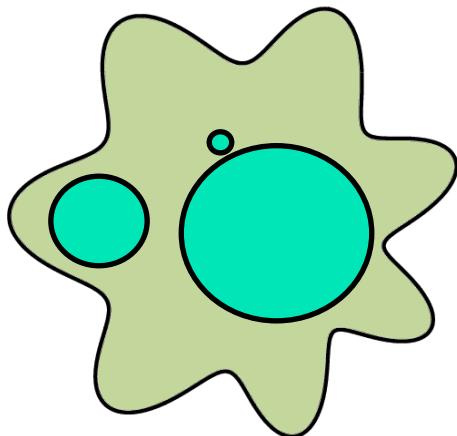
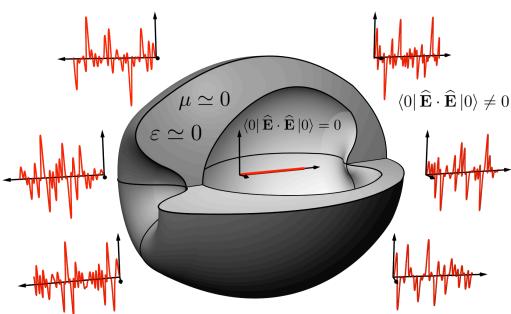
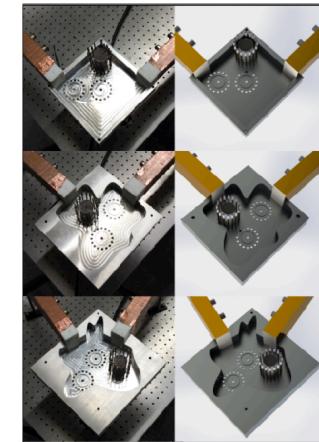
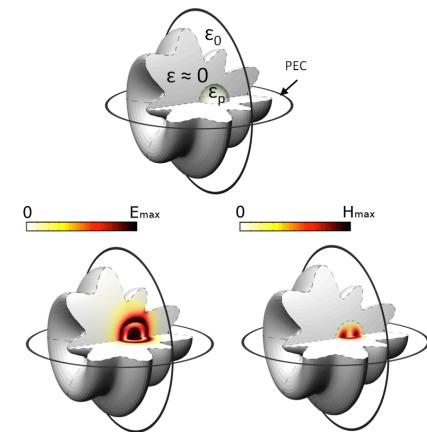
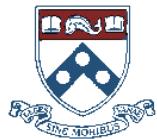


# *Extreme Platforms for Extreme Photonics*



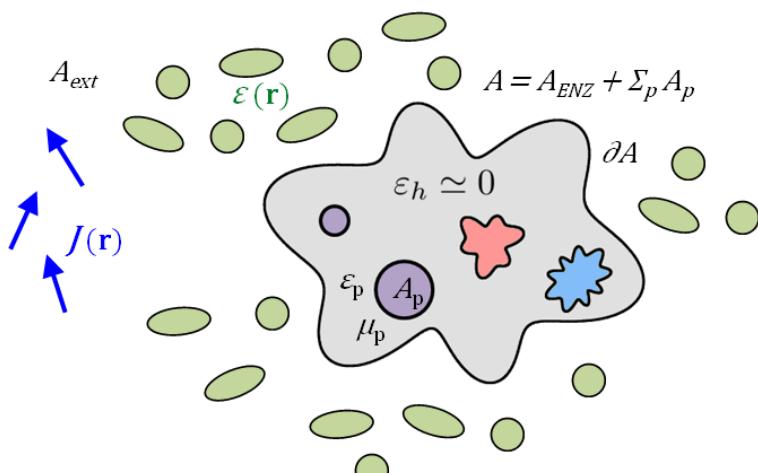
Nader Engheta  
With special thanks to  
*Brian Edwards*  
*Inigo Liberal*  
*Nasim Mohammadi Estakhri*  
*Ahmed Mahmoud*  
*Yue Li*  
*Yaakov Lumer*



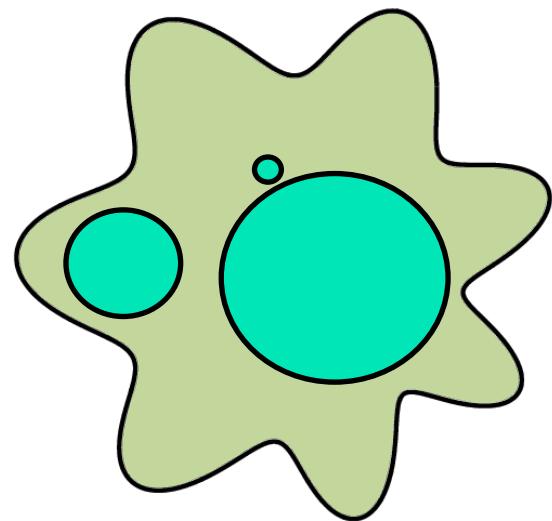


# Extreme Photonics - 1

## Photonic Doping



## Peculiar Effective Medium Properties



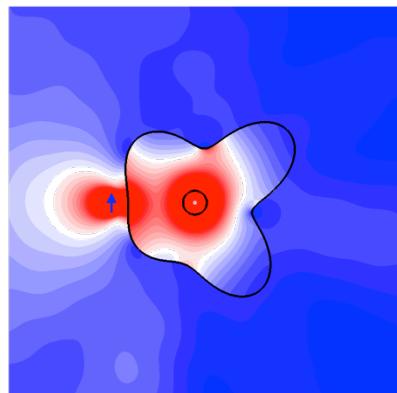
Liberal, Mahmoud, Li, Edwards, *Engheta, Science, 2017*



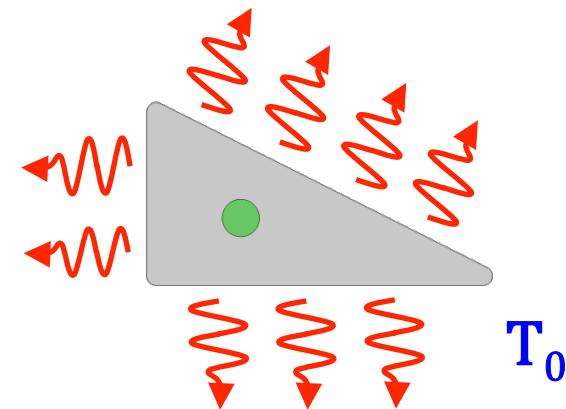
# Extreme Photonics - 2

## Thermal Engineering with Zero-Index Media

*Photonic Doping*



*Engineering Thermal Emission*



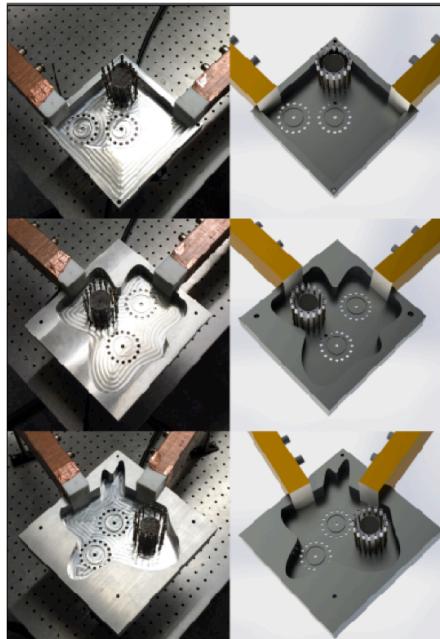
*Liberal & Engheta, CLEO Conference, May 15, 2017*



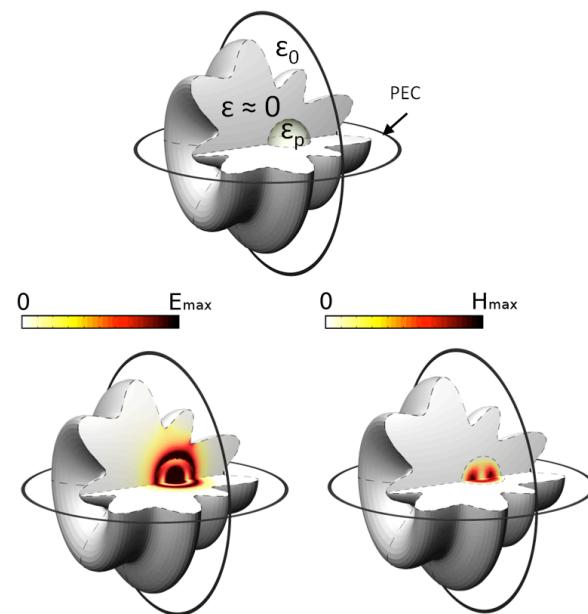
# Extreme Photonics - 3

## Extreme Resonant Cavities

*Geometry-Independent Cavities*



*Bound State in the Continuum*



*Liberal and Engheta, Nature Photonics, March 2017*

*Liberal, Mahmoud, Li, Edwards, Engheta, Science, 2017*

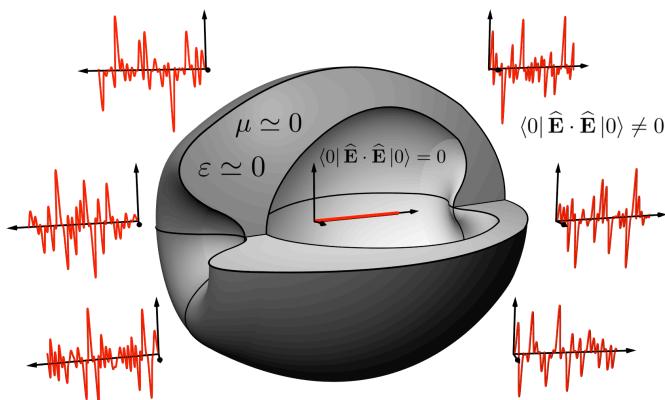
*Mahmoud, Liberal and Engheta, Nature Communications, 2016*



