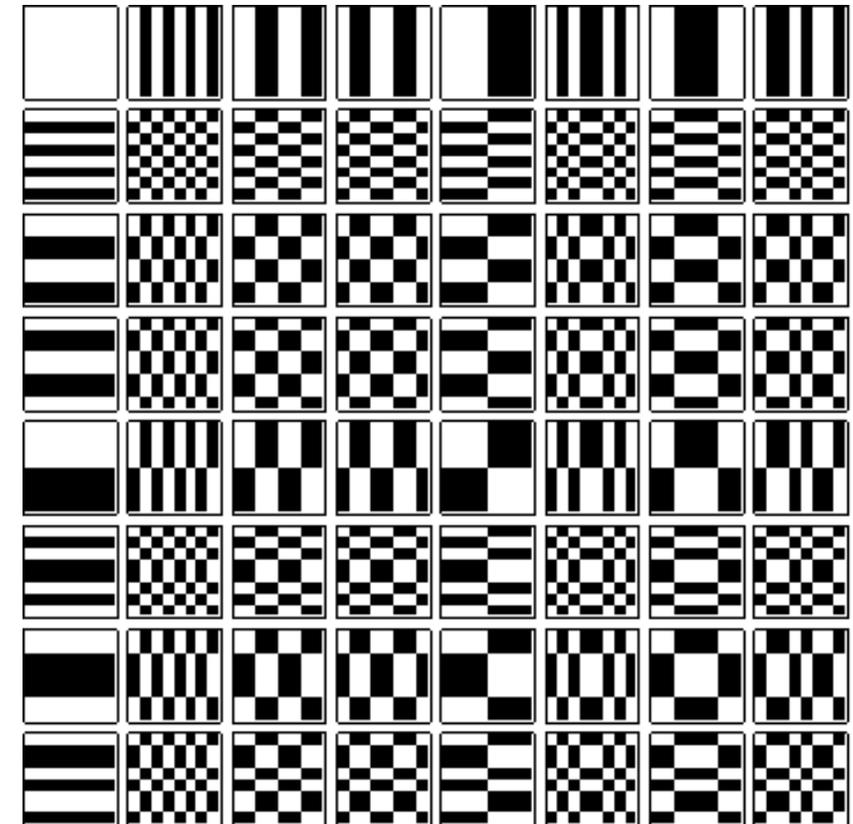


## Sensing patterns



Matrix basis

$\{+1, -1\}$



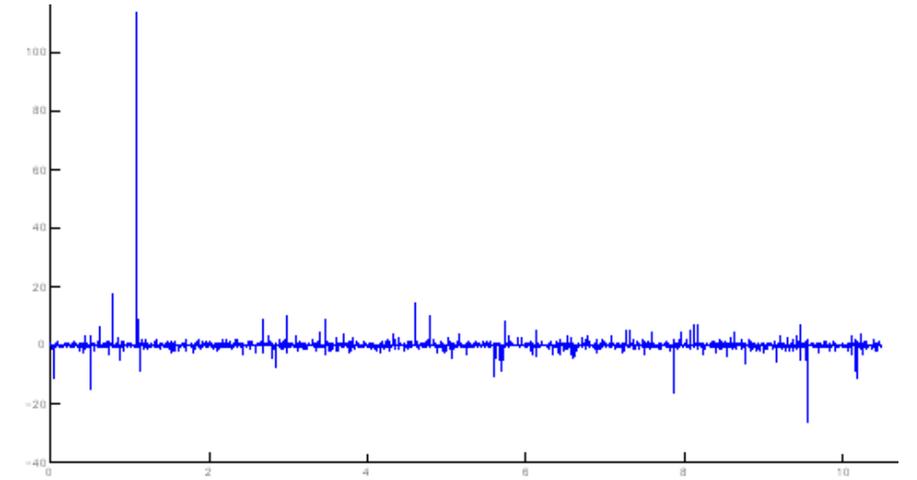
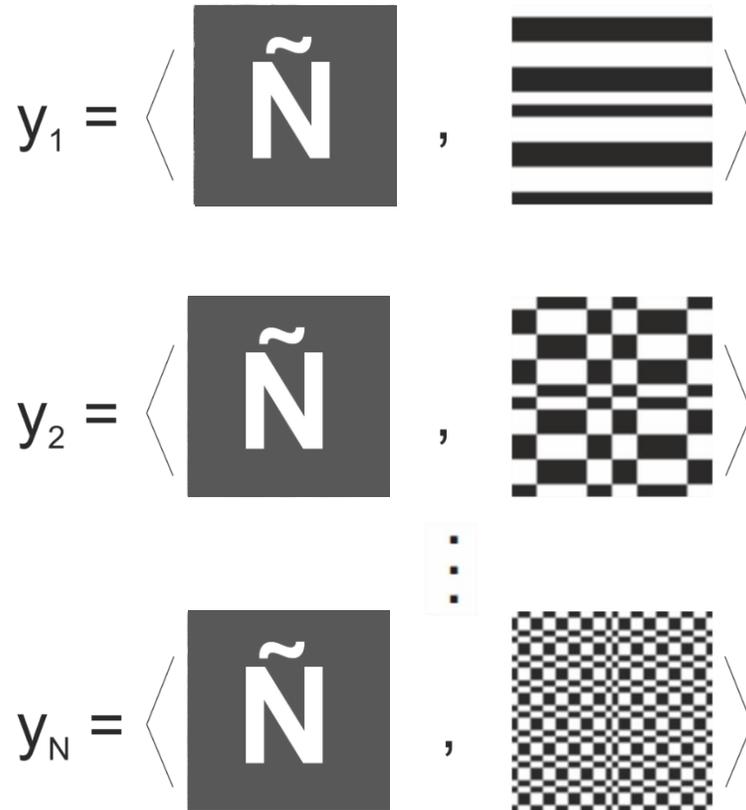
# The single pixel camera

Sample  
 $O(x, y)$

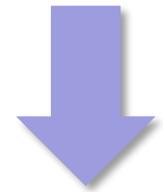


N pixels

Projections with  
 $H_p(x, y)$

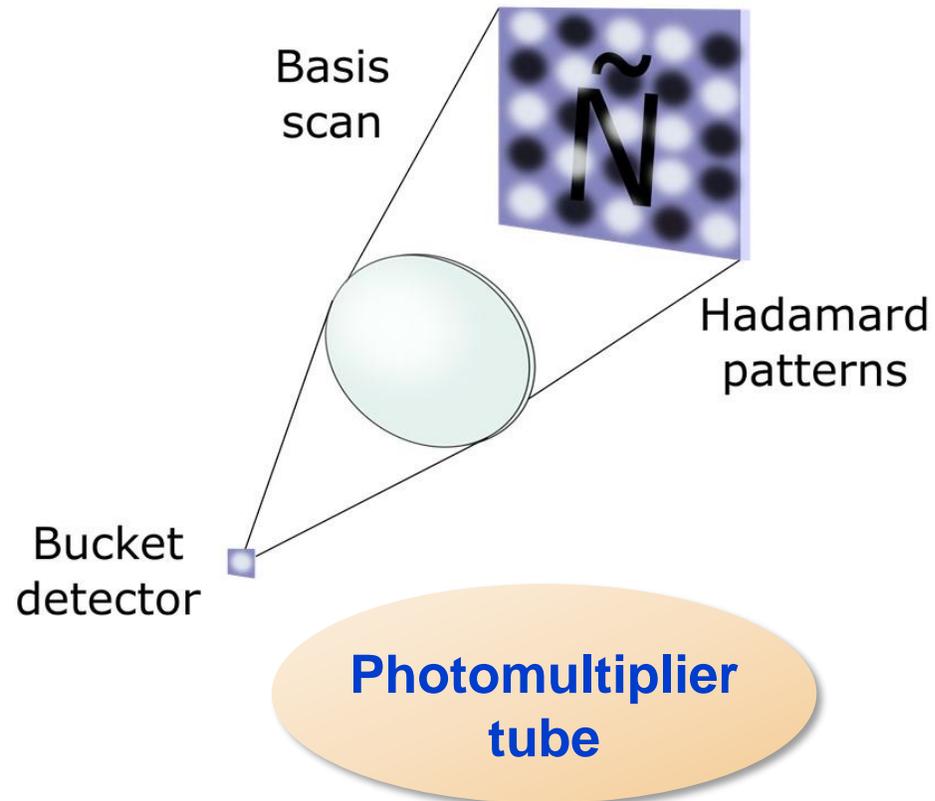


Inverse Hadamard  
transform



## Advantages

Single-pixel detection can be more **efficient** and less expensive when light is scarce



## Advantages

Pixels are not cheap **when light is out of visible range**

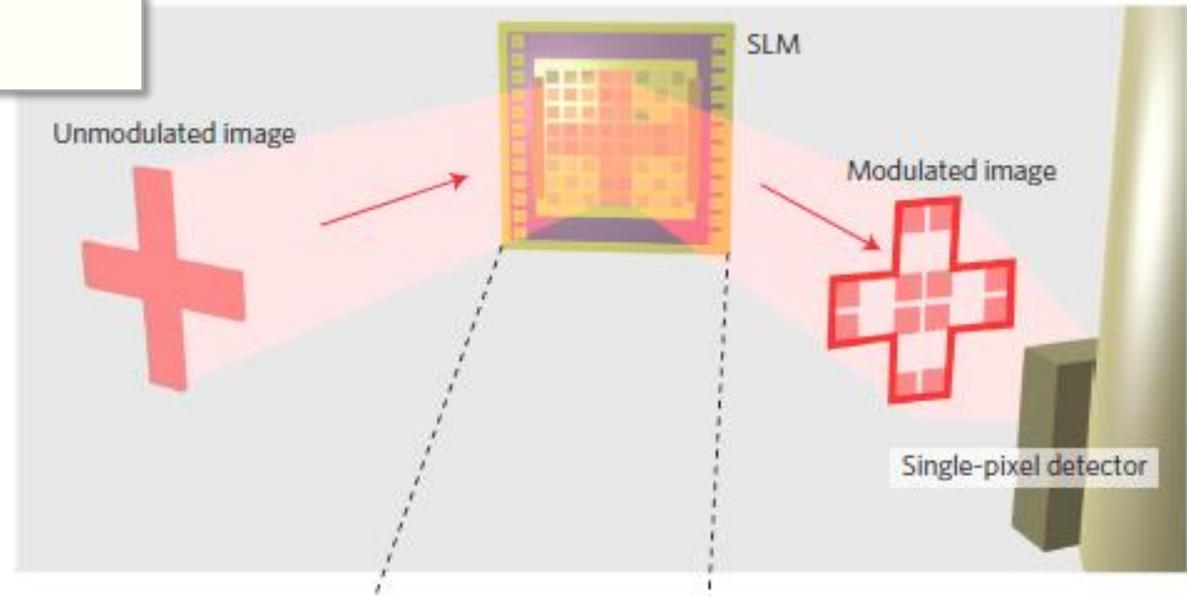
nature  
photonics

LETTERS

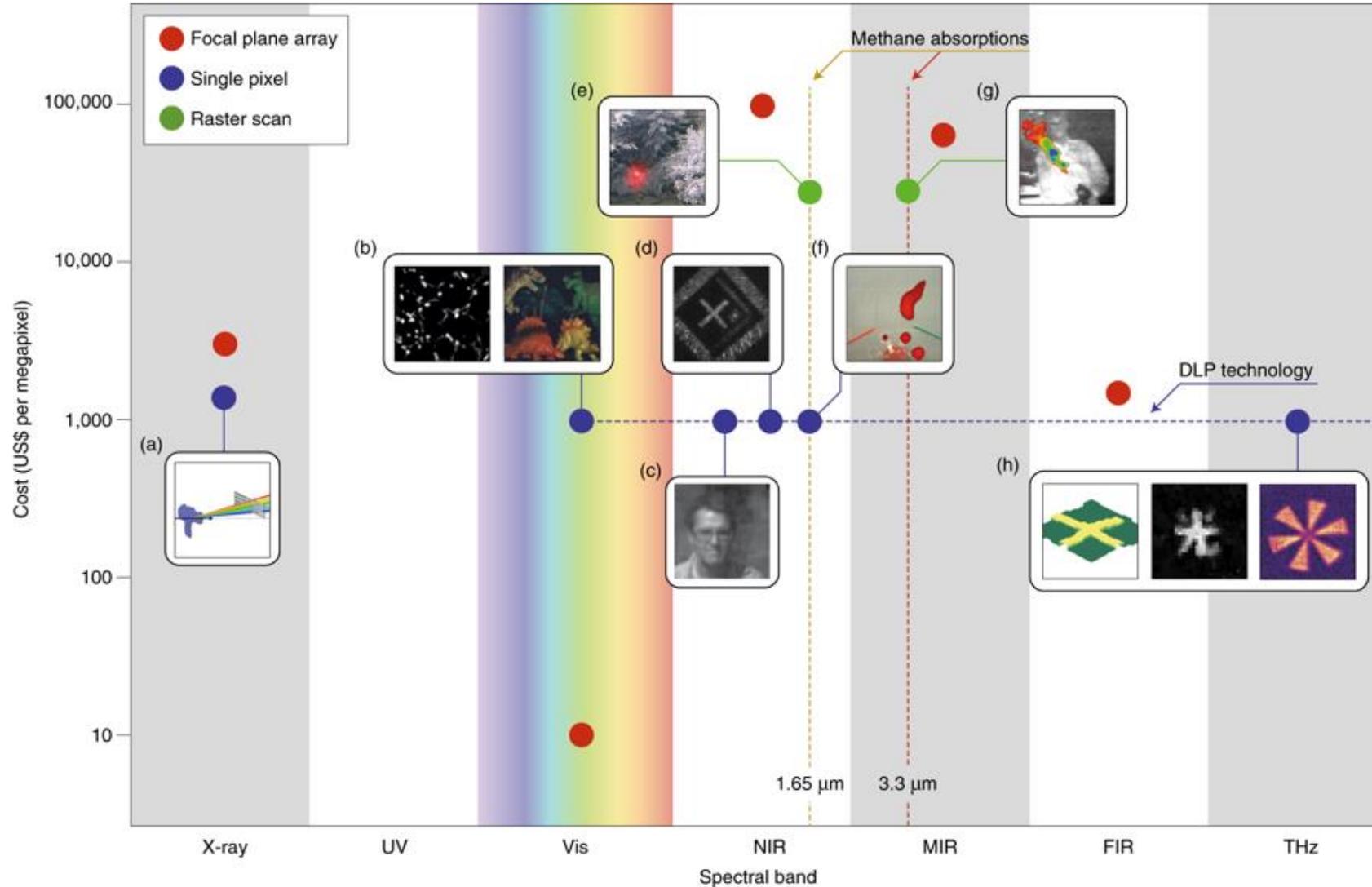
PUBLISHED ONLINE: 29 JUNE 2014 | DOI: 10.1038/NPHOTON.2014.139

### Terahertz compressive imaging with metamaterial spatial light modulators

Claire M. Watts<sup>1</sup>, David Shrekenhamer<sup>1</sup>, John Montoya<sup>2</sup>, Guy Lipworth<sup>3</sup>, John Hunt<sup>3</sup>, Timothy Sleasman<sup>1</sup>, Sanjay Krishna<sup>2</sup>, David R. Smith<sup>3</sup> and Willie J. Padilla<sup>1\*</sup>



# The single pixel camera



nature  
photonics

Review Article | Published: 03 December 2018

## Principles and prospects for single-pixel imaging

Matthew P. Edgar, Graham M. Gibson & Miles J. Padgett

Nature Photonics 13, 13–20 (2019) | Download Citation

## Advantages

Single-pixel detectors can have **timing resolutions approaching picoseconds**

April 1987 / Vol. 12, No. 4 / OPTICS LETTERS 239

### Coherent laser radar at 1.06 $\mu\text{m}$ using Nd:YAG lasers

Thomas J. Kane,\* W. J. Kozlovsky, and Robert L. Byer

Edward L. Ginzton Laboratory, Stanford University, Stanford, California 94305

Charles E. Byvik

NASA Langley Research Center, Hampton, Virginia 23665

Received December 16, 1986;

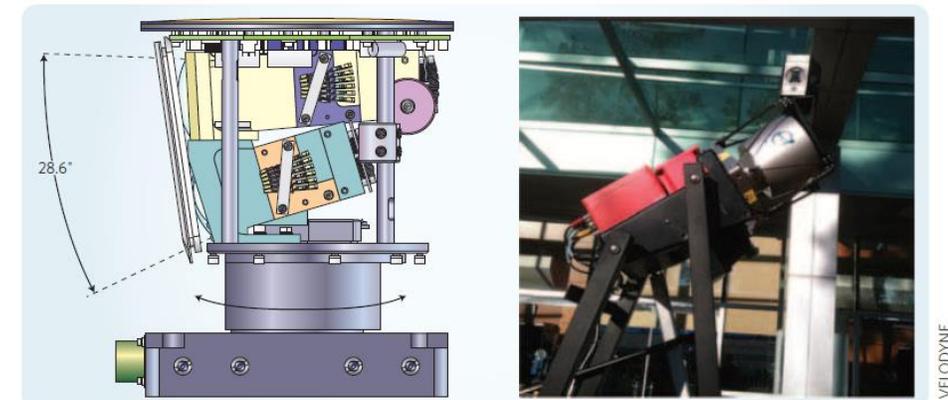
A coherent laser radar system operating at the 1.06- $\mu\text{m}$  Nd:YAG laser wavelength has been built and operated. A laser-diode-pumped monolithic ring laser served as the master oscillator. A single flash-lamp-pumped zigzag slab amplified the oscillator output to a power of 2.3 kW. Single-mode optical fiber was used to collect and mix the return signal with the local-oscillator output. Signals from clouds at a range of 2.7 km and from atmospheric aerosols at a range of 600 m were detected.

LIDAR

## Mapping the world in 3D

Brent Schwarz

NATURE PHOTONICS | VOL 4 | JULY 2010 | [www.nature.com/naturephotonics](http://www.nature.com/naturephotonics)

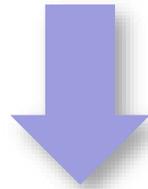


Internal (left) and external (right) views of Velodyne's high-definition LIDAR. The sensor features a total of 64 semiconductor lasers and matched detectors, arranged into two sets (upper and lower) of linear arrays. The sensor head is spun at high speed during data collection to give the LIDAR system a complete 360° field-of-view.

