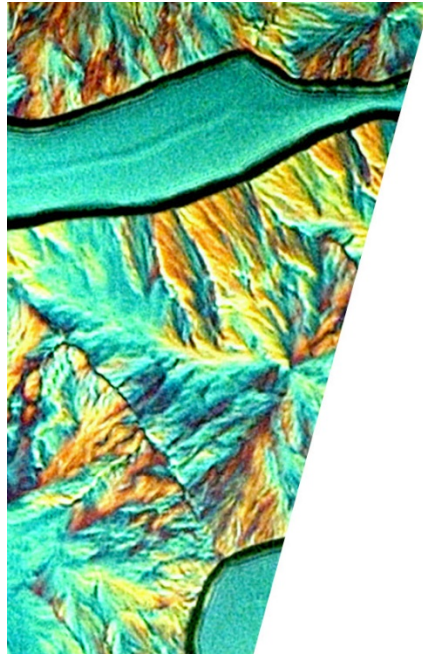


Surface Plasmon Resonance Sensors: Science and Technology

Presented by:



The OSA Optical Biosensors (BB) Technical Group Welcomes You!



SURFACE PLASMON RESONANCE SENSORS: SCIENCE & TECHNOLOGY

10 October 2018 • 10:30 EDT

OSA Optical
Biosensors
Technical Group

Technical Group Leadership



Chair
Filiz Yesilkoy
EPFL, Switzerland



Vice Chair
Priyanka Dey
University of Exeter, UK



Events Leader
Sachin Kumar Srivastava
CSIR-CSIO, Chandigarh, India



Industrial Relations Leader
John Kohoutek
McKinsey



Publication Leader
Pilgyu Kang
George Mason University



Publication Leader
Ibrahim S. Abdulhalim
Ben Gurion University of the Negev

Technical Group at a Glance

- **Focus**

- This group's interests are related to optical technologies for the targeted detection of biological compounds for medical diagnostics, healthcare, environmental and food safety applications.
- Over 2,000 members within OSA.

- **Mission**

- Promotion of the developments in the field to the society through webinars, social media, publications, technical and outreach events...
- Create a platform to enhance the community network.
- Interested in presenting your research? Have ideas for TG events? Contact: filizyesilkoy@gmail.com

- **Find us here**

- Website: www.osa.org/OpticalBiosensorsTG
- LinkedIn: <https://www.linkedin.com/groups/8260947/>
- Social Media: #OSABiosensorsTG

Today's Webinar



Surface Plasmon Resonance Sensors: Science & Technology

Prof. Ibrahim S. Abdulhalim

Head of Applied Nano-Photonics Group

Department of Electro-Optic Engineering

Ben Gurion University of the Negev, Israel

Surface Plasmon Resonance Sensors: Science and Technology

Prof. Ibrahim Abdulhalim

abdulhlm@bgu.ac.il

<http://aizena.wix.com/abdulhalim-group>



Department of Electro-Optics and Photonics Engineering
Ilse Katz Institute for Nanoscale Science and Technology,
Ben-Gurion University of the Negev, Be'er Sheva, Israel

Motivation

Global SPR Market

Global Surface Plasmon Resonance Market Share
By Region , 2017 (US\$ Mn)



245.5

(US\$ Mn)

North
America



XX.X
Western
Europe



XX.X
APEJ



XX.X
Japan



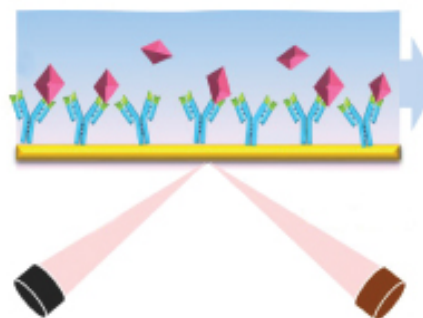
XX.X
Eastern
Europe



XX.X
Latin
America



XX.X
MEA



CAGR of **6.3%**
(2017-2027)

Source: Future Market Insights, 2017

Motivation

Importance to Human Health

Environmental pollutants detection

Blood analytes detection

Biomarkers identification/detection

Drug discovery

Food inspection

.

.

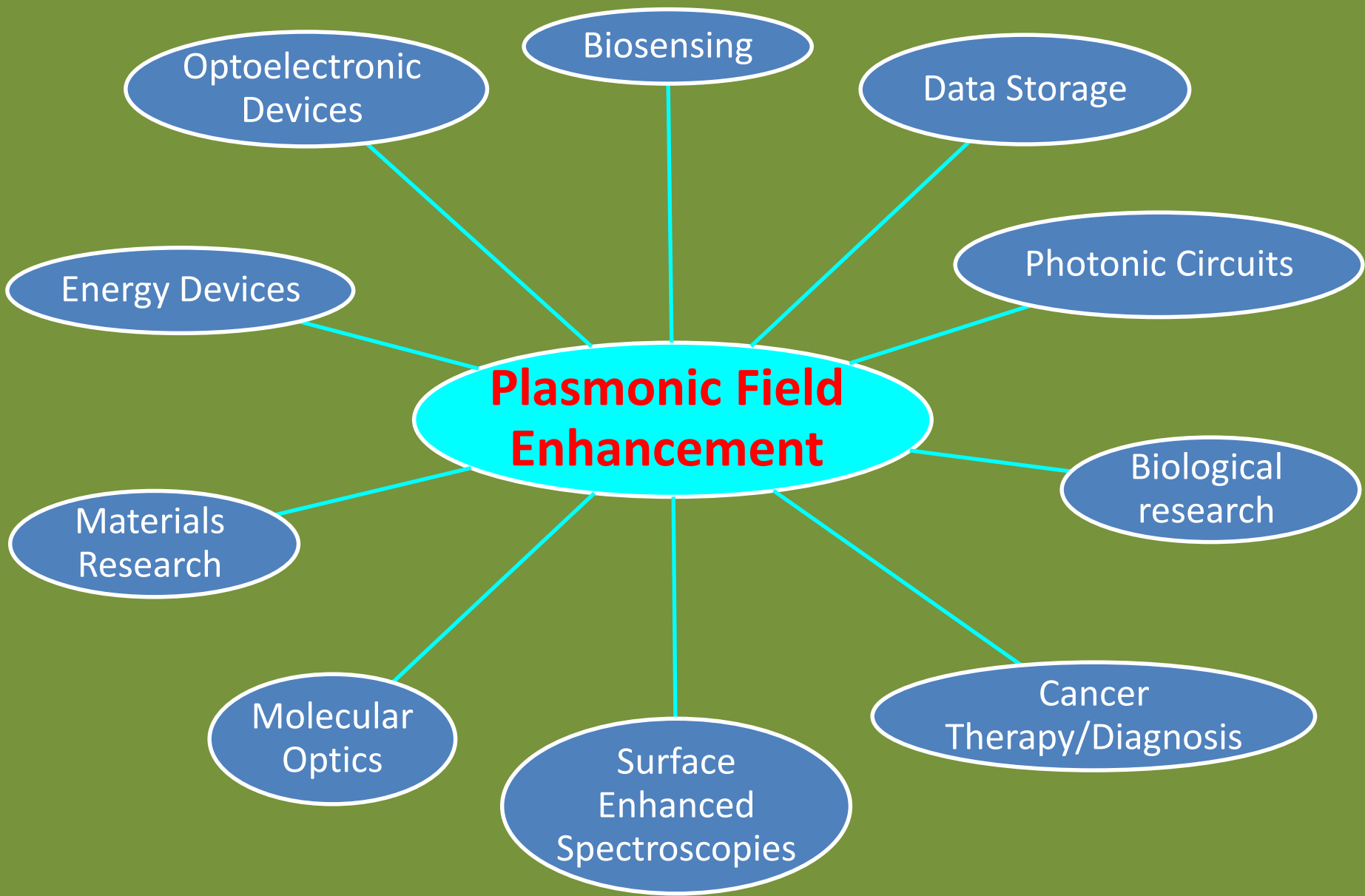
.

.....

Key Points to be Covered

- **Motivation** ✓
- **SPR Sensing:**
 - **Physics of Plasmonic Sensing**
 - **Resolution improvement with Optics/Physics**
 - **Penetration depth enhancement**
 - **Self referencing**
 - **Reading Methodologies-System**
- **Extended versus Localized SPR**
- **Summary and Future**

Plasmonic Field Enhancement is a Key Factor



Factors Influencing Field Enhancement

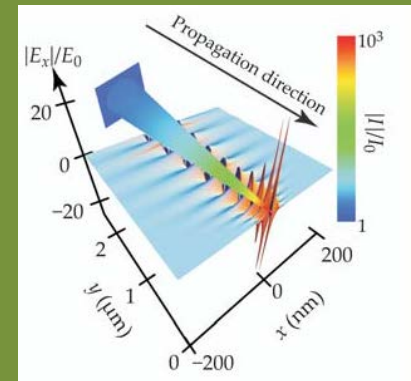
➤ Material factor:

$$\left(\frac{\epsilon_{mr}}{\epsilon_{mi}} \right)^2$$



➤ Geometry:

$$\left(\frac{1}{L_j} \right)^2$$

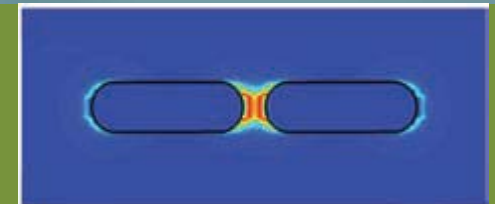
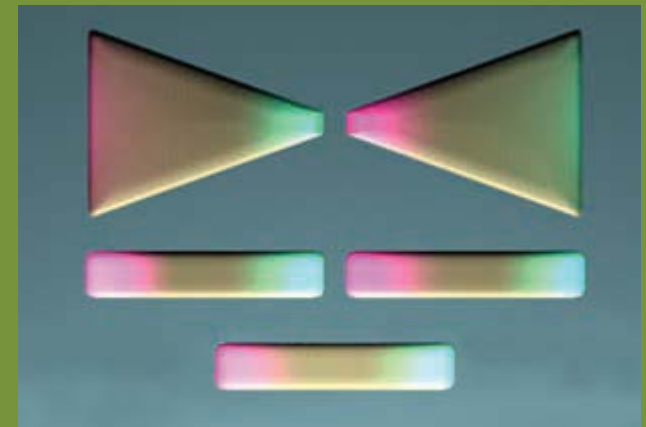


M.I. Stockman., Physics Today 64, 39 (2011)

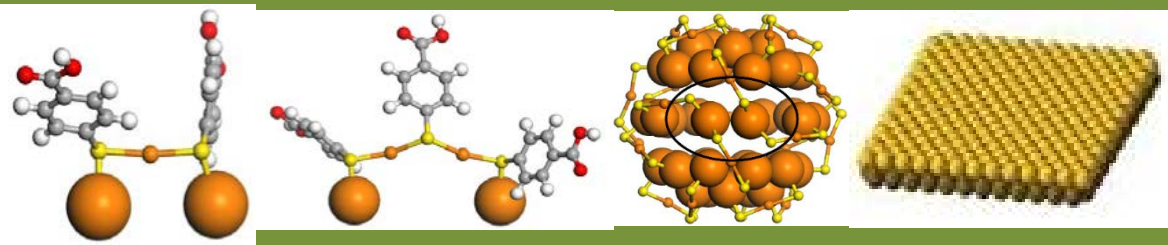
➤ Interference:

➤ Optical Antenna Effect:

➤ Arrangement of NPs:

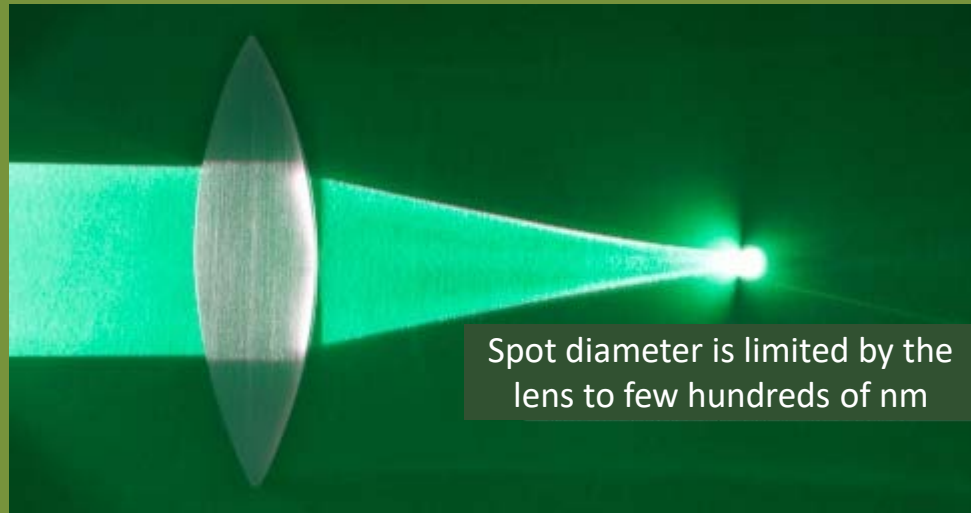


F. Capasso et al., OPN, May 2009

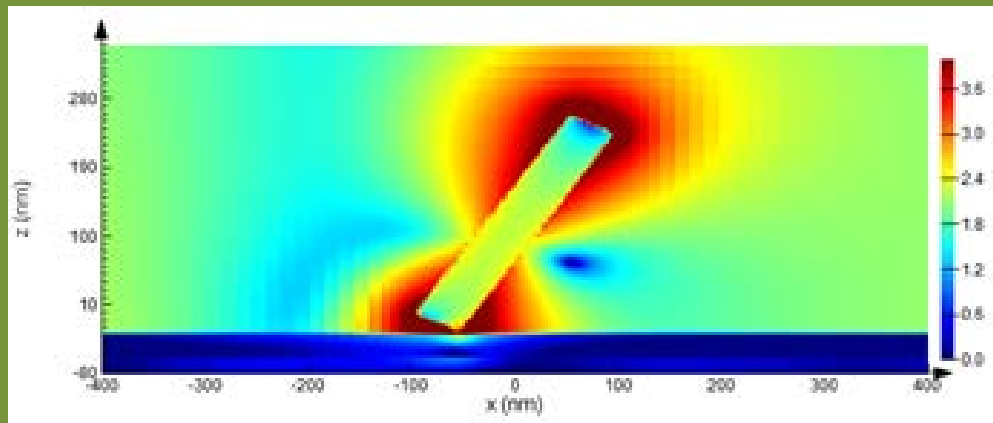


Plasmonics Allow the Nanoscale Enhancement

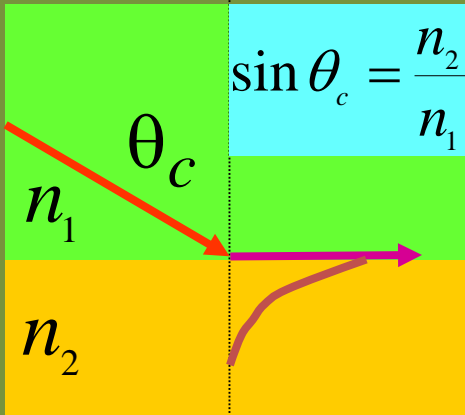
Limitations of Standard Optics



Field Intensity is Enhanced nearly 10 Million Times Near the Tip of a Silver Nanorod on Metal Film



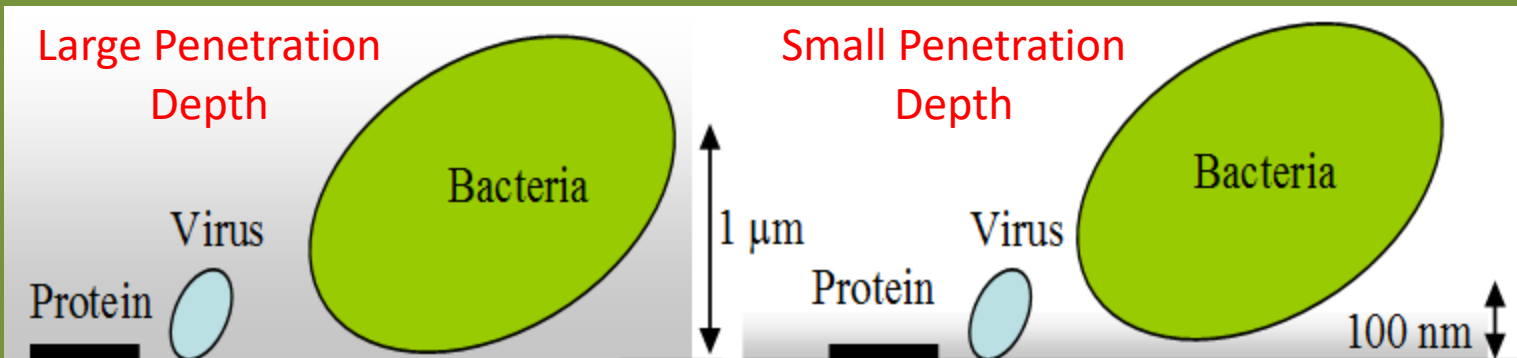
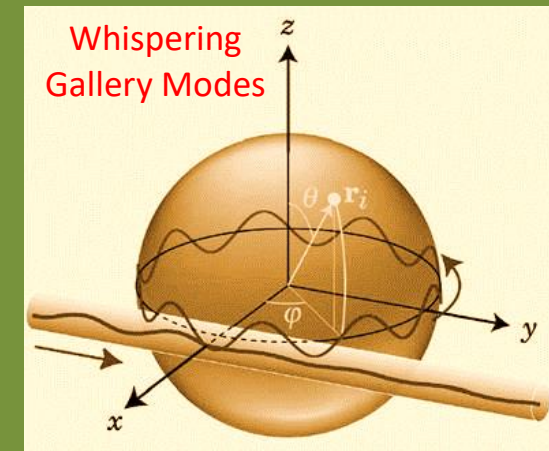
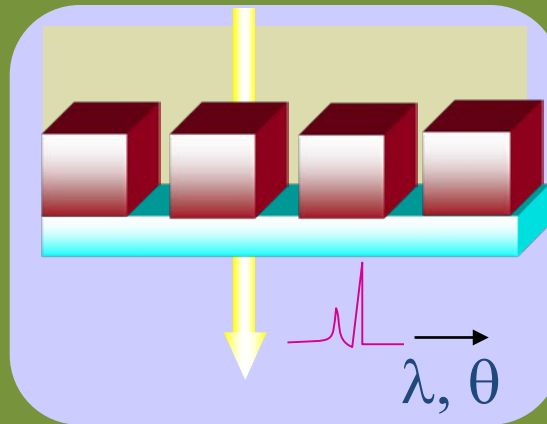
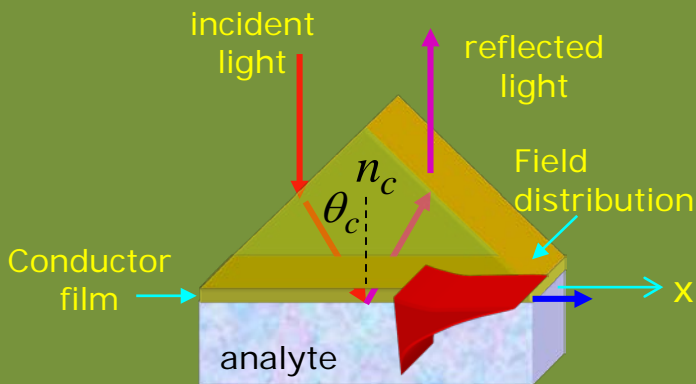
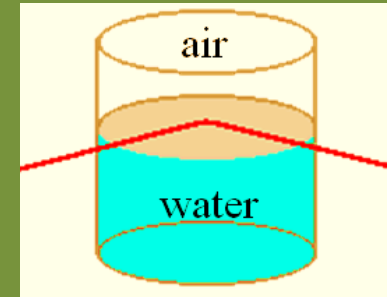
Surface Waves and Sensing