# Extreme Photonics - 4

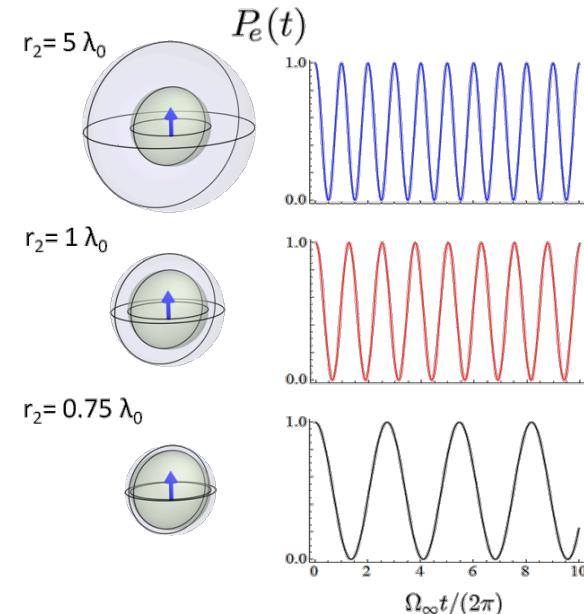
## Quantum Optics of ZIM

*Extreme Quantum Optics*



*Liberal and Engheta, PNAS, 2017*

*Engineering Rabii Frequencies  
without detuning*



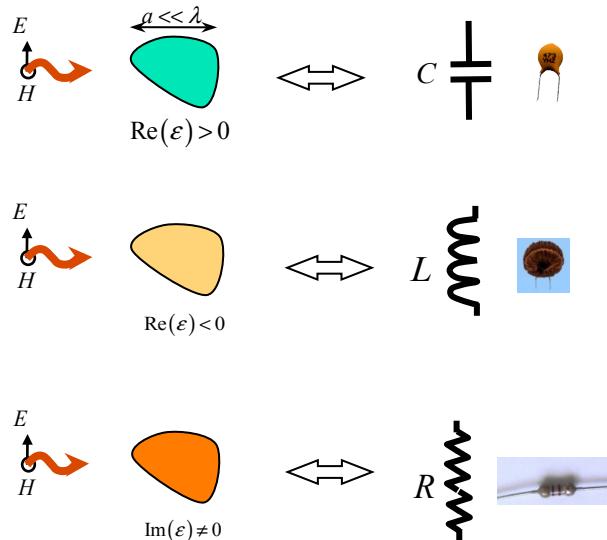
*Liberal and Engheta, PNAS, 2017*



# Extreme Photonics - 5

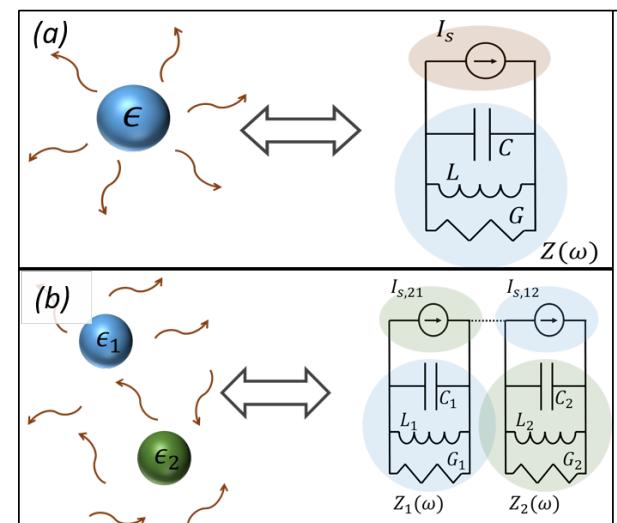
## Optical Metatronics

### Optical Metatronics



N. Engheta, et al. [PRL, 2005](#)  
 N. Engheta, [Science, 2007](#)

### Quantum Metatronics



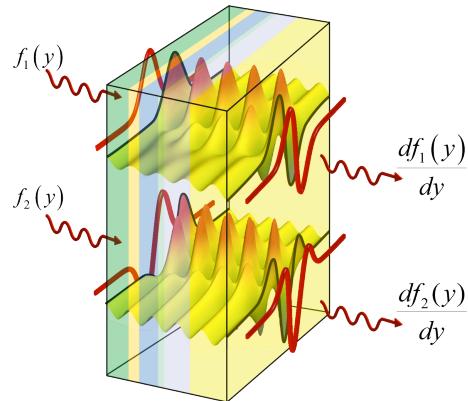
Lumer, Liberal and Engheta, [CLEO Conference, May 16, 2017](#)



# Extreme Photonics - 6

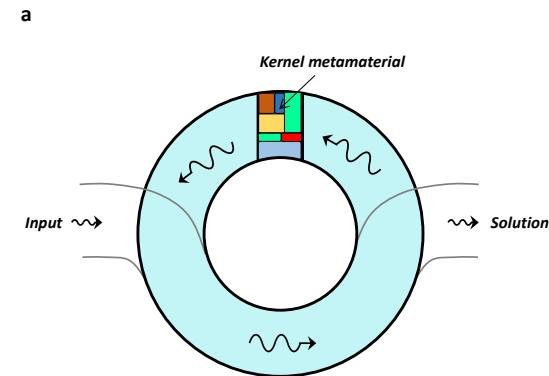
## Extreme Platforms for Mathematical Operations

### Informatic Metastructures



Silva, Monticone, Castaldi, Galdi, Alu, Engheta, Science, 2014

### Metastructures to Solve Equations with Waves



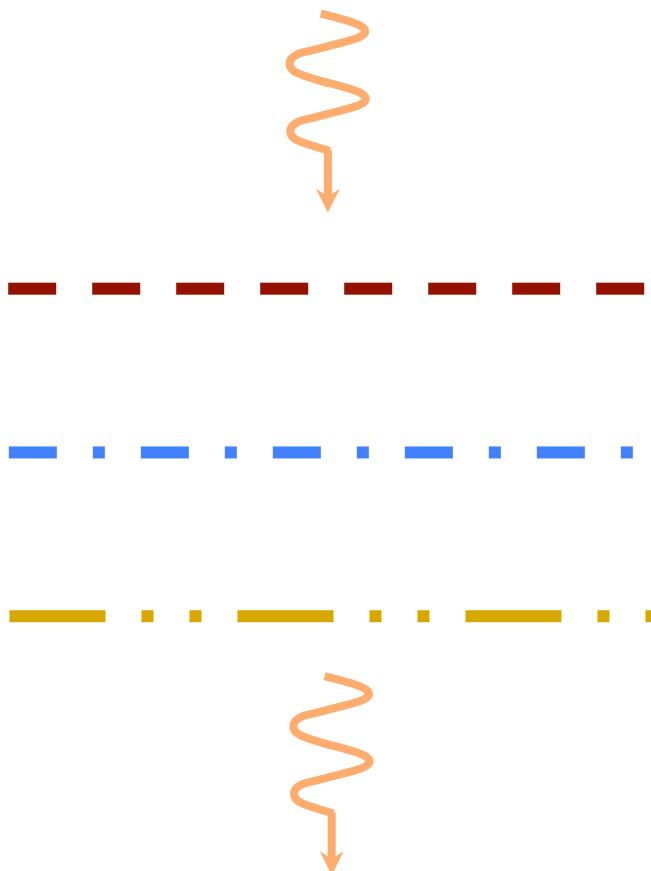
N. Mohammadi Estakhri, B. Edwards, N. Engheta  
CLEO Conference, May 18, 2017

B. Edwards, N. Mohammadi Estakhri, N. Engheta  
MRS Spring Meeting, April 11, 2017

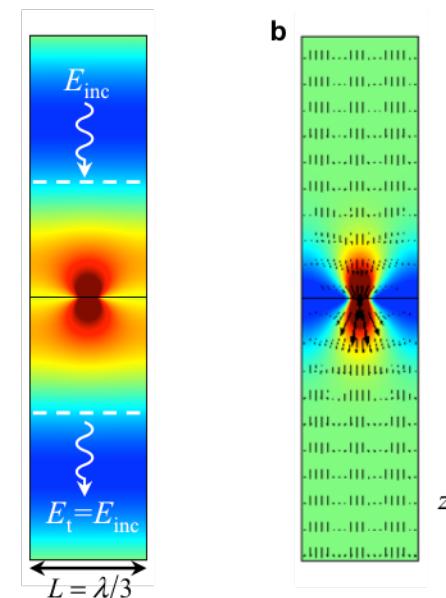


## Extreme Metasurfaces

### Cascaded Metasurfaces



### Transparent Metasurfaces with Prescribed Aperture Fields



Mohammadi Estakhri, Kastner, Engheta,  
IEEE AP-S Symposium, San Diego, July 2017

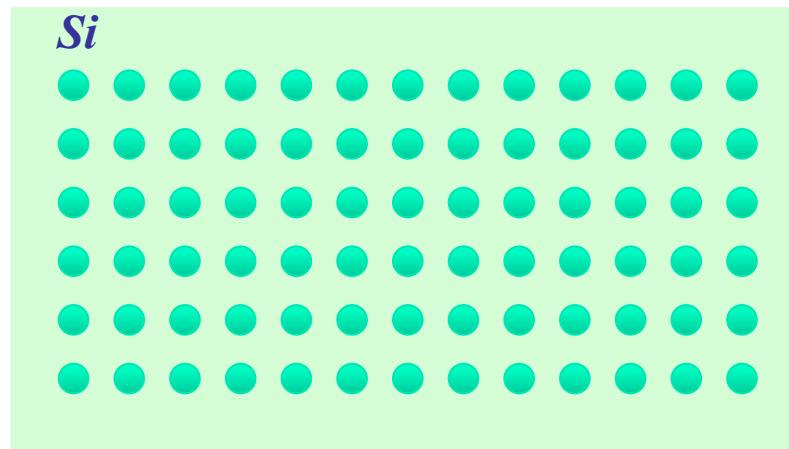


# *Photonic Doping*

*Liberal, Mahmoud, Li, Edwards, Engheta, Science, 355, 1058-1062, March 10, 2017*