## Drawbacks

The light scanning process takes time

Image reconstruction process may require time

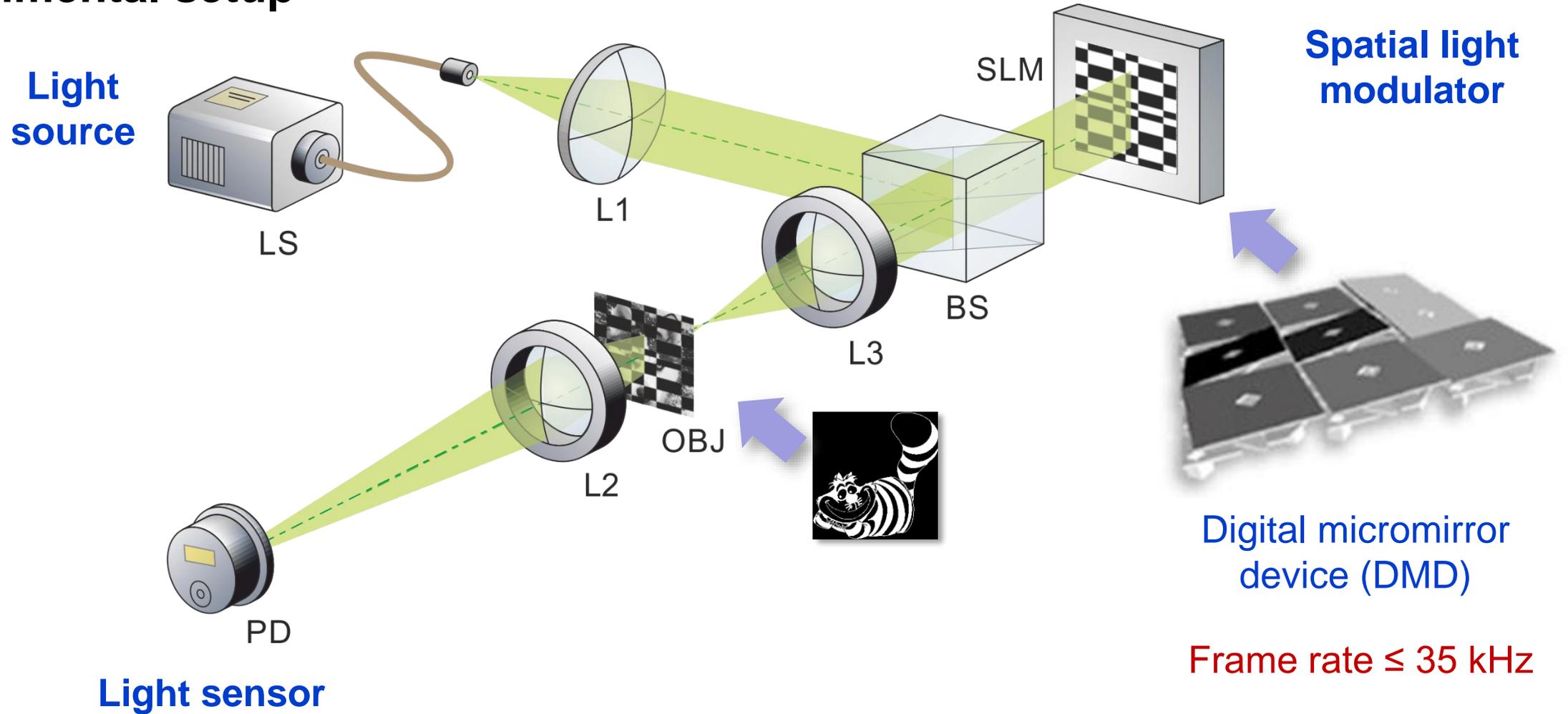


## Solution

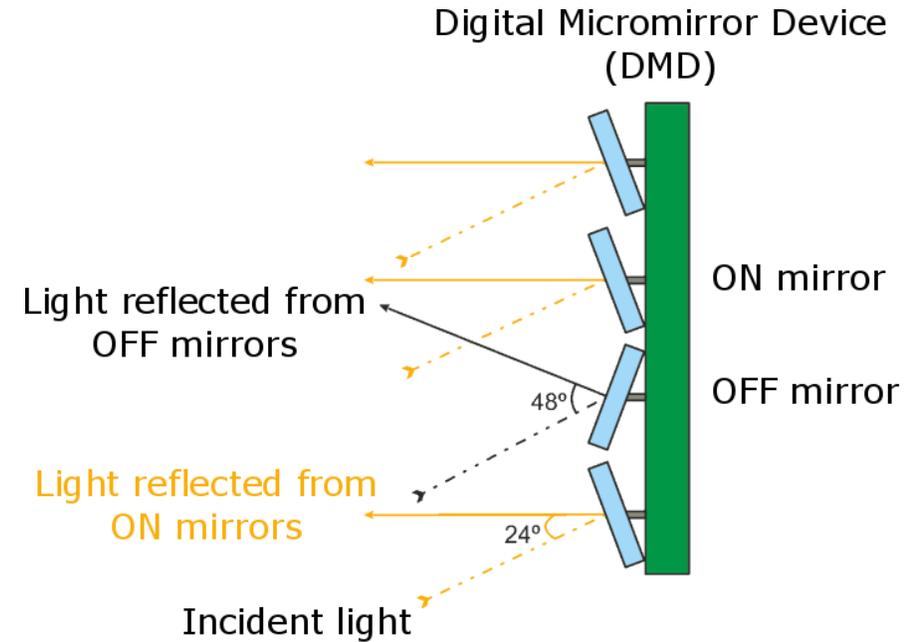
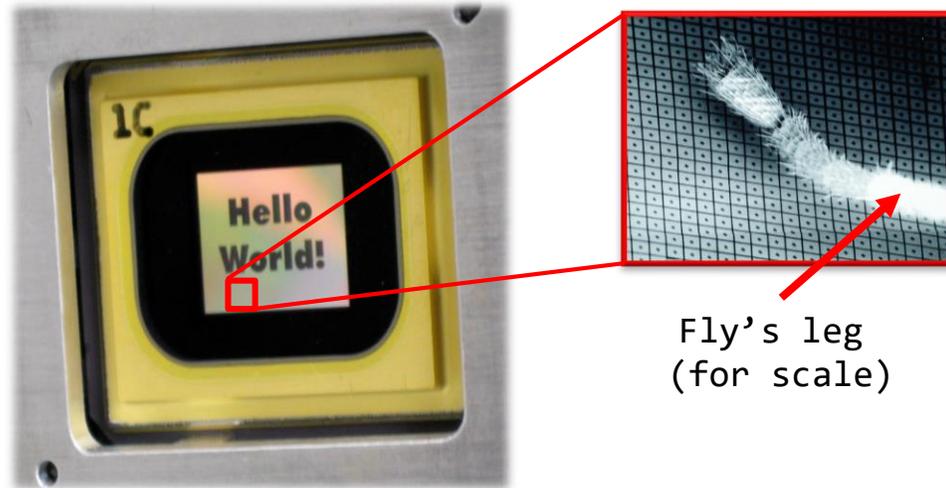
Use fast spatial light modulators for light structured illumination

Use efficient algorithms for image reconstruction

## Experimental setup

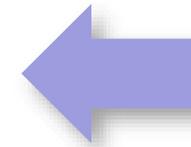
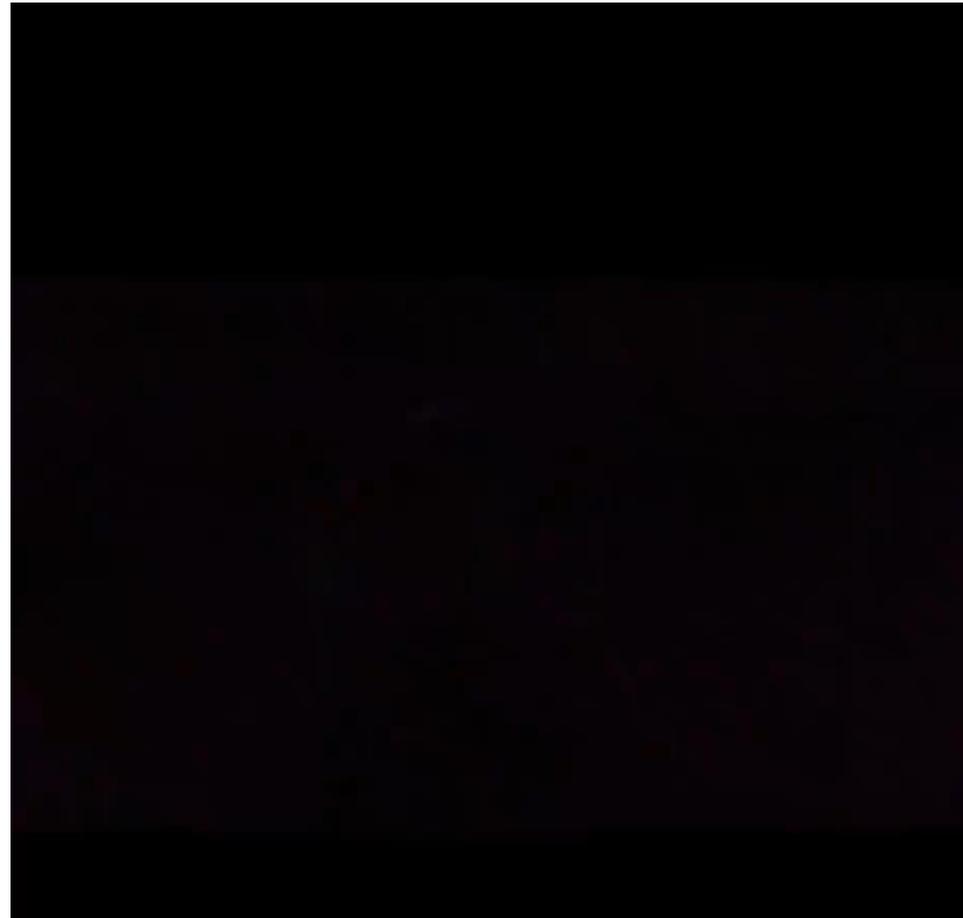
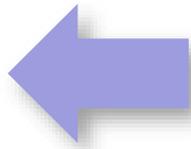


## Digital micromirror device (DMD)



- Array of micrometric ( $\sim 10 \mu\text{m}$ ) mirrors with two possible orientations
- Fast refresh rate ( $\sim 35 \text{ kHz}$ )
- Binary intensity modulation

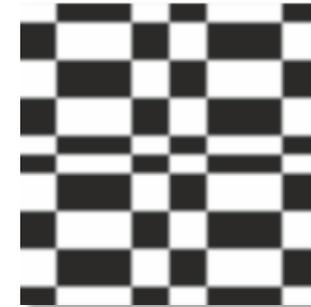
# The single pixel camera



## Algorithms

- **Basis scan**

Number of measurements equal to the number of pixels



- **Compressive sensing or matrix completion**

Number of measurements reduced to 10 – 20 %



- **Adaptive algorithms**

Number of measurements reduced by adapting the patterns to the image



# Single-pixel camera with CS

Sample  
 $O(x, y)$



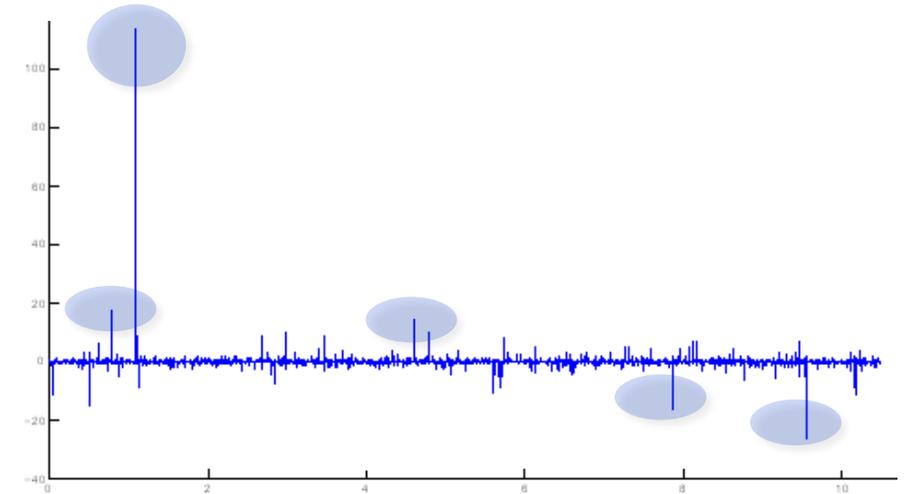
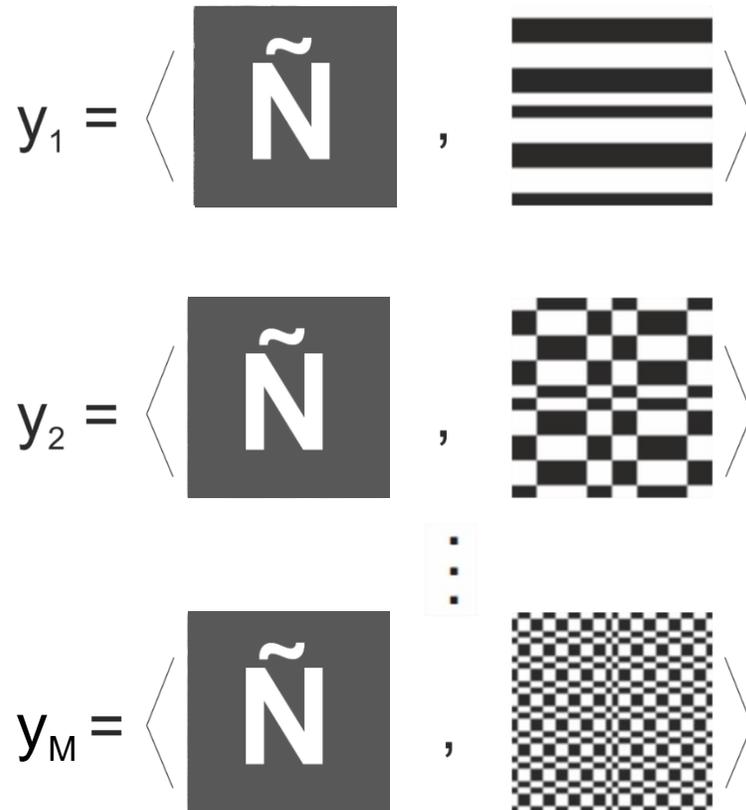
N pixels

M measurements

$M < N$

Projections with

$H_p(x, y)$



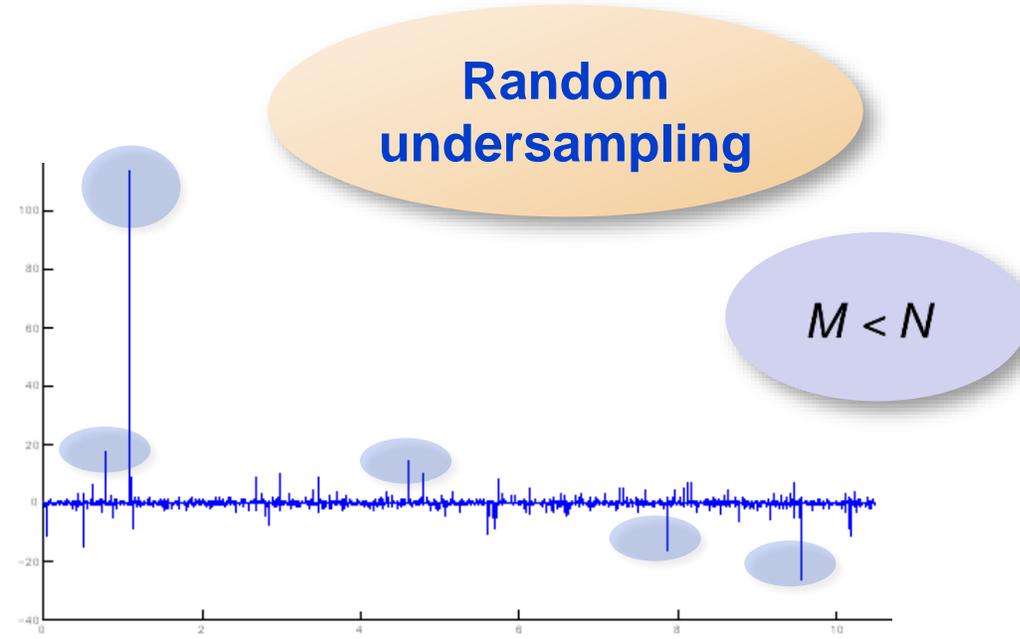
**S-sparse  
signal**

# Single-pixel camera with CS

Sample  
 $O(x, y)$

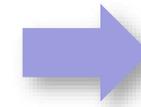


N pixels

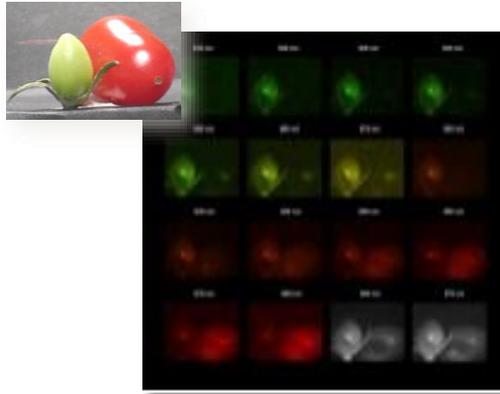


Compressive algorithms

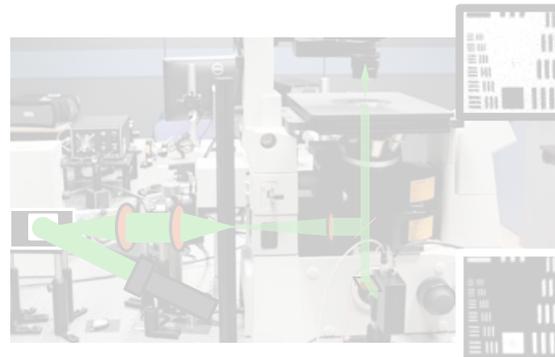
L1-magic, GSPR, or TwIST



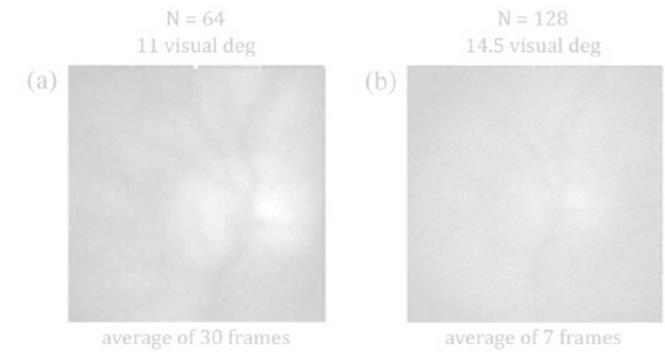
## Multidimensional cameras



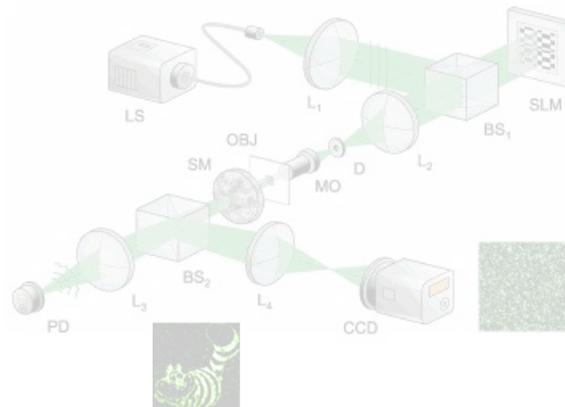
## Microscopy



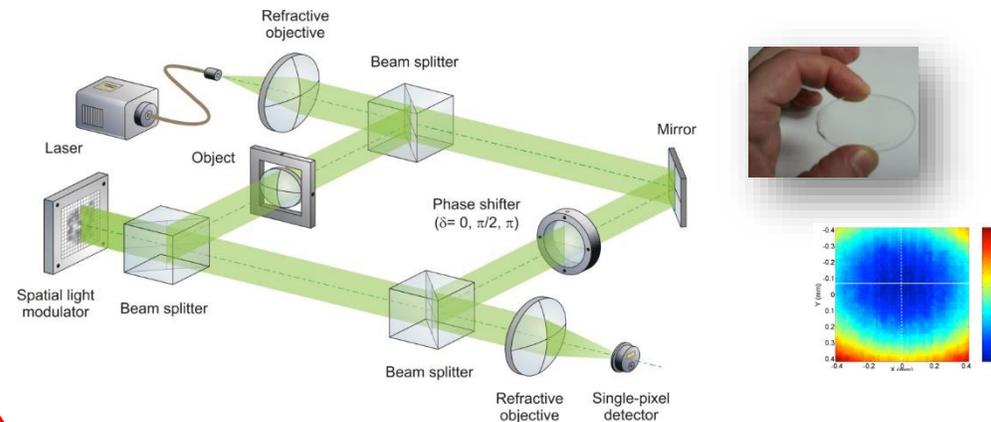
## Ophthalmoscope



## Imaging through scattering



## Holographic cameras



Description of **computational imaging techniques based on single-pixel detection** with microstructured illumination and compressive sensing.

Application on multispectral imaging and **complex (amplitude and phase) imaging** with interferometric and non interferometric approaches.