The simplest example:
Total Internal Reflection

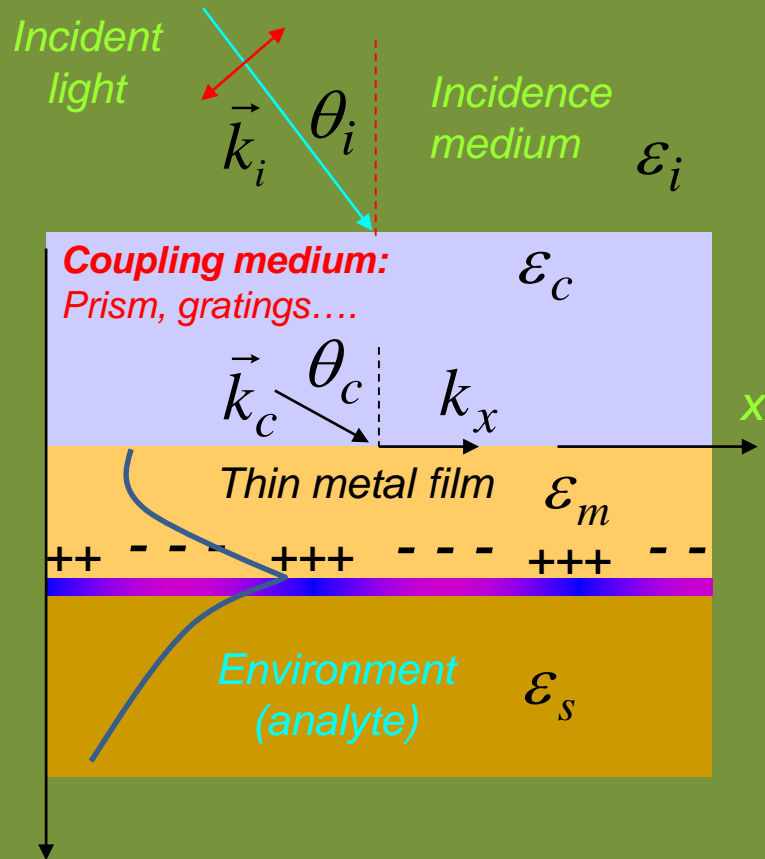
$$E \propto \exp(-z / \delta_e)$$

$$\delta_e = \lambda_0 / (2\pi \sqrt{n_1^2 \sin^2 \theta_i - n_2^2})$$



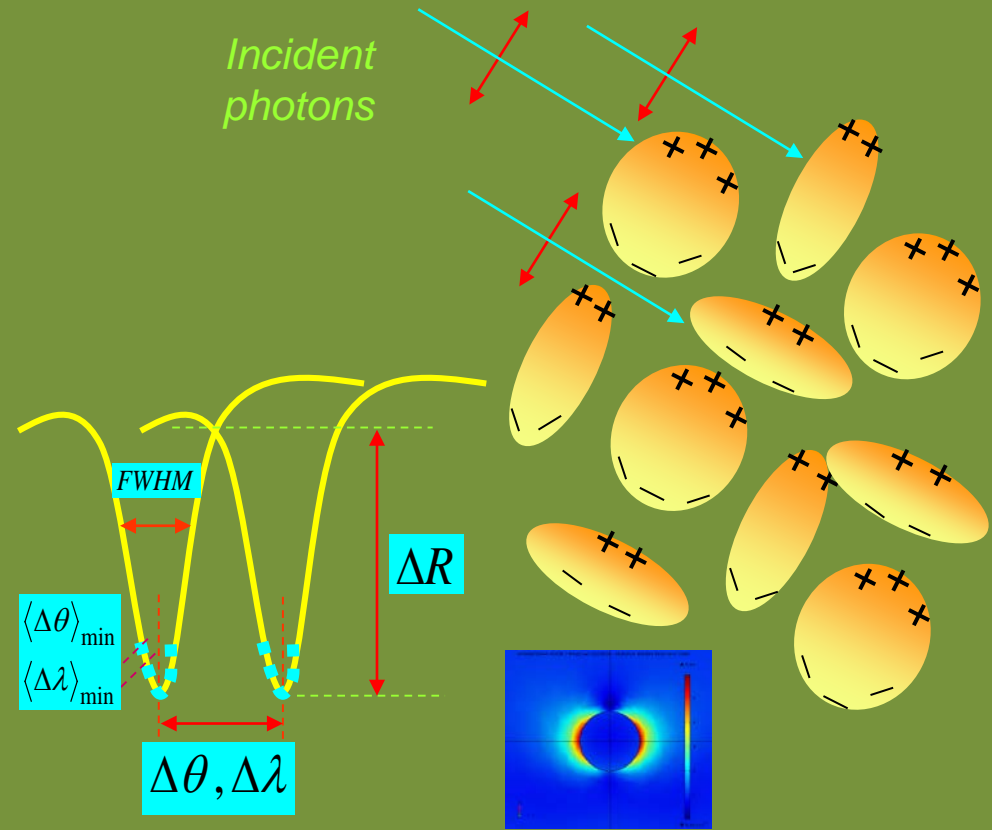
Two Main Types of Plasmonic Waves

Extended SPW



- ❑ Field penetrates few hundred nm and more in the analyte!
- ❑ Field enhancement at the interface $\sim \times 10-20$
- ❑ Sensitivity $\sim 1000-50000 \text{ nm/RIU}$

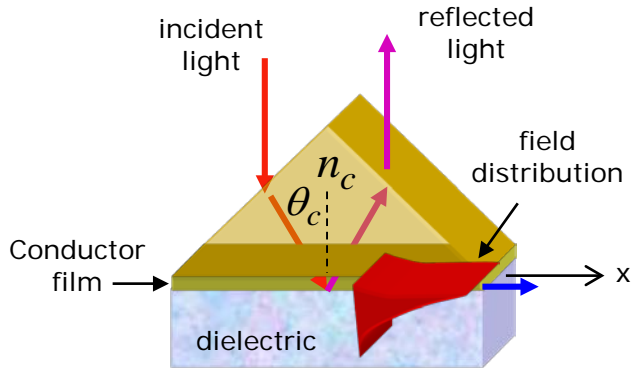
Localized SPW



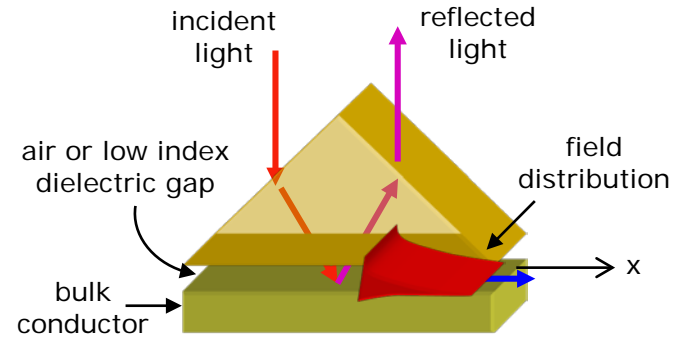
- ❑ Field penetrates few nm in the analyte. Highly localized!
- ❑ Field enhancement at the interface is $\sim \times 20-100$
- ❑ Sensitivity $\sim 100-500 \text{ nm/RIU}$

Extended Plasmonic Waves

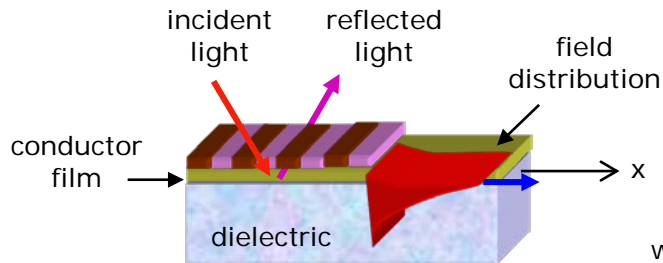
$$k_x = \frac{2\pi}{\lambda} n_c \sin \theta_c \pm \frac{2\pi}{\Lambda} j = \frac{2\pi}{\lambda} \operatorname{Re} \left\{ \left(\frac{n_m^2 n_{a,s}^2}{n_m^2 + n_{a,s}^2} \right)^{1/2} \right\} = \operatorname{Re} \{ k_{sp} \}$$



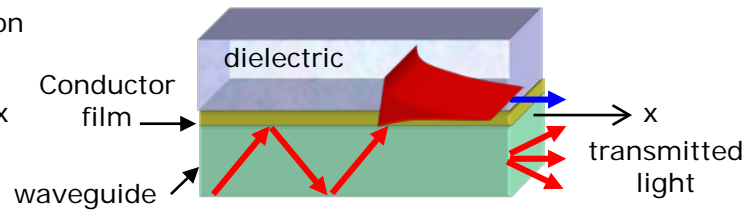
(a) Kretschmann-Raether



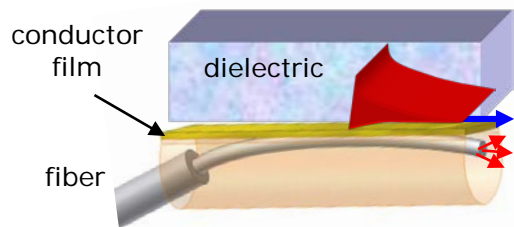
(b) Otto



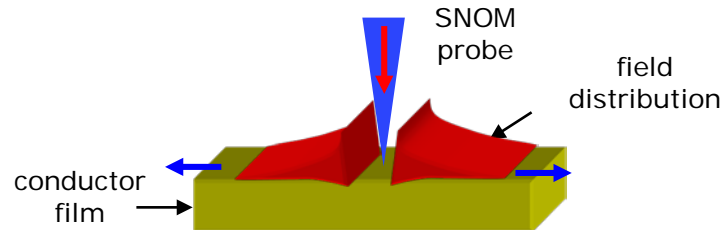
(c) Grating



(d) Waveguide



(e) Fiber



(f) Nano-tip

Plasmonics is the Science and Technology Dealing with Surface Plasmon Waves

SPW- (Surface Plasmon Wave) : Is a charge density wave occurring at the interface between a metal and a dielectric.

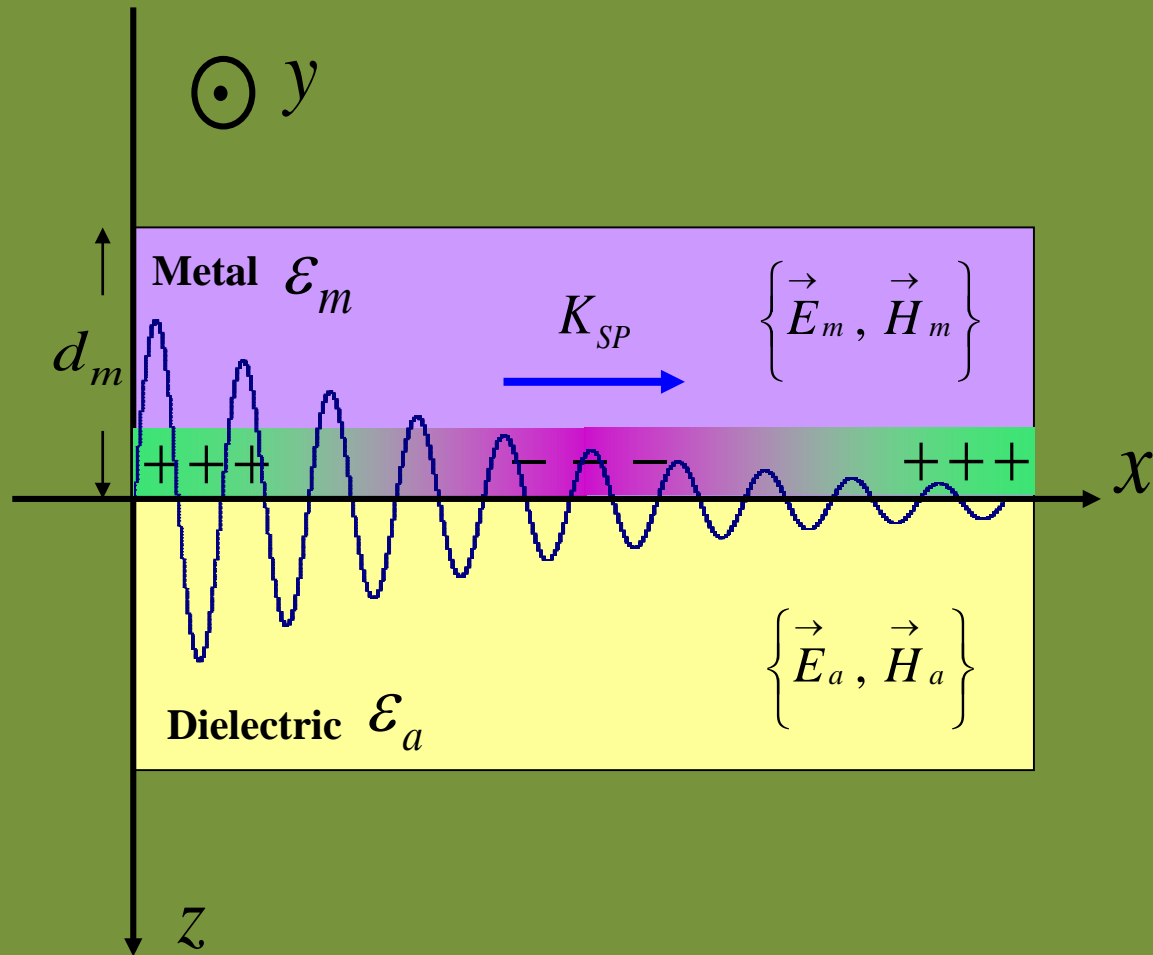
To generate charge density:

$$\vec{H}_i = (0, H_{yi}, 0)$$

$$\vec{E}_i = (E_{xi}, 0, E_{zi})$$

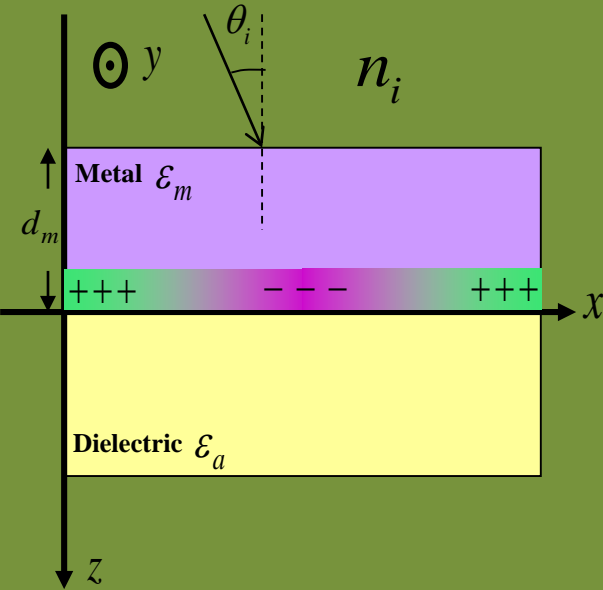
TM polarization only!

1st condition!



Momentum of Propagating SP

Plasmon propagation K vector:



In the infinite metal thickness limit:

$$H_{yi} = H_{0i} \cdot \exp i(k_x x - \omega t) \cdot \exp(ik_i z)$$

medium i :

$$E_{xi} = \frac{H_{0i}}{\omega \epsilon_0} \left(\frac{k_i}{\epsilon_i} \right) \cdot \exp i(k_x x - \omega t) \cdot \exp(ik_i z)$$

$$E_{zi} = \frac{-H_{0i} \cdot k_x}{\omega \epsilon_0} \left(\frac{1}{\epsilon_i} \right) \cdot \exp i(k_x x - \omega t) \cdot \exp(ik_i z)$$

Applying the continuity relations of the tangential field's components (E_{xi} , H_{yi}):

$$k_{sp} = k_0 \operatorname{Re} \left\{ \sqrt{\frac{\epsilon_m \epsilon_a}{\epsilon_m + \epsilon_a}} \right\} \Rightarrow k_x = \operatorname{Re} \{ k_{sp} \} = k_0 \sqrt{\frac{\epsilon_{mr} \epsilon_a}{\epsilon_{mr} + \epsilon_a}}$$

2nd condition!

$$k_x = k_0 n_i \sin \theta_i \Rightarrow \sin \theta_{spr} = \frac{1}{n_i} \sqrt{\frac{\epsilon_{mr} \epsilon_a}{\epsilon_{mr} + \epsilon_a}}$$

Since $\epsilon_{mr} < 0$ then the

3rd condition!

is: $|\epsilon_{mr}| > \epsilon_a$

Two Important Parameters

Penetration Depths

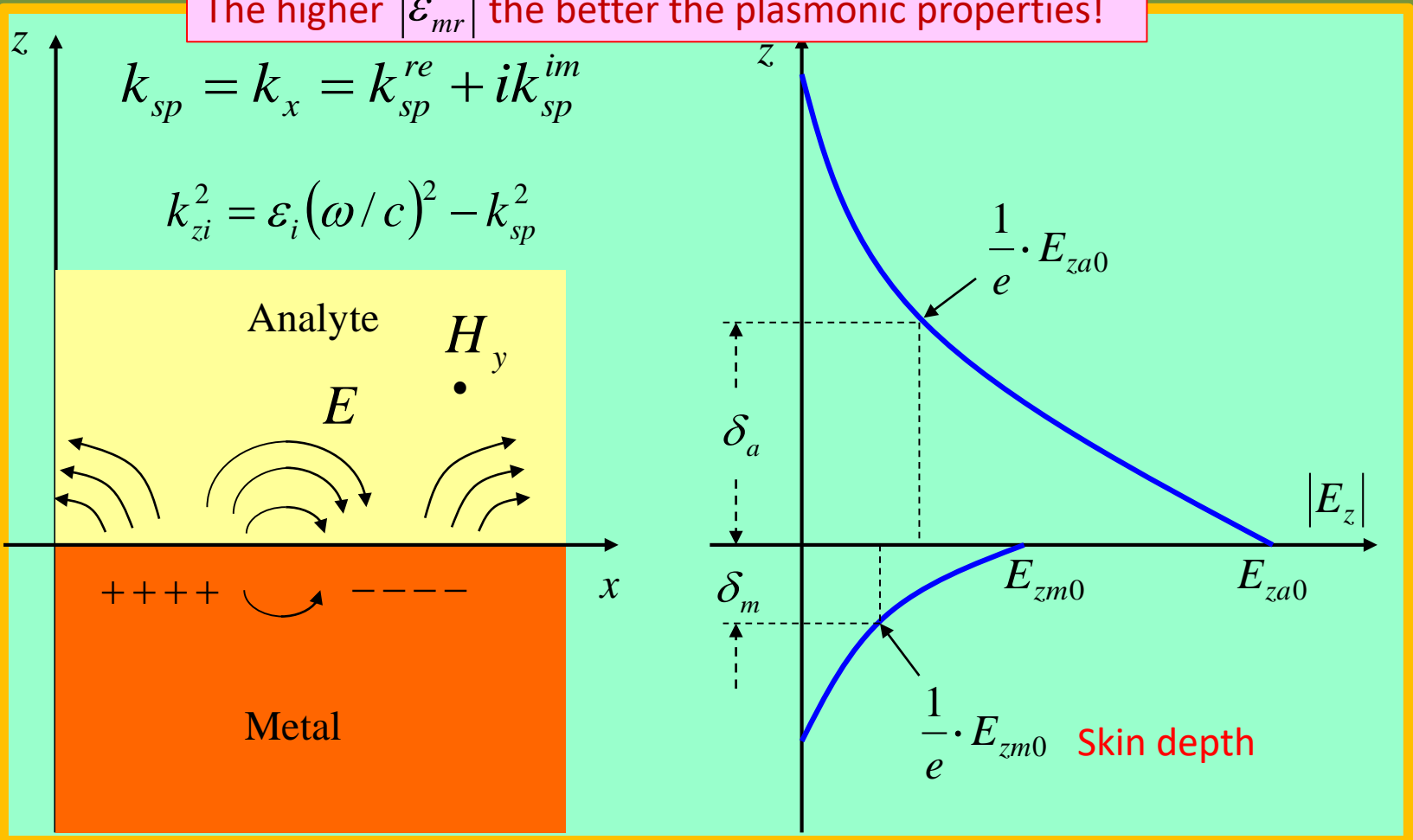
$$\delta_m = \frac{\lambda}{2\pi} \cdot \sqrt{\frac{\epsilon_a + \epsilon_{mr}}{-\epsilon_{mr}^2}}$$

$$\delta_d = \frac{\lambda}{2\pi} \cdot \sqrt{\frac{\epsilon_a + \epsilon_{mr}}{-\epsilon_a^2}}$$