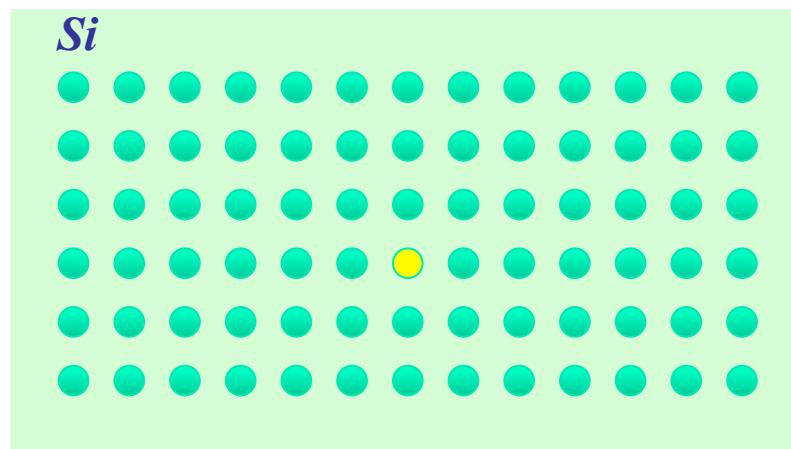
# *Background: Electronic Doping*



*Pure Intrinsic Semiconductor*



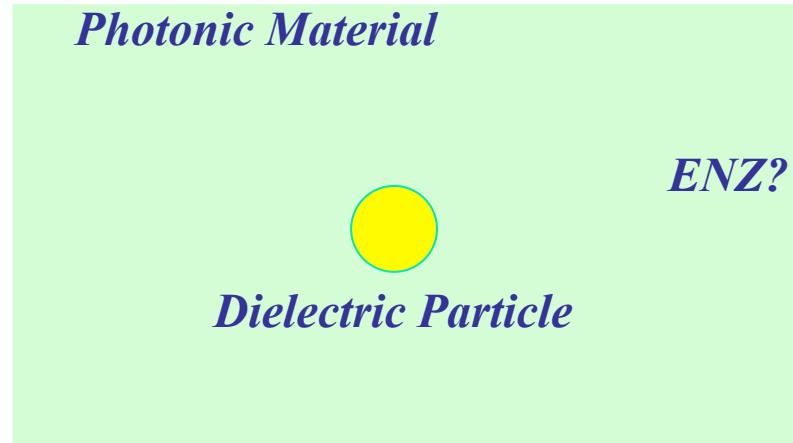
# *Background: Electronic Doping*



*Doped Semiconductor*



# *How about “photonic doping”?*

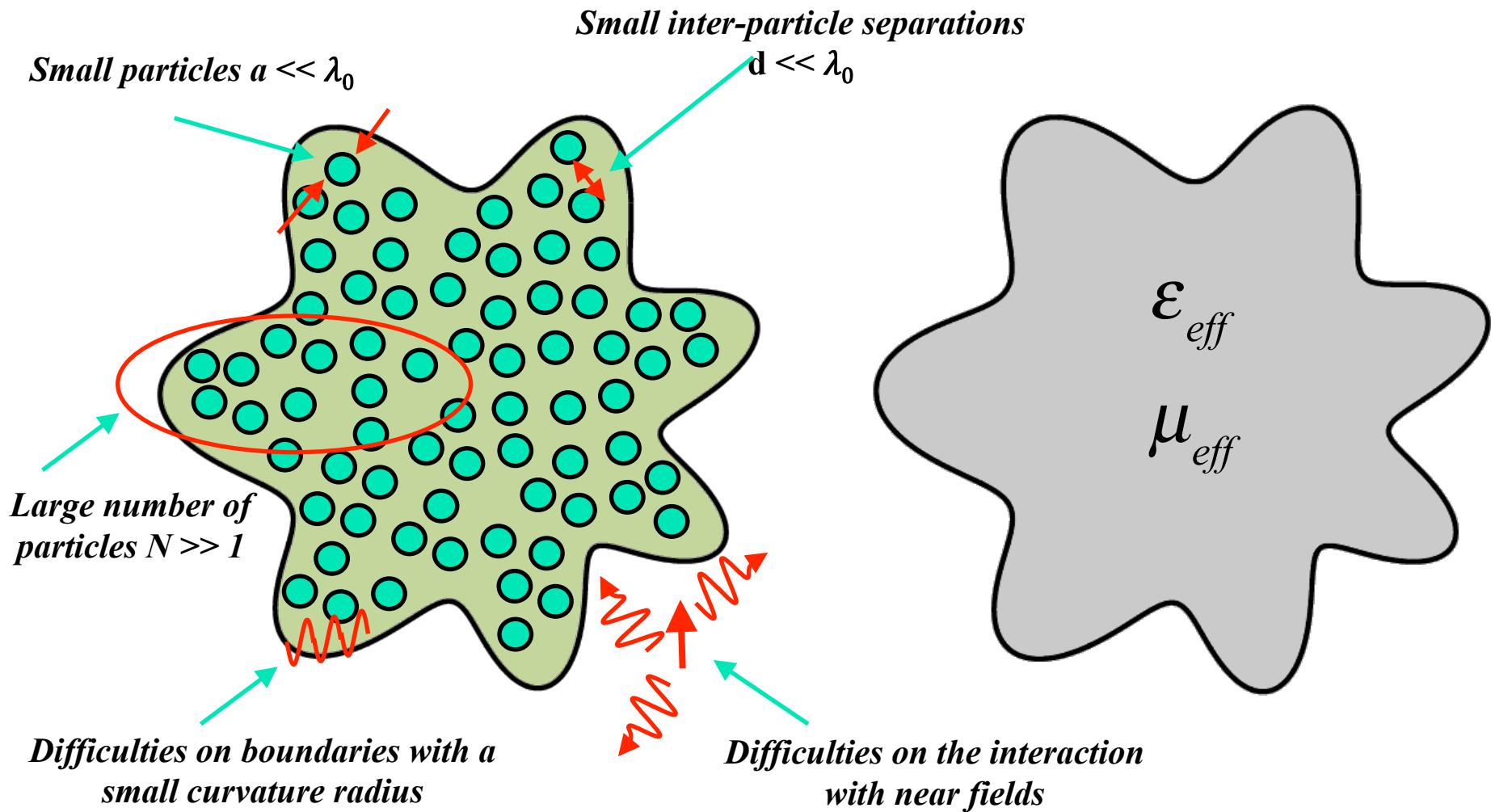


*“Pure” Photonic Material*

# Conventional Effective Medium Theory (EMT)



## 2D structure



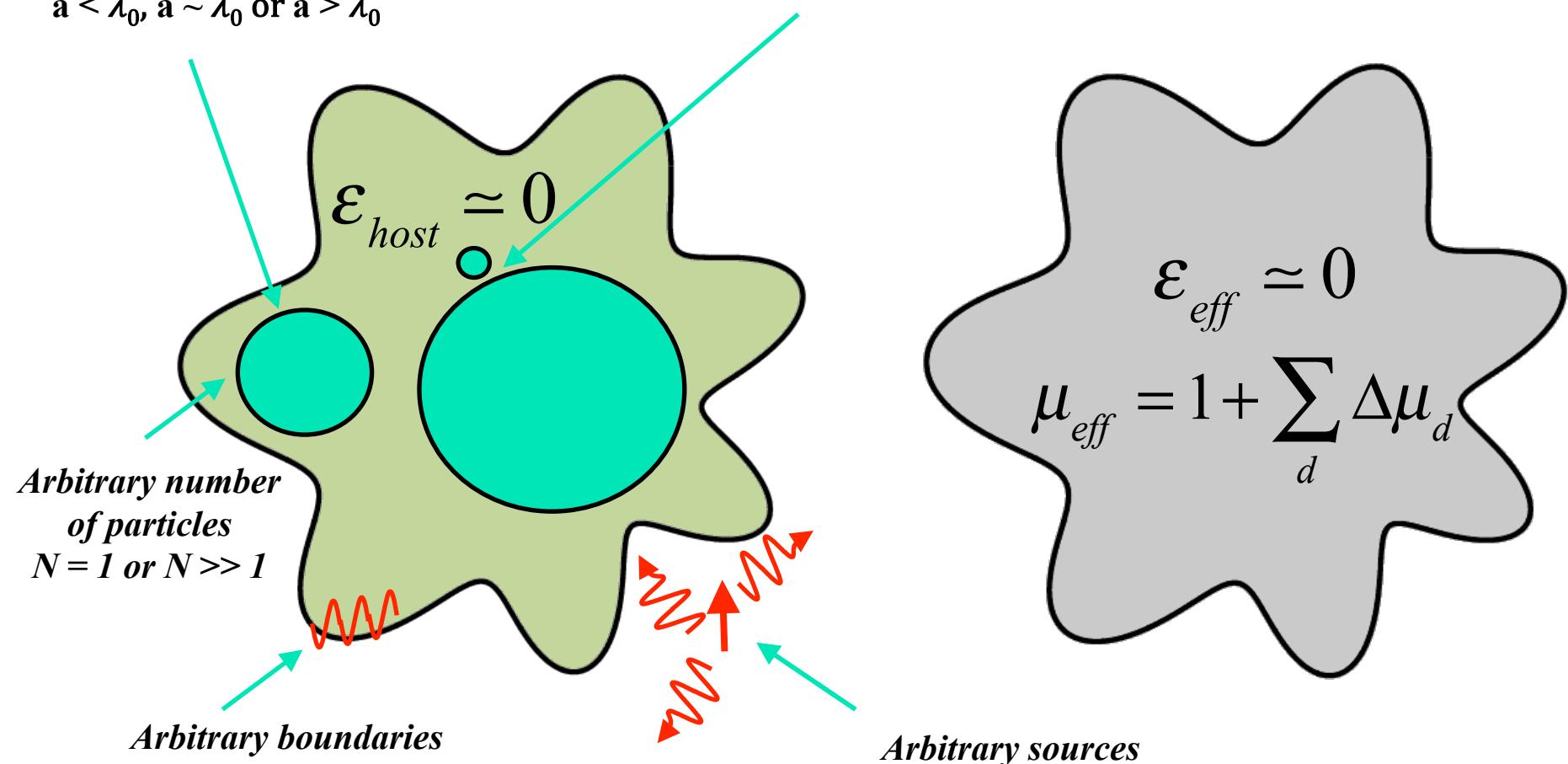


# What if the host is an ENZ medium?

Arbitrary particle size  
 $a < \lambda_0$ ,  $a \sim \lambda_0$  or  $a > \lambda_0$

Arbitrary inter-particle separation  
 $d < \lambda_0$ ,  $d \sim \lambda_0$  or  $d > \lambda_0$

2D structure



# Background on Epsilon-Near-Zero (ENZ)



PRL 97, 157403 (2006)

PHYSICAL REVIEW LETTERS

week ending  
13 OCTOBER 2006

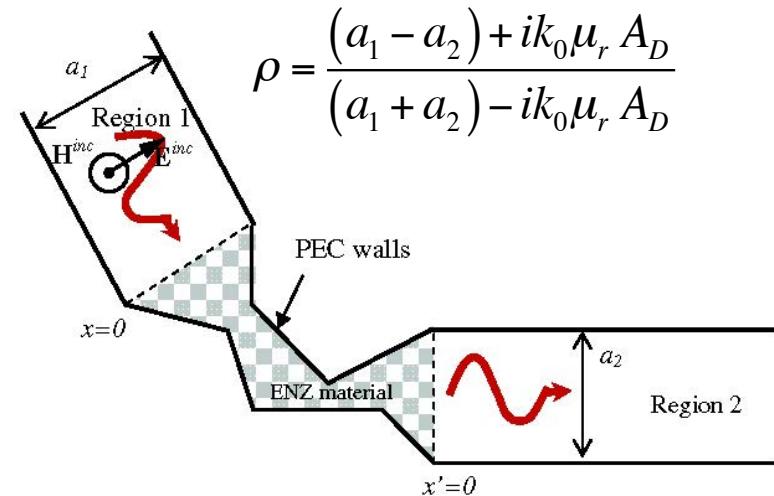
## Tunneling of Electromagnetic Energy through Subwavelength Channels and Bends using $\epsilon$ -Near-Zero Materials

Mário Silveirinha\* and Nader Engheta†

Department of Electrical and Systems Engineering, University of Pennsylvania, Philadelphia, Pennsylvania 19104, USA

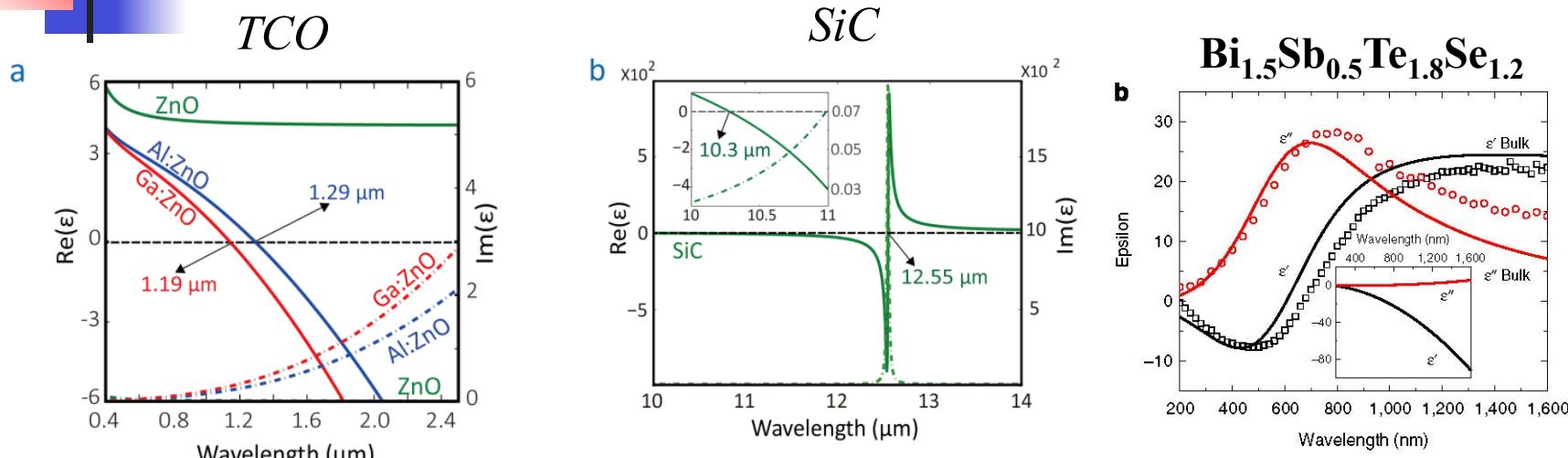
(Received 23 March 2006; published 10 October 2006)