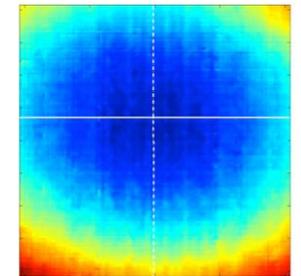
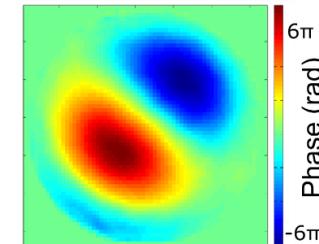
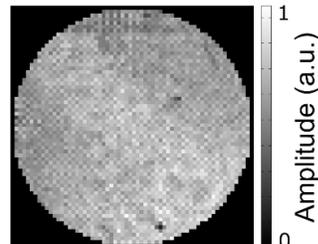
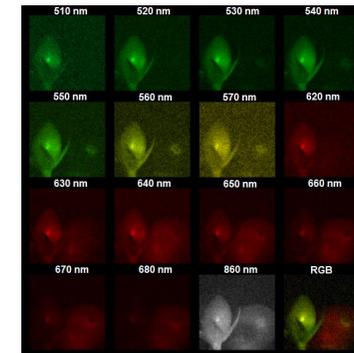
## 1. The single-pixel camera

## 2. Multispectral imaging

## 3. Complex amplitude imaging

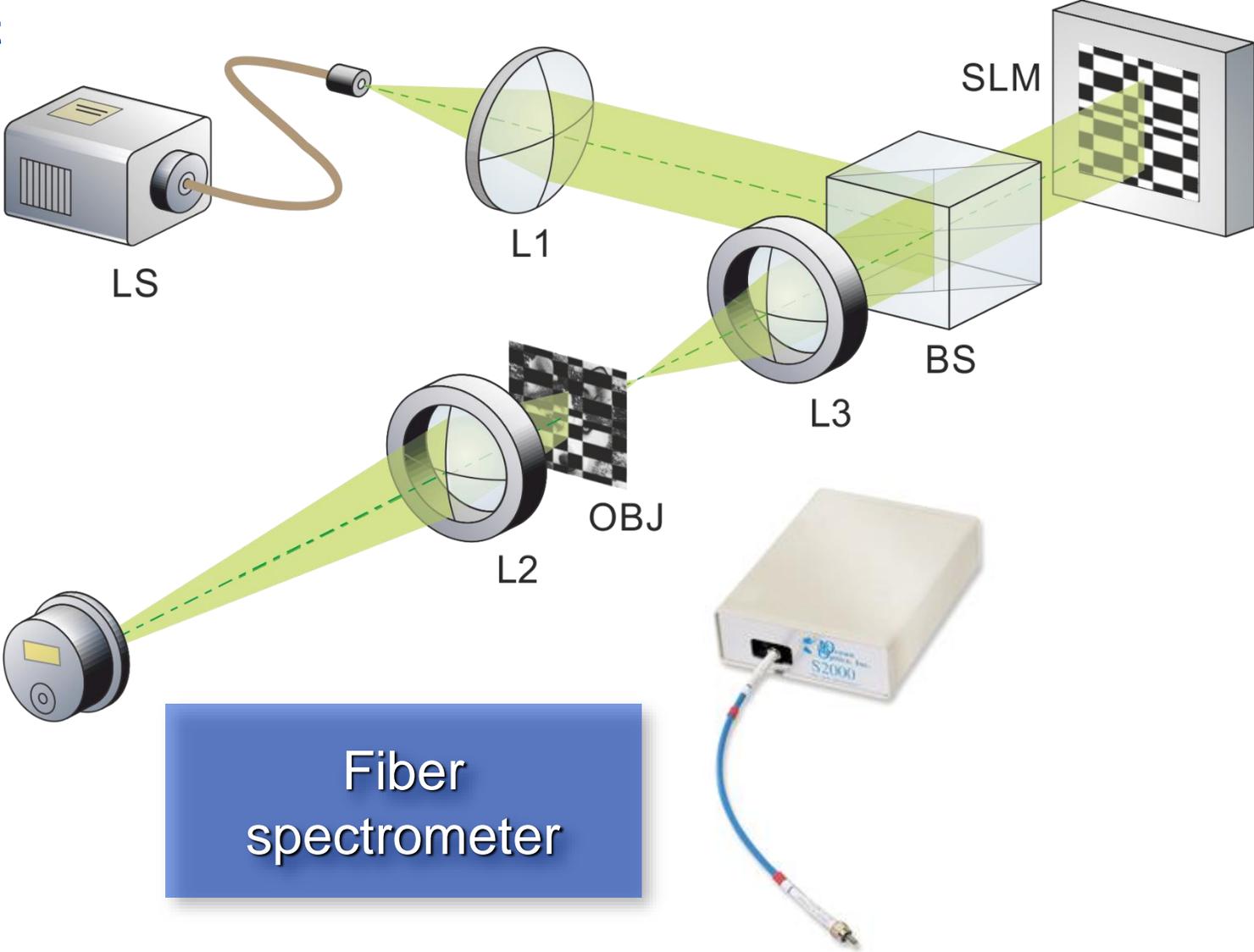
**Non-interferometric setups**

**Interferometric setups**



# Multidimensional imaging

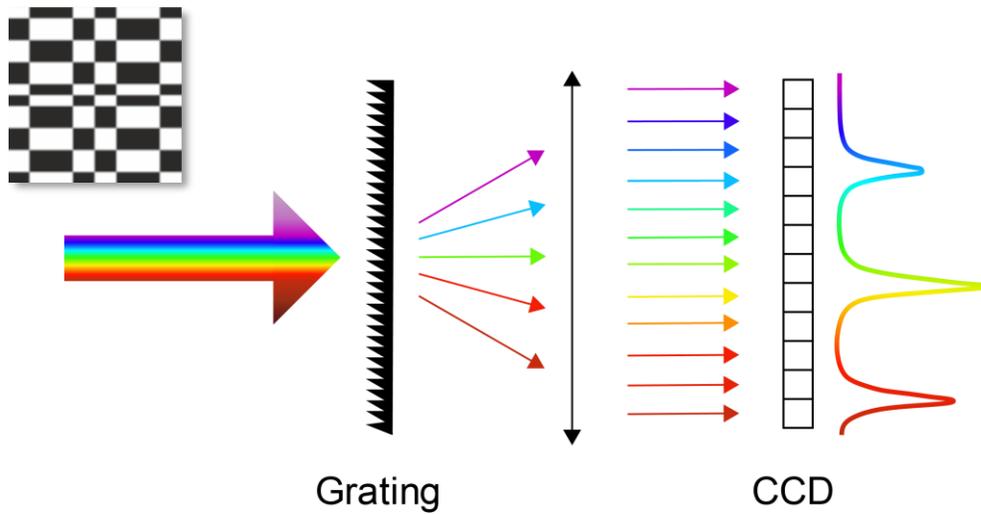
White-light source



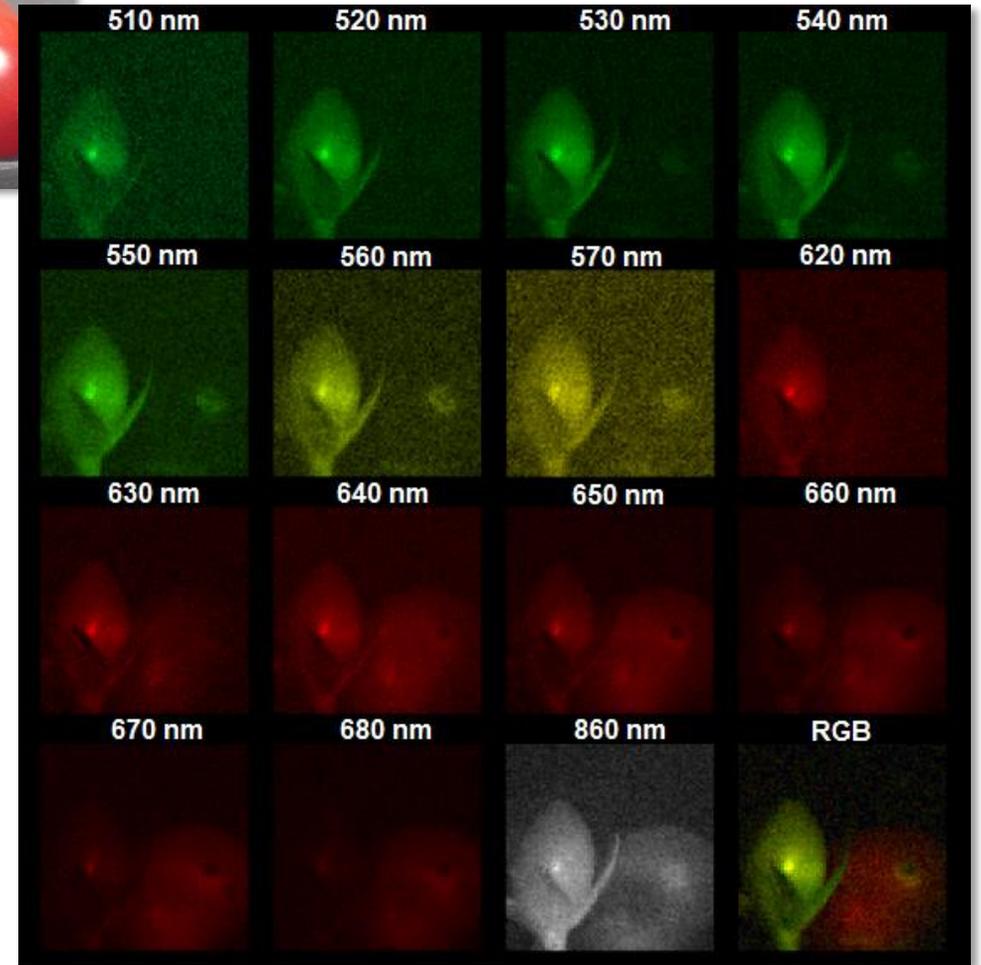
Spatial light modulator

Fiber spectrometer

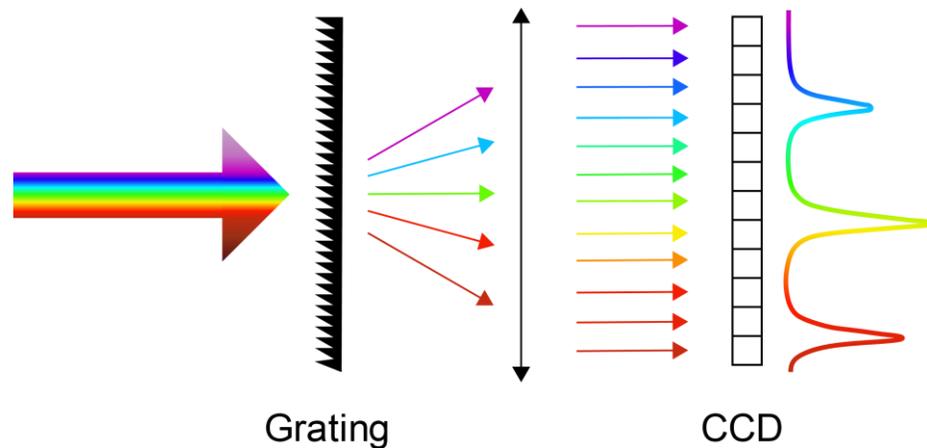
## Conventional spectrometer



- Single-shot
- CCD/CMOS based detector

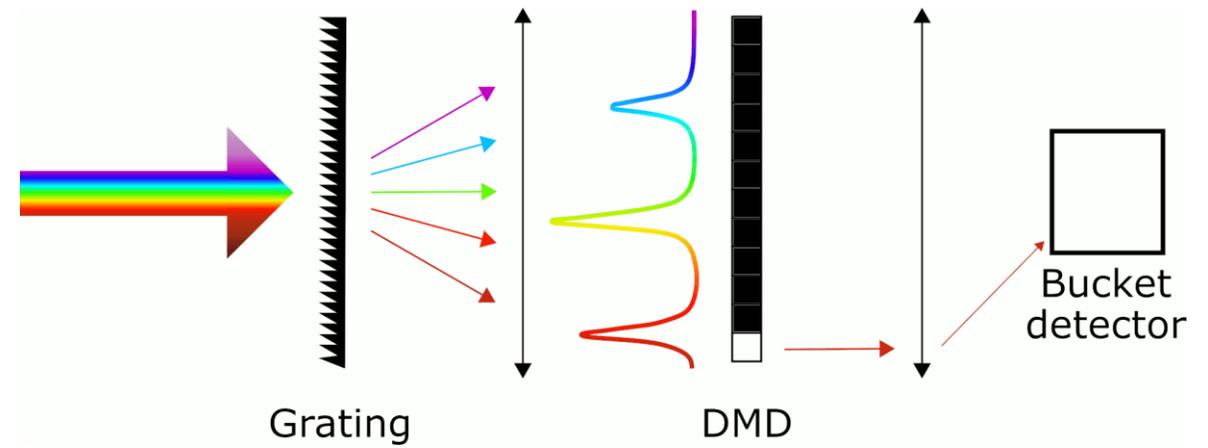


## Conventional spectrometer



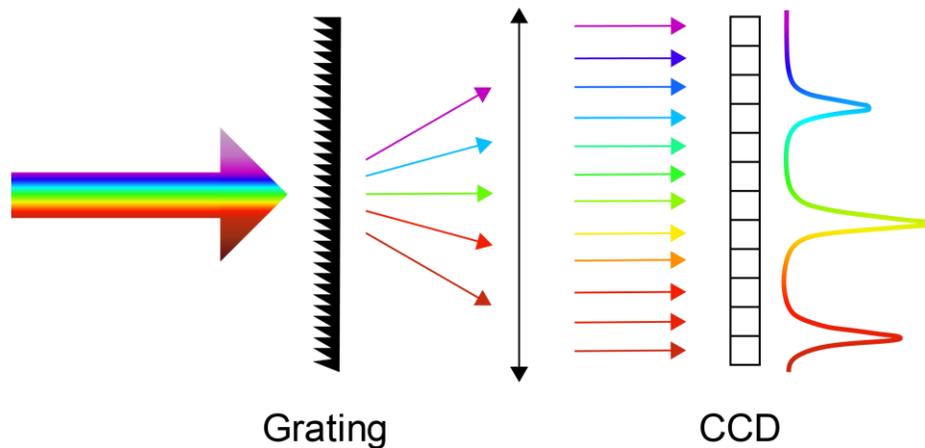
- Single-shot
- CCD/CMOS based detector

## Single-pixel spectrometer



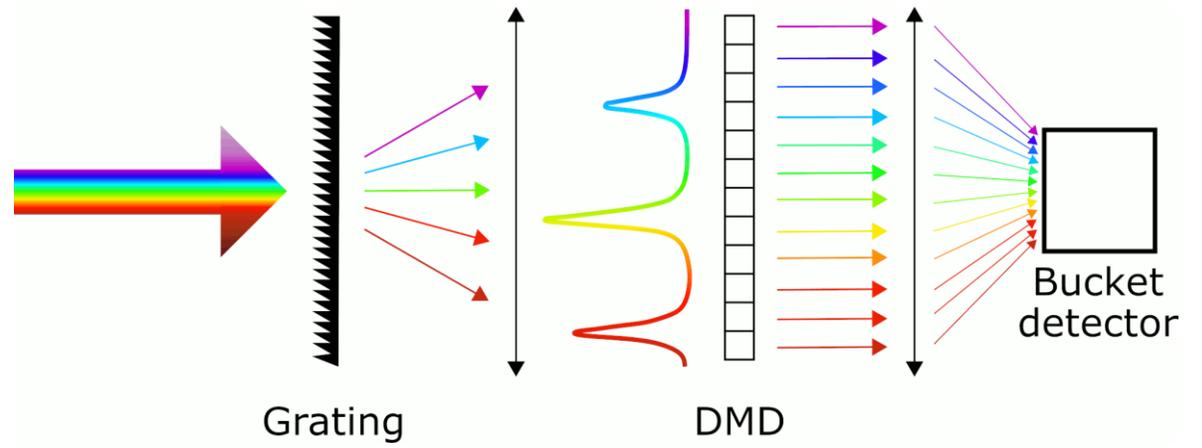
- Sequential measurement
- Single-pixel (PMT, SPAD, etc.)
- Programmable (CS, ML, MC, etc.)

## Conventional spectrometer



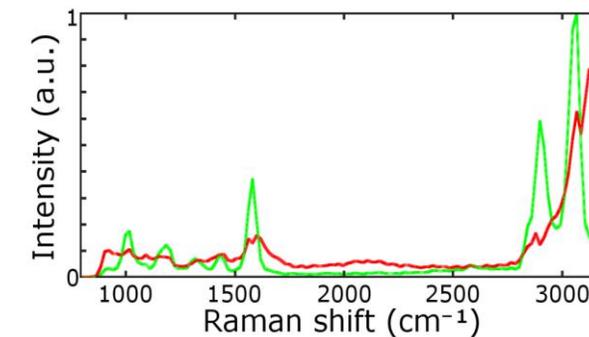
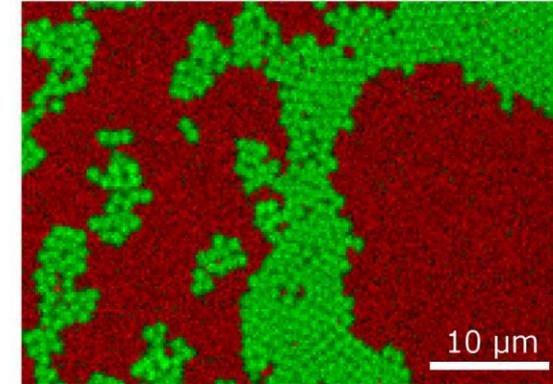
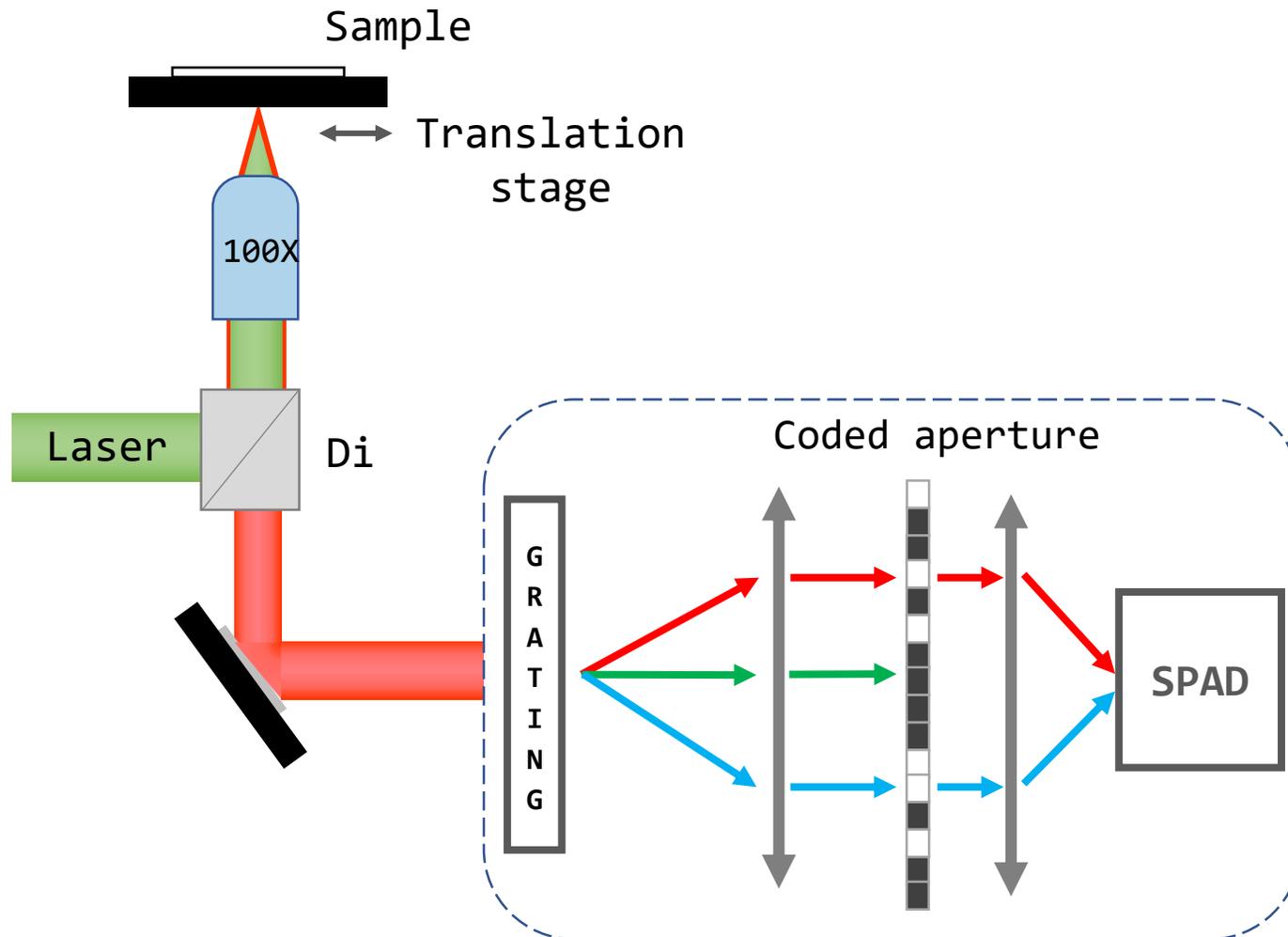
- Single-shot
- CCD/CMOS based detector

## Single-pixel spectrometer



- Sequential measurement
- Single-pixel (PMT, SPAD, etc.)
- Programmable (CS, ML, MC, etc.)