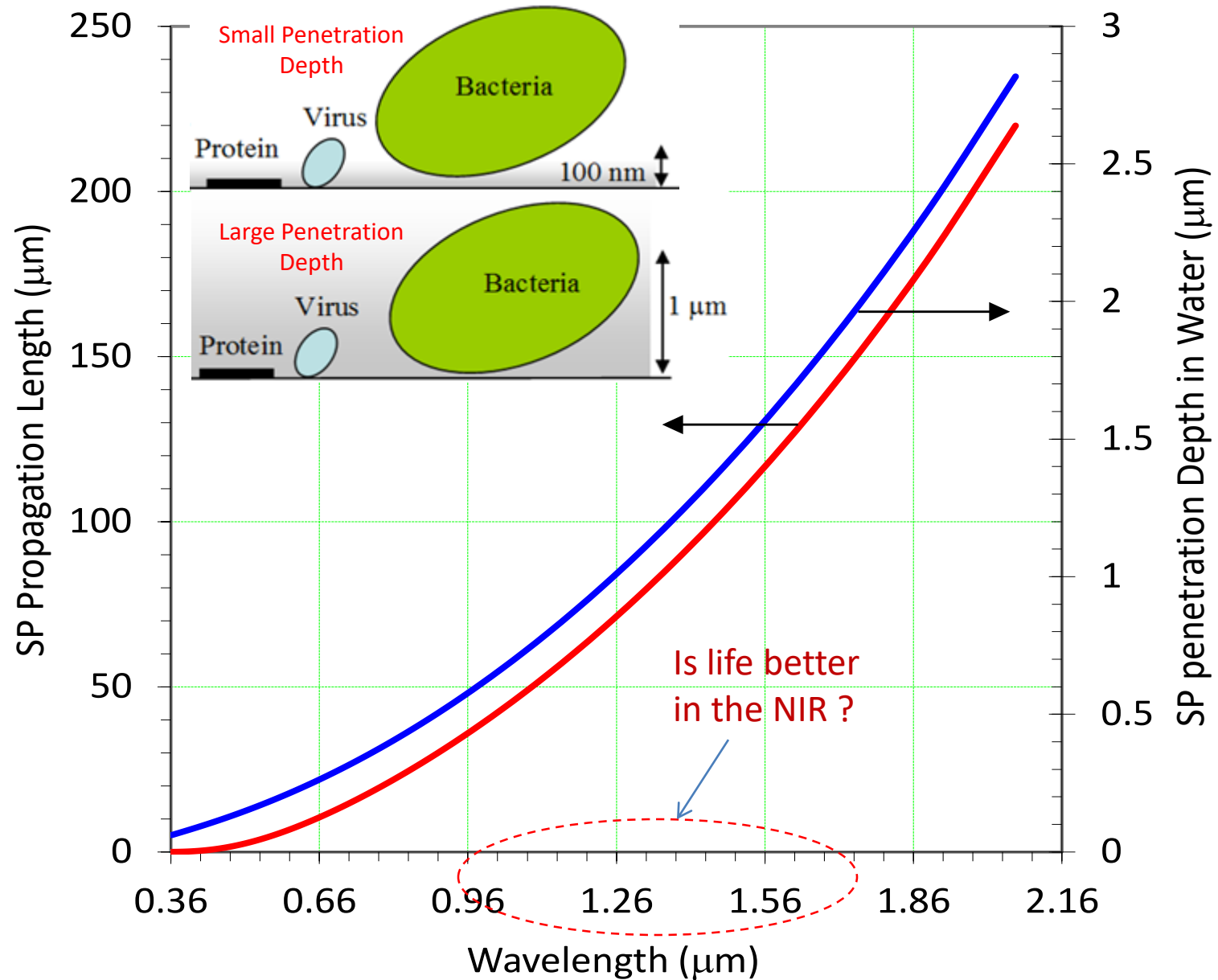
Propagation Length

$$L_x = \frac{1}{2|k_x''|} = \frac{\lambda}{2\pi} \frac{\epsilon_{mr}^2}{\epsilon_{mi}} \left[\frac{\epsilon_a + \epsilon_{mr}}{\epsilon_a \epsilon_{mr}} \right]^{3/2}$$

The higher $|\epsilon_{mr}|$ the better the plasmonic properties!



Silver as an Example



Exciting SPR- Prism Coupling

Introducing the Drude model for the metal permittivity gives the dispersion relation of the SP:

$$\epsilon_m = 1 - \frac{\omega_p^2}{\omega(\omega + i\eta)}$$

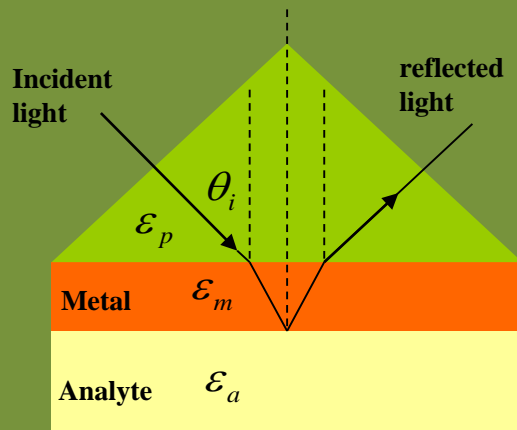


$$k_{spr} = k_0 \sqrt{\frac{\epsilon_{mr} \epsilon_a}{\epsilon_{mr} + \epsilon_a}}$$

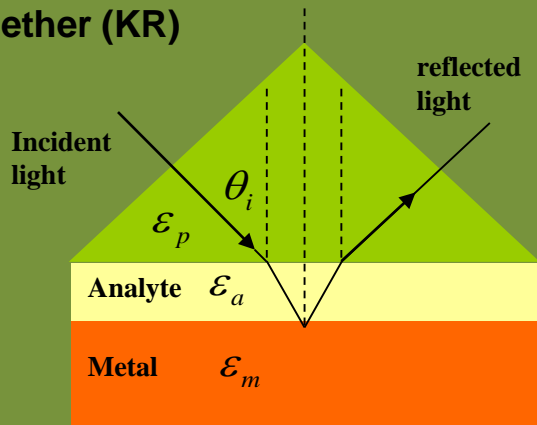
4th condition!

$$n_p \sin \theta_i > 1 \quad \text{TIR}$$

Dispersion relation of SP

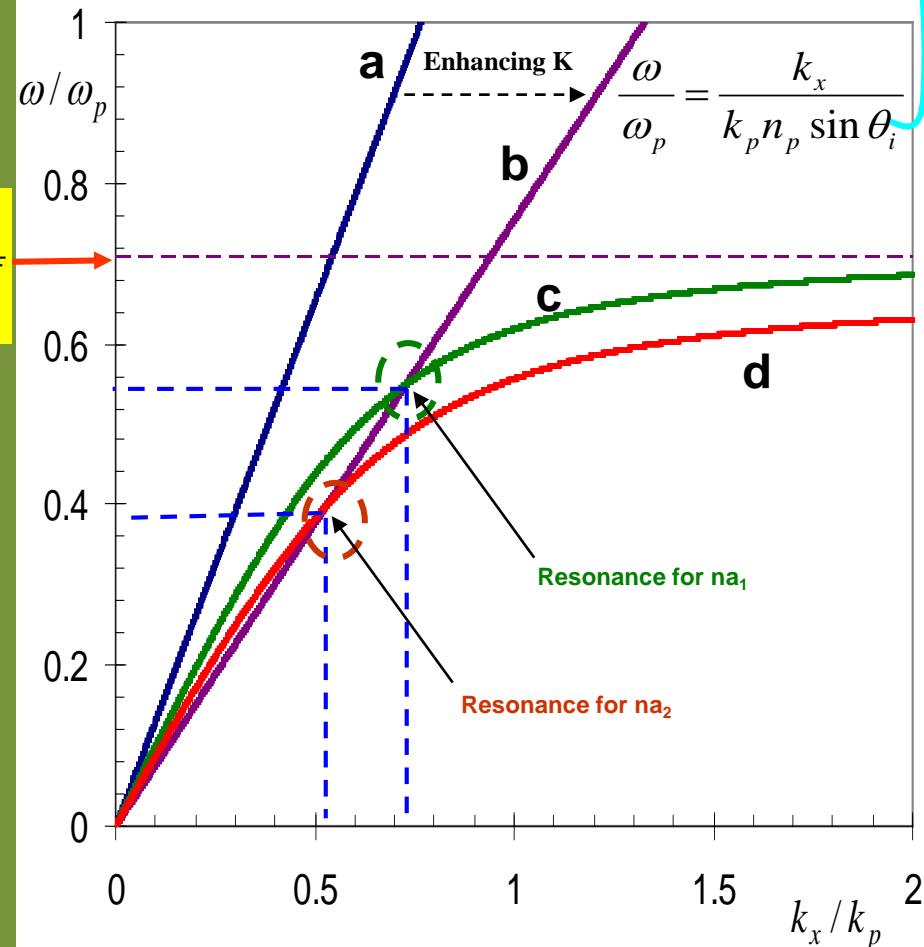


Kretschmann-Raether (KR)

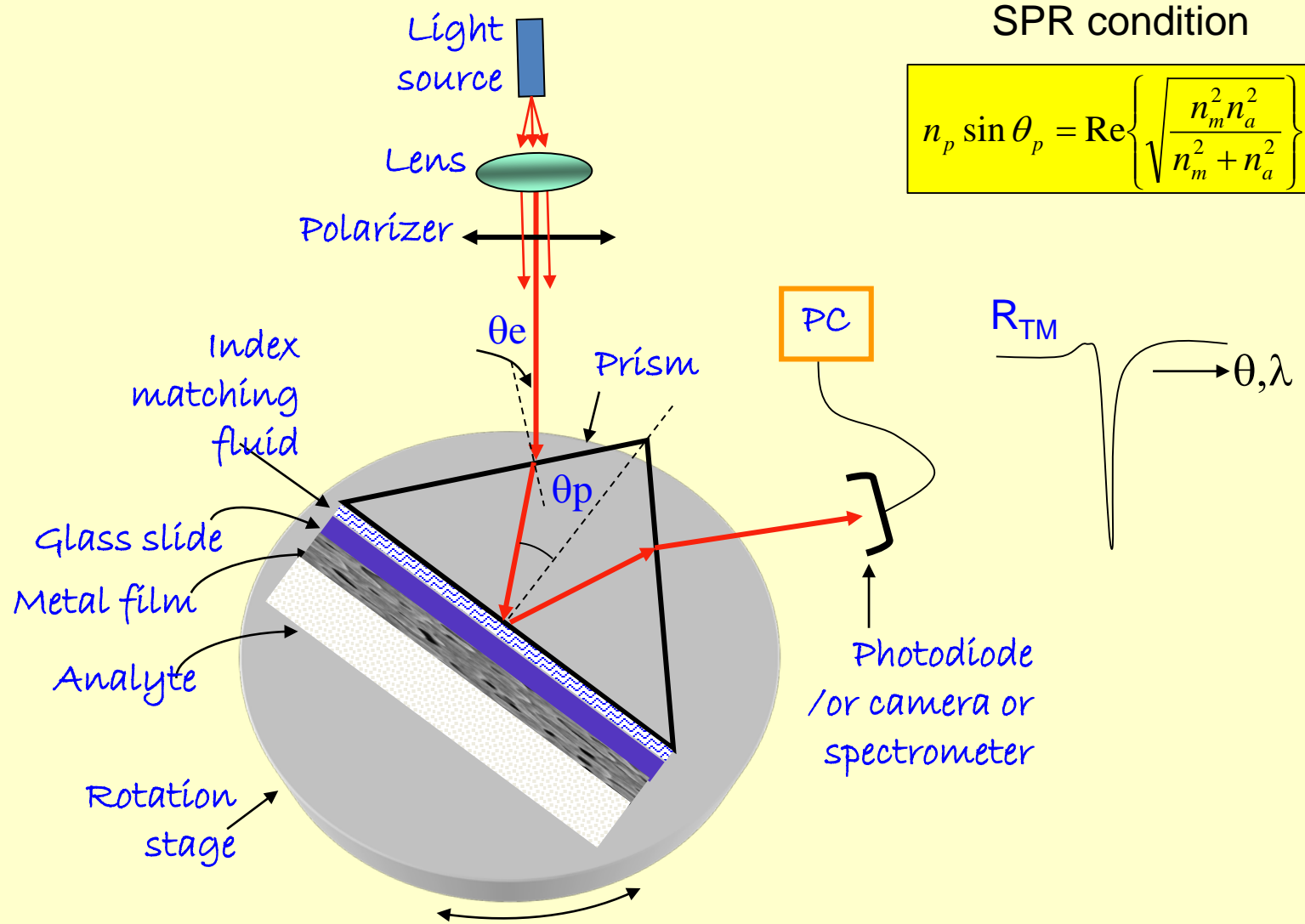


Otto

$$\frac{1}{\sqrt{1 + \epsilon_a}}$$

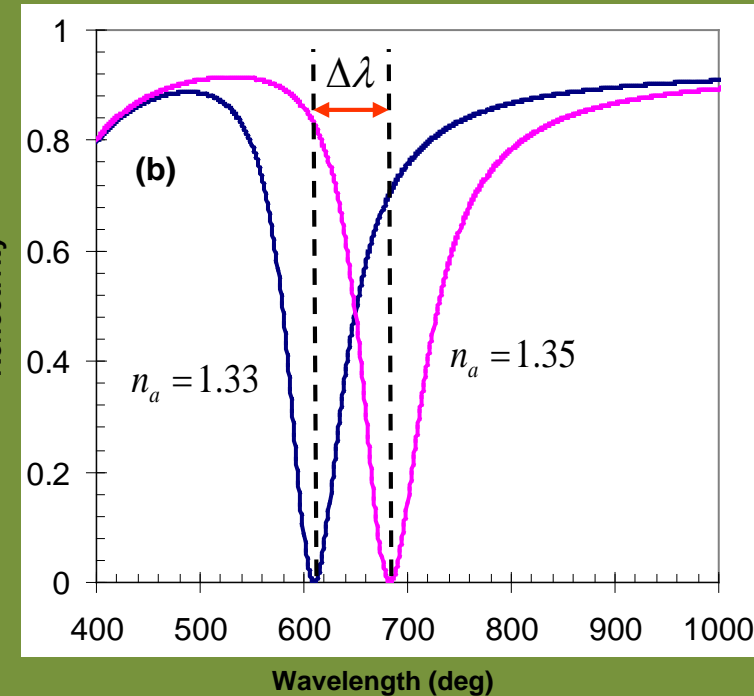
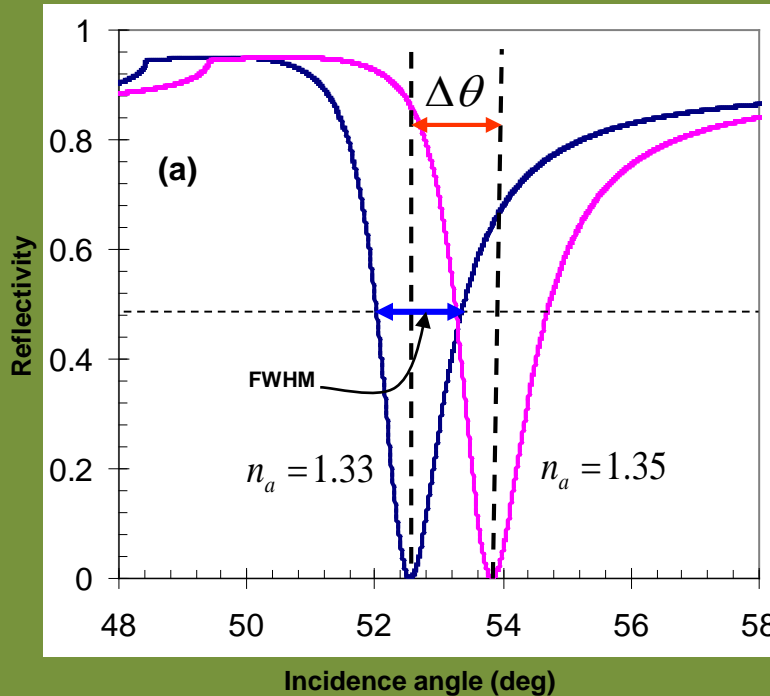


Prism Coupling-General Setup



Angular and Spectral Modes for Sensing

Sensing in the KR configuration



- Angular Sensitivity: $\sim 100\text{-}200$ deg/RIU

$$S_{\theta} = \frac{\partial \theta_{dip}}{\partial n_a} = \frac{\epsilon_{mr} \sqrt{-\epsilon_{mr}}}{(\epsilon_{mr} + n_a^2) \sqrt{\epsilon_{mr} (n_a^2 - n_p^2) - n_p^2 n_a^2}}$$

$$FOM \equiv \frac{S_{\theta, \lambda}}{FWHM}$$

- Spectral sensitivity: $\sim 1000\text{-}30000$ nm/RIU

$$S_{\lambda} = \frac{\partial \lambda}{\partial n_a} = \frac{\epsilon_{mr}^2}{\frac{n_a^3}{\lambda} \left| \frac{d\epsilon_{mr}}{d\lambda} \right| + (n_a^2 + \epsilon_{mr}) \epsilon_{mr} \frac{dn_p}{d\lambda} \frac{n_a}{n_p}}$$

➔ $\delta n \sim 10^{-7}$ RIU
(1pg/mm²)

Sensitivity and Detection Limit (Resolution)

$$S_{\theta} = \frac{\Delta\theta}{\Delta n}, \quad S_{\lambda} = \frac{\Delta\lambda}{\Delta n}, \quad S_R = \frac{\Delta R}{\Delta n}$$

$$DL_{\theta} = \langle \Delta n \rangle_{\min} = \frac{\langle \Delta\theta \rangle_{\min}}{S_{\theta}}$$

$$DL_{\lambda} = \langle \Delta n \rangle_{\min} = \frac{\langle \Delta\lambda \rangle_{\min}}{S_{\lambda}}$$

$$DL_R = \langle \Delta n \rangle_{\min} = \frac{\langle \Delta R \rangle_{\min}}{S_R}$$

$$S_{\theta}, S_{\lambda}$$

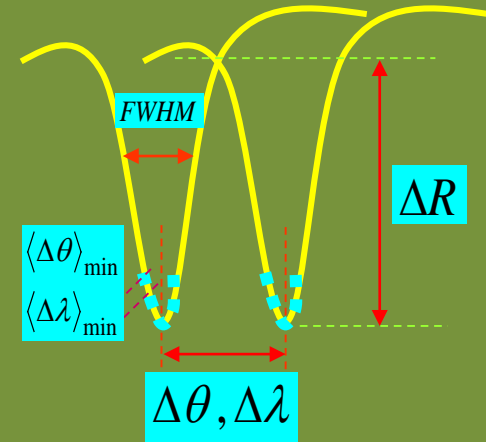


Physics / Optics / Materials

$$\langle \Delta\theta \rangle_{\min}, \langle \Delta\lambda \rangle_{\min}$$



System

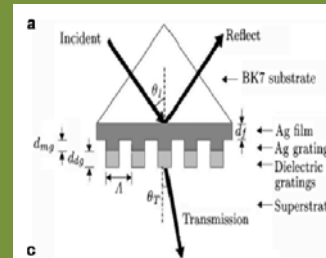


$$FoM = \frac{S_{\lambda, \theta, R}}{FWHM}$$

Existing Methods for Sensitivity Enhancement of SPR Sensors

Double-metal layer

J. Opt. A: Pure Appl. Opt. **8** (2006) 959–963

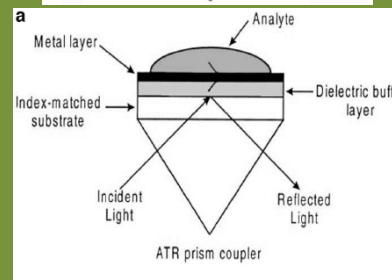


Gratings (Transmission)

W. Bin, and W. Q. Kang, Chin. Phys. Lett. **25**, 1668–1671 (2008).

Prism RI- Spectral

J. S. Yuk, et al. Eur. Biophys. J **35**, 469–476 (2006).

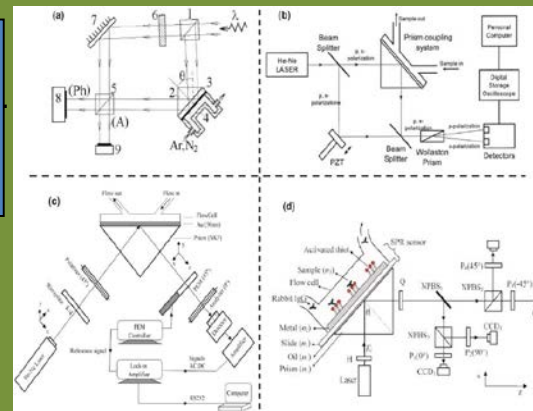


Long Range SPR

G. G. Nenninger, P. Tobiška, J. Homola, and S. S. Yee, Sens. Actuators B **74**, 145–151 (2001).

Prism RI- Angular

G. Gupta, and J. Kondoh, Sens. Actuators B, **122**, 381–388 (2007).



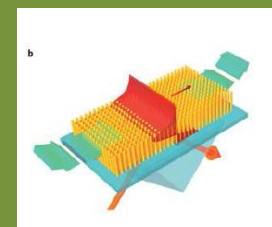
Phase sensitive SPR

A.V. Kabashin, and P. I. Nikitin, Opt. Commun. **150**, 5–8 (1998).