$$\epsilon_{ch} = 0.001$$





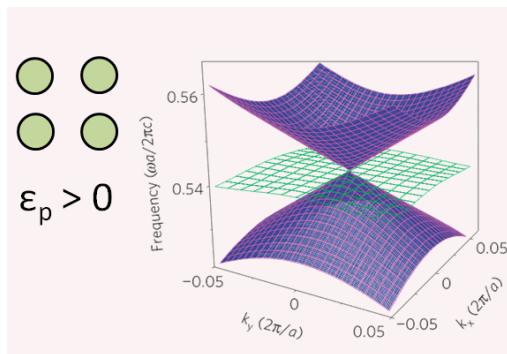
# Background: ENZ Structures



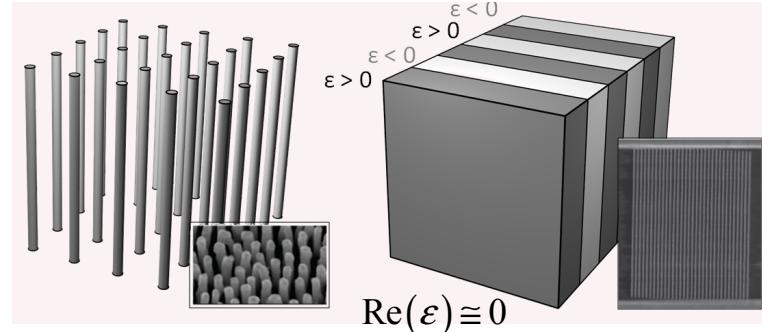
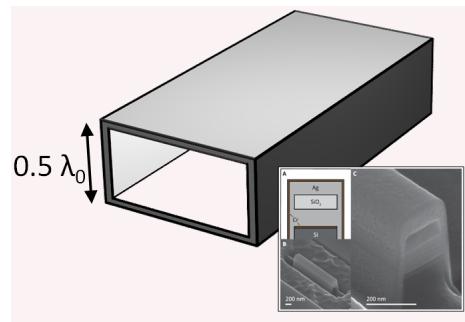
From: A. Boltasseva (Purdue)  
Kim, et al., Optica (2016)

From: J. Caldwell(NRL)  
Kim, et al., Optica (2016)

From: N. Zheludev(Southampton)  
Ou et al., Nat. Commun. (2014)



From: CT Chan's  
Huang, et al., Nat. Mater. (2011)



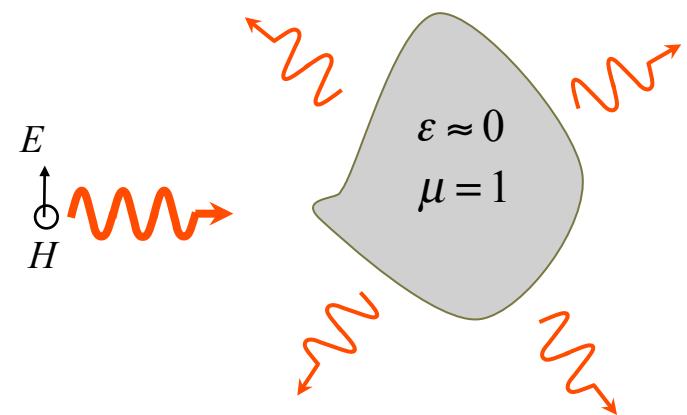


# Background: One of ENZ Properties

- **Maxwell Equations**  $\nabla \times \mathbf{H} = -i\omega\epsilon E \rightarrow \nabla \times \mathbf{H} = 0$
- **2-D Scenario with TM polarization**

$$\mathbf{H} = H(x, y) \hat{\mathbf{u}}_z$$

$$\mathbf{E} = \frac{1}{-i\omega\epsilon} \nabla H(x, y) \times \hat{\mathbf{u}}$$



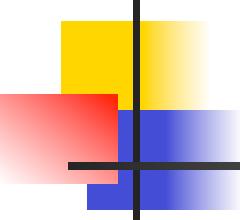
R. W. Ziolkowski, PRE, (2004)

N. Engheta, Science, 340, 286 (2013)

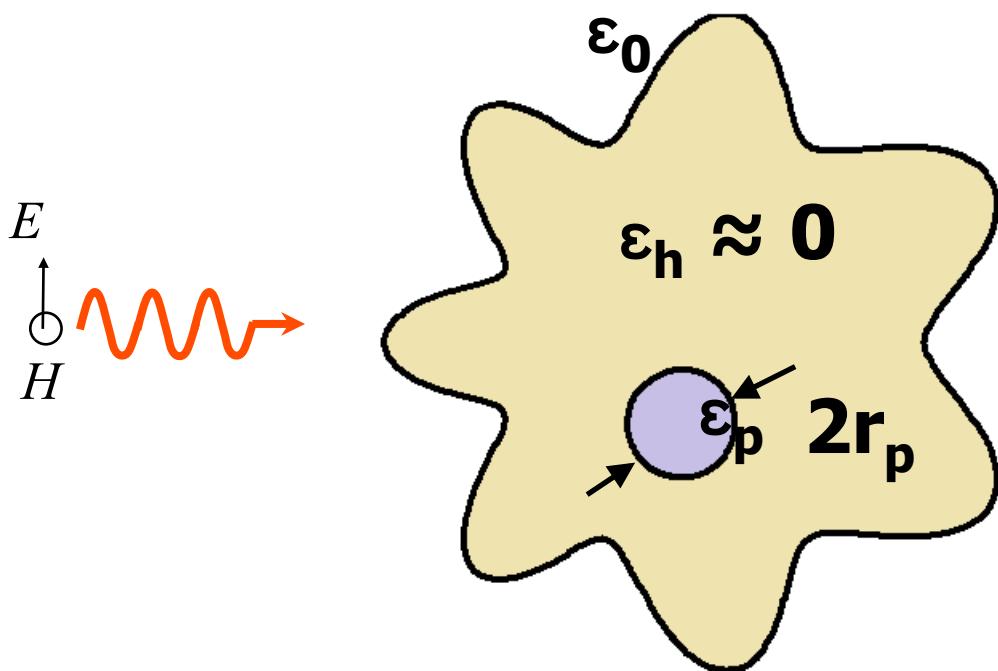
M. Silveirinha & N. Engheta, PRL, (2006)



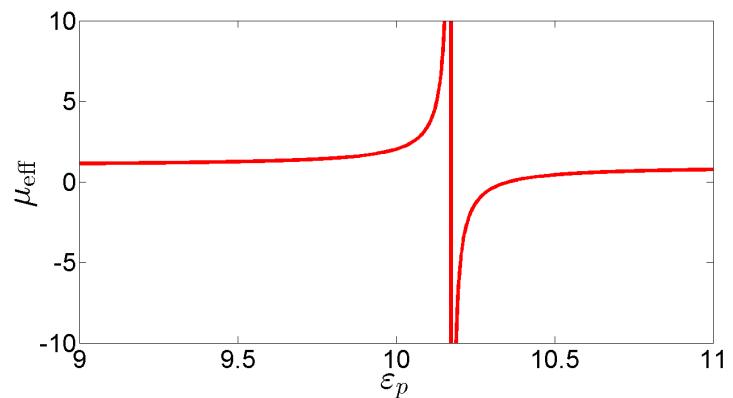
# Photonic “Doping”



$$\varepsilon_{\text{eff}} \simeq 0$$

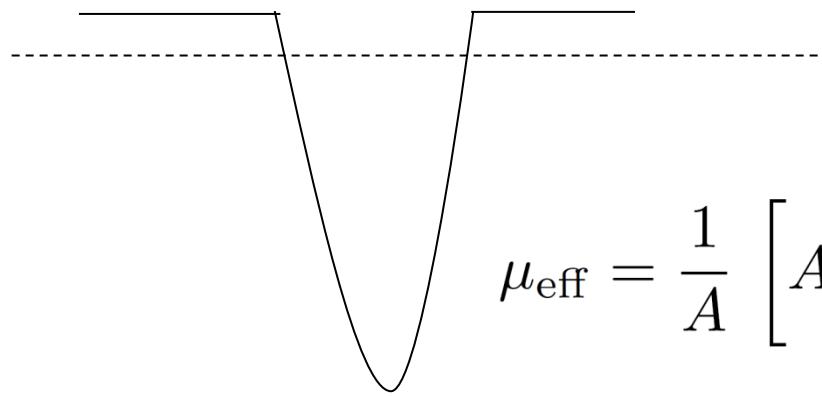
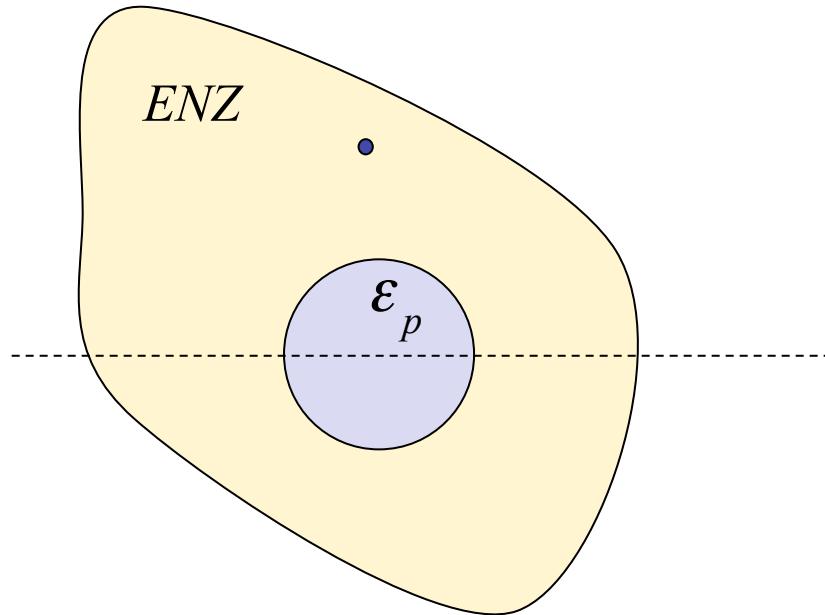
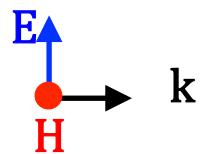


$$\mu_{\text{eff}} = \frac{1}{A} \left[ A_h + \frac{2\pi r_p}{k_p} \frac{J_1(k_p r_p)}{J_0(k_p r_p)} \right]$$