# Raman imaging via matrix completion

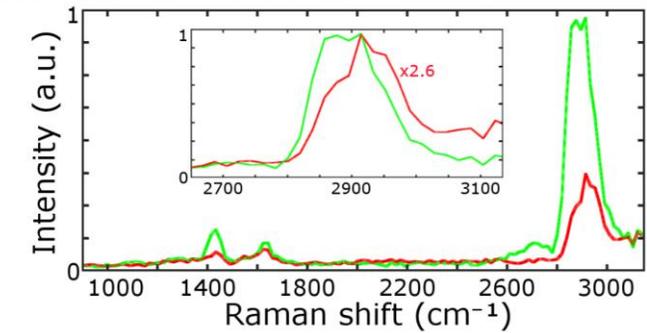
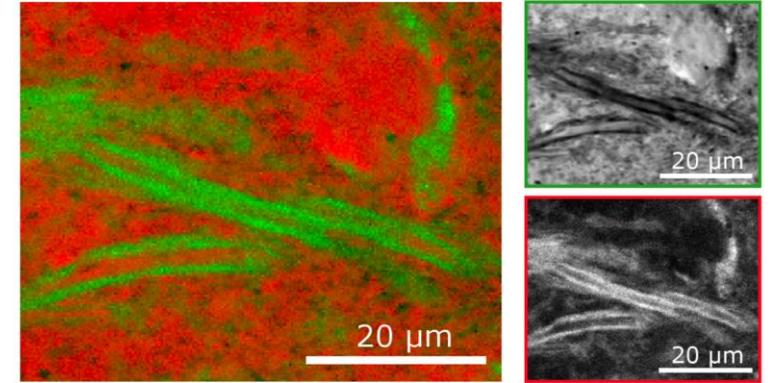
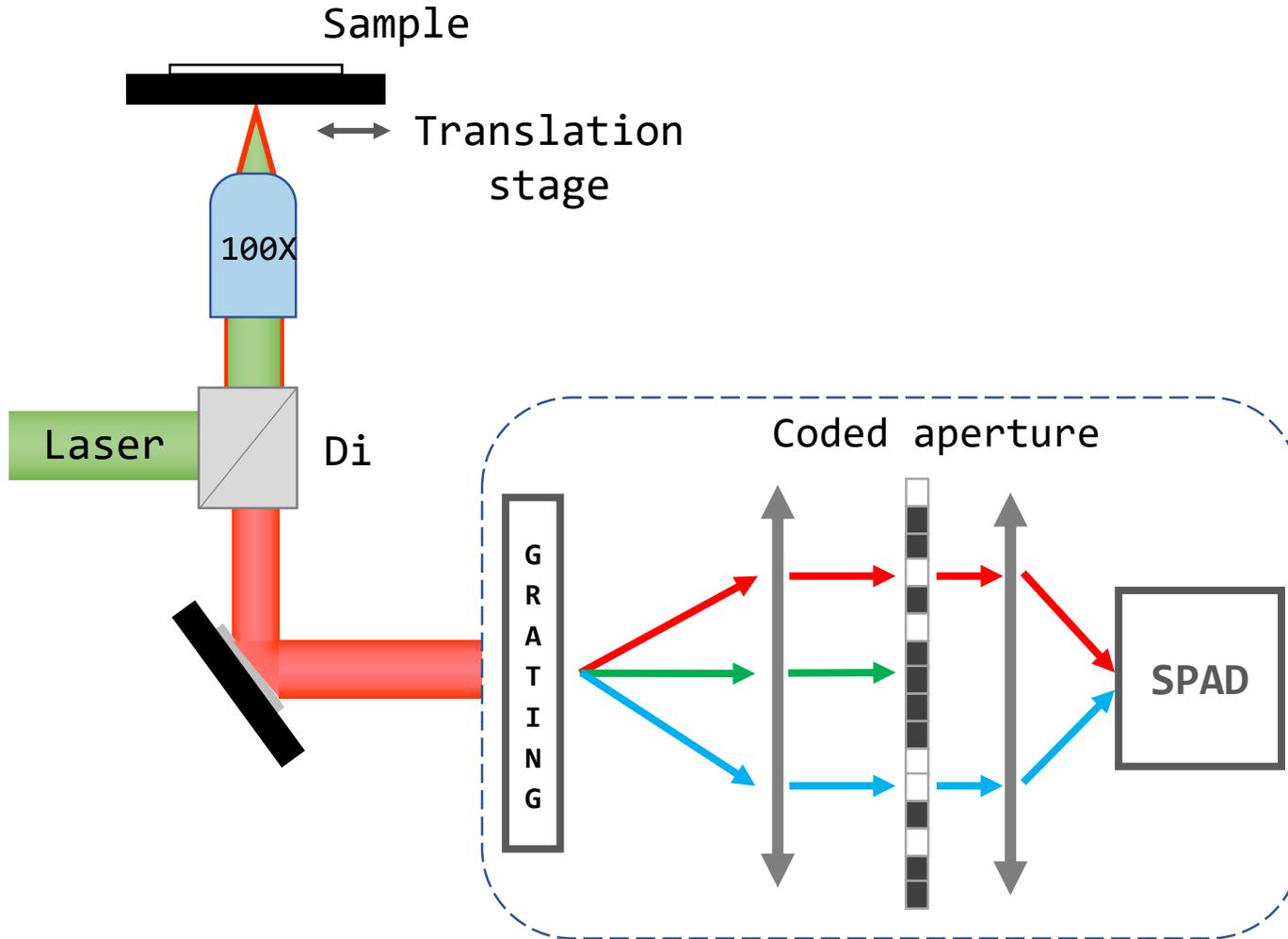


*Polystyrene beads*  
suspended in *water*

(66% compression, 8 ms pixel dwell time)

F. Soldevila, J. Dong, E. Tajahuerce,  
S. Gigan, H. B. de Aguiar, *Optica* (2019)

# Raman imaging via matrix completion



**Myelin-rich tubular structures** and **protein-rich axons** in a brain slice

(42% compression, 20 ms pixel dwell time)

Description of **computational imaging techniques based on single-pixel detection** with microstructured illumination and compressive sensing.

Application on multispectral imaging and **complex (amplitude and phase) imaging** with interferometric and non interferometric approaches.

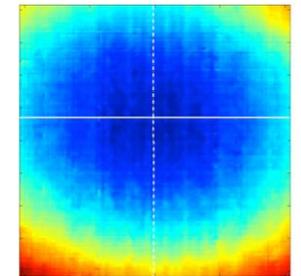
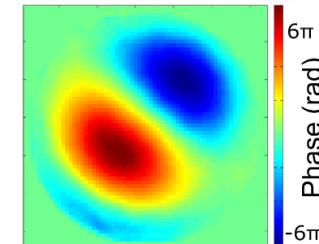
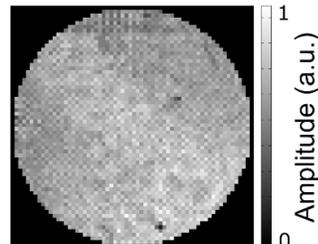
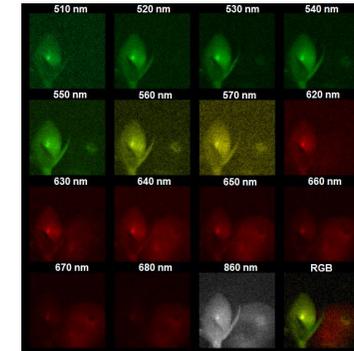
## 1. The single-pixel camera

## 2. Multispectral imaging

## 3. Complex amplitude imaging

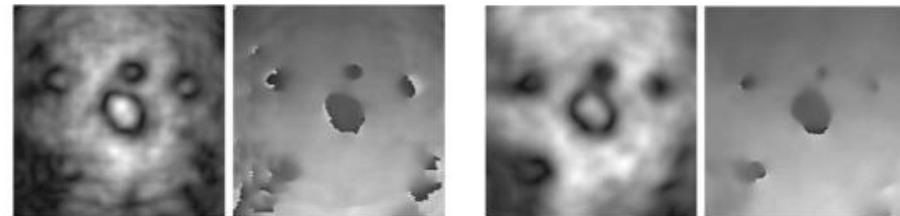
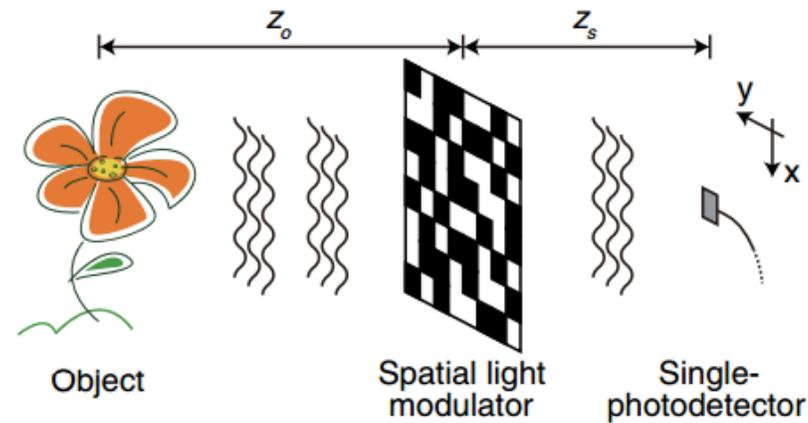
**Non-interferometric setups**

**Interferometric setups**



## Single-pixel camera by coherent diffraction imaging

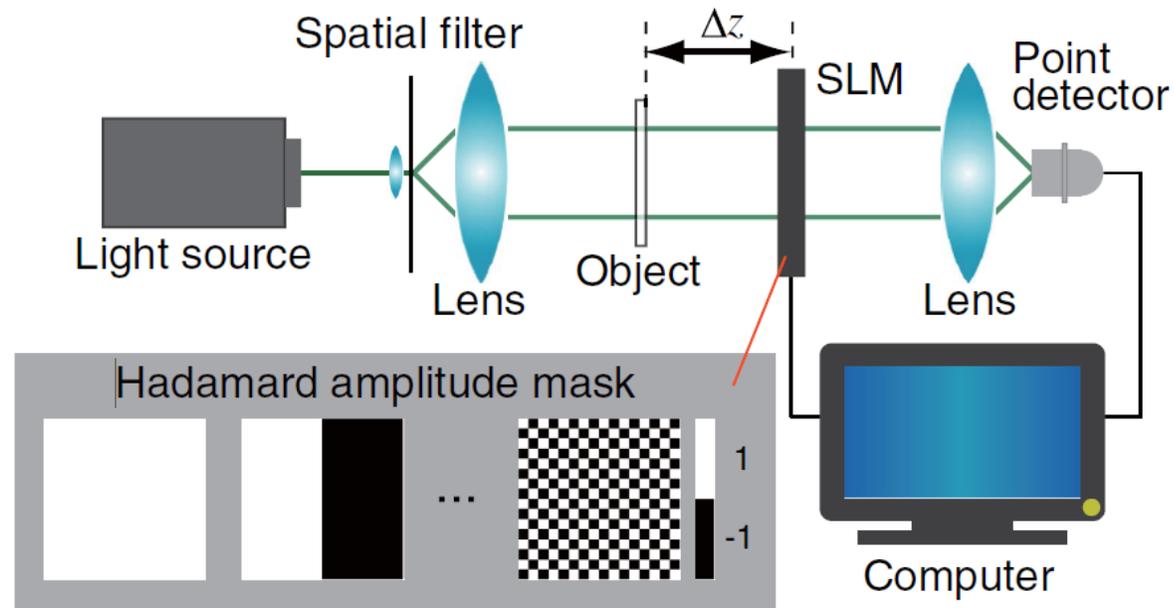
Ryoichi Horisaki



R. Horisaki et al. "Single-pixel compressive diffractive imaging",  
Applied Optics 56, 1353 (2017)

## Transport-of-intensity single-pixel imaging

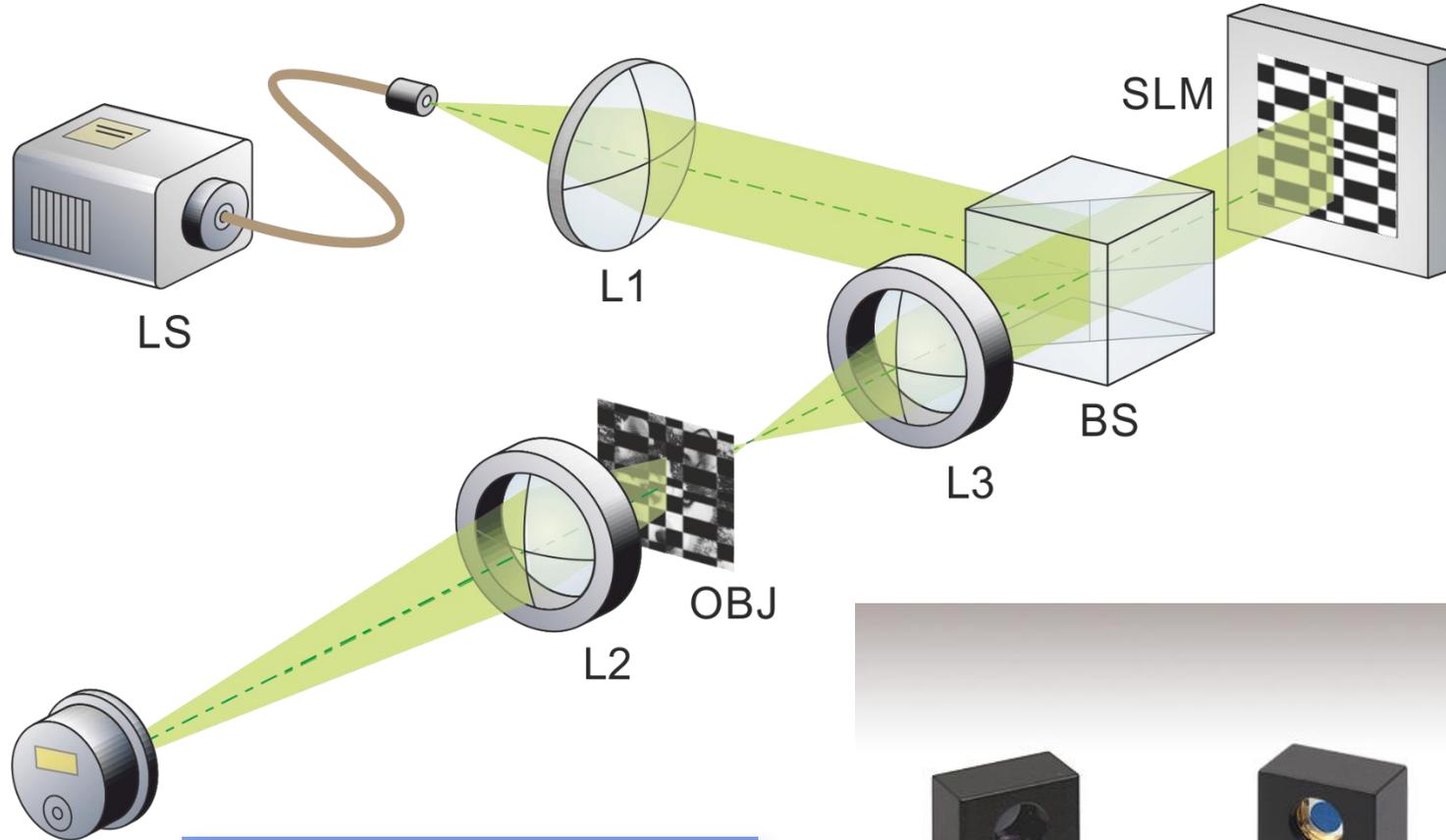
Takanori Nomura



Koshi Komuro, Yuya Yamazaki, and Takanori Nomura, "Transport-of-intensity computational ghost imaging," *Appl. Opt.* 57, 4451-4456 (2018)

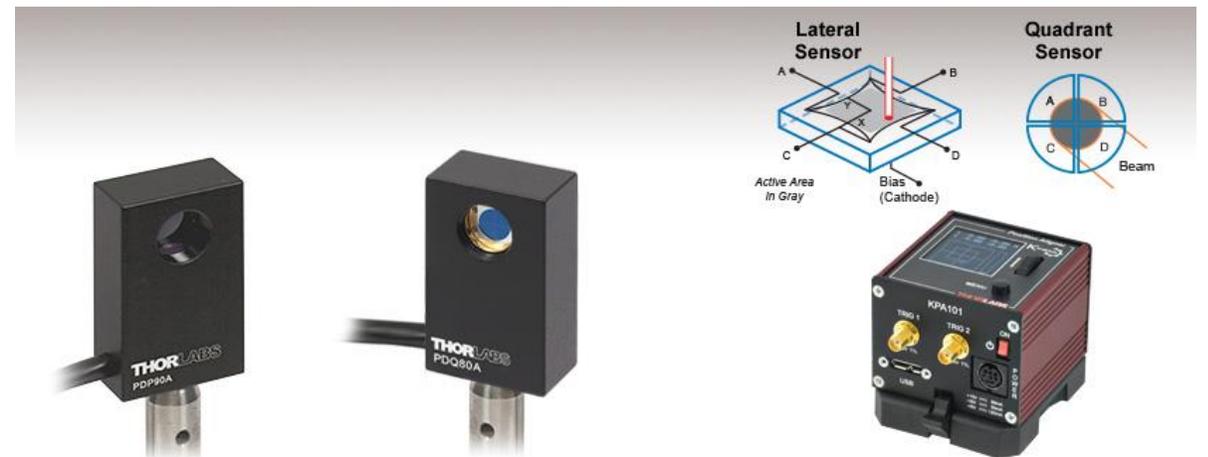
# Single-pixel holographic cameras

Light source



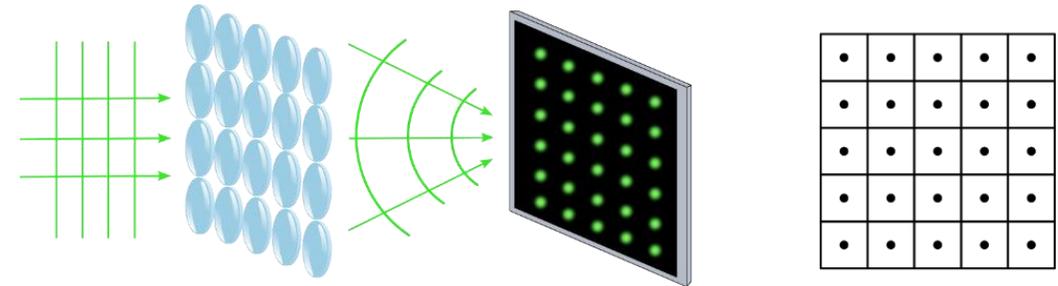
Spatial light modulator

Position sensing detector



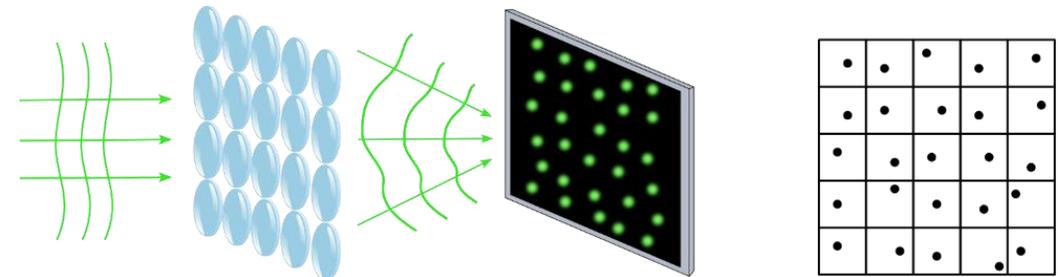
## Shack-Hartmann wavefront sensing

For a plane wave the lenslet array generates a **regular distribution of focal spots**



If the wavefront presents **aberrations**, the spots change their **position**.

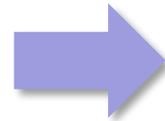
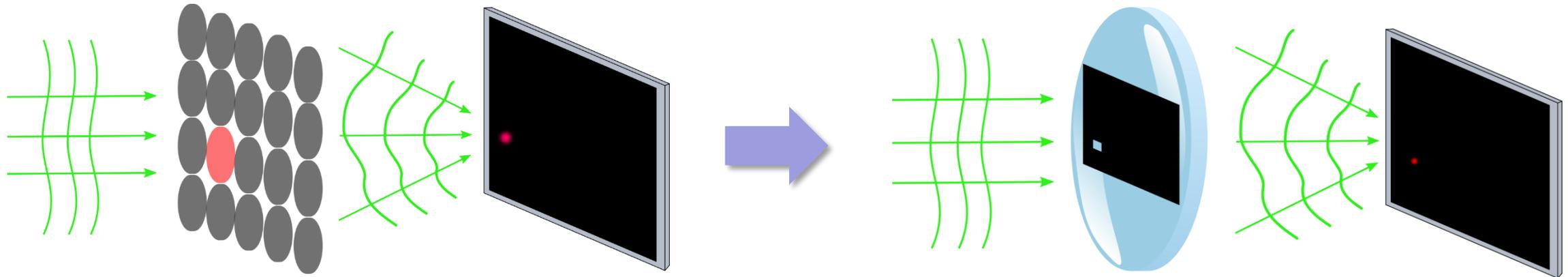
This change provides **phase information**



$$\vec{\Delta} = (\Delta x, \Delta y) = \frac{\lambda f}{2\pi} \vec{\nabla} \varphi$$

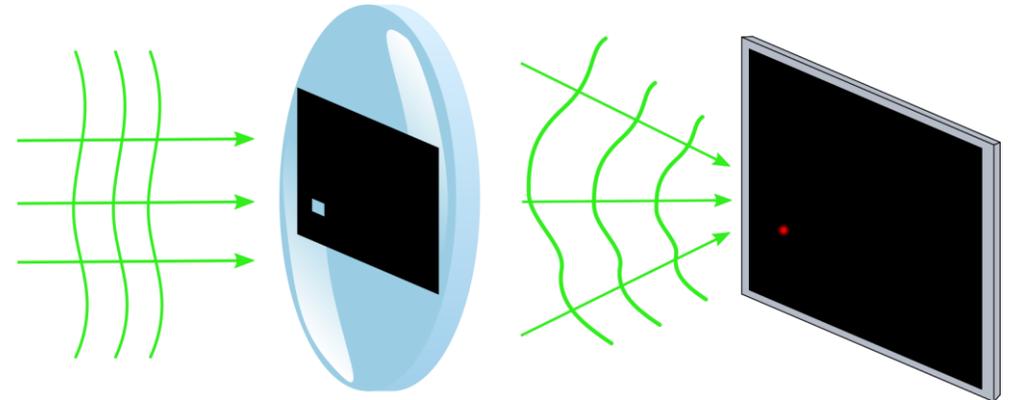
The Shack-Hartmann sensor can be used for complex amplitude imaging!