S.Y. Wu, H. P. Ho, W. C. Law, C. Lin, and S. K. Kong, Opt. Lett. **29**, 2378–2380 (2004).

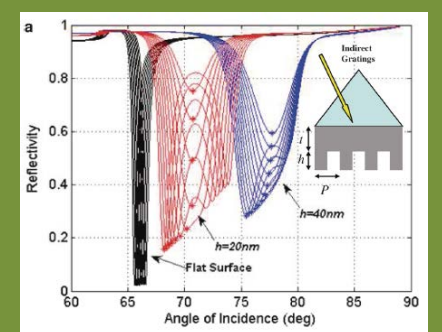
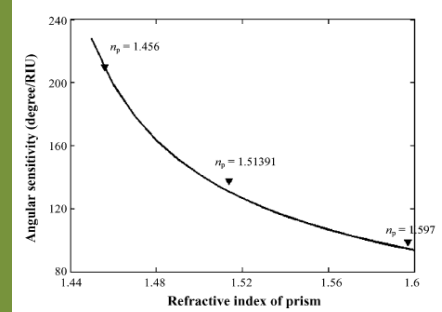
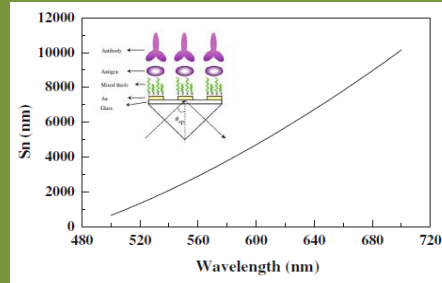
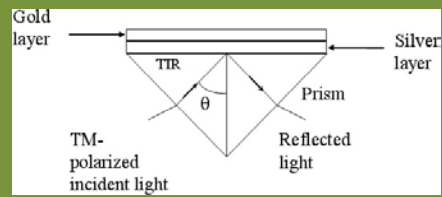
Gratings (Reflection)

C. J. Alleyne et. al., Opt. Express **15**, 8163–8169 (2007).



Metamaterials

A.V. Kabashin, et al., Nature Mater. **8**, 867–71 (2009).



Phase SPR (Polarimetric, Ellipsometric)

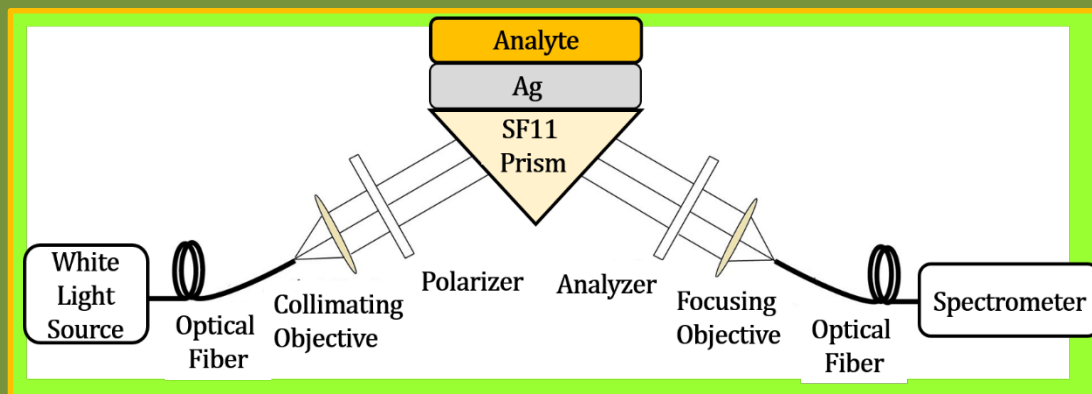
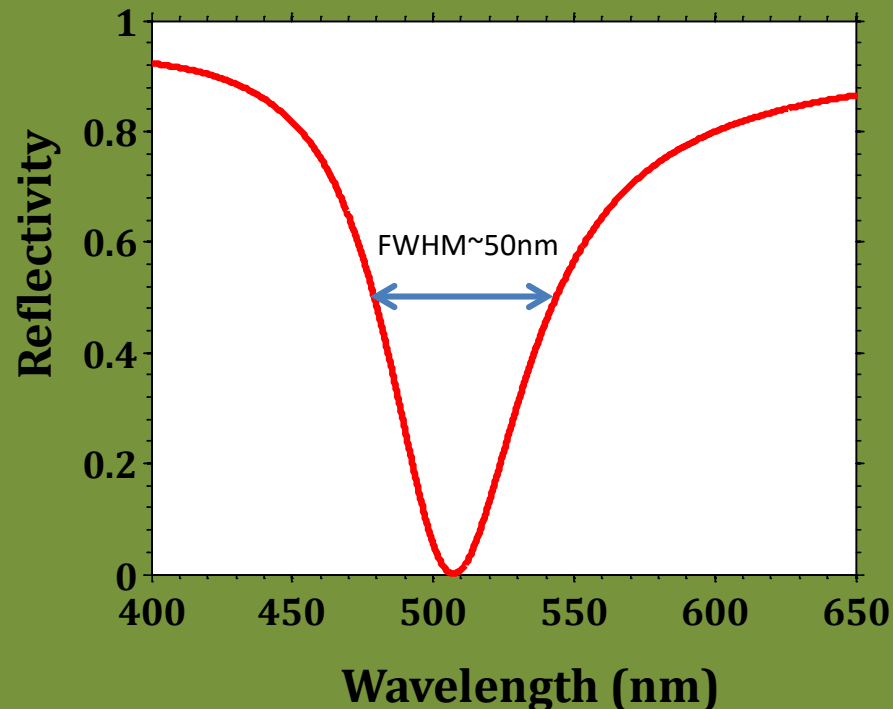
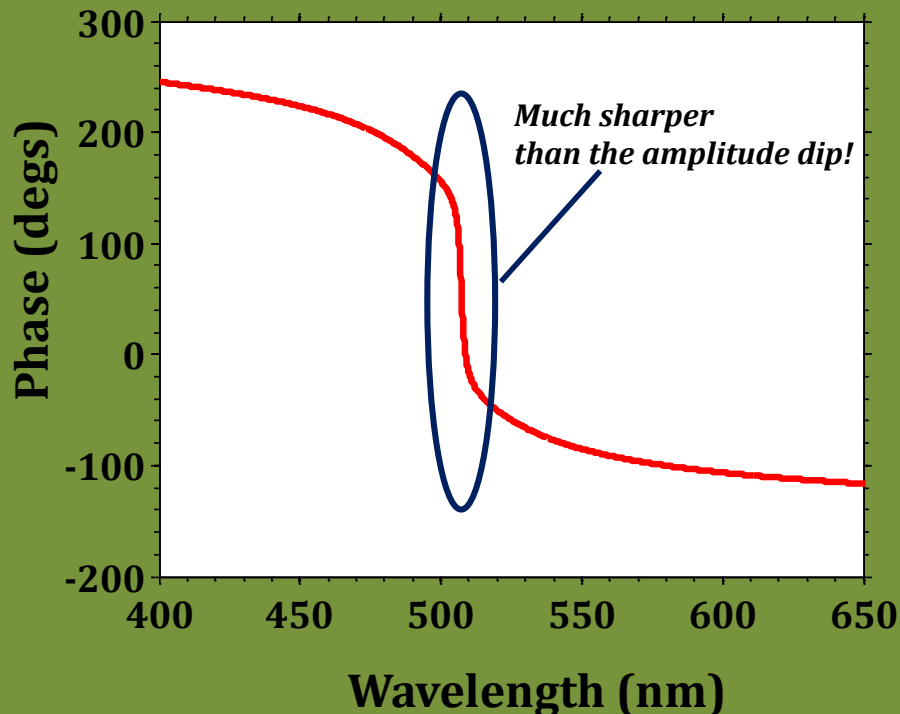
$$r_{TM,TE} = |r_{TM,TE}| \exp(i\phi_{TM,TE})$$

Amplitude

Phase

$$\tan \psi = \left| \frac{r_{TM}}{r_{TE}} \right|$$

$$\Delta = \phi_{TM} - \phi_{TE}$$

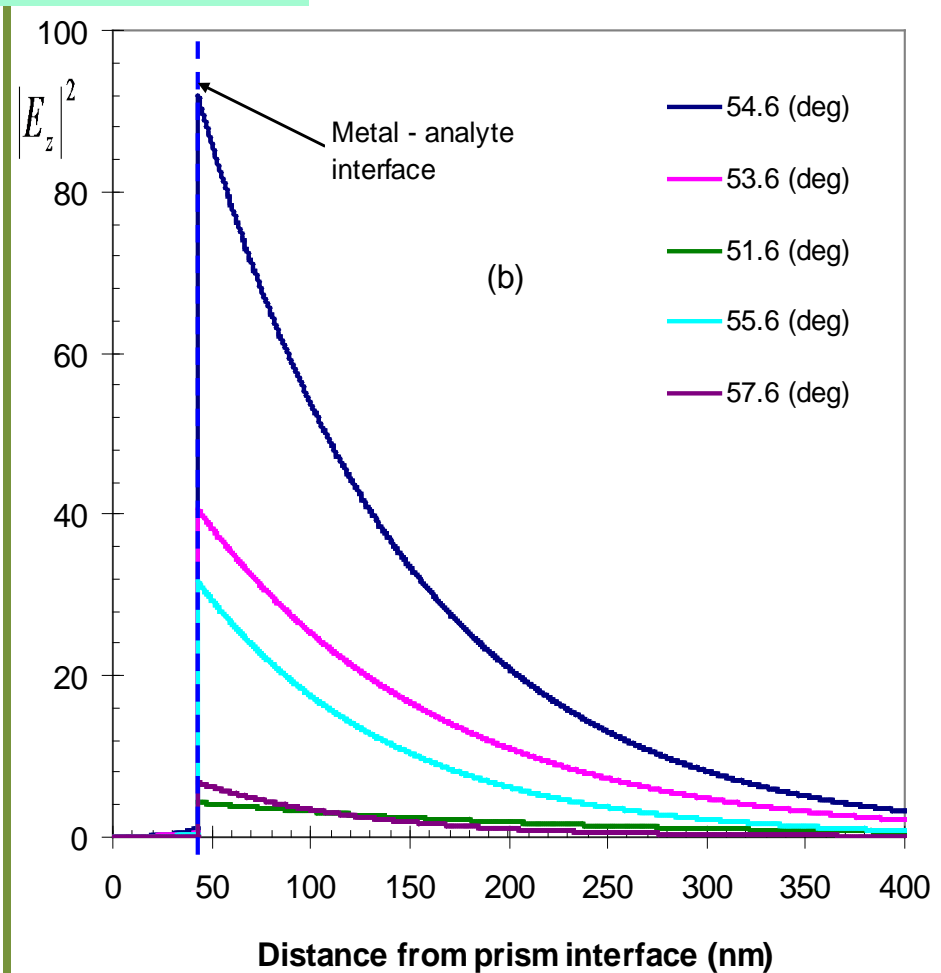
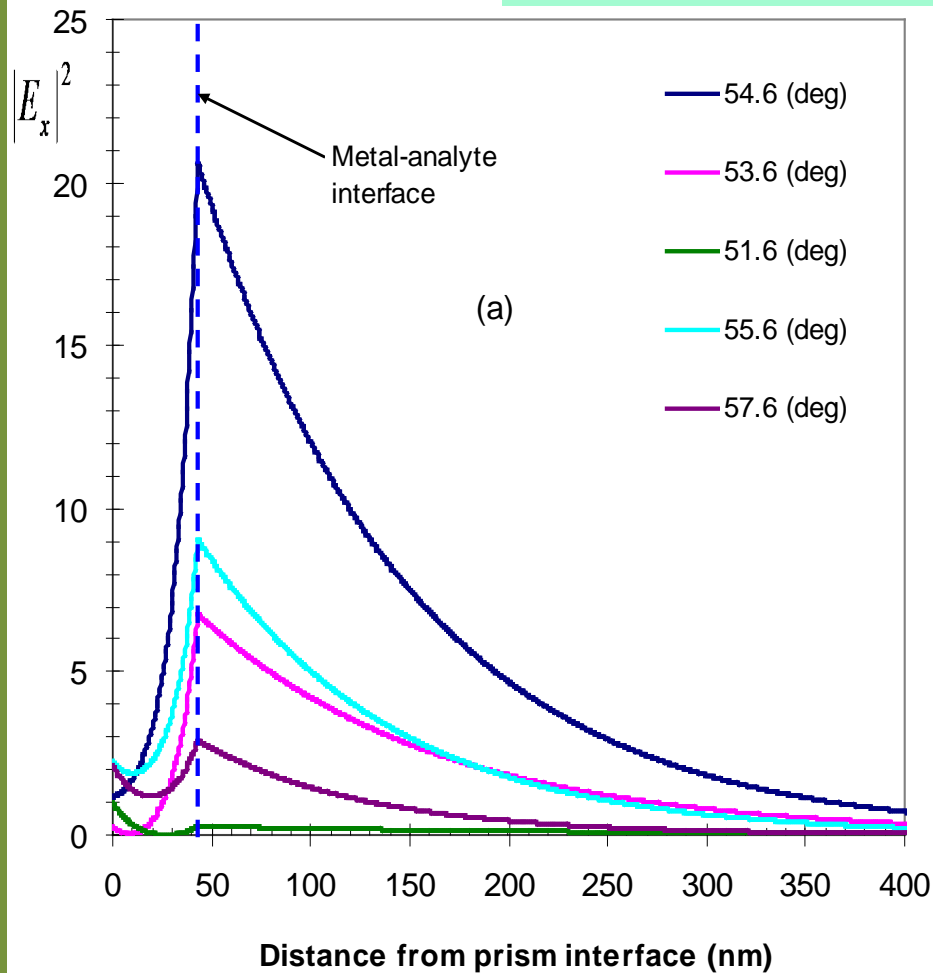


$$\tan \psi = \sqrt{\frac{I_{45}}{I_{\parallel} + I_{\perp} - I_{45}}}$$

$$\cos \Delta = \frac{1}{2 \tan \psi} \frac{I_{\parallel} - I_{\perp}}{I_{\parallel} + I_{\perp} - I_{45}}$$

EM Field Enhancement at the Resonance

$$\lambda = 633\text{nm}, d_m = 43\text{nm}, n_a = 1.33, n_p = 1.732, \theta_r = 54.61^\circ$$



Transfer matrix calculation:

$$\begin{bmatrix} H_{yj}(z) \\ -E_{xj}(z) \end{bmatrix} = P_j(z) \cdot \left(\prod_{l=j-1}^1 P_l \right) \cdot \begin{bmatrix} (1+r) \\ q_1(1-r) \end{bmatrix}, Z_j \leq z \leq Z_{j+1}$$

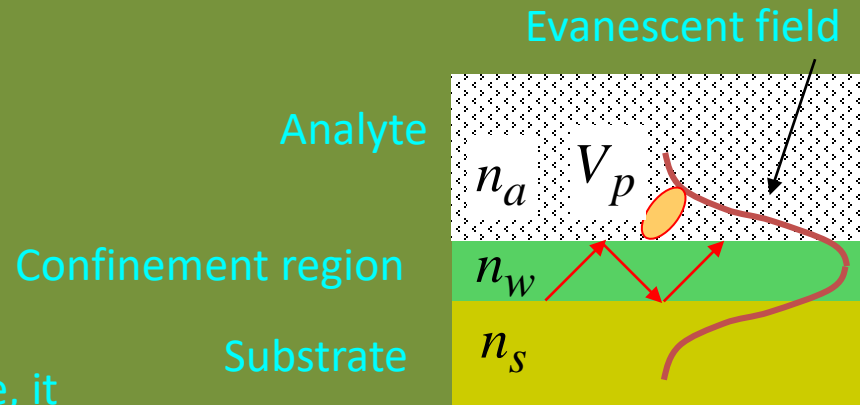
Evanescent Field Sensing

$$\varepsilon = \begin{cases} n_w^2 & r \in V_w \\ n_{a,s}^2 & r \notin V_w \end{cases}$$

Assuming a particle is added to the analyte, it creates a variation in the dielectric function:

$$\Rightarrow \delta\varepsilon = \begin{cases} n_p^2 - n_a^2 & r \in V_p \\ 0 & \textit{otherwise} \end{cases}$$

\Rightarrow The wave vector will change by: $\delta k = k_f - k_i$ and the field from: E_i to E_f



Evanescent Field Sensing

Wave equation before the perturbation:

$$\nabla_x \nabla_x E_i = k_i^2 \epsilon E_i$$

The wave equation after the particle is added:


$$\nabla_x \nabla_x E_f = k_f^2 (\epsilon + \delta\epsilon) E_f$$

Multiplying by E_i^* and integrating over the entire volume and subtracting yields:

$$(k_i^2 - k_f^2) \int_V E_f \cdot \epsilon E_i^* dr = k_f^2 \int_{V_{\text{int}}} E_i^* \cdot \delta\epsilon E_f dr$$

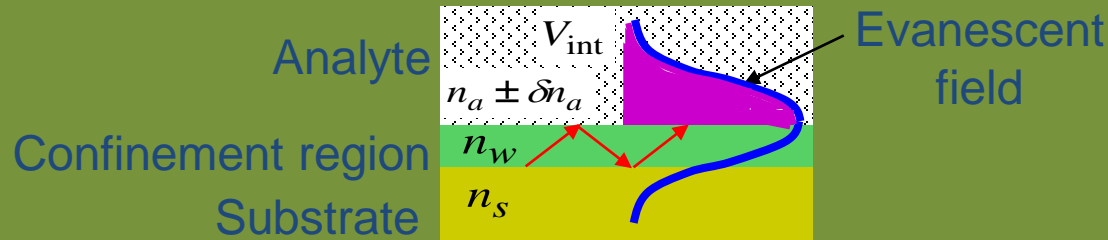


Up to the first order in δk

The shift in the wave vector is equal to the overlap integral normalized by the mode energy integral.  Sensing in the evanescence region!

$$\delta k \approx -\frac{k_i}{2} \frac{\int_{V_{\text{int}}} \delta\epsilon E_i^* \cdot E_f dr}{\int_V \epsilon E_i^* \cdot E_i dr}$$

Correlation Between EM Intensity and Sensitivity Enhancement



$$\frac{\delta k}{k_i} = \frac{\delta n_{eff}}{n} = \frac{\delta \lambda}{\lambda} \approx - \frac{1}{2} \frac{V_{int} \int \delta \epsilon E_i^* \cdot E_f dr}{\int_V \epsilon E_i^* \cdot E_i dr}$$