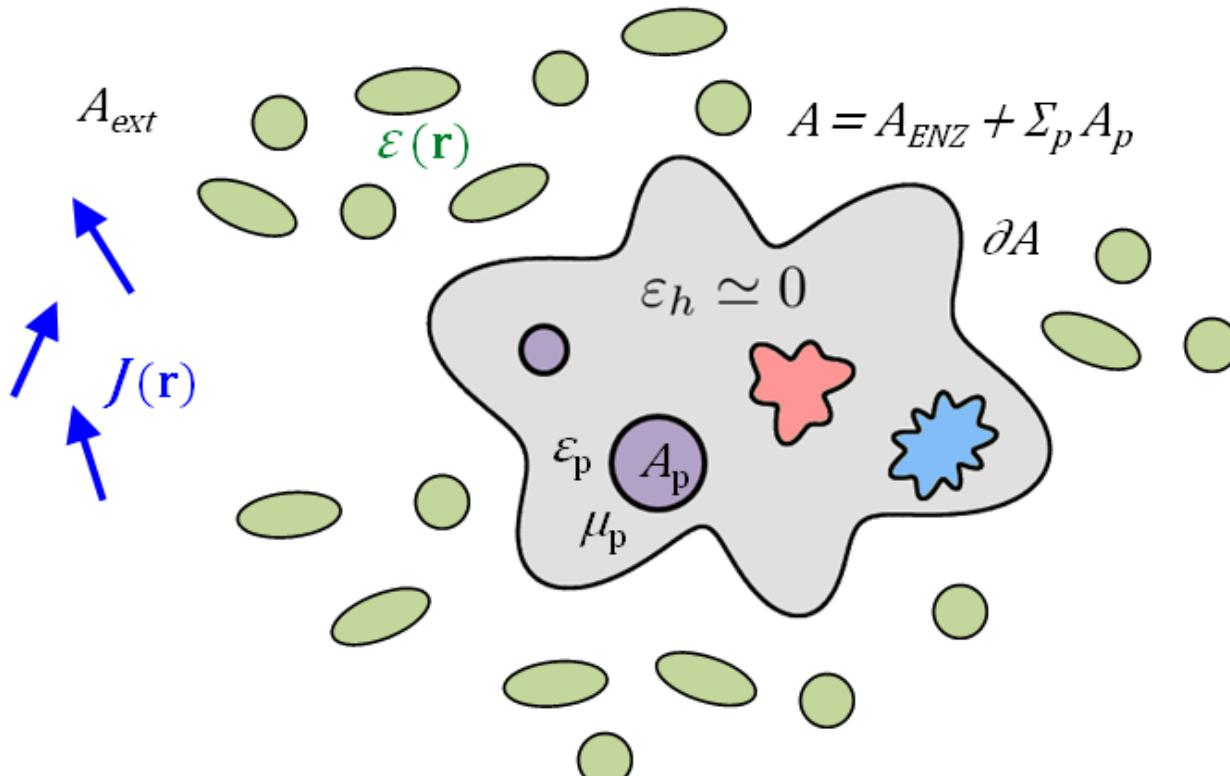


# Physical Explanation



$$\mu_{\text{eff}} = \frac{1}{A} \left[ A_h + \frac{2\pi r_p}{k_p} \frac{J_1(k_p r_p)}{J_0(k_p r_p)} \right]$$

# Photonic “Doping” 2D Generic Structures



$$\epsilon_{eff} \simeq 0$$

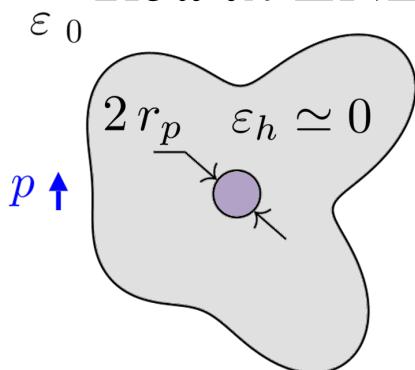
$$\mu_{eff} = 1 + \sum_d \Delta\mu_d$$

$$\Delta\mu_d = \frac{1}{A} \left[ \int_{A_d} \psi^d(r) dA - A_d \right]$$

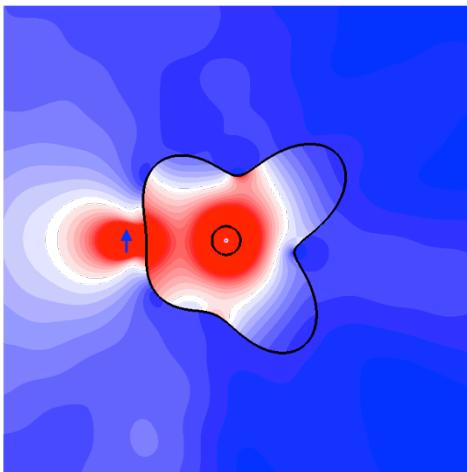


# Example 1: EMNZ $\mu_{eff} = 0$

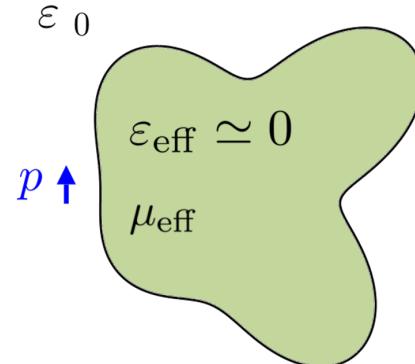
**Rod in ENZ**



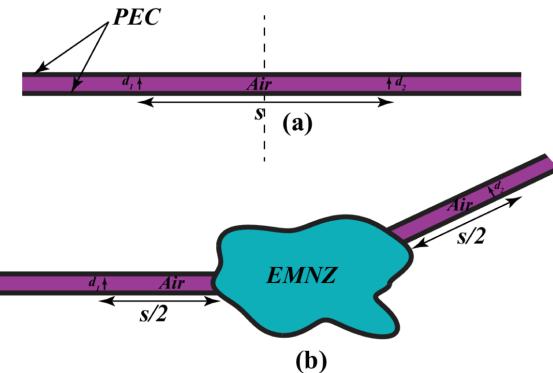
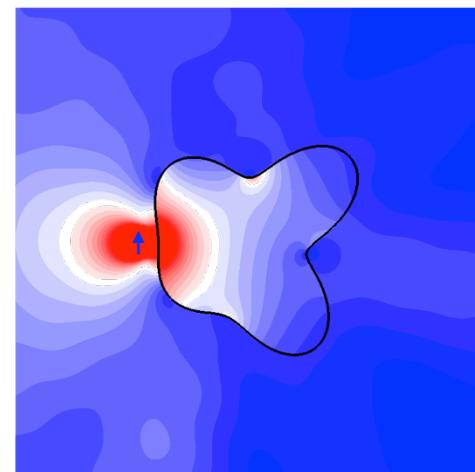
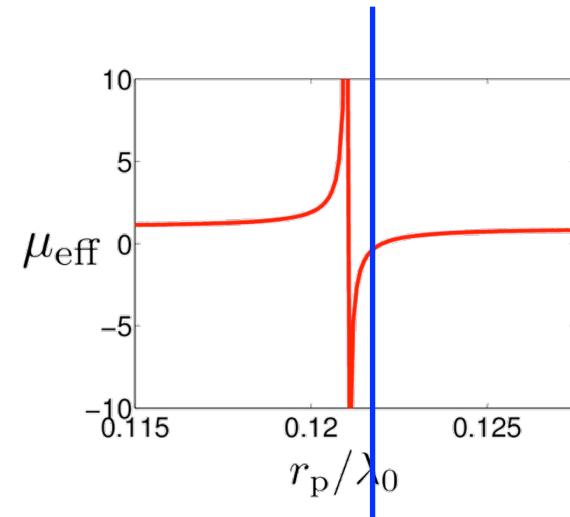
$$\epsilon_{eff} = 0 \quad \mu_{eff} = 0$$



**EMNZ Body**



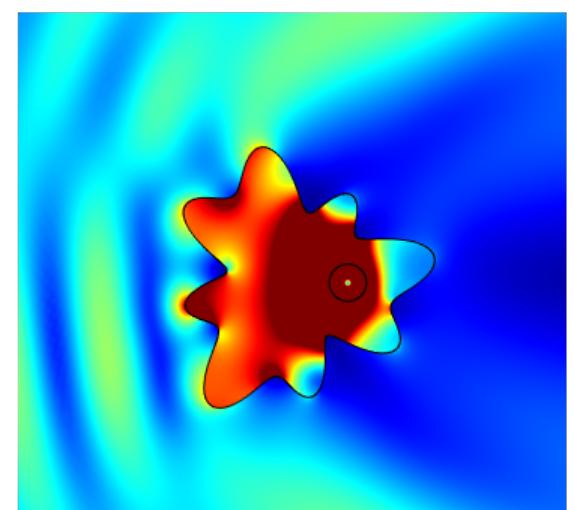
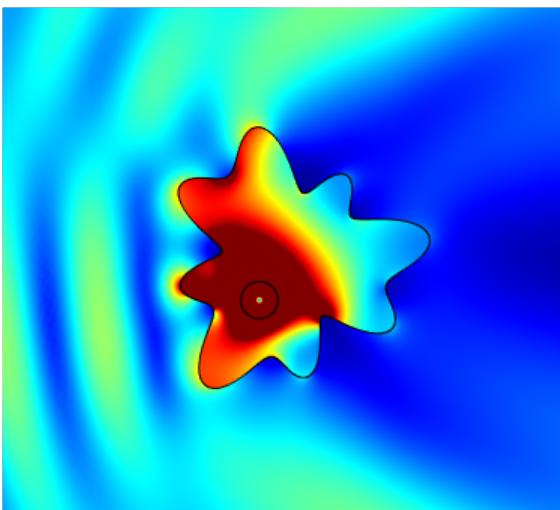
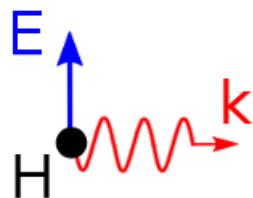
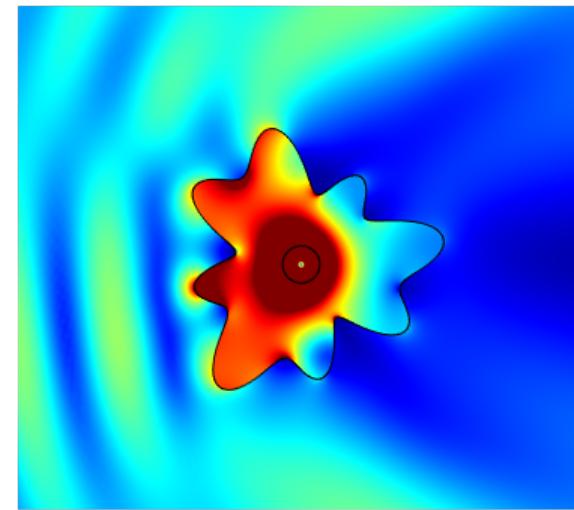
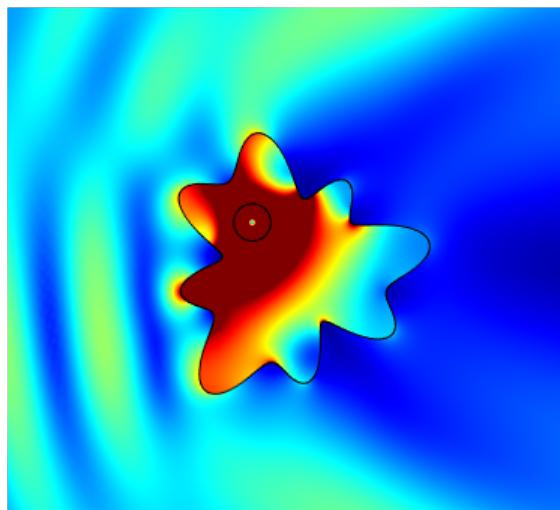
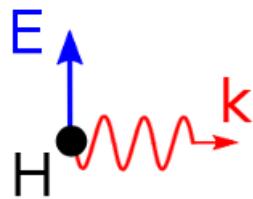
**EMNZ**