# Single-pixel complex amplitude imaging

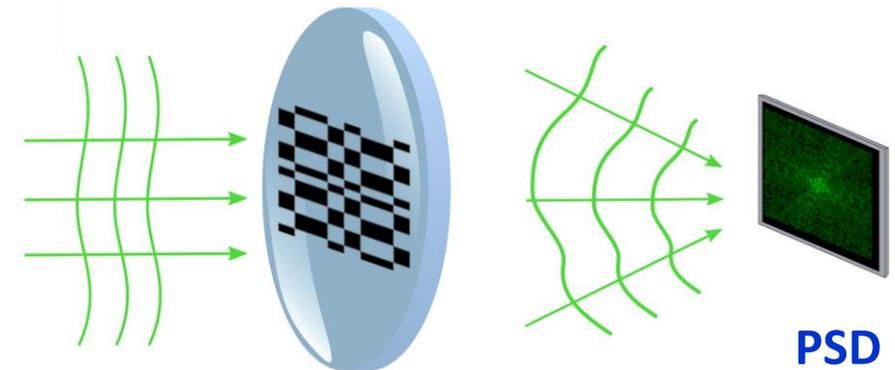


New approach:

- Use a **single lens**
- Codify apertures with a **fast SLM**
- Measure spots with a **fast PSD**

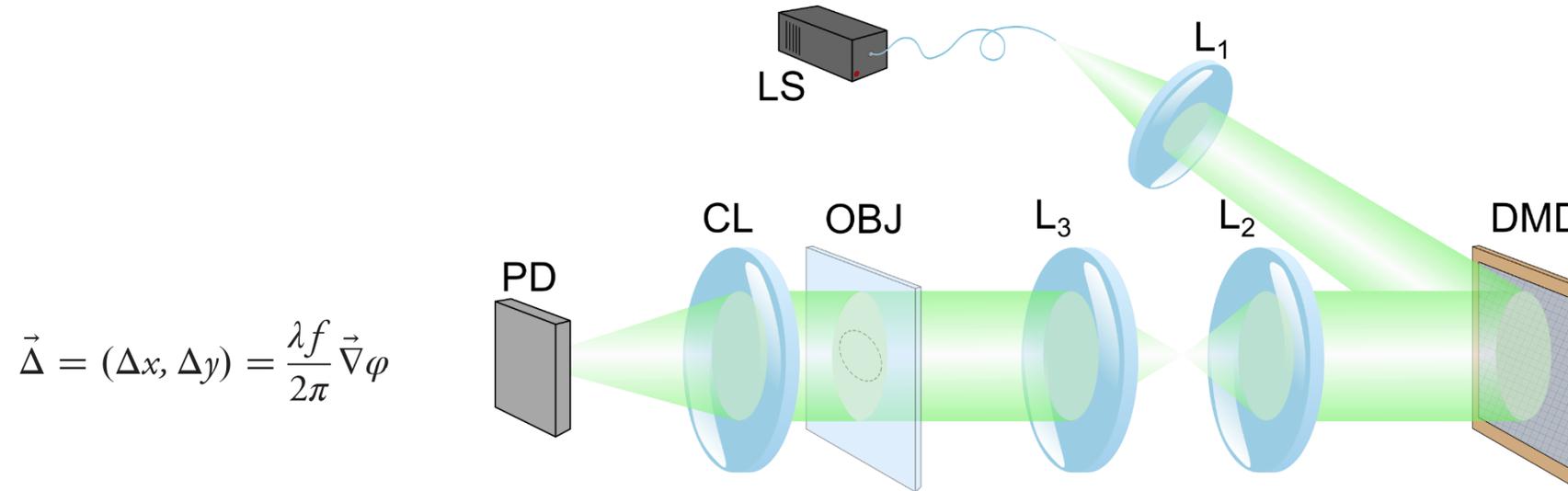


CCD



PSD

# Single-pixel complex amplitude imaging

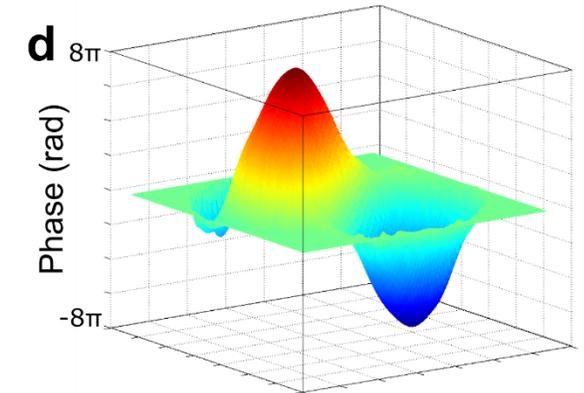
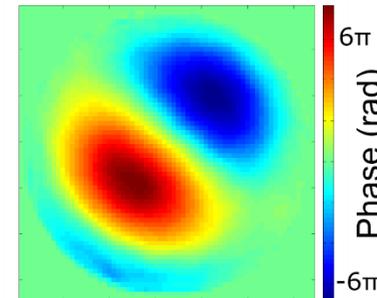
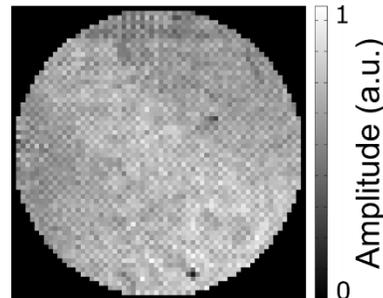


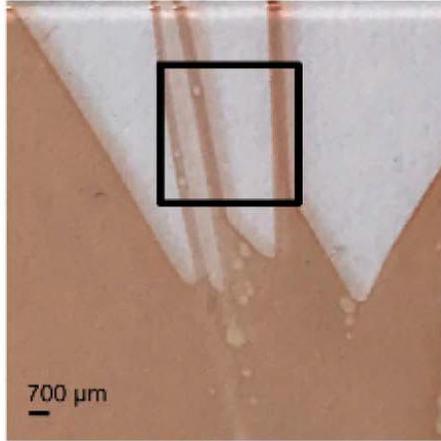
Object: **Coma aberration plate**

Size: 64×64 pixels (~80 μm pixel pitch)

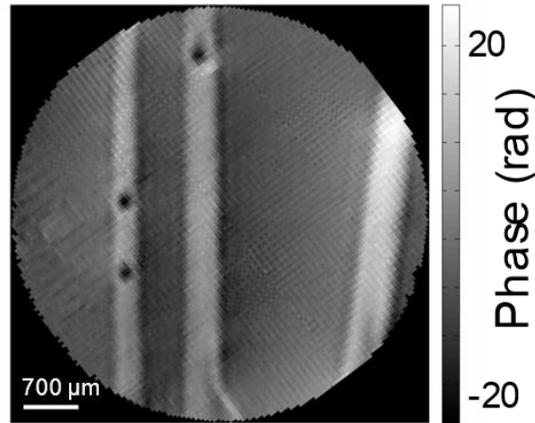
Acquisition time: ~200 ms

(~22 kHz refresh rate)

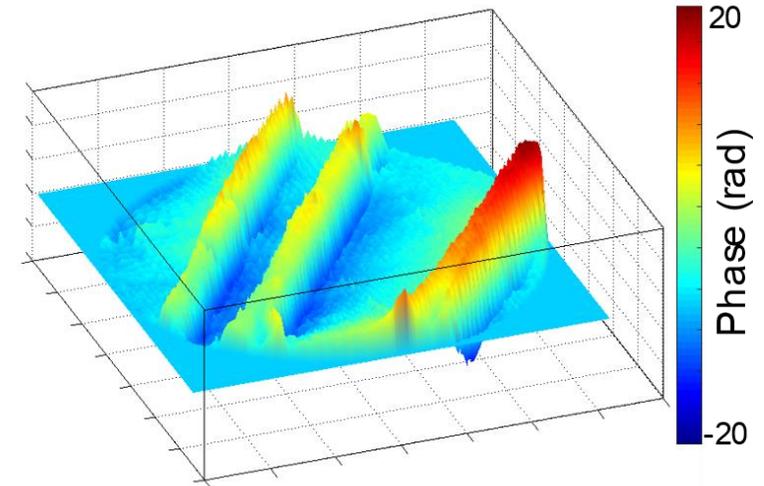




Object: Photoresist layer

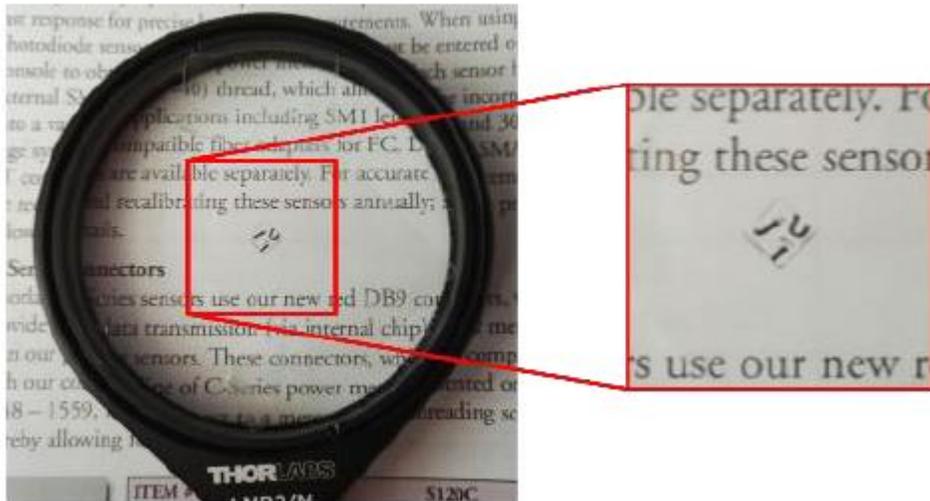


Size: 128×128 pixels (~40 μm pixel pitch)  
Acquisition time: ~0.8 s

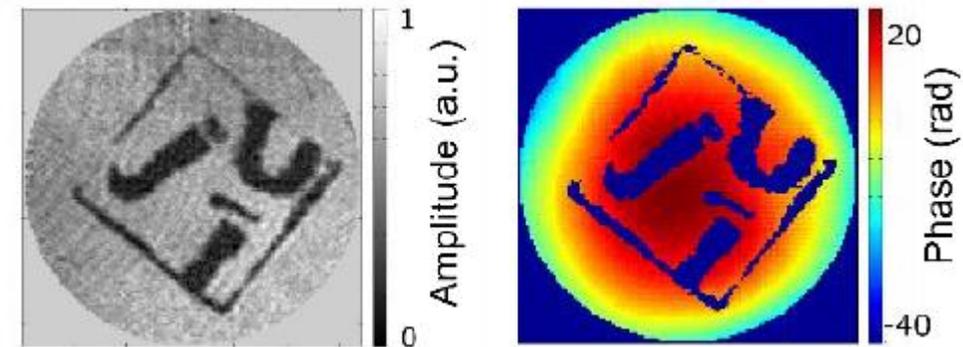


**High detail** can be recovered: small holes caused by air bubbles with ~80 μm diameter

# Single-pixel complex amplitude imaging

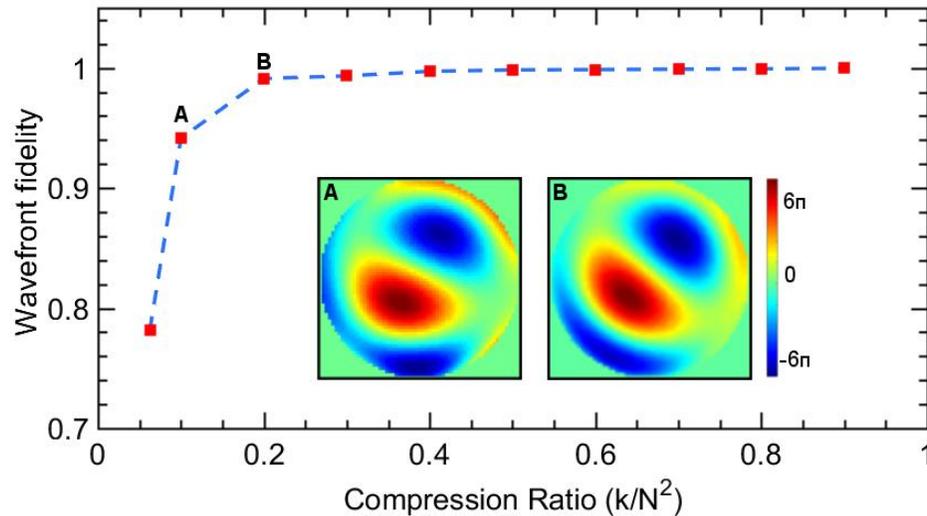


Object: Lens with an amplitude mask

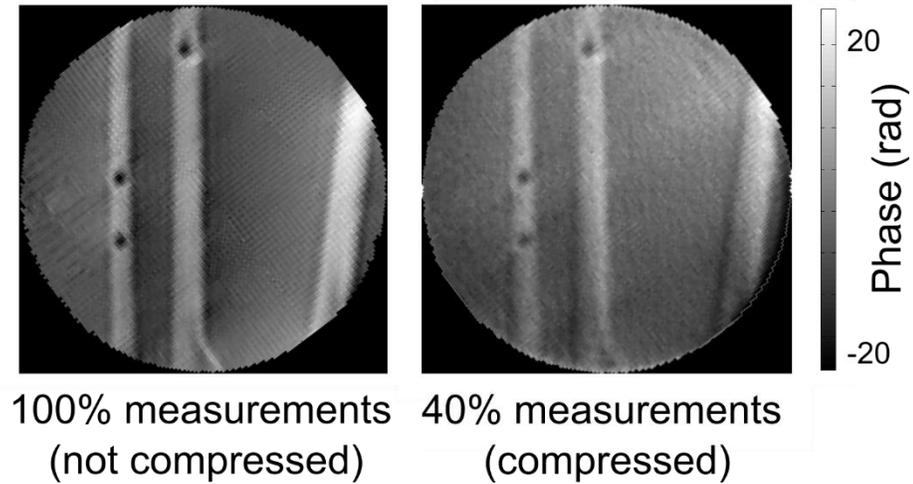


Size: 128×128 pixels (~40 μm pixel pitch)  
Acquisition time: ~0.8 s

## Speeding up: compressive sensing



Object: Coma aberration plate  
Size: 64×64 pixels (~80 μm pixel pitch)  
Acquisition time: ~**10-20 ms** (at ~22 kHz)



Object: Photoresist layer  
Size: 128×128 pixels (~40 μm pixel pitch)  
Acquisition time: ~**0.3 s** (at ~22 kHz)

Description of **computational imaging techniques based on single-pixel detection** with microstructured illumination and compressive sensing.

Application on multispectral imaging and **complex (amplitude and phase) imaging** with interferometric and non interferometric approaches.

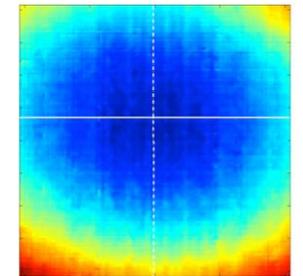
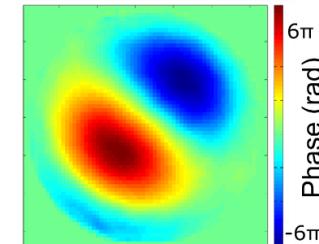
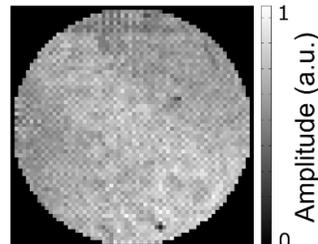
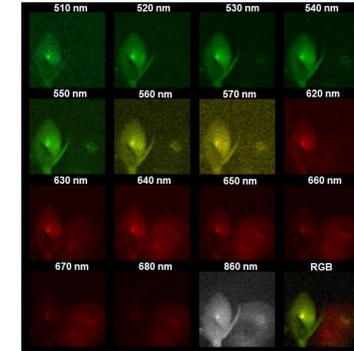
## 1. The single-pixel camera

## 2. Multispectral imaging

## 3. Complex amplitude imaging

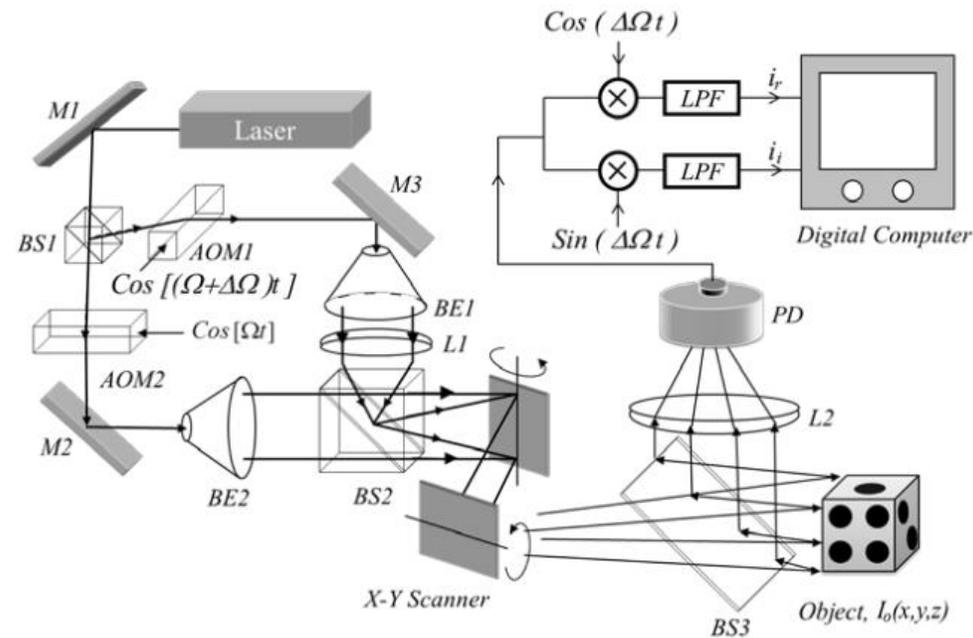
Non-interferometric setups

**Interferometric setups**



## Optical scanning holography (OSH)

Ting-Chung Poon

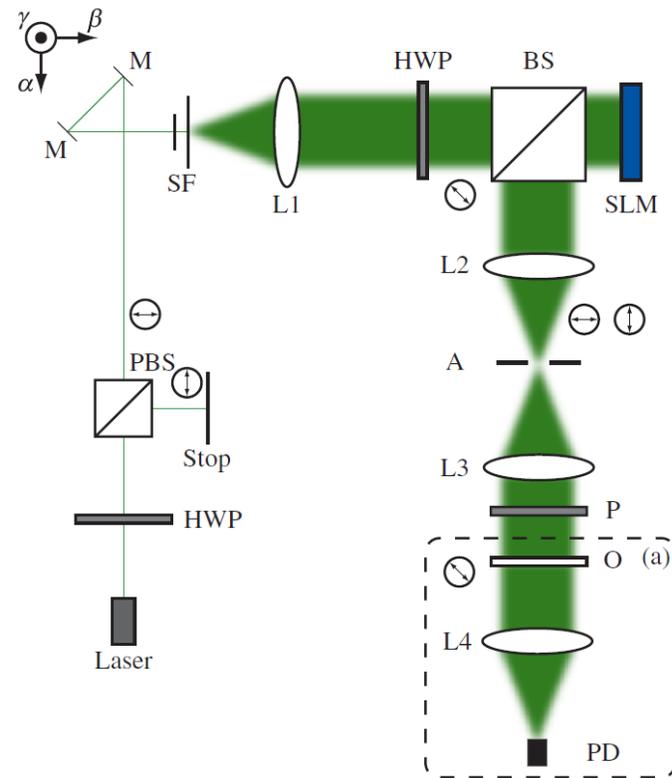


Y. S. Kim et al. "Speckle-free digital holographic recording of a diffusely reflecting object", Opt. Express 21, 8183 (2013)