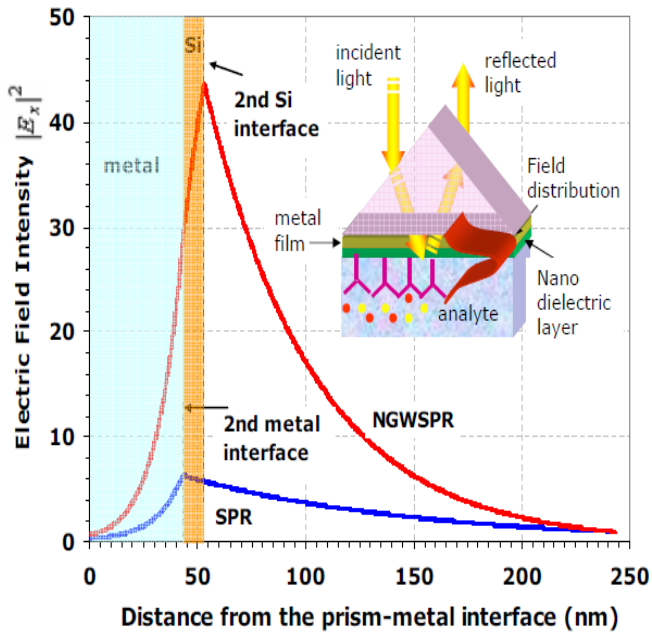
Field Strength

Sensors geometry, nano-structures, localization, band gaps, material parameters

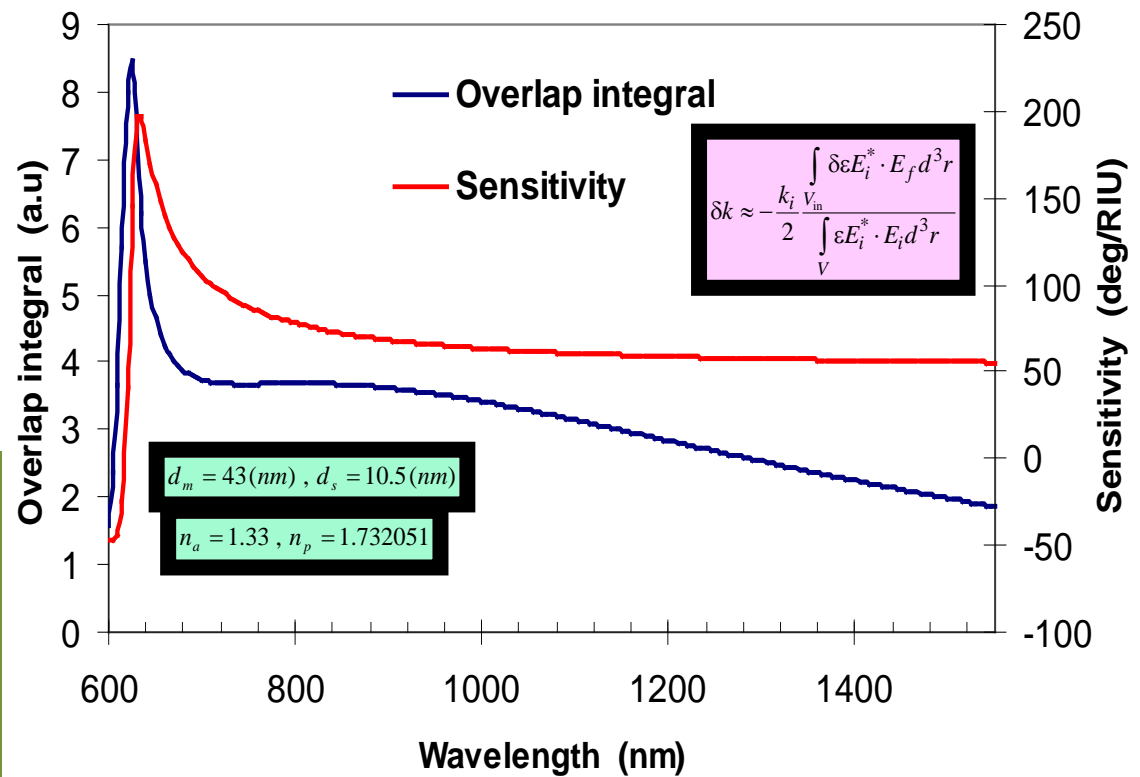
Interaction volume

Evanescence region, lateral propagation length, porosity

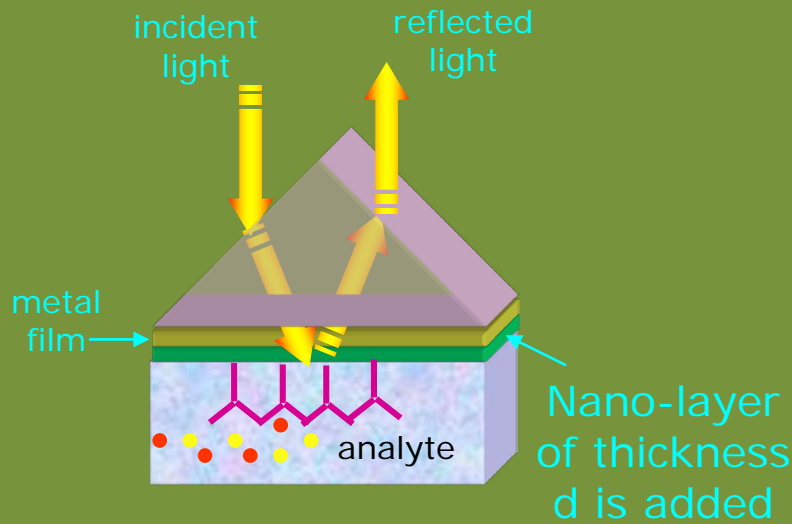
Correlation Between EM Intensity and Sensitivity Enhancement



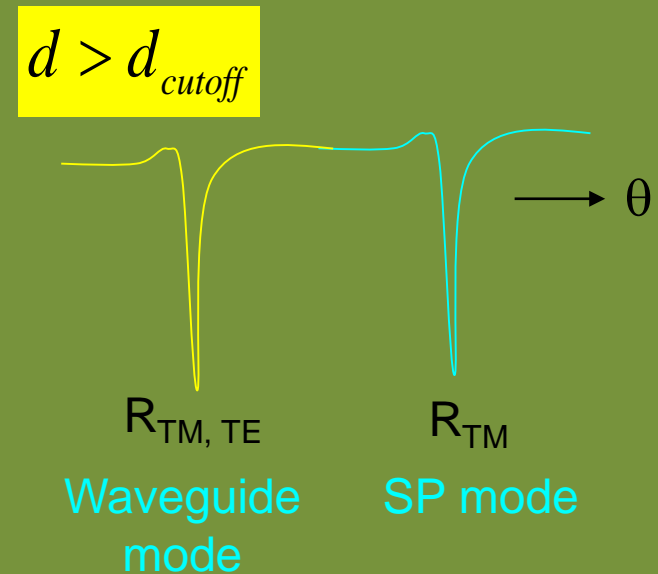
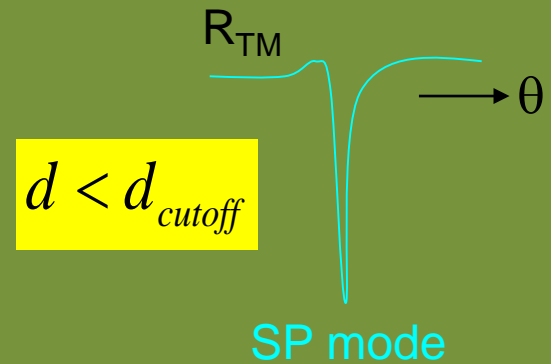
Case of adding nano-overlayer with high refractive index on top of the metal layer!



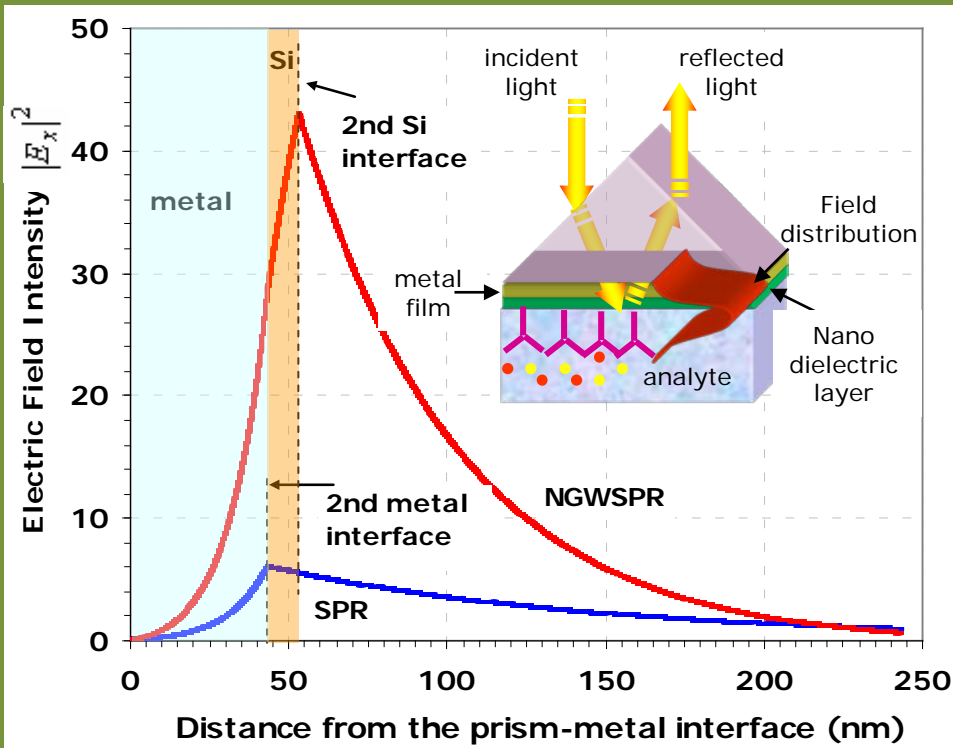
1st case: Adding top nano-dielectric Layer



GWSPR vs. NGWSPR



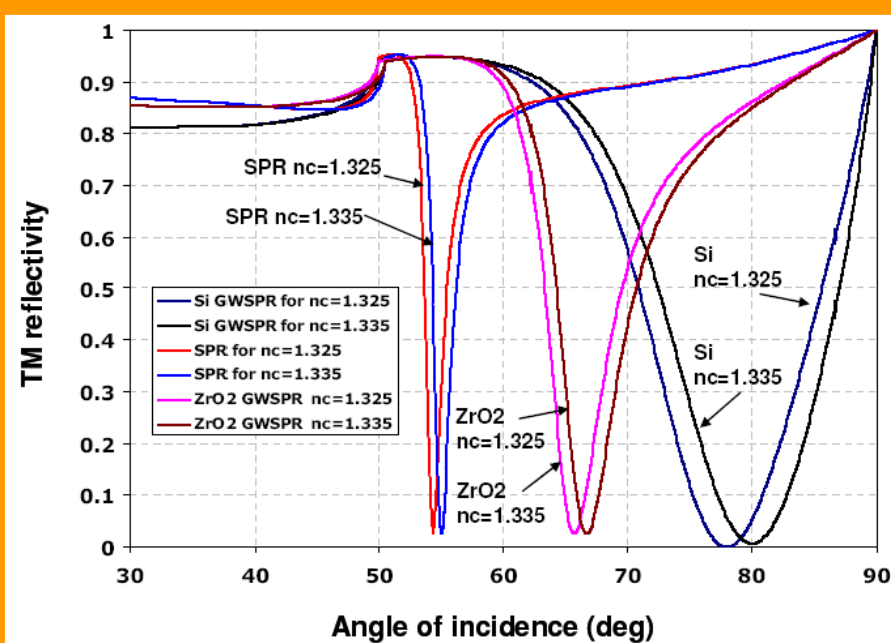
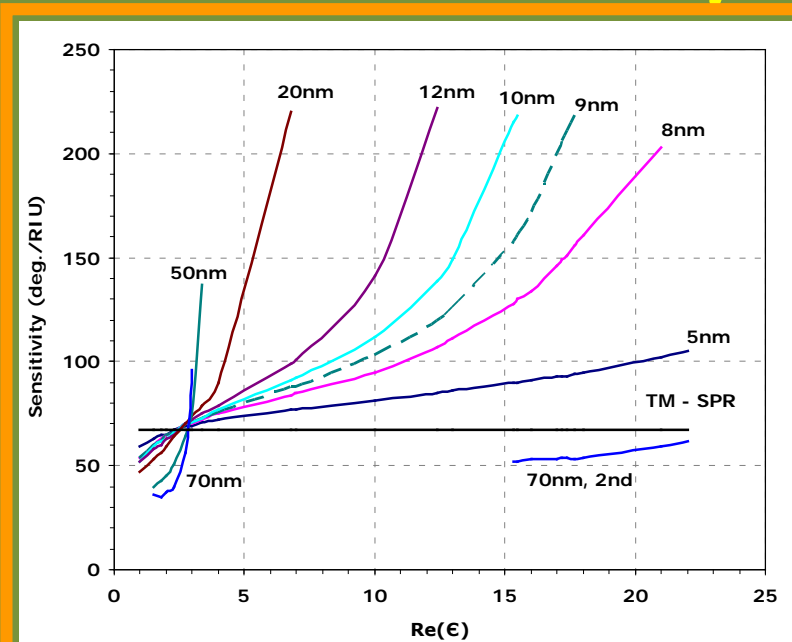
1st case: Adding top nano-dielectric Layer



Amit Lahav, Mark Auslender and I. Abdulhalim, Sensitivity enhancement of guided wave surface plasmon resonance sensors, *Opt.Lett.* 33, 2539-2541 (2008).

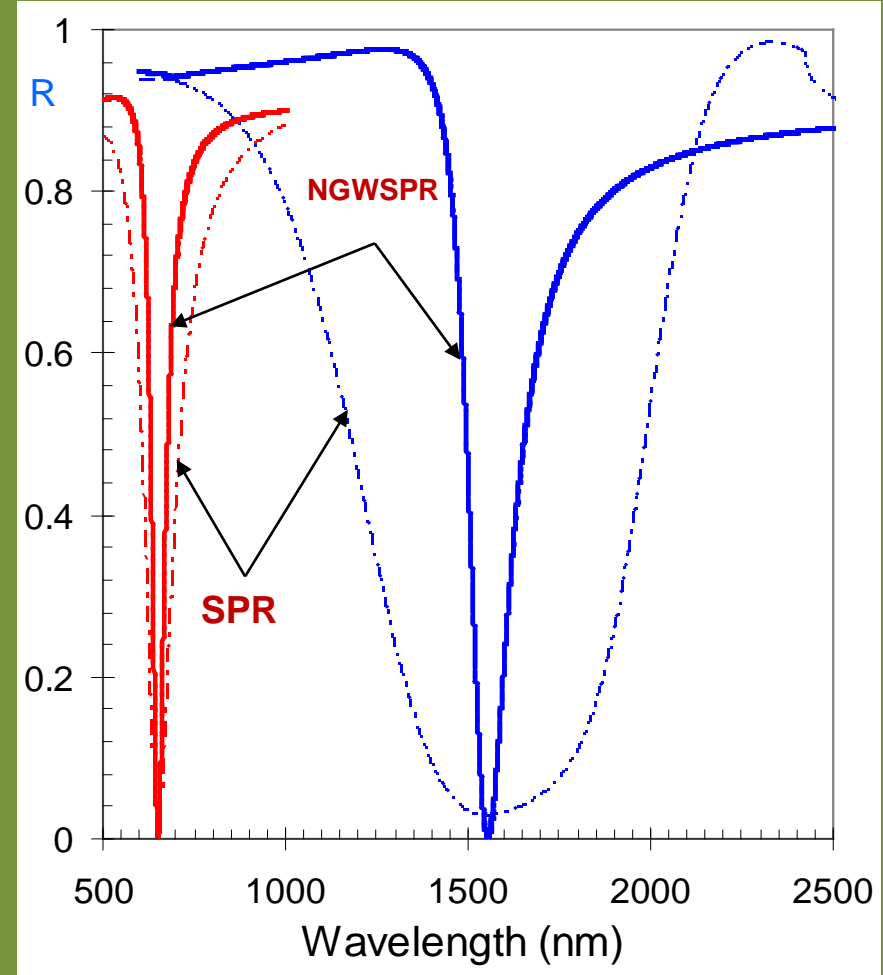
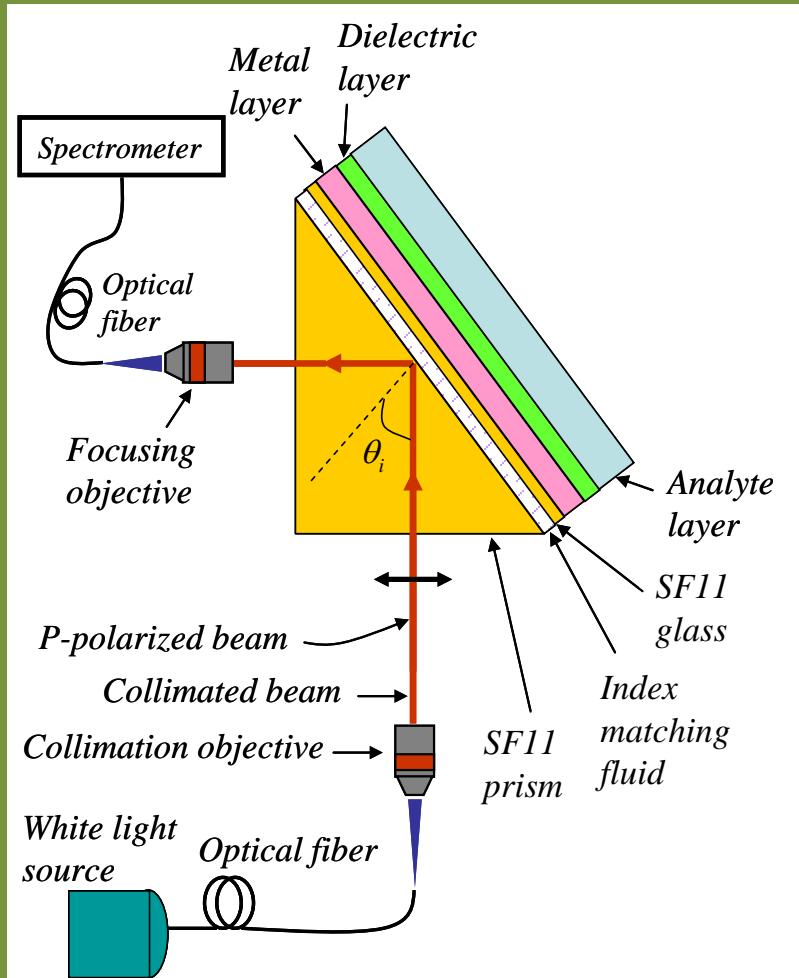
Amit Lahav, Atef Shalabney, I. Abdulhalim, Surface plasmon resonance sensor with enhanced sensitivity using nano-top dielectric layer, *Journal of Nano-photonics* 3, 031501 (2009).

Sabine Szunerits, Atef Shalabney, Rabah Boukherroub and I. Abdulhalim, Dielectric coated plasmonic interfaces: their interest for sensitive sensing of analyte-ligand interactions, *Anal.Chem.* 31, 15-28 (2012).