*Mahmoud, Liberal & Engheta  
Optical Materials Express, Feb 2017*



# Rod Position Independence

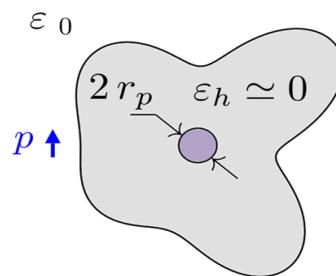


# Example 2: *PMC*      $\mu_{eff} = \infty$



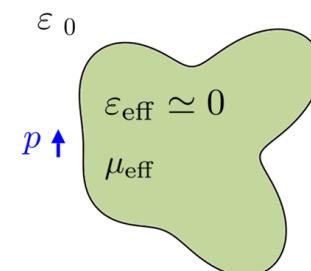
*Rod in ENZ*

**A**



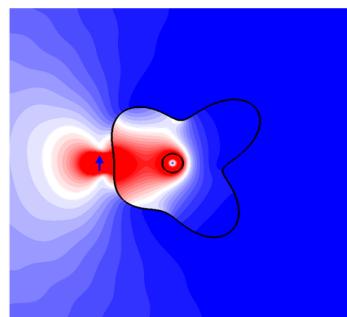
*PMC Body*

**B**

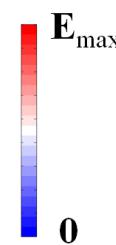
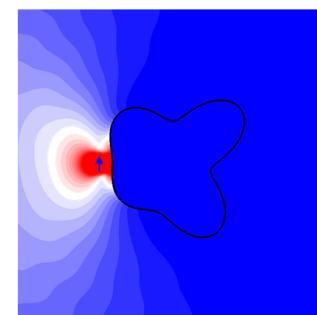


**C**

$$\epsilon_{eff} \approx 0 \quad \mu_{eff} \rightarrow \infty$$

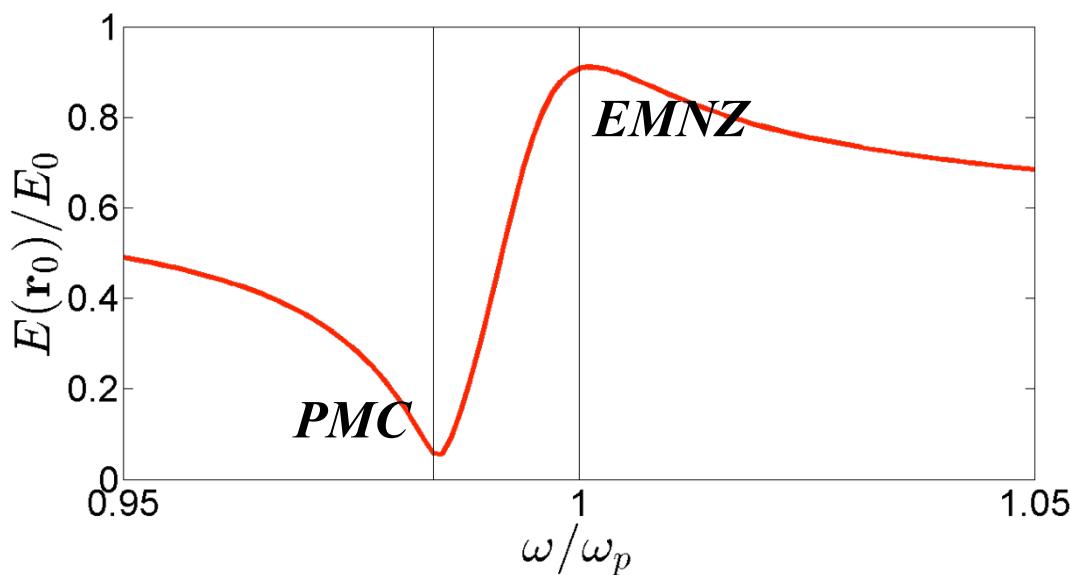
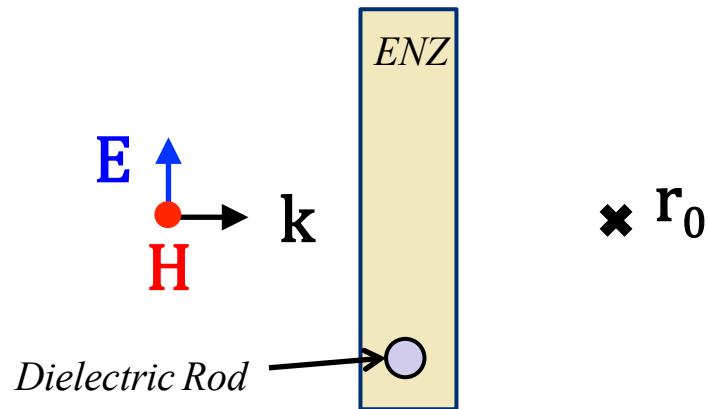


**PMC**



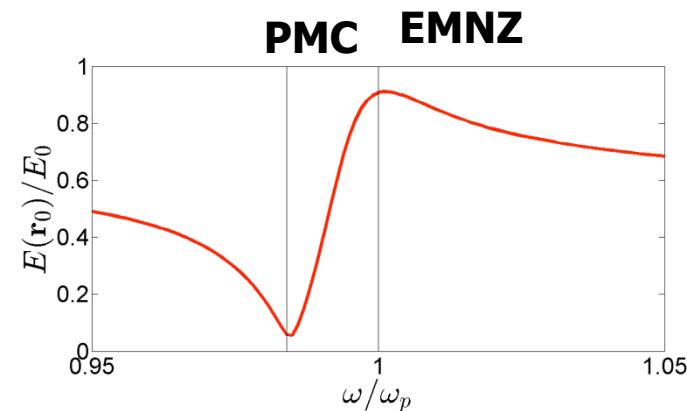
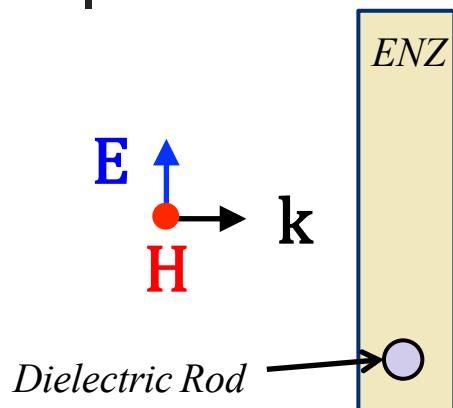


## Example 3: Single ENZ 2D slab

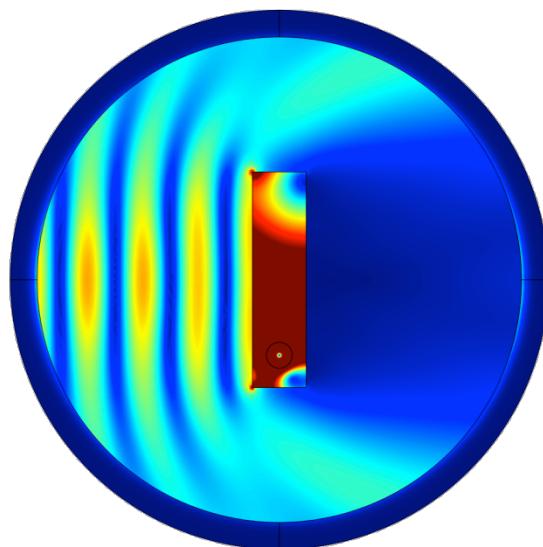




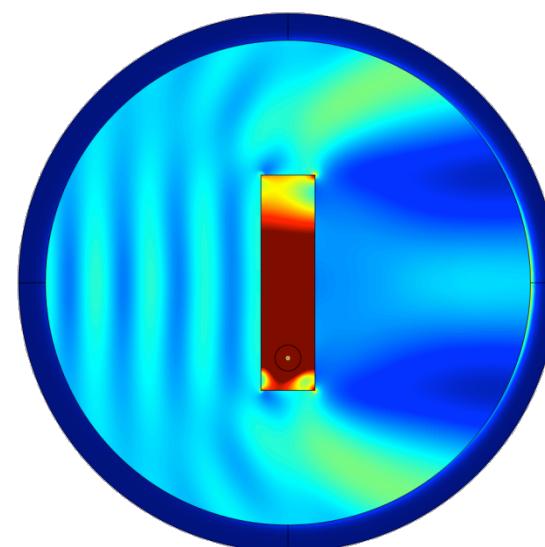
## Example 3: Single ENZ 2D slab



**PMC point ( $\omega = 0.985 \omega_p$ )**

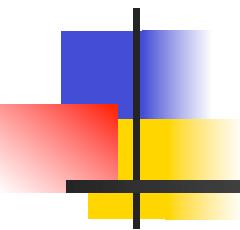


**EMNZ Point ( $\omega = \omega_p$ )**

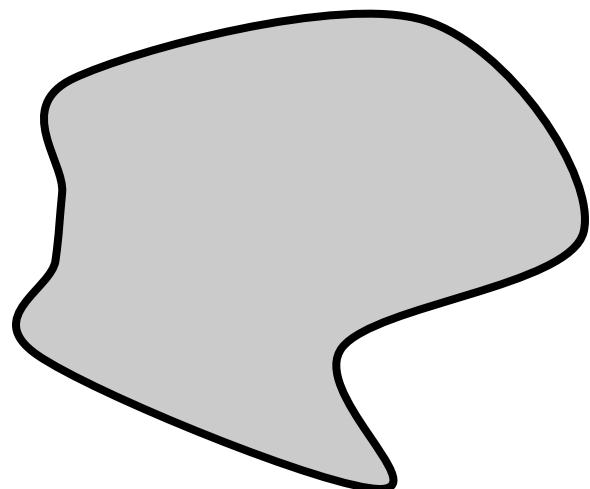
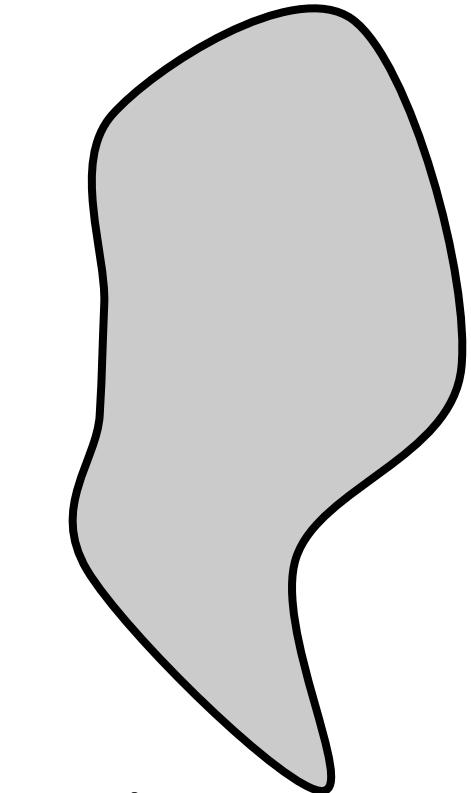