J. P. Liu et al., "Coherence-Experiments-Single-Pixel-Digital-Holography", Opt. Lett. 40, 2366 (2015)

## Motionless optical scanning holography

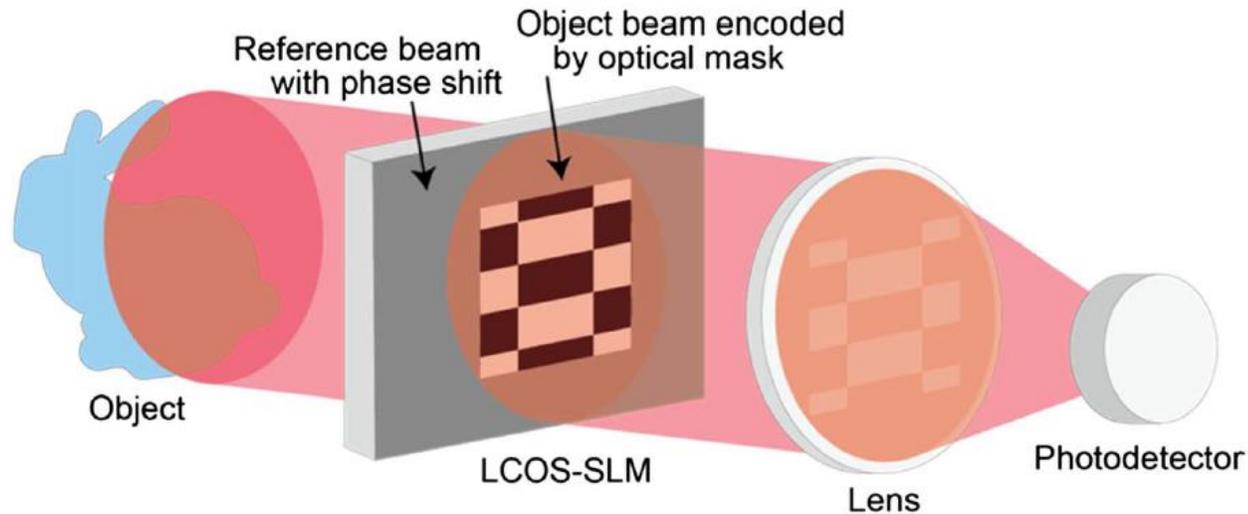
Takanori Nomura



Naru Yoneda, Yusuke Saita, and Takanori Nomura, Motionless optical scanning holography, Opt. Lett. 45, 3184-3187 (2020)

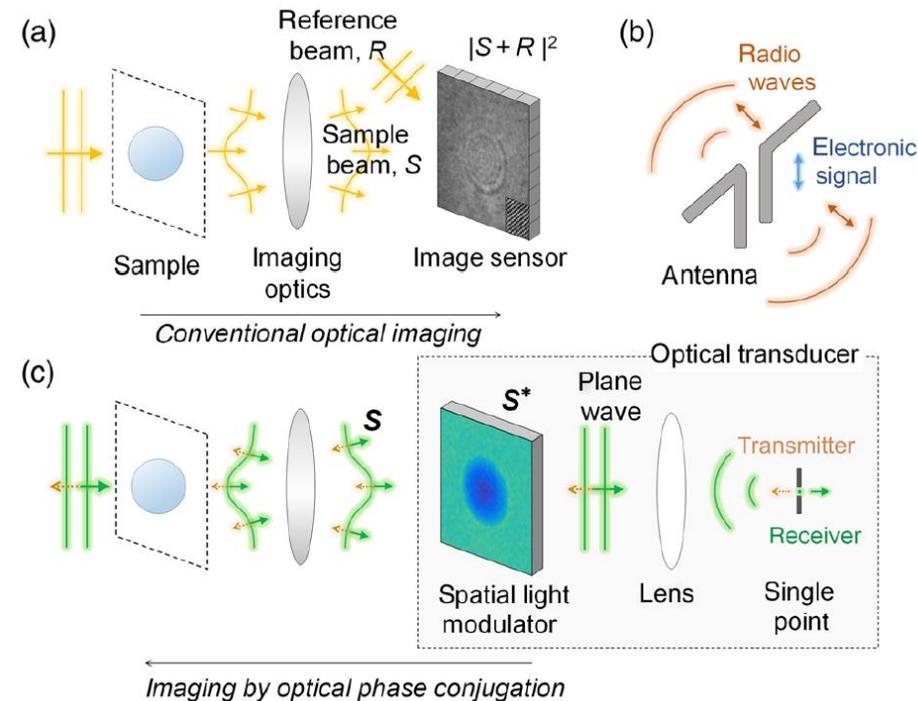
## Complex amplitude single-pixel imaging with a common-path interferometer

Yoshio Hayasaki



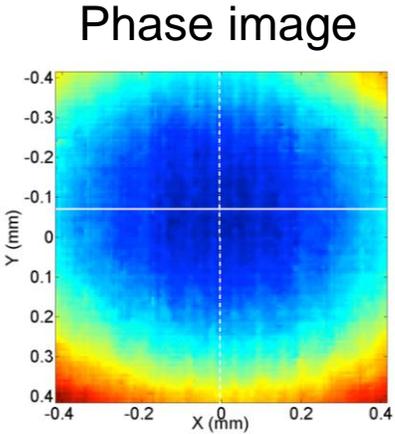
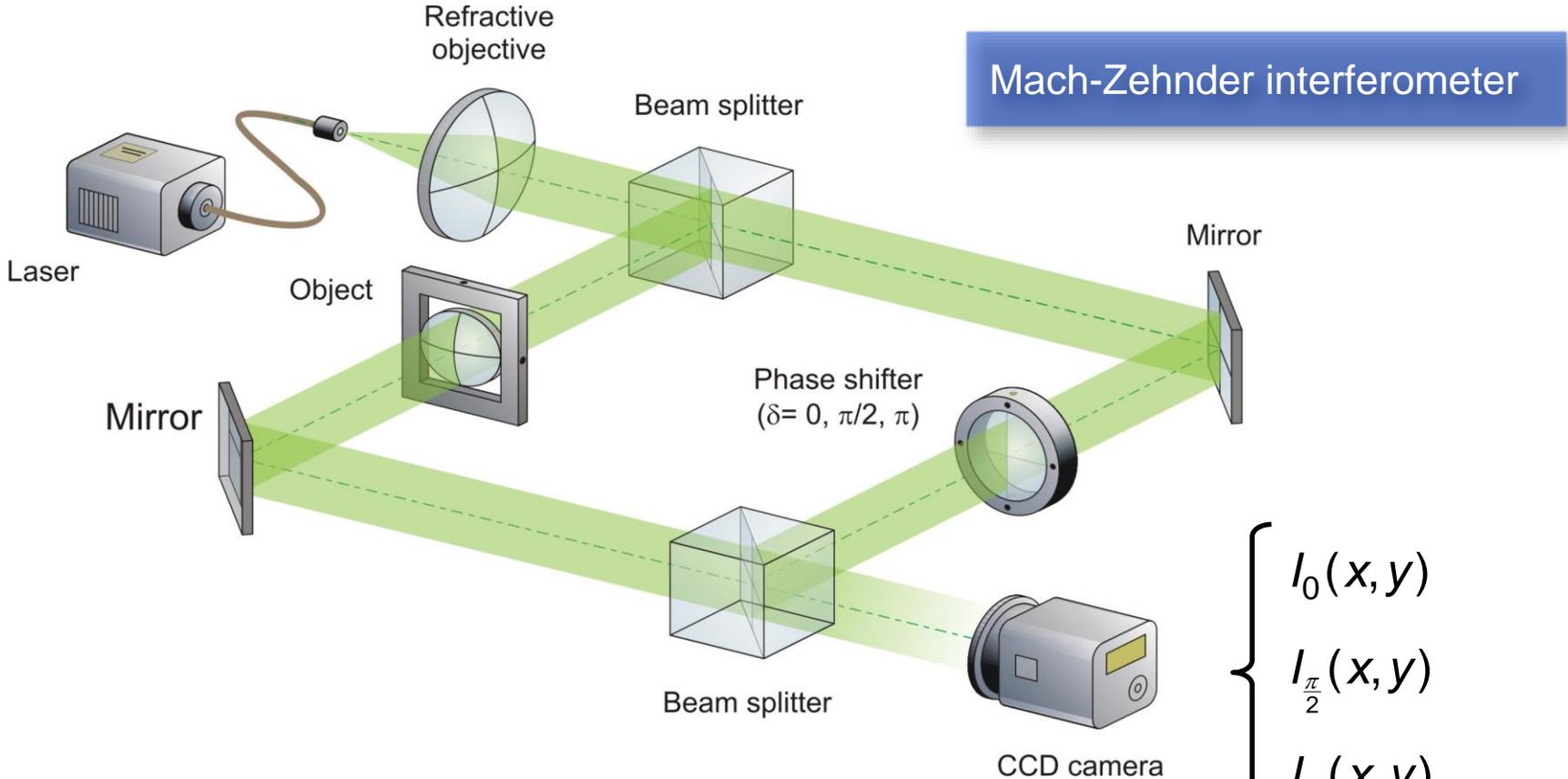
Kazuki Ota and Yoshio Hayasaki, "Complex-amplitude single-pixel imaging," *Opt. Lett.* 43, 3682-3685 (2018)

## Reference-free single-pixel holographic imaging YongKeun Park



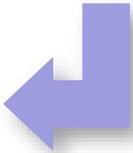
Seungwoo Shin, KyeoReh Lee, YoonSeok Baek, and YongKeun Park, "Reference-free single-point holographic imaging and realization of an optical bidirectional transducer," Phys. Rev. Appl. 9, 044042 (2018)

# Single-pixel holographic camera



Fresnel propagation

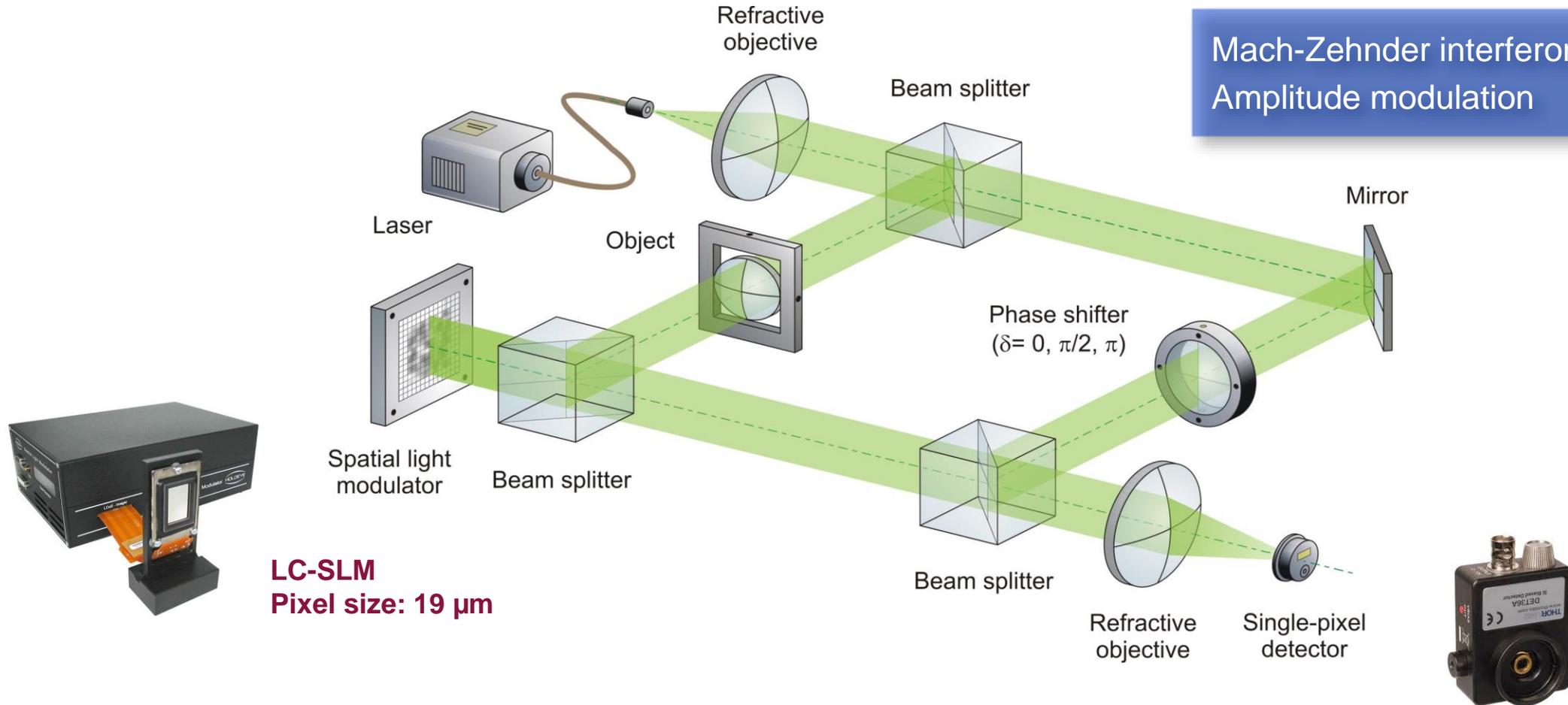
$$H(x, y) = \frac{1}{4} [I_0(x, y) - I_\pi(x, y)] + \frac{j}{4} [2I_{\pi/2}(x, y) - I_0(x, y) - I_\pi(x, y)]$$



Phase shifting

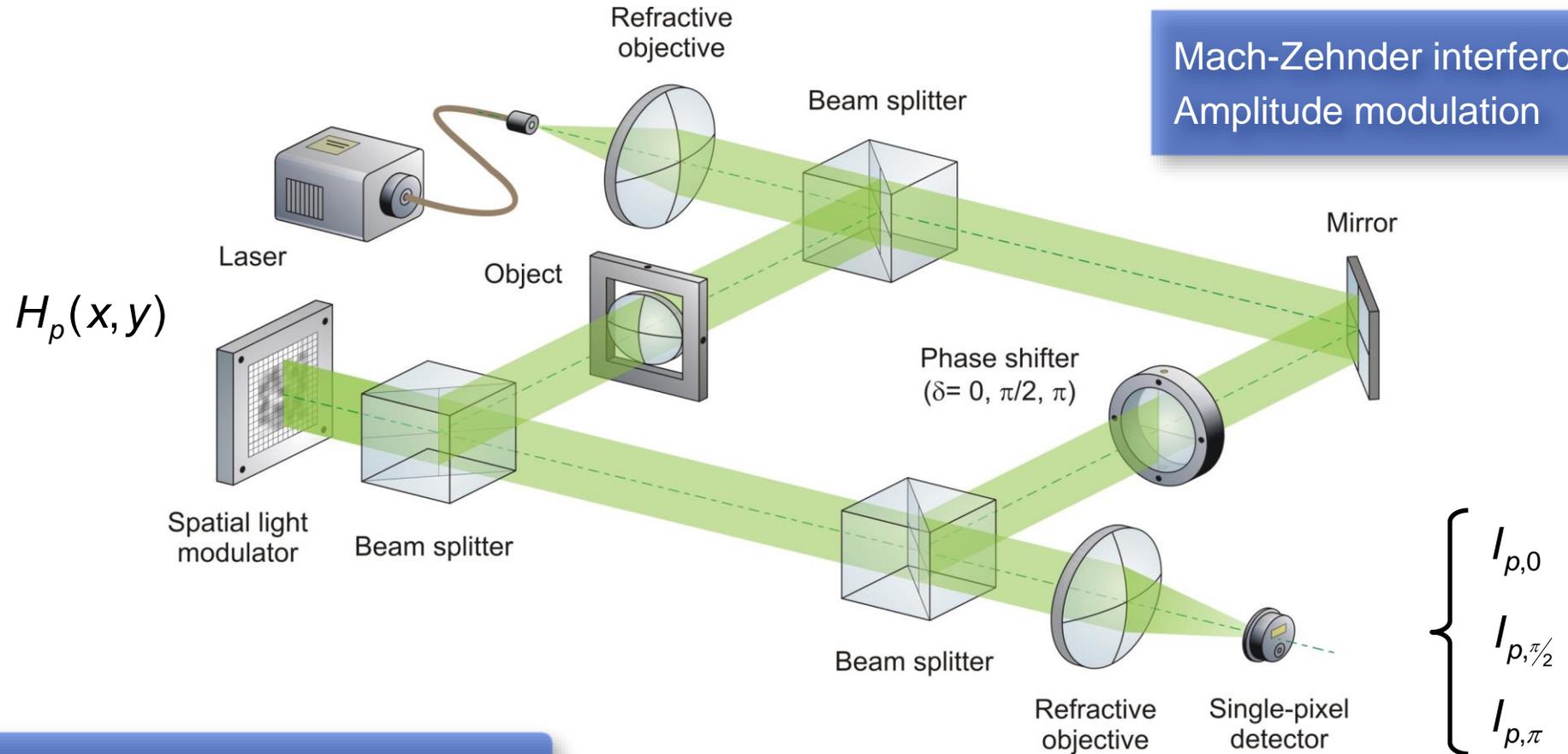
$$\left\{ \begin{array}{l} I_0(x, y) \\ I_{\pi/2}(x, y) \\ I_\pi(x, y) \end{array} \right.$$

# Single-pixel holographic camera



P. Clemente et al.  
Optics Letters 38, 2524 (2013)

# Single-pixel holographic camera



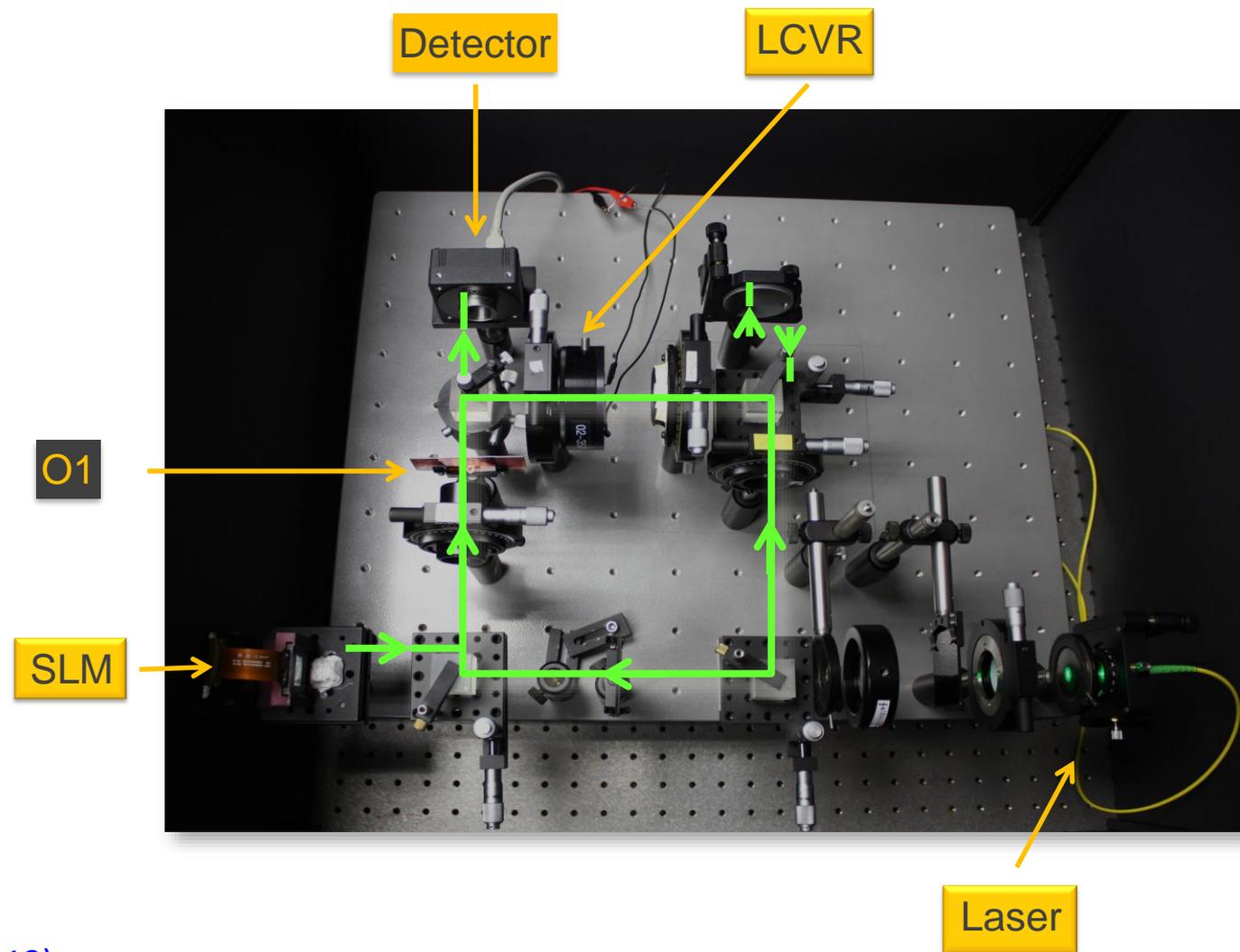
Reconstruction algorithm

$$H(x, y) = \sum_{p=1}^M y_p \cdot H_p(x, y)$$

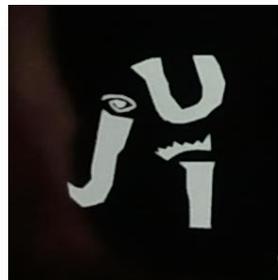
$$y_p = \frac{1}{4} [I_{p,0} - I_{p,\pi}] + \frac{j}{4} [2I_{p,\pi/2} - I_{p,0} - I_{p,\pi}]$$