Improving the FoM with top Nanofilm

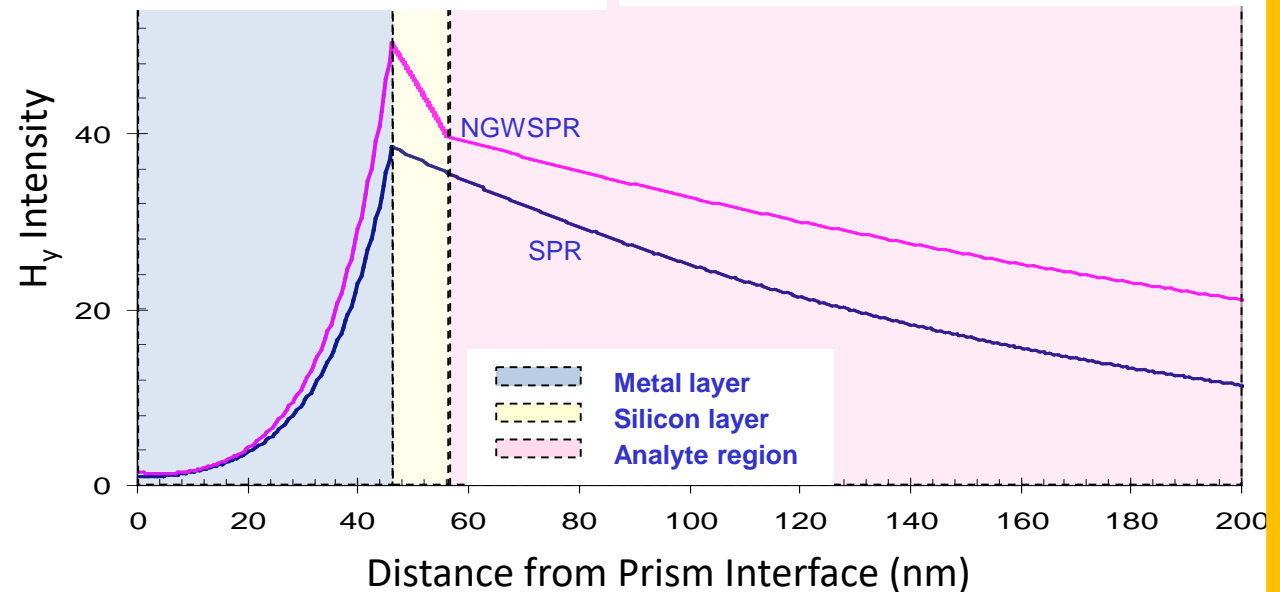
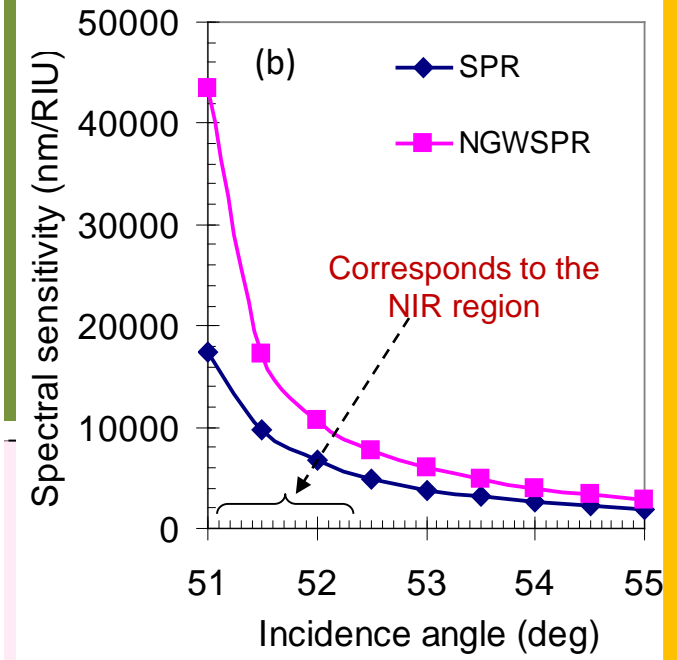
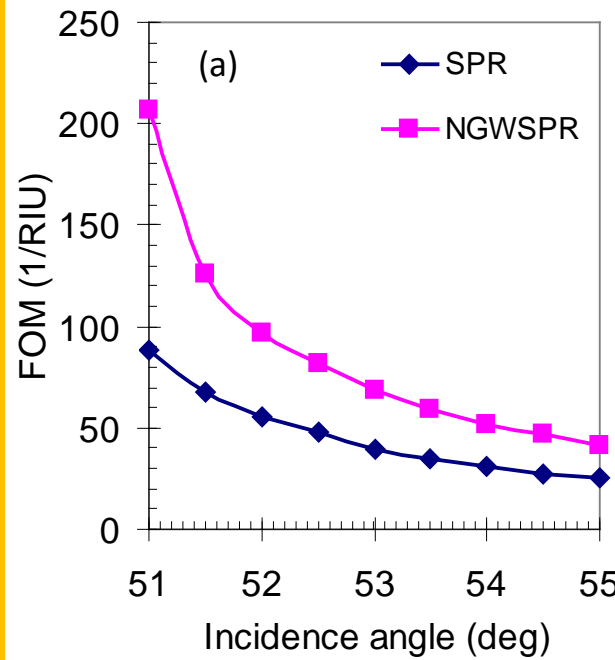
NGWSPR- spectral interrogation- dip narrowing



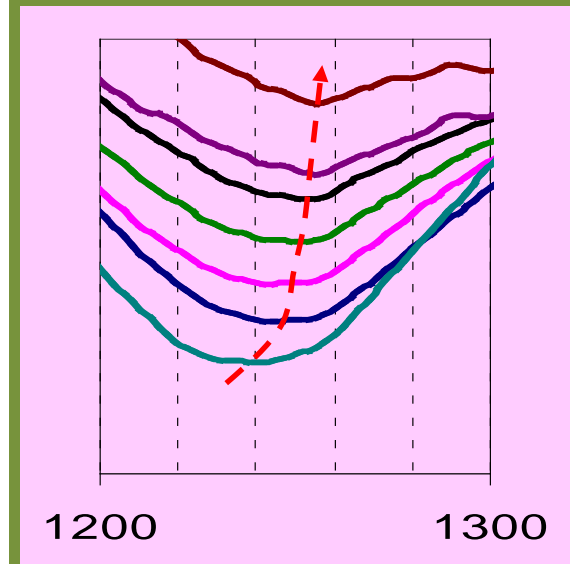
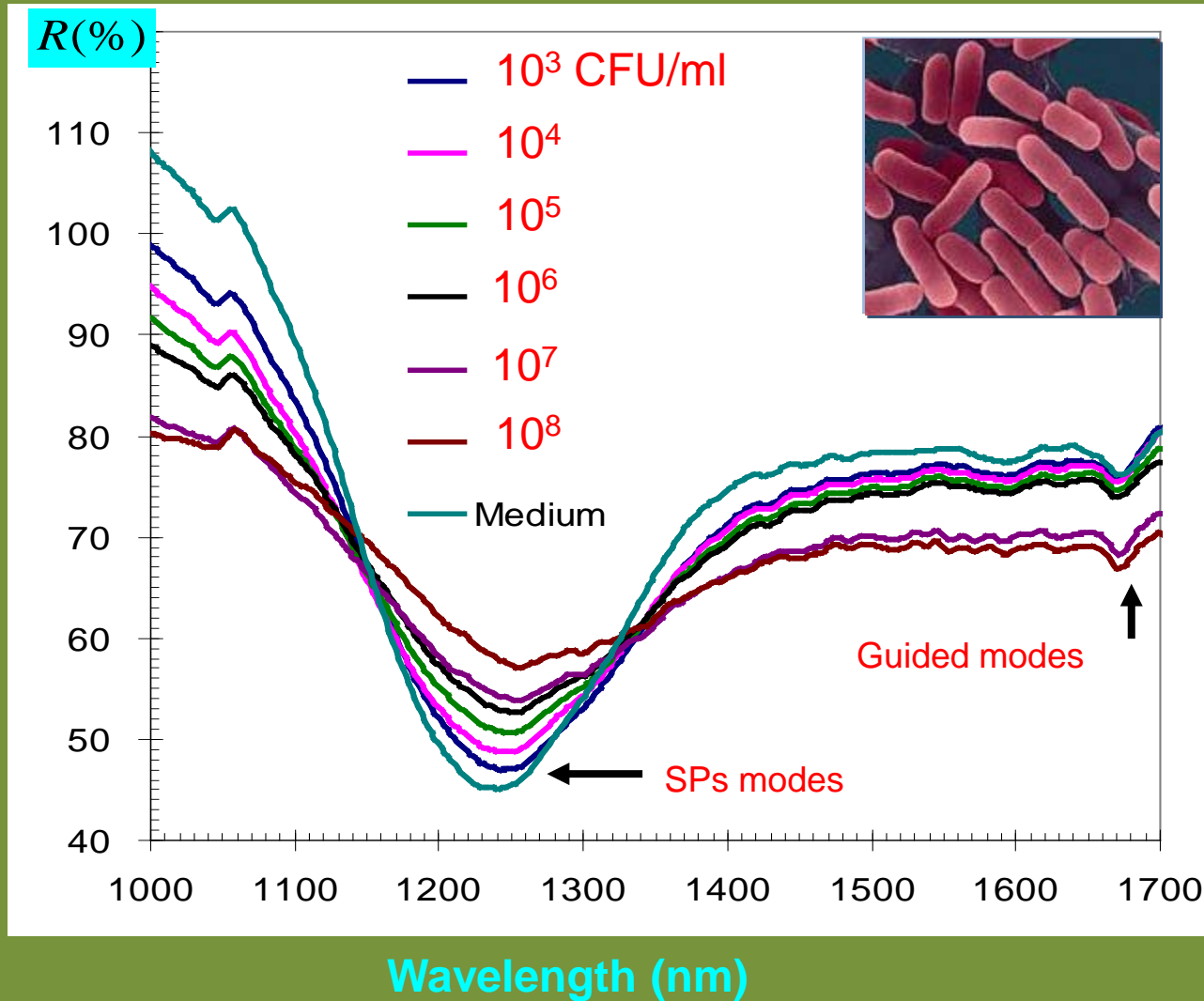
The incident angle is adjusted for both SPR and NGWSPR to determine the wavelength location

Improving the S-FoM with top Nanofilm

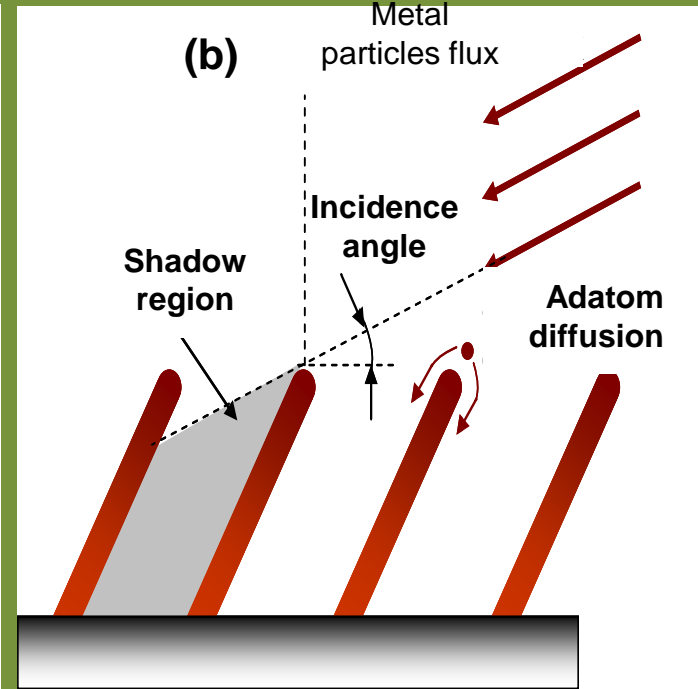
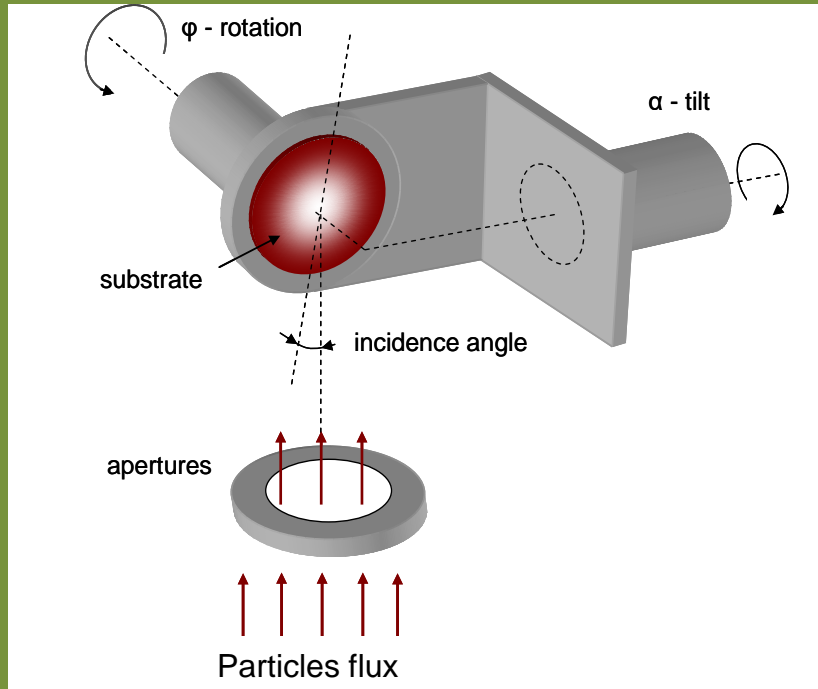
- Same incidence angle
- Larger EM fields
- Larger sensitivity
- Larger penetration depth
- Larger FOM



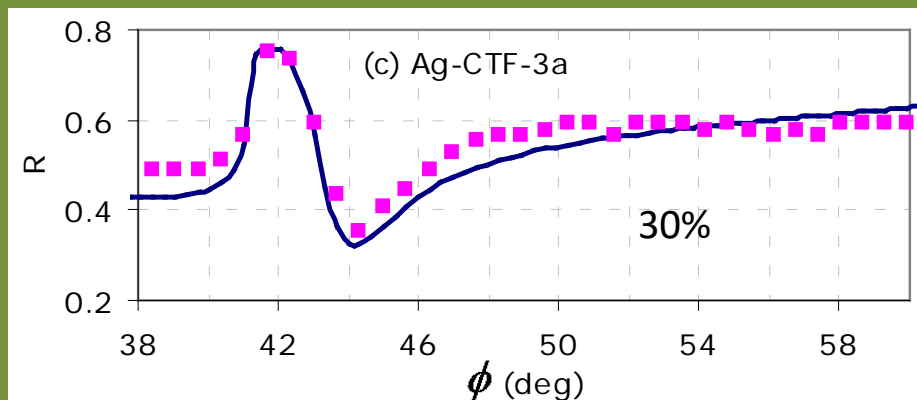
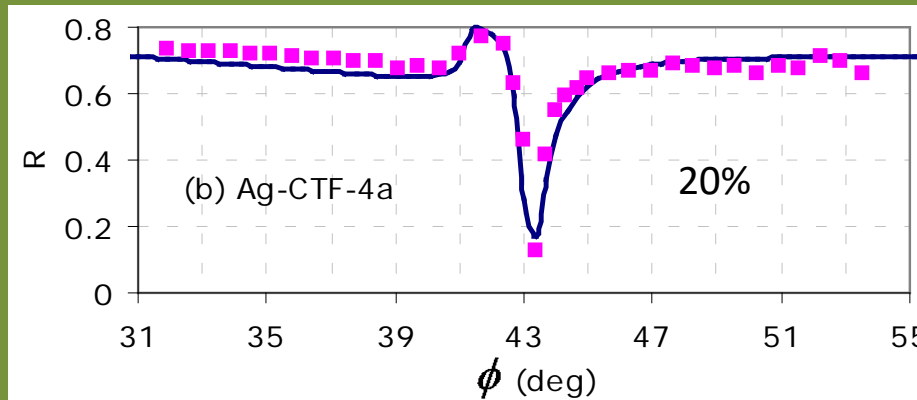
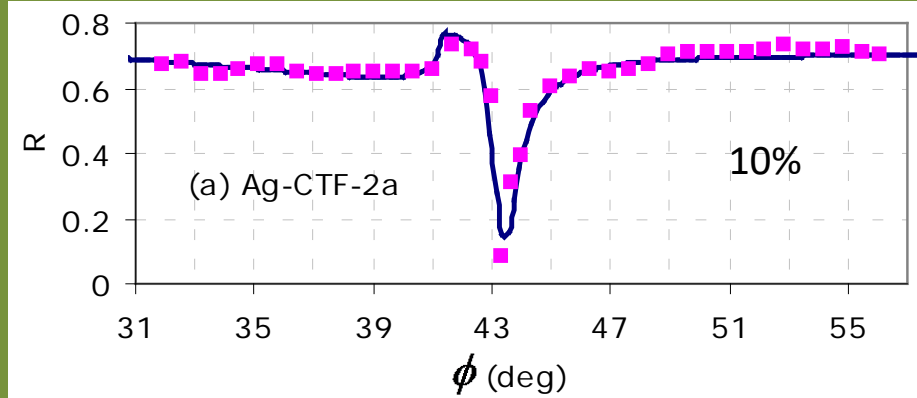
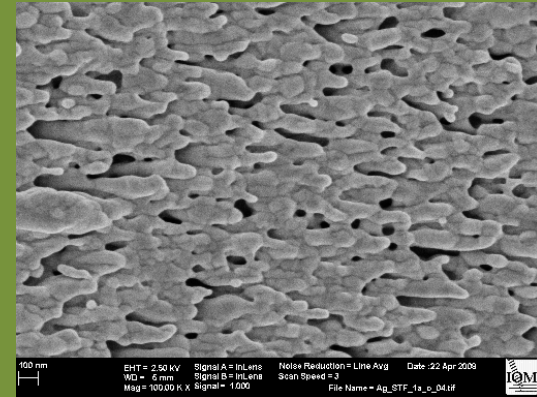
It Enables Detecting Bacteria with NIR