# *“Extreme” Cavity Resonators*



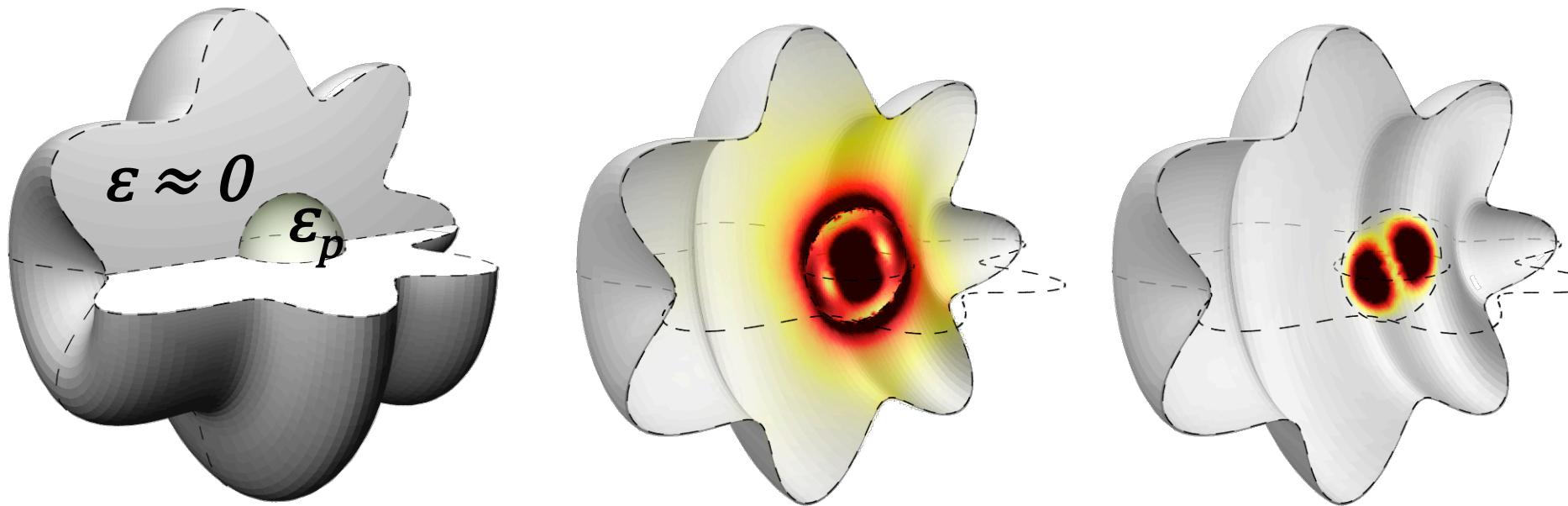
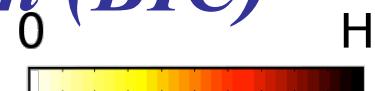
# *Conventional Cavity*

 $\omega_n$  $\omega'_n \neq \omega_n$

# “Ph-Doped” ENZ and “Open Cavity”



## Photonic Bound State in the Continuum (BIC)



I. Liberal and N. Engheta, *Science Advances*, 2016

I. Liberal and N. Engheta, *Optics and Photonics News (OPN)*, 2016

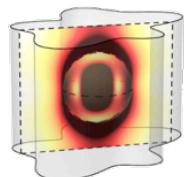
I. Liberal and N. Engheta, *Nature Photonics*, March 2017

Mahmoud, Liberal and Engheta, *Nature Communications*, 2016

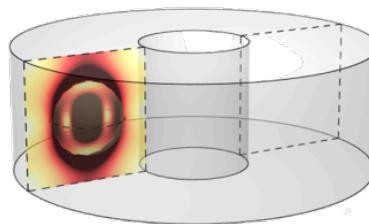
# Flexible “Open” Cavity: Photonic BIC



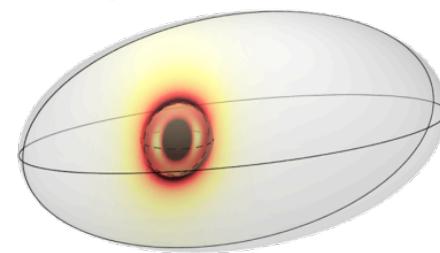
Cavity I



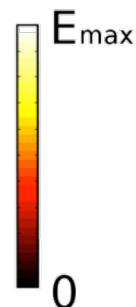
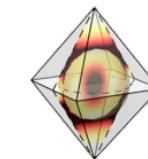
Cavity II



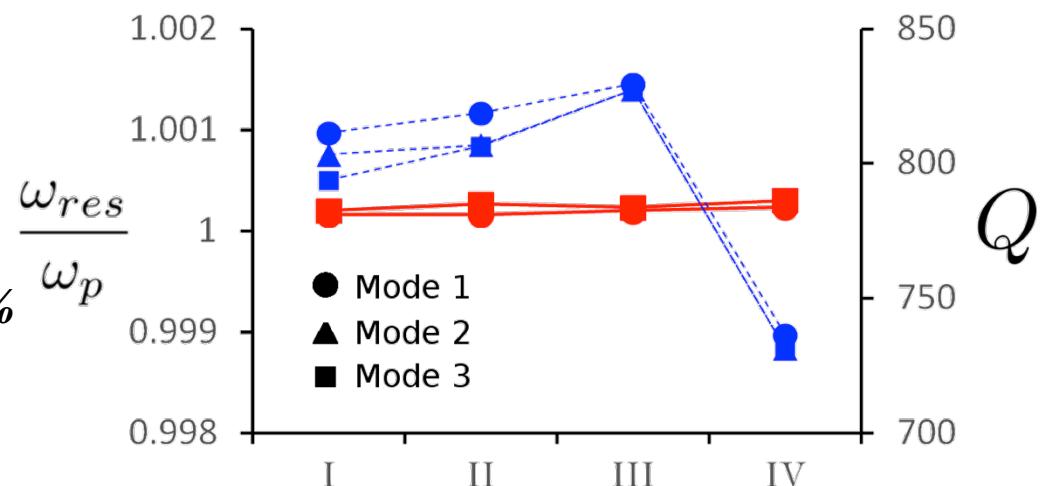
Cavity III



Cavity IV



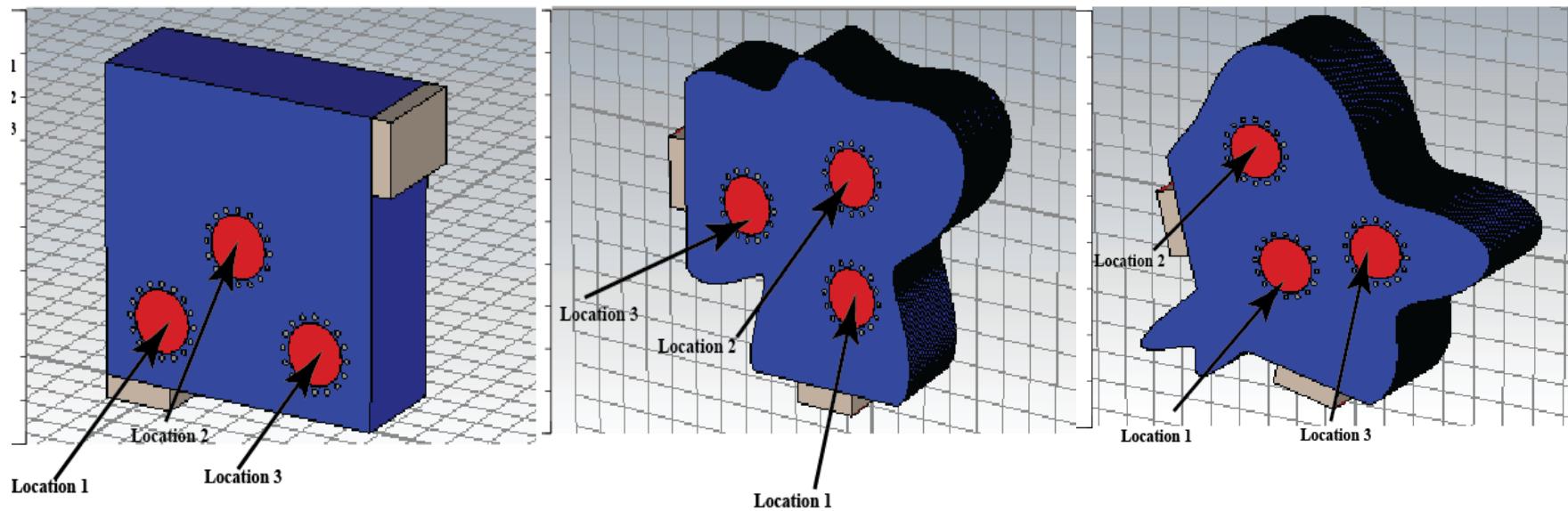
- Three degenerate eigenmodes (spherical defect)
- Eigenfrequency variation < 0.05% (induced by losses)  
 $\epsilon''(\omega_p) \approx 0.03$



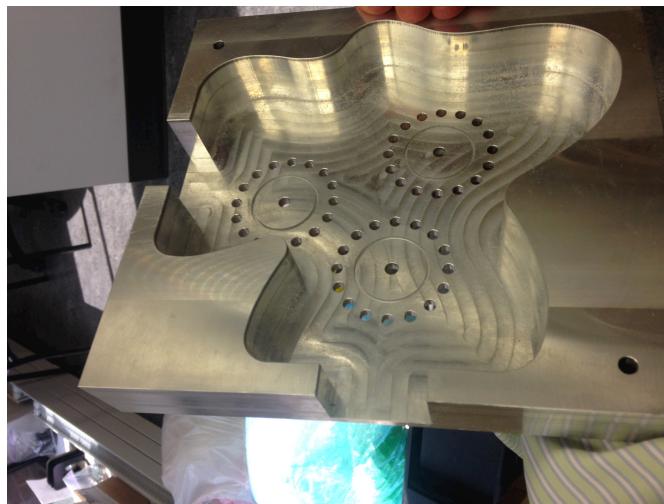
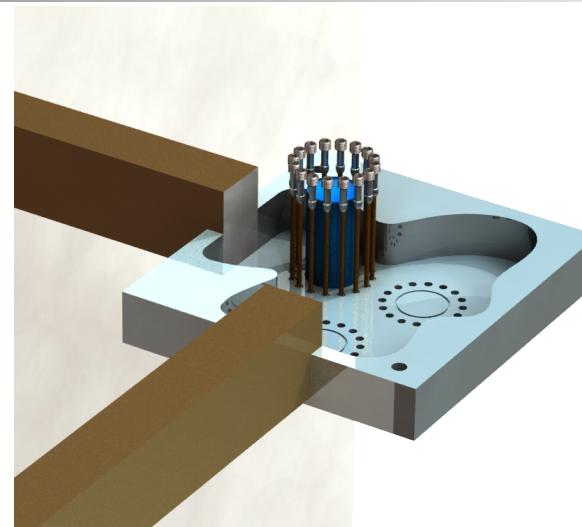
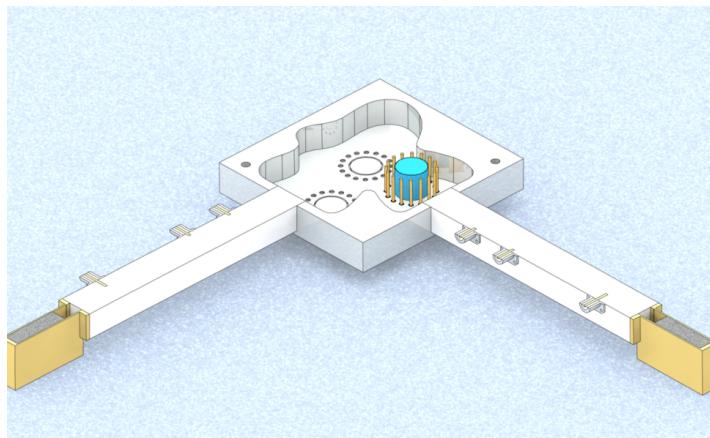
I. Liberal and N. Engheta, *Science Advances*, 2016