# Single-pixel holographic camera



P. Clemente et al.  
Optics Letters 38, 2524 (2013)



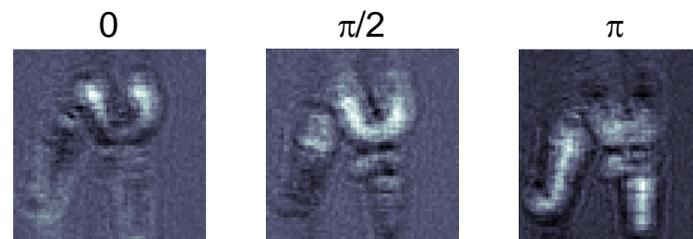
**Amplitude object**

**Size:** 4,864 x 4,864 mm<sup>2</sup>

**Resolution:** 38 μm

**Propagated distance:** 253 mm

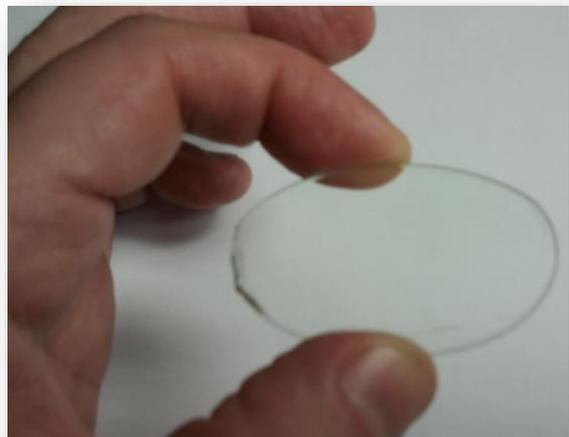
**Compression ratio:** 5:1



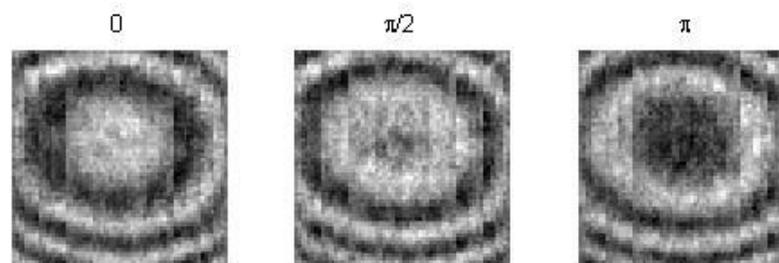
**Phase-shifted Interferograms**



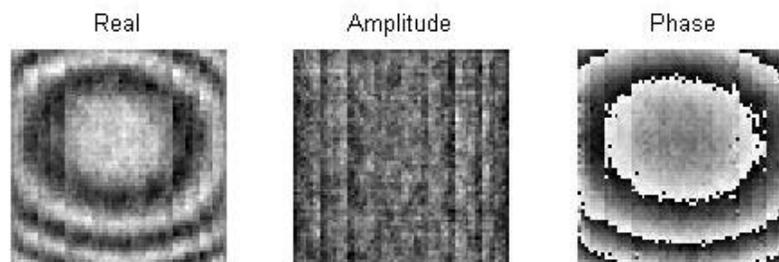
**Reconstructed object**



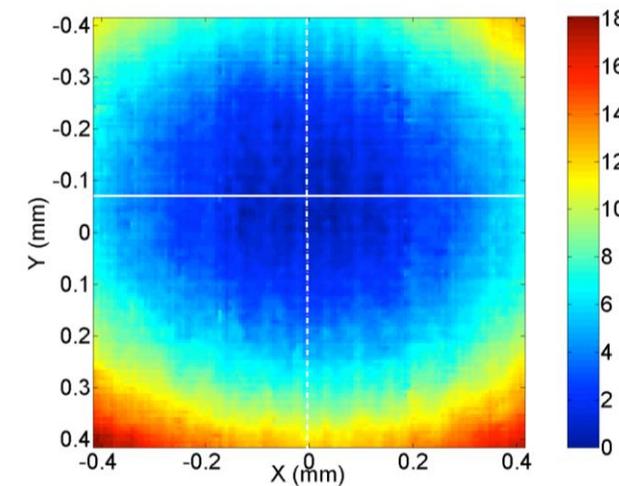
Phase object



Phase-shifted Interferograms



Reconstructed phase



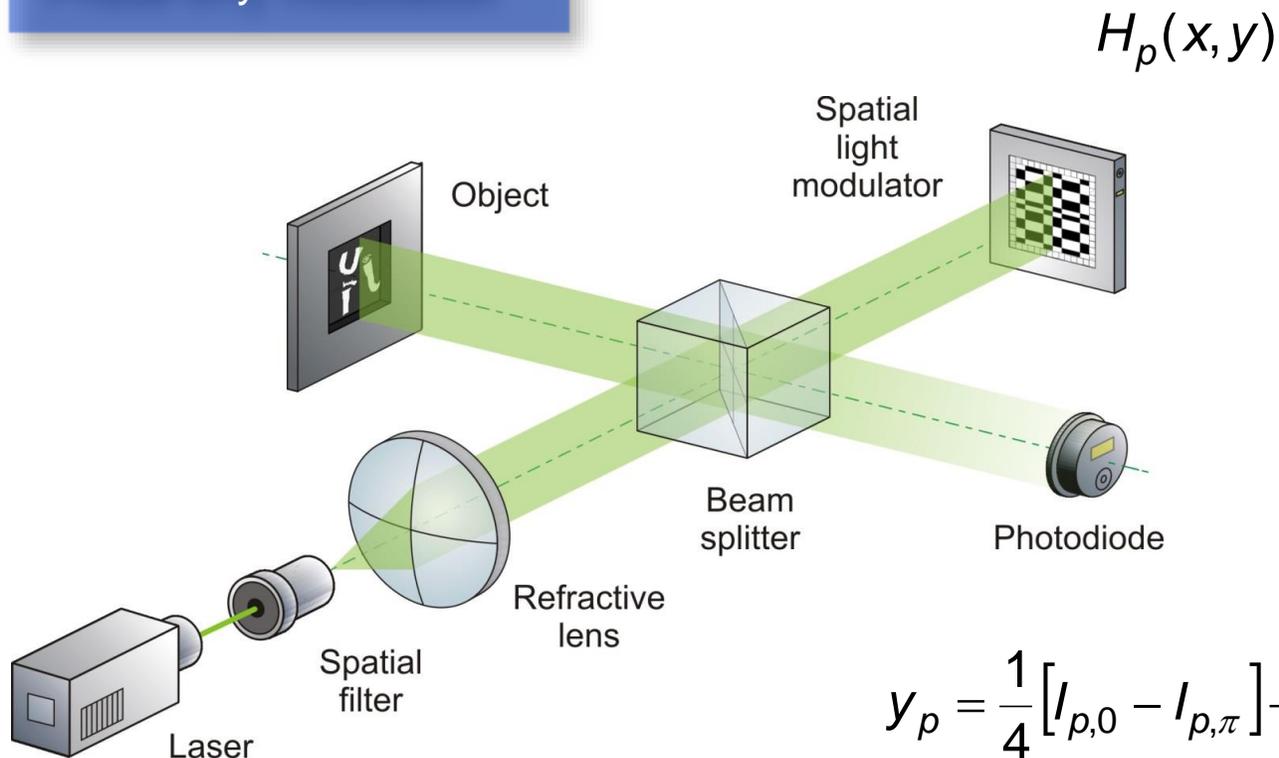
Size : 128 x 128 pixels

Resolution : 19  $\mu\text{m}$

Prop. distance: -153 mm

Compression ratio: 5:1

Michelson interferometer  
Phase-only modulation



Microstructured  
phase patterns

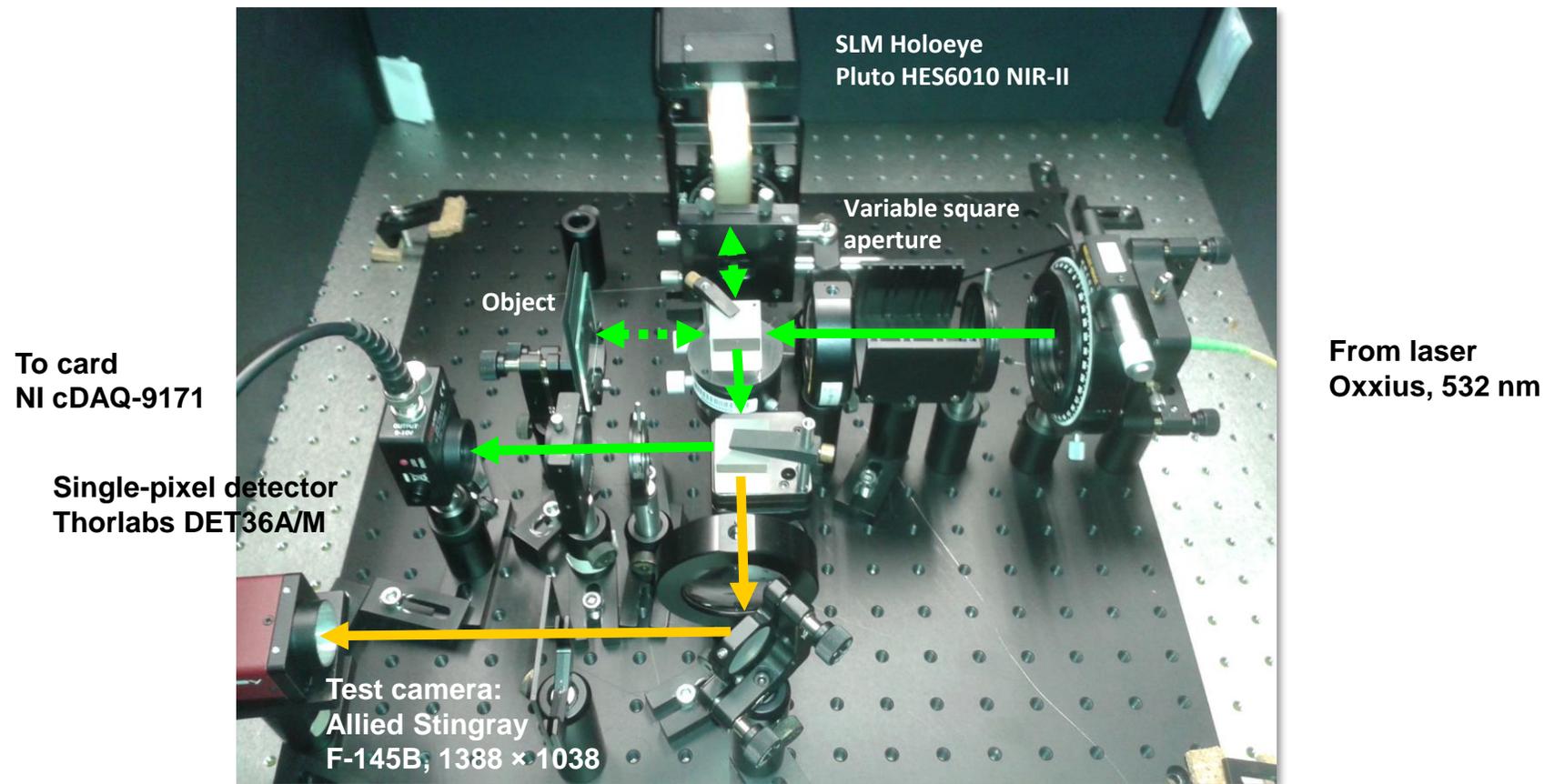
Sampling patterns  
encoded in the  
reference beam

$$y_p = \frac{1}{4} [I_{p,0} - I_{p,\pi}] + \frac{j}{4} [2I_{p,\pi/2} - I_{p,0} - I_{p,\pi}]$$

$$O(x, y) = \frac{1}{N} \sum_{p=1}^M I_p \cdot H_p(x, y)$$

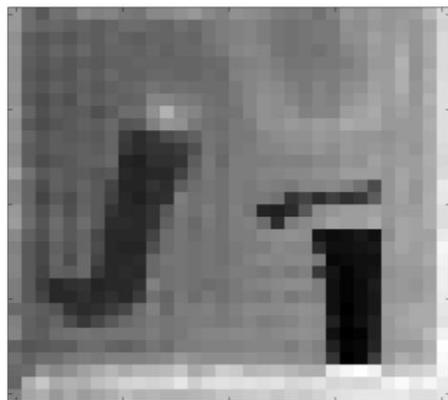


# Single-pixel holographic camera with phase patterns





Amplitude hologram reconstruction,  
(1600 patterns)

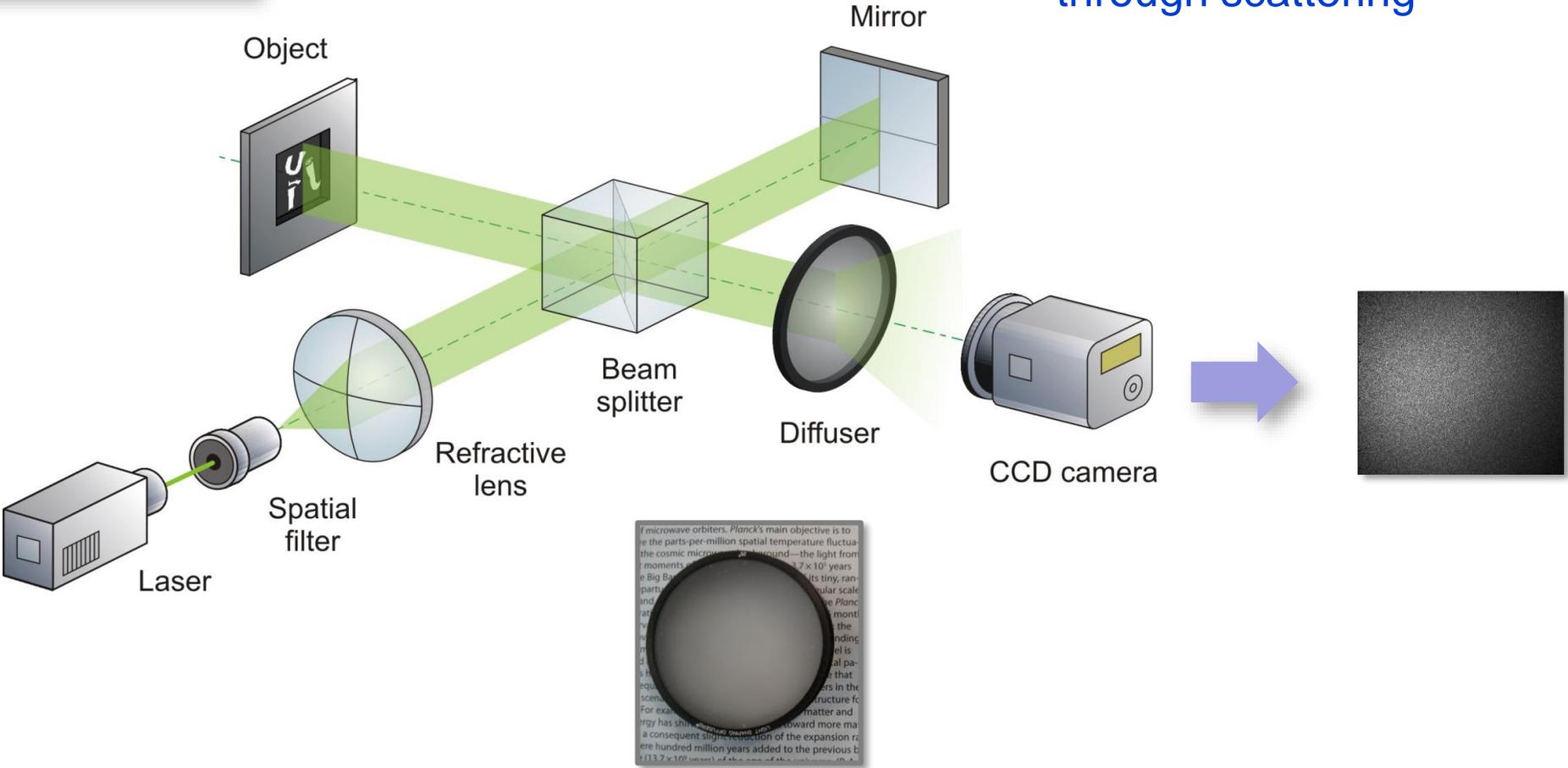


Phase hologram reconstruction by  
single-pixel holography  
(784 patterns)

# Single-pixel holographic camera with phase patterns

Conventional phase-shifting  
Michelson interferometer

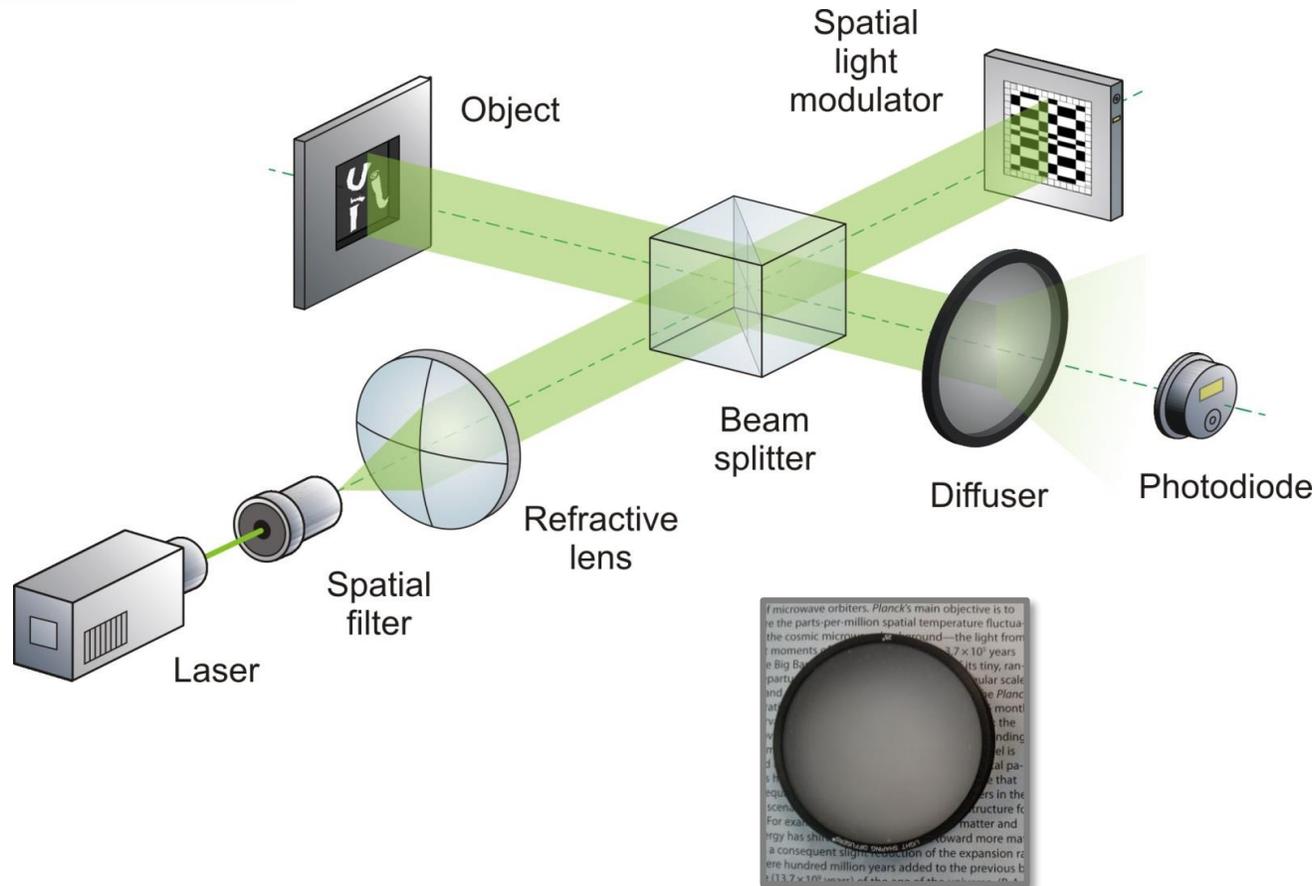
Complex amplitude imaging  
through scattering