2nd Case: Porosity Effect - nSTFs



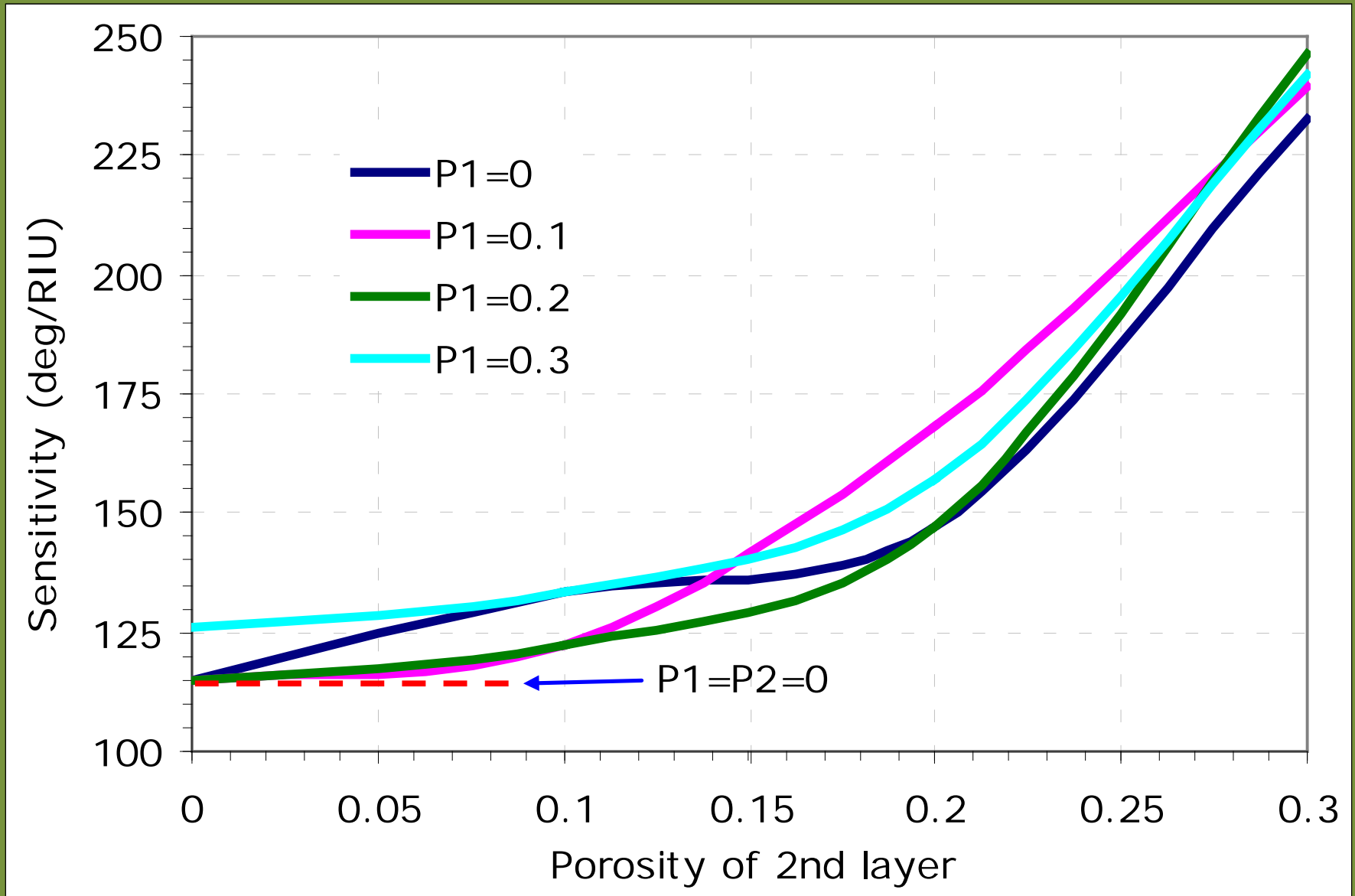
SPR at Different Porosities



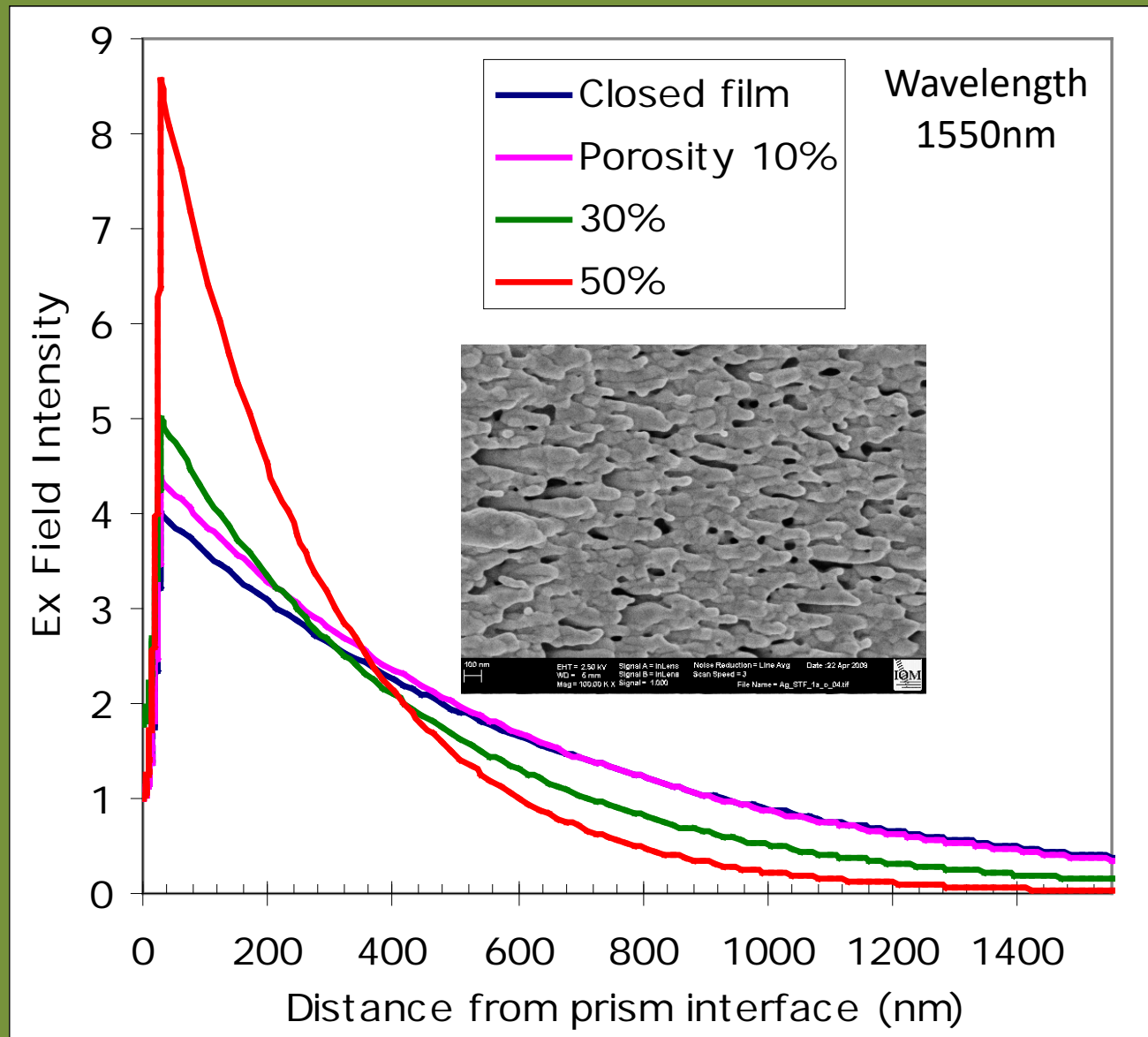
Increasing
film
porosity

A. Shalabney, A. Lakhtakia, I. Abdulhalim, A. Lahav, Christian Patzig, I. Hazeq, A. Karabchevsky, Bernd Rauschenbach, F. Zhang, J. Xu, Surface plasmon resonance from metallic columnar thin films, *Photon Nanostruct: Fundam Appl.* 7, 176-185 (2009)

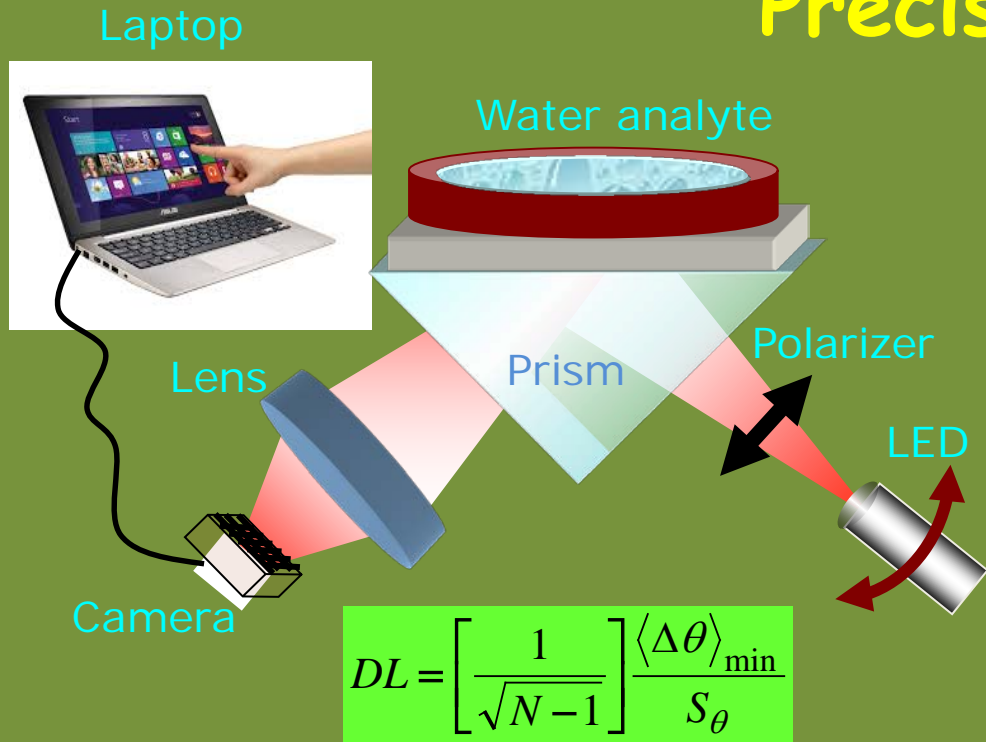
Sensitivity Increases with Porosity



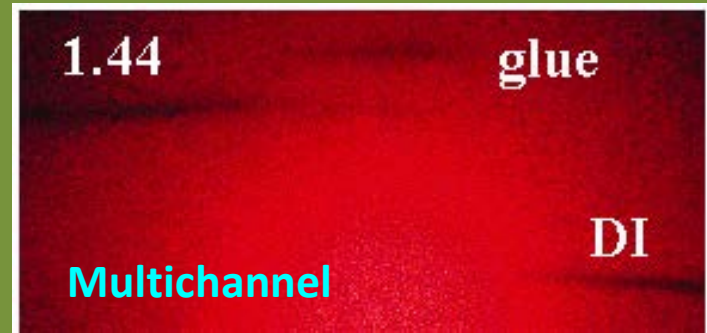
Field Enhancement with Porosity



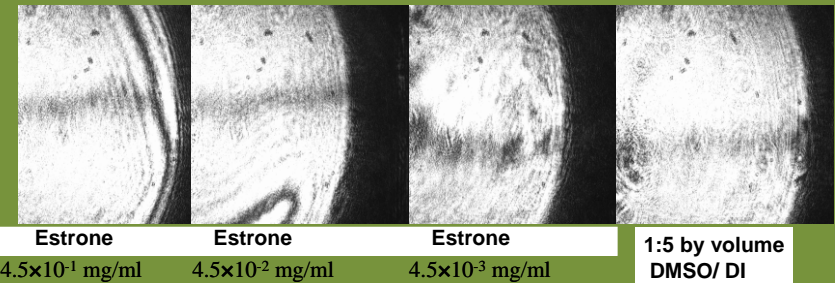
System Simplification and Improved Precision



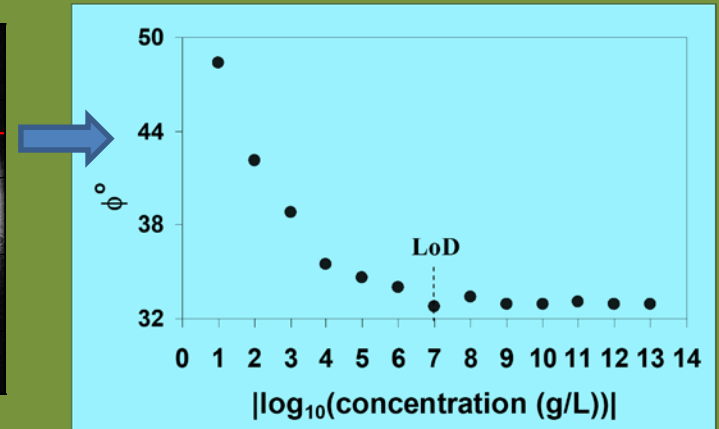
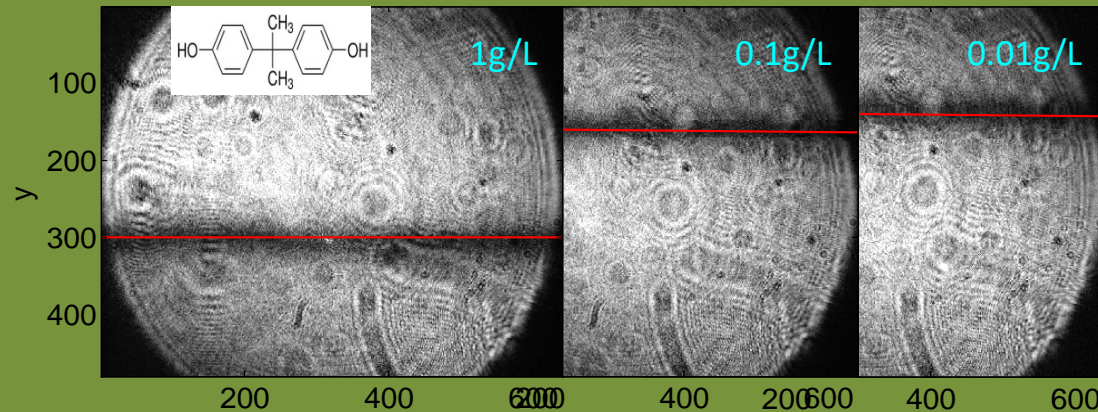
$$DL = \left[\frac{1}{\sqrt{N-1}} \right] \frac{\langle \Delta\theta \rangle_{\min}}{S_\theta}$$



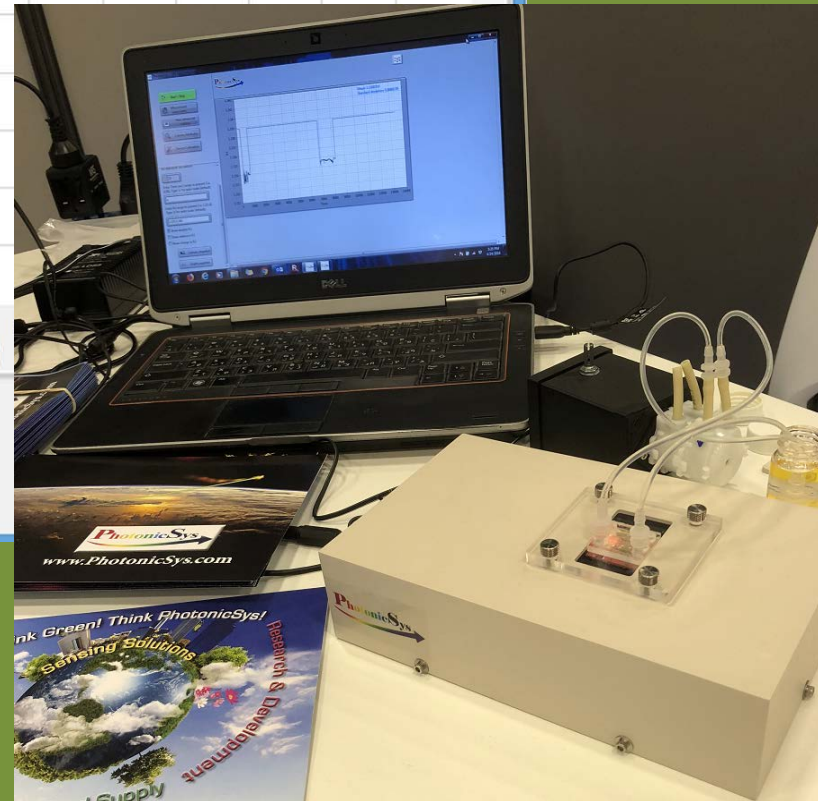
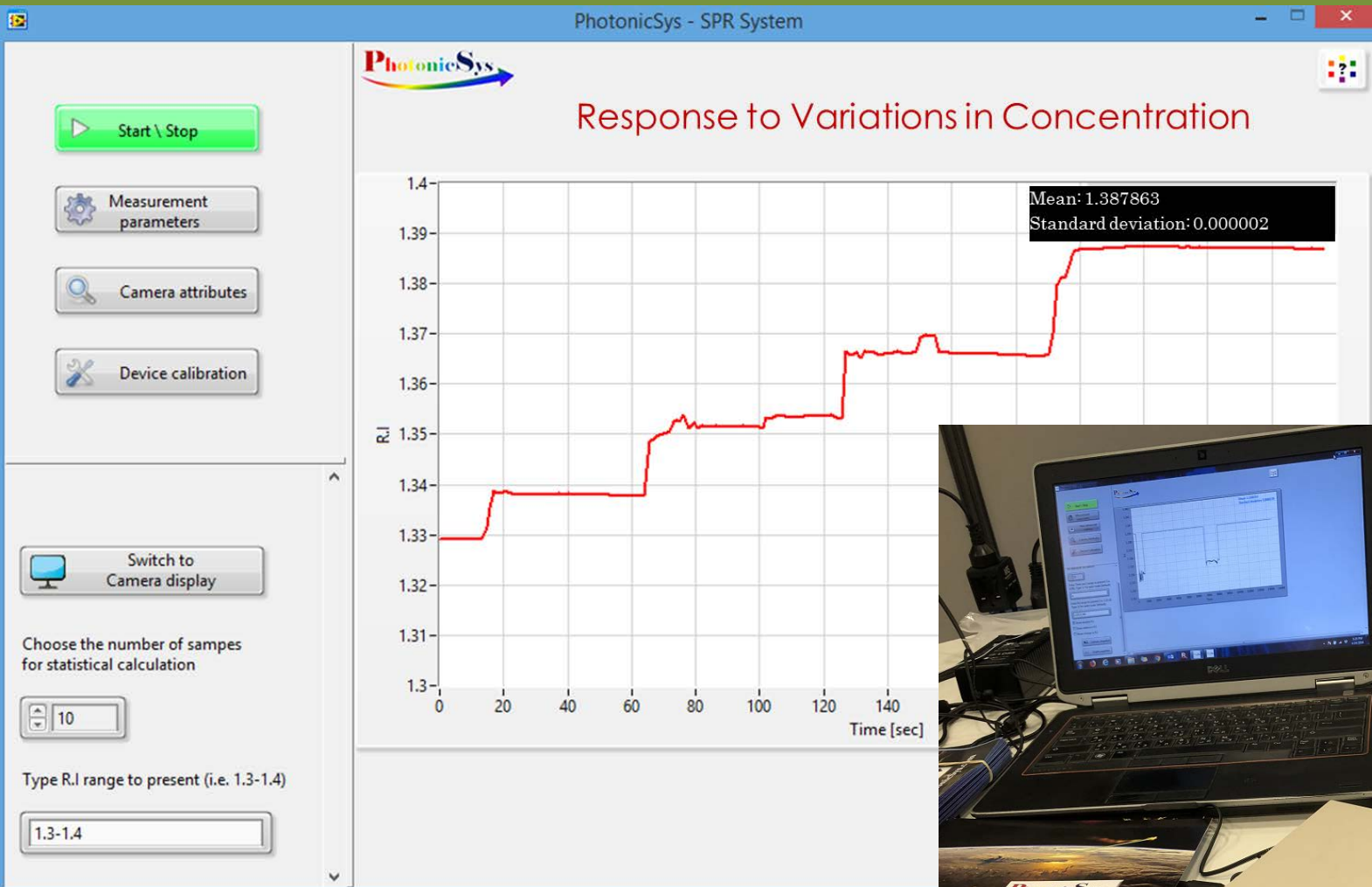
Estrone Detection in Water



BPA Detection in Water

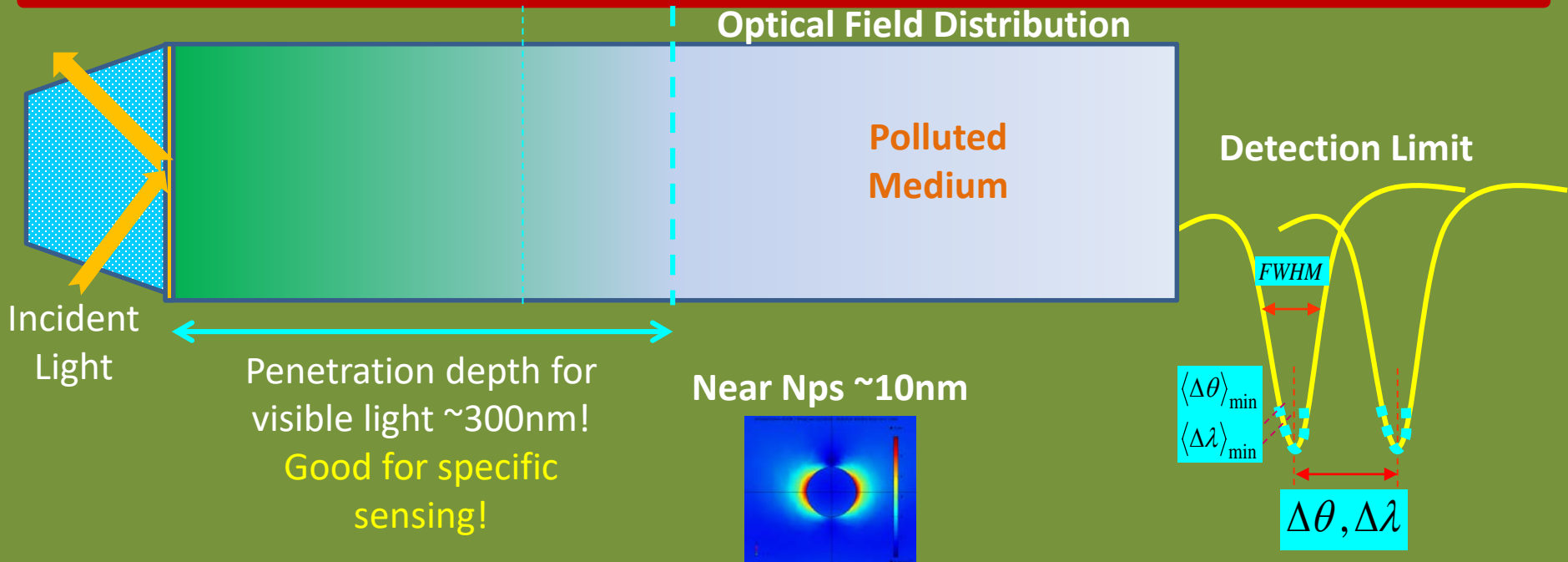
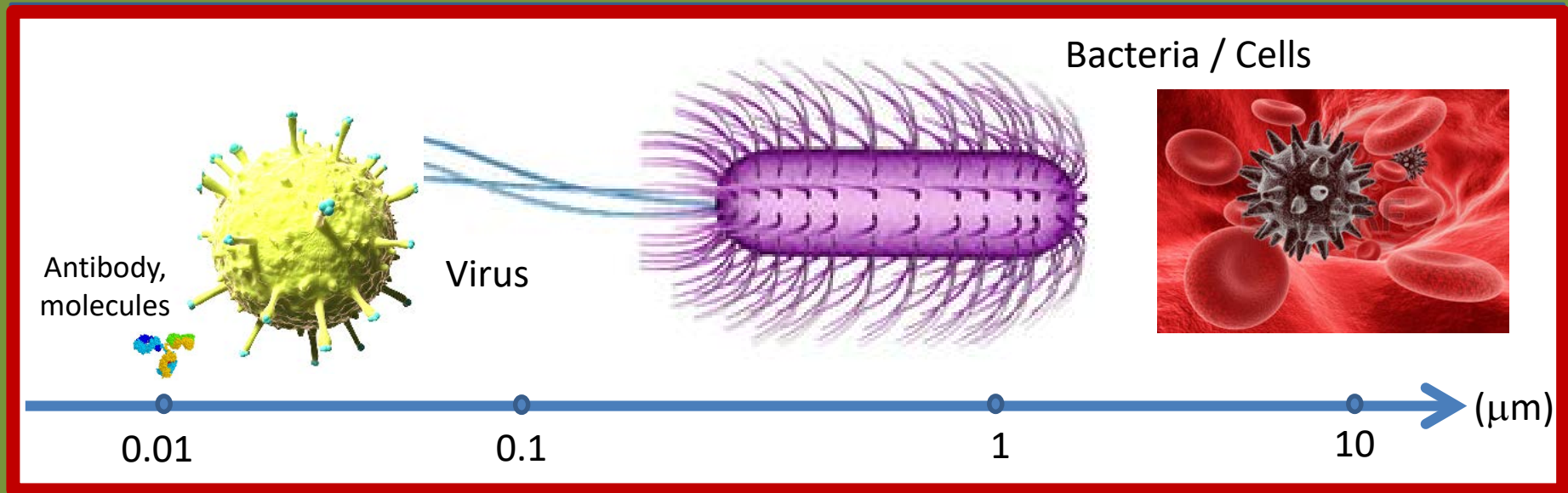


System Miniaturization

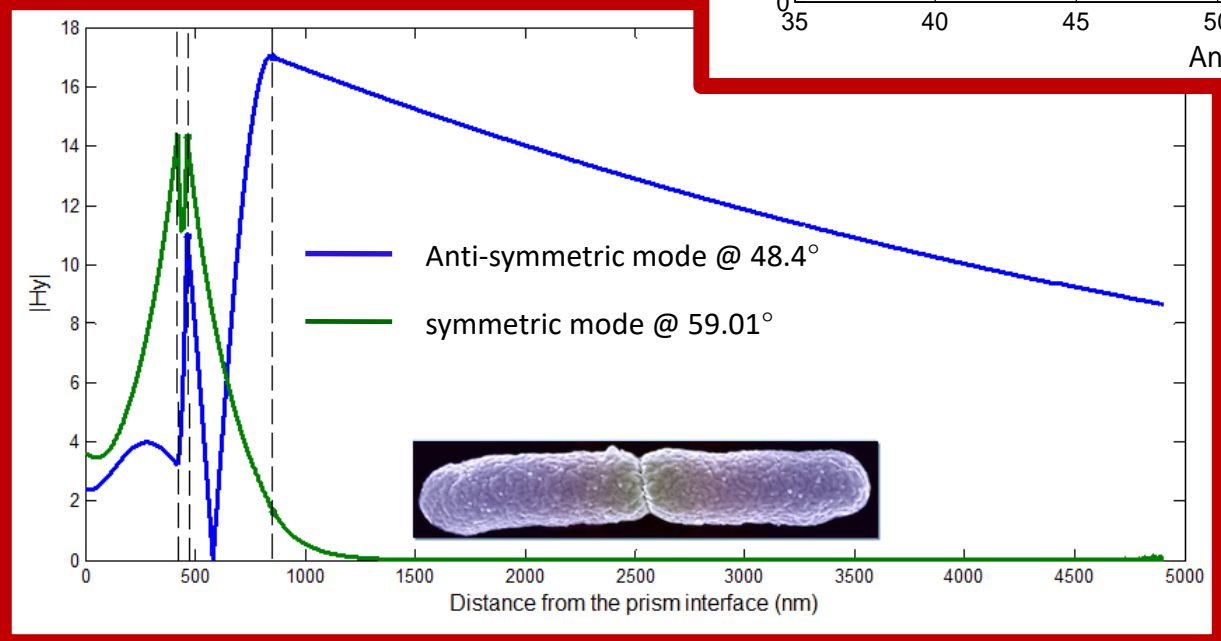
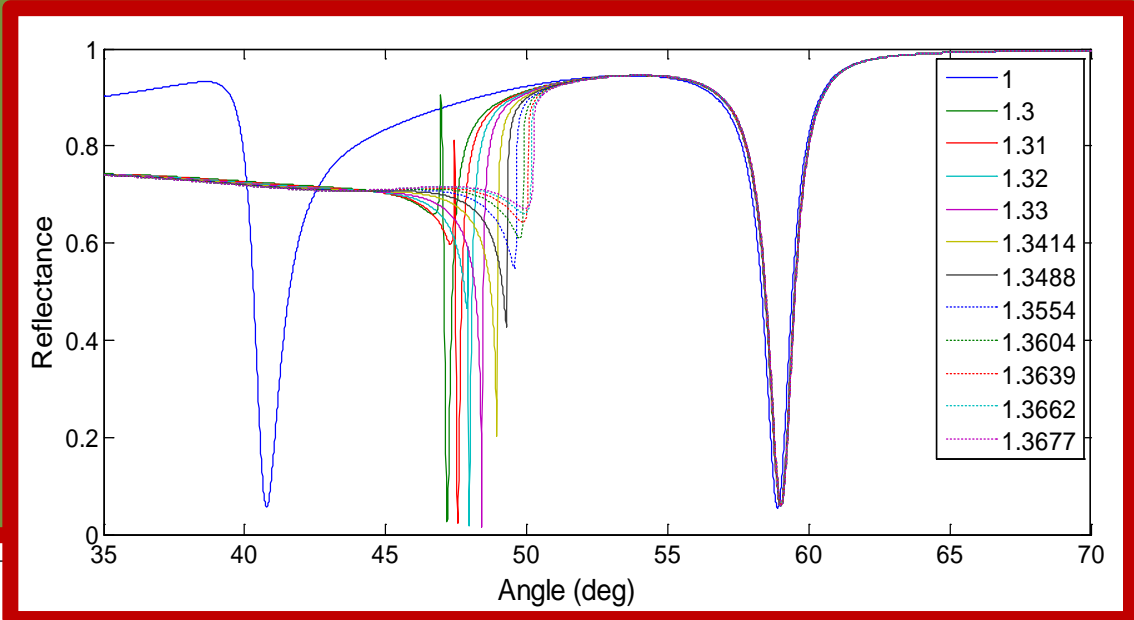


With permission from: www.photonicsys.com

The Field Penetration Depth Importance

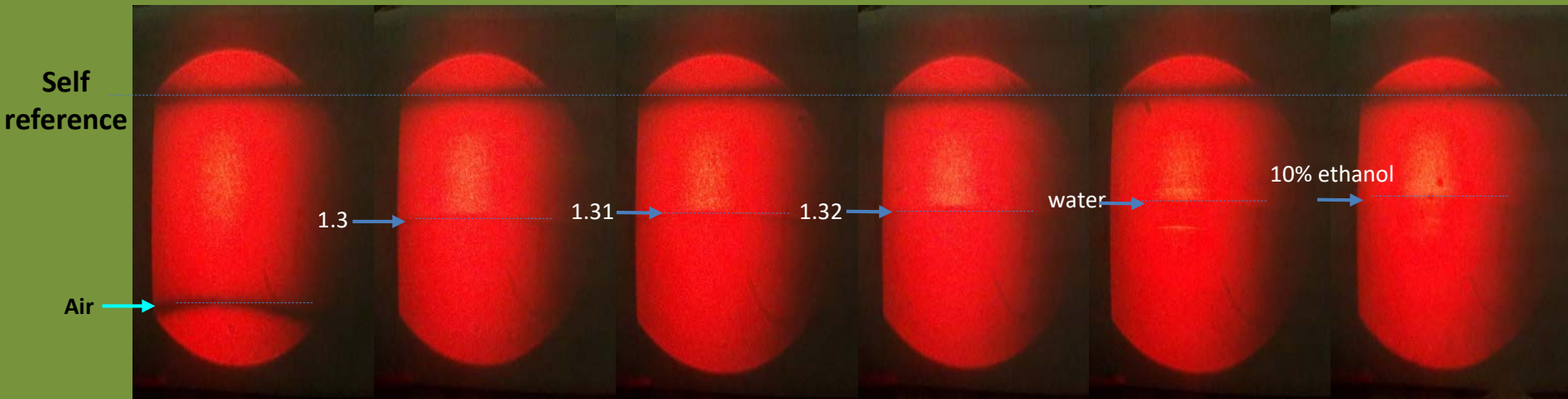


Ultra-high Penetration Depth Self Referenced GW-SPR Sensor

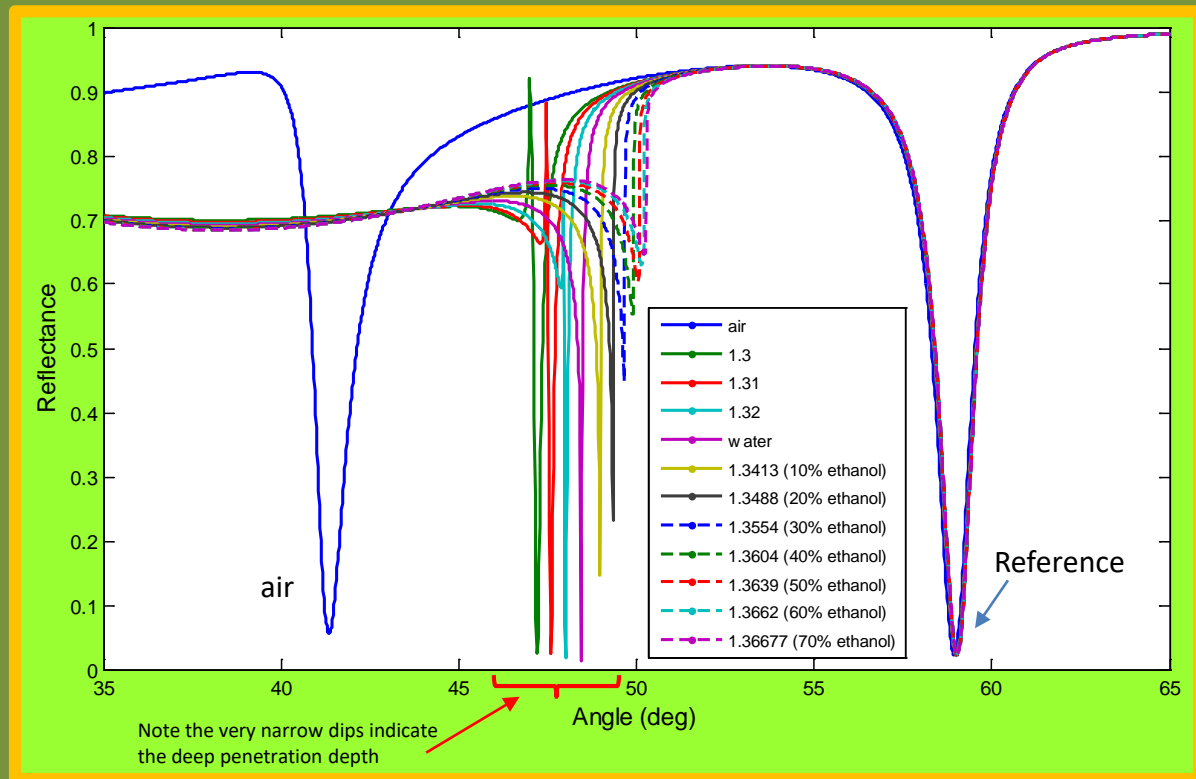


Sivan Issacs and Ibrahim Abdulhalim, *Appl.Phys.Lett.* 106, 193701-4 (2015).

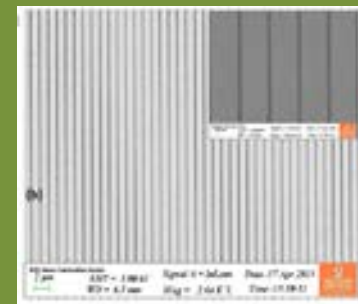
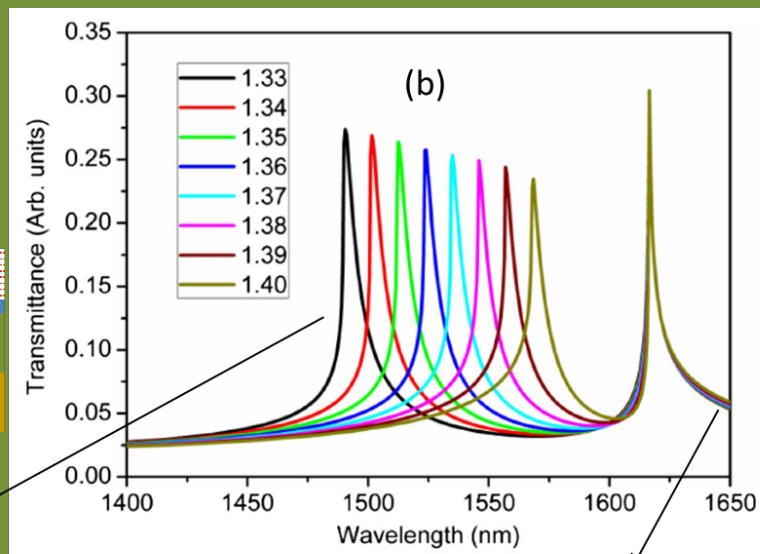
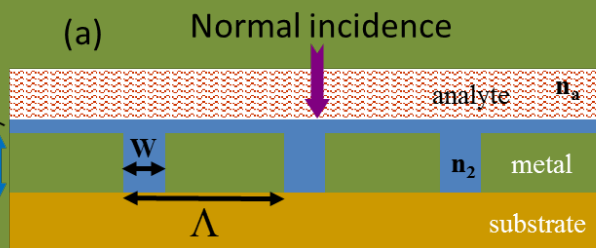
Experimental Confirmation



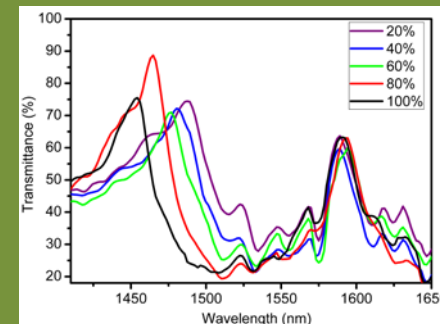
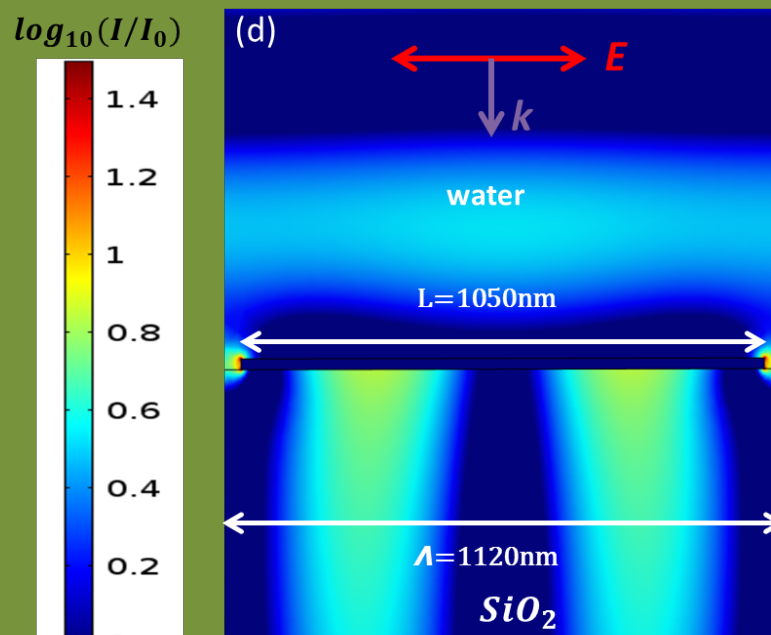
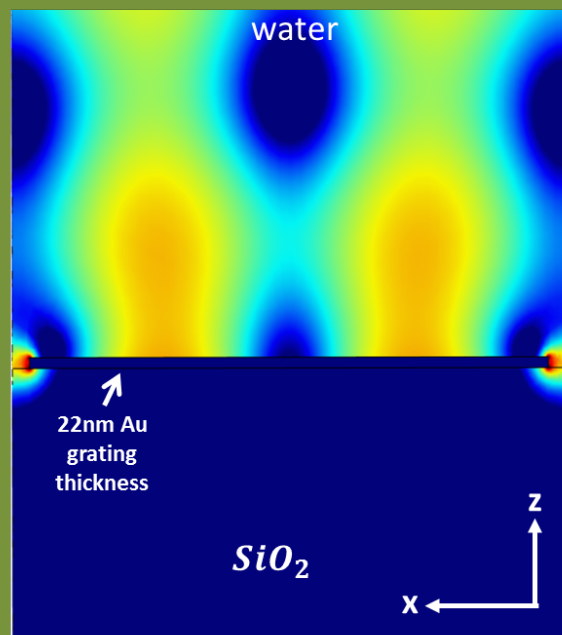
Sivan Issacs et.al., Long range surface plasmon resonance with ultrahigh penetration depth for self-referenced sensing and ultralow detection limit using diverging beam approach, *Appl.Phys.Lett.* 106, 193701-4 (2015).



Self Referenced SPR with Grating Coupling

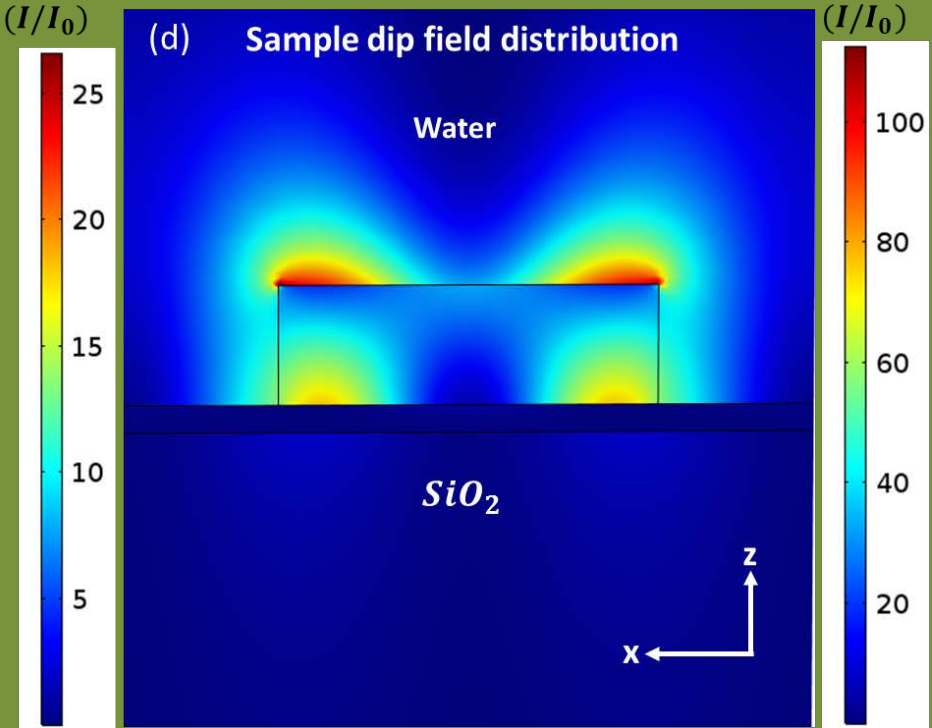
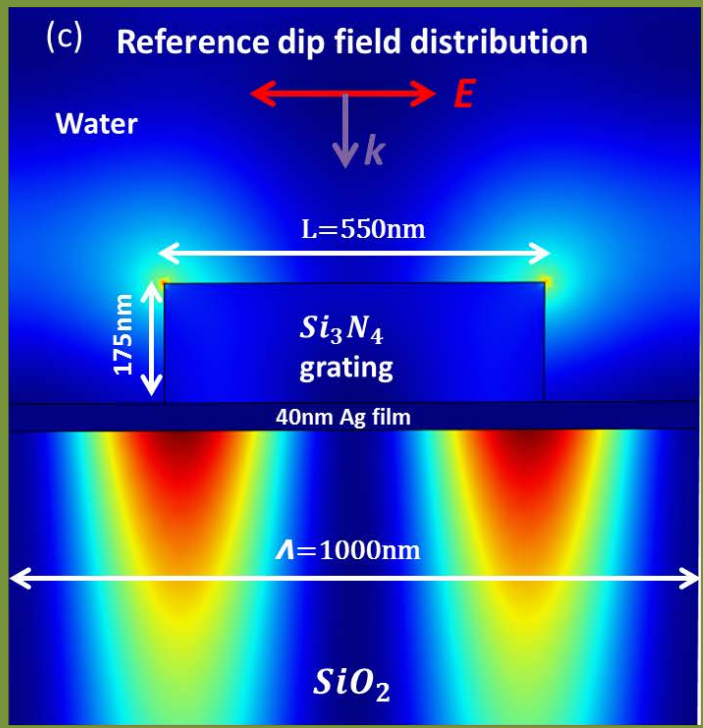