I. Liberal and N. Engheta, *Optics and Photonics News (OPN)*, 2016

# Experimental Verification of EMNZ Cavity

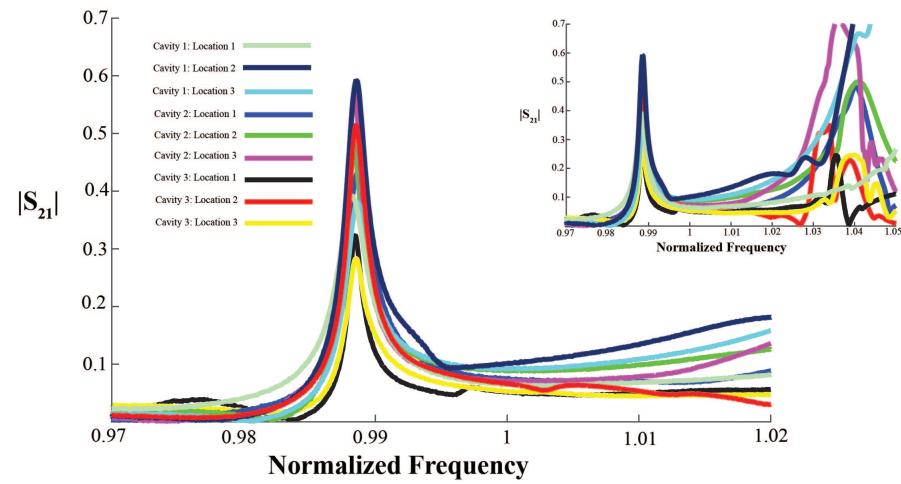
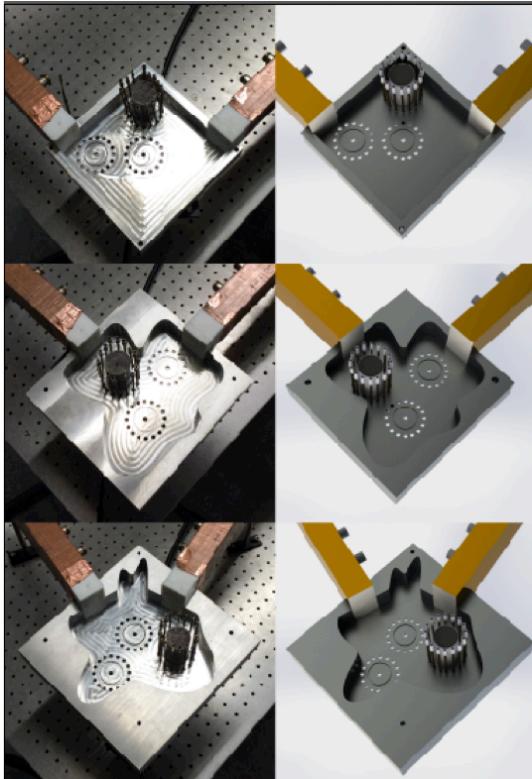


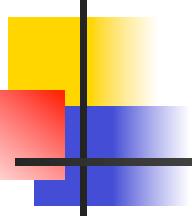
# *Experimental Verification of EMNZ Cavity*



*I. Liberal, Y. Li, A. Mahmoud, B. Edwards and N. Engheta, Science, March 10, 2017*

# *Experimental Verification of EMNZ Cavity*

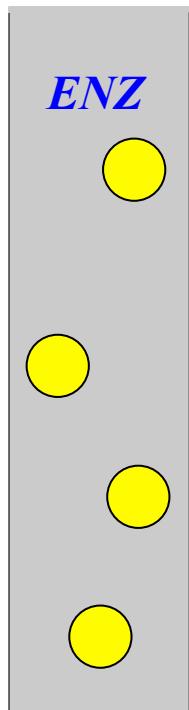




# *Several rods embedded in ENZ metasurface*



*Filling ENZ Metasurface with several rods*



$$\varepsilon_{\text{eff}} \simeq 0$$

$$\mu_{\text{eff}} = \frac{1}{A} \left[ A_h + \frac{2\pi r_p}{k_p} \frac{J_1(k_p r_p)}{J_0(k_p r_p)} \right]$$

$$\mu_{\text{eff}} = \frac{1}{A} \left[ A_{\text{ENZ}} + \sum \mu_d \int_{A_d} \psi_d(\mathbf{r}) dA \right]$$

$$\mu_{\text{eff}} = 1 + \sum \Delta \mu_d$$

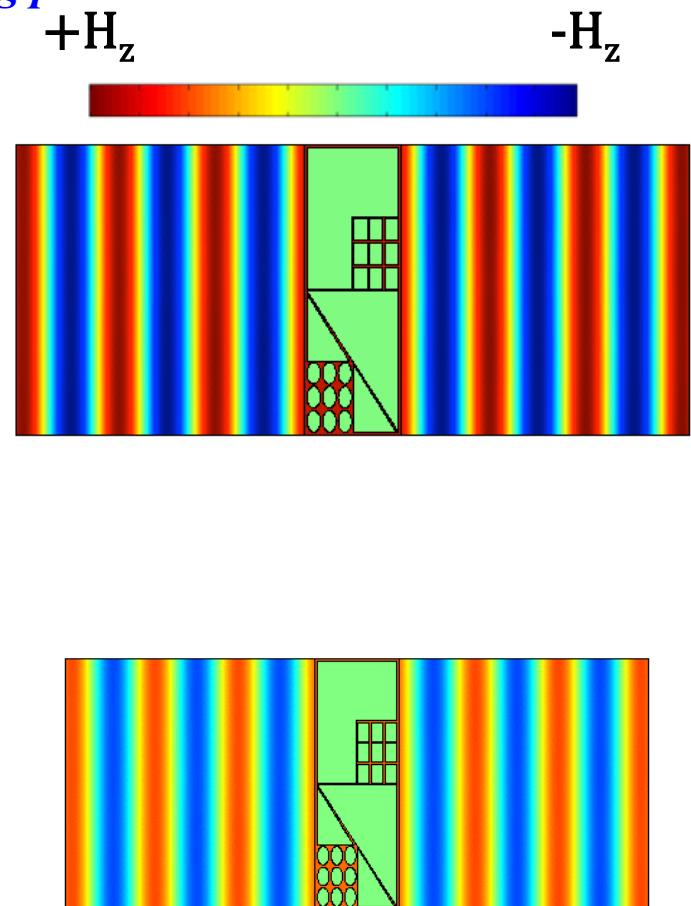
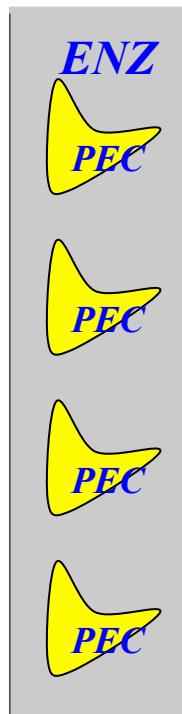


$$\Delta \mu_d = \frac{1}{A} \left[ \mu_d \int_{A_d} \psi_d(\mathbf{r}) dA - A_d \right]$$

# *ENZ-based Metasurface with PEC rods*



*Filling ENZ Metasurface with conducting parts*



$$\varepsilon_{\text{eff}} \simeq 0$$

$$\mu_{\text{eff}} \approx 1 - \frac{A_{\text{PEC}}}{A}$$

$$\mu_{\text{eff}} \rightarrow 0$$

# *ENZ Metasurface filled with Conductors*



*Filling ENZ Metasurface with conducting parts*

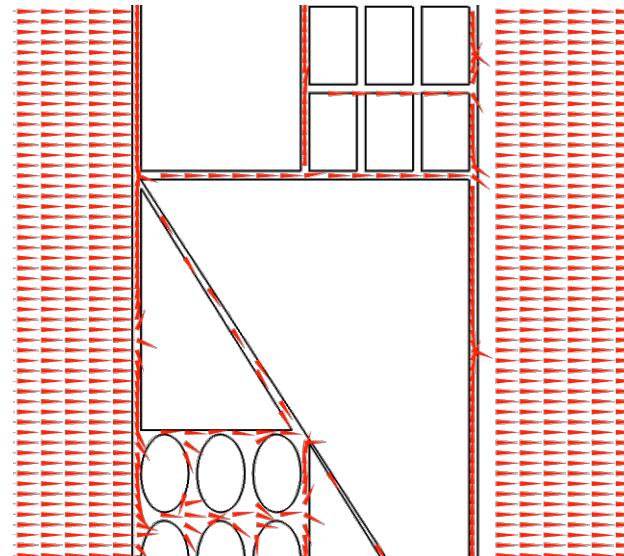
$$L_x = 1 \lambda_0$$

$$L_y = 3 \lambda_0$$

$$\mu_{\text{eff}} = 1 - \frac{A_{PEC}}{A}$$

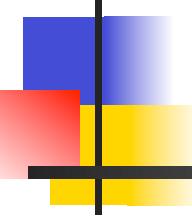
$$\varepsilon_{\text{eff}} \simeq 0$$

Poynting vector



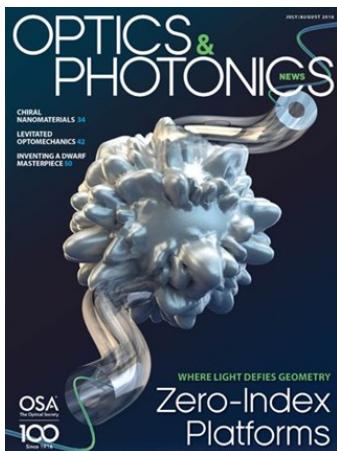


# Summary

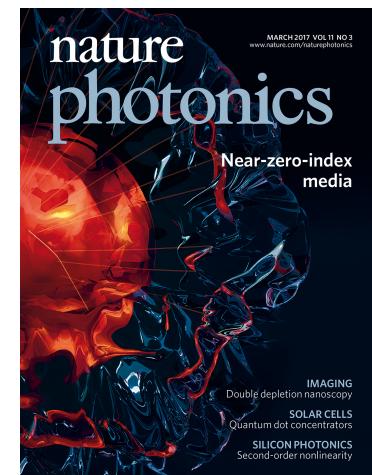
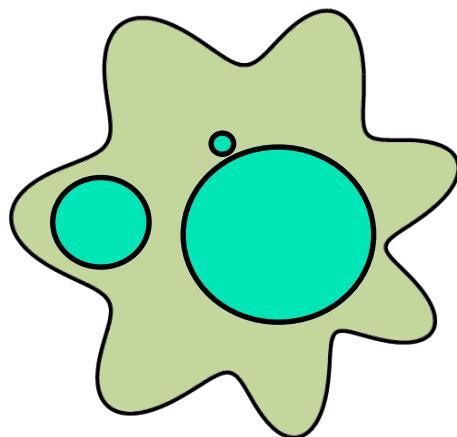


*Extreme platforms can play interesting roles in light-matter interaction*

*Extreme photonics offers unique functionality*



*July/Aug 2016*



*March 2017*



*Thank you very much*