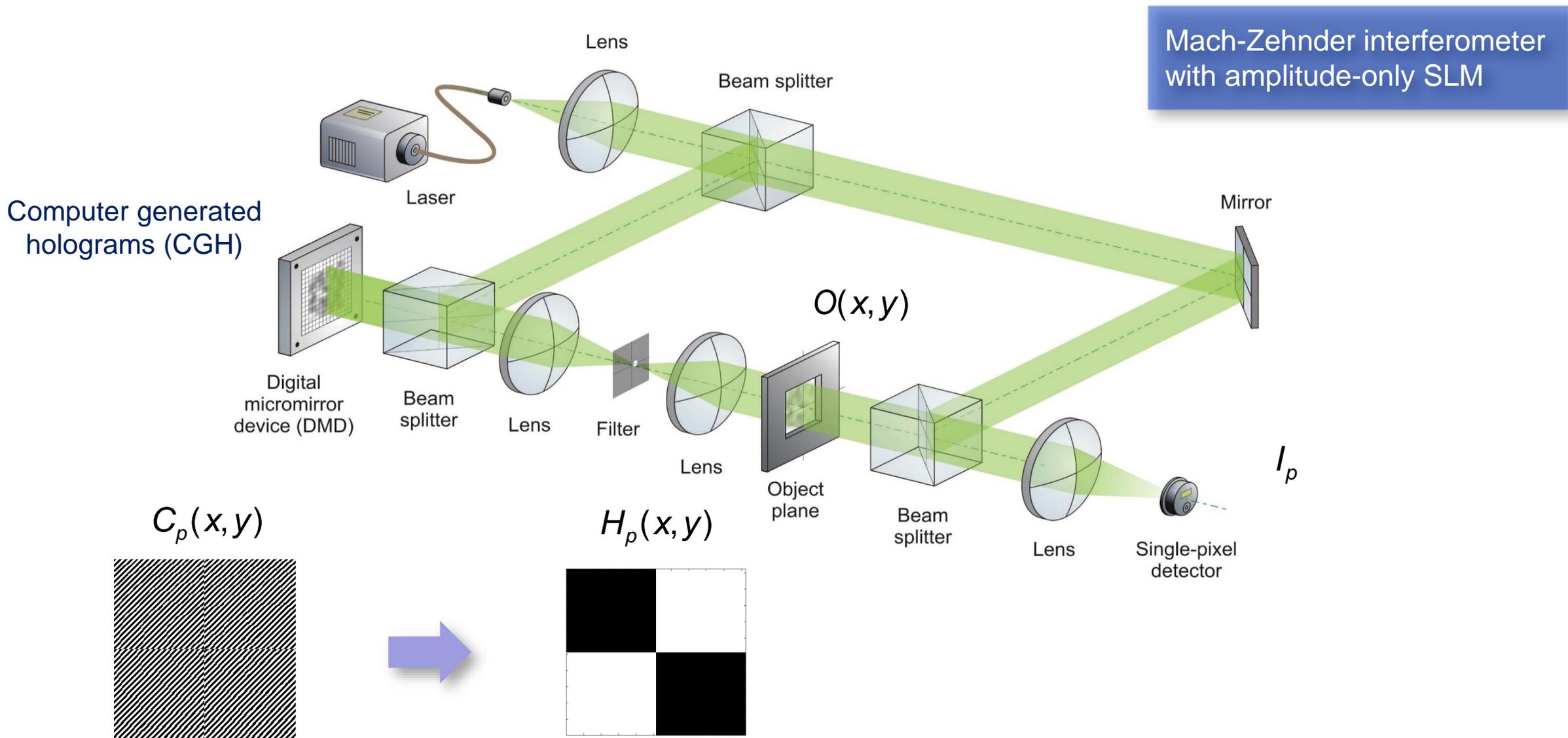
# Single-pixel holographic camera with phase patterns

Michelson interferometer  
Phase-only modulation

Complex amplitude imaging  
through scattering

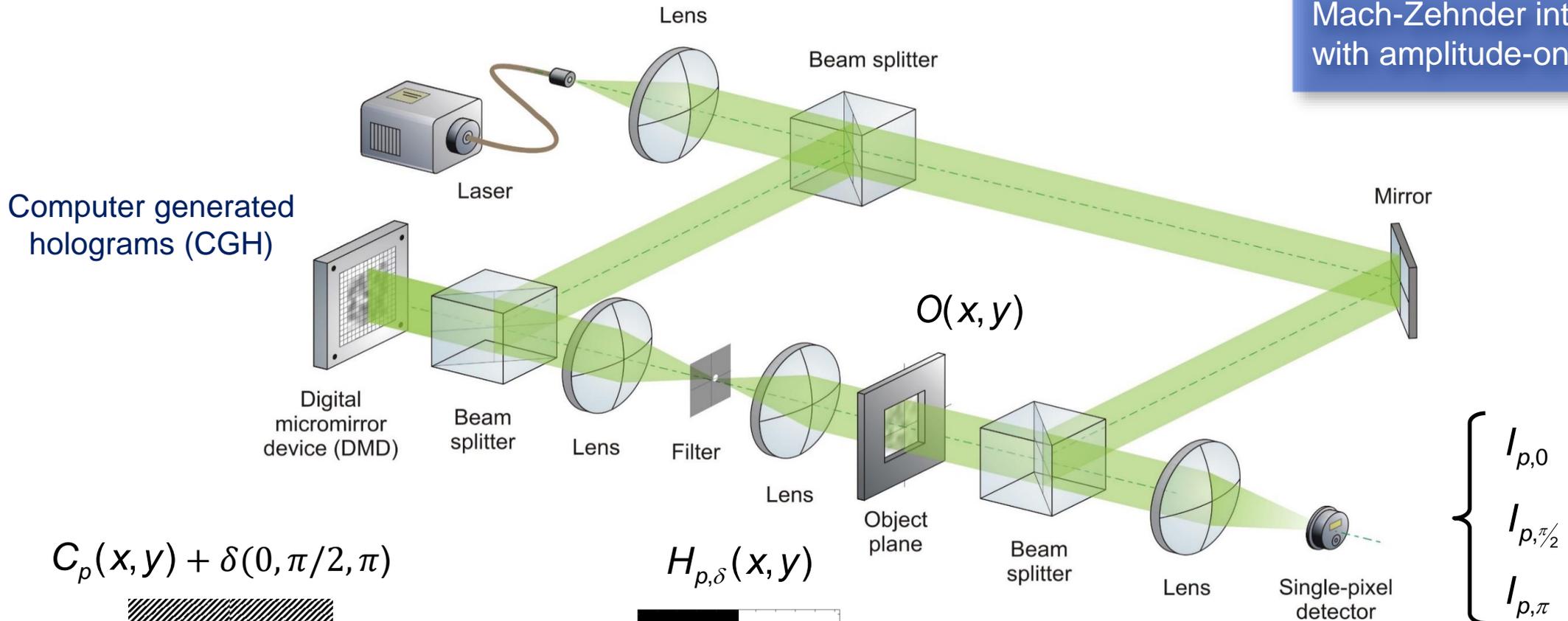


# Single-pixel holographic camera with DMD

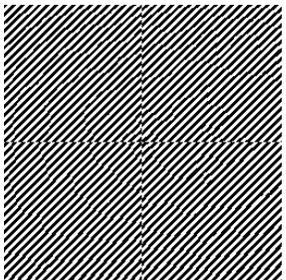


# Single-pixel holographic camera with DMD

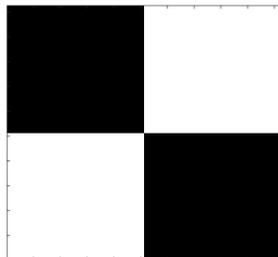
Mach-Zehnder interferometer with amplitude-only SLM



$$C_p(x,y) + \delta(0, \pi/2, \pi)$$



$$H_{p,\delta}(x,y)$$

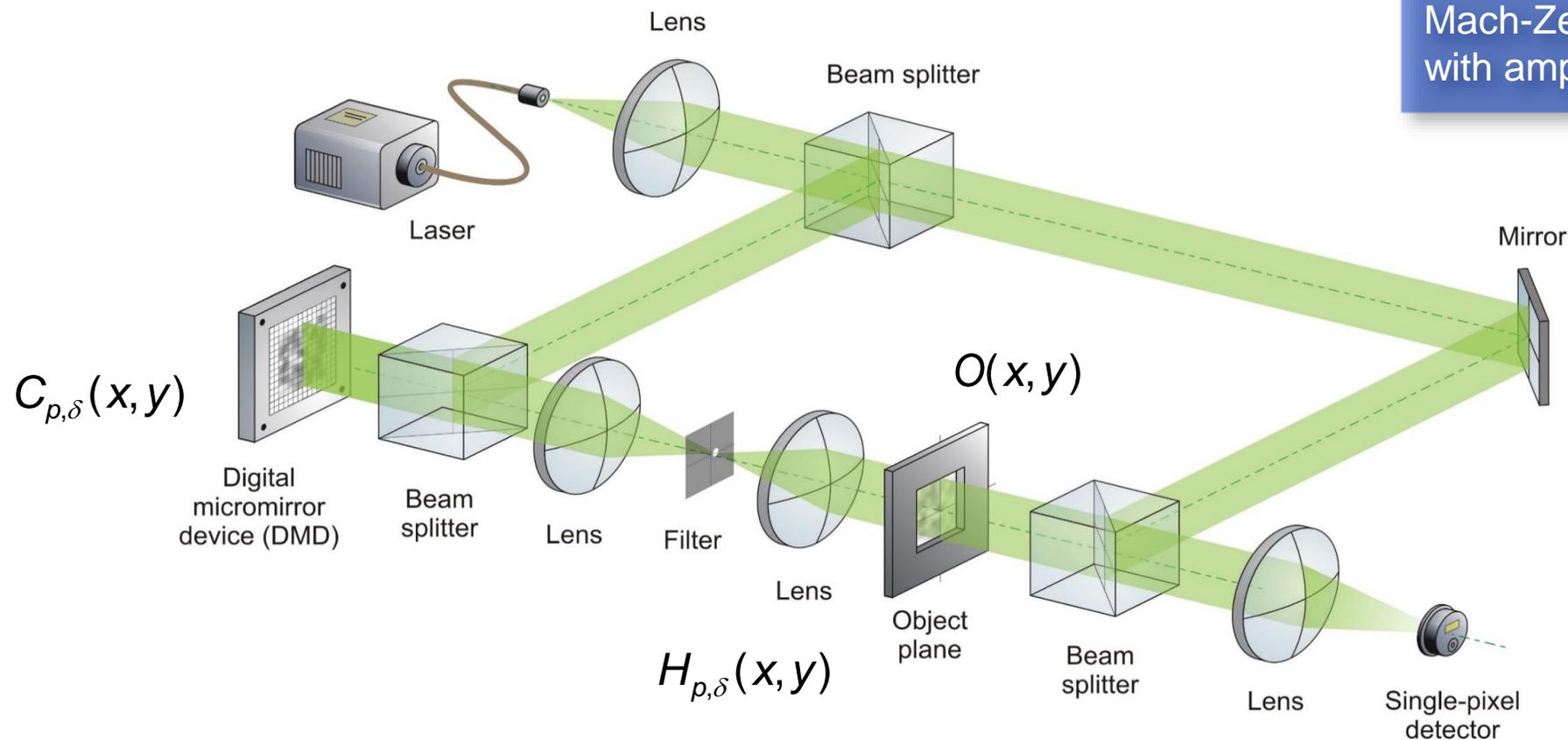


$$\left\{ \begin{array}{l} I_{p,0} \\ I_{p,\pi/2} \\ I_{p,\pi} \end{array} \right.$$

$$y_p = \frac{1}{4} [I_{p,0} - I_{p,\pi}] + \frac{j}{4} [2I_{p,\pi/2} - I_{p,0} - I_{p,\pi}]$$

# Single-pixel holographic camera with DMD

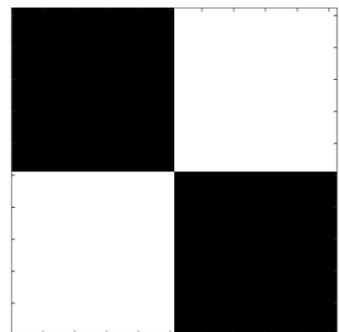
Mach-Zehnder interferometer with amplitude-only SLM



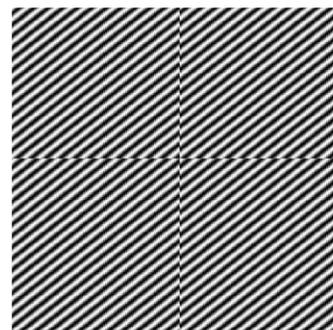
$$O(x,y) = \frac{1}{N} \sum_{p=1}^M y_p \cdot H_p(x,y)$$



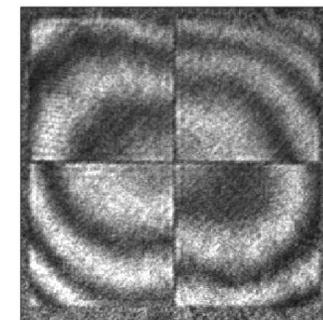
$$y_p = \frac{1}{4} [I_{p,0} - I_{p,\pi}] + \frac{j}{4} [2I_{p,\pi/2} - I_{p,0} - I_{p,\pi}]$$



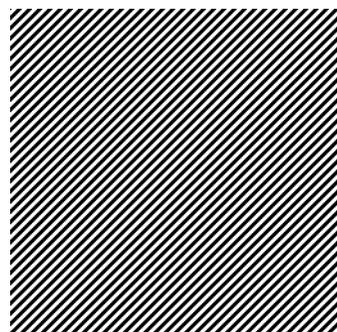
Hadamard pattern  
to be codified



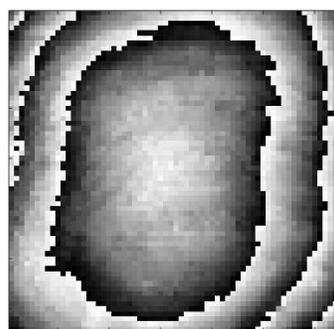
Hadamard pattern  
CGH



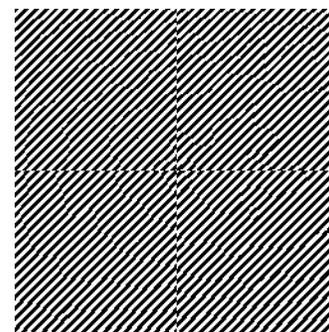
Interference pattern  
(at the object plane)



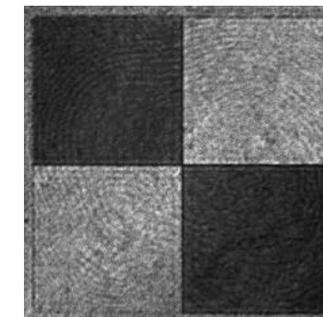
Plane wave  
CGH



Phase aberration

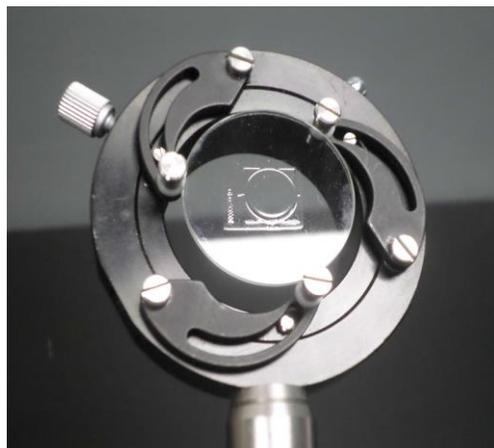


Corrected  
Hadamard pattern  
CGH

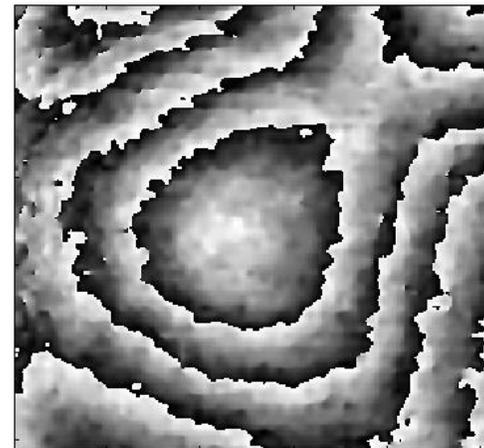


Interference pattern  
corrected

Image of a photoresist layer simulating an aberration



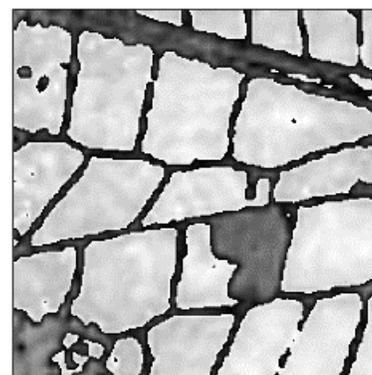
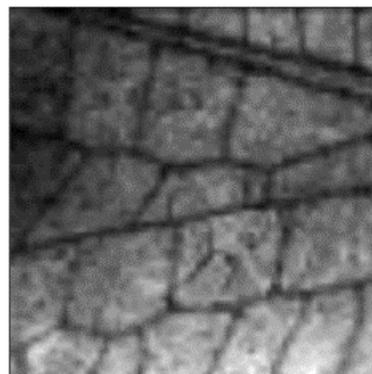
Phase object



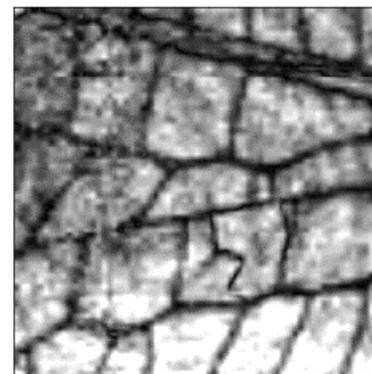
Phase image



Object



Conventional  
holography



Single-pixel  
holography

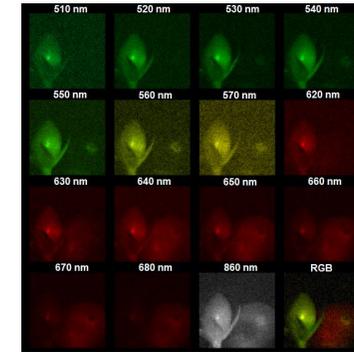


We have described **computational imaging techniques based on single-pixel detection** with microstructured illumination and compressive sensing.

We have shown several applications on **complex (amplitude and phase) imaging**.

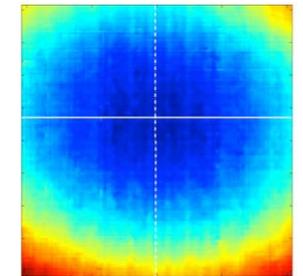
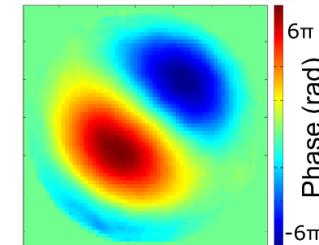
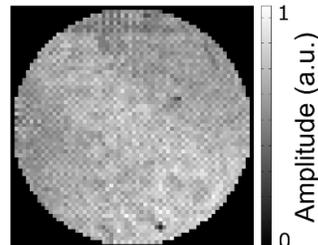
## Advantages:

- Simplicity of the sensor
- Efficient light sensors
- Broad spectral range
- Measure multiple optical parameters



## Challenge:

- Faster sampling methods
- Smart reconstruction algorithms



# Acknowledgements

## Research group

Jesús Lancis , Pedro Andrés, Vicent Climent, Enrique Tajahuerce, Gladys Mínguez-Vega, Lluís Martínez-León, Omel Mendoza, Pere Clemente, Dani Torrent, Vicente Durán, Armin Lenz, Marc Martí, Erick Ipus, Luis Ordóñez, Sergio Fernández, Francis Rey

Jesús Lancis



Lluís Martínez



Pere Clemente



<https://www.init.uji.es>

 @photonicsuji

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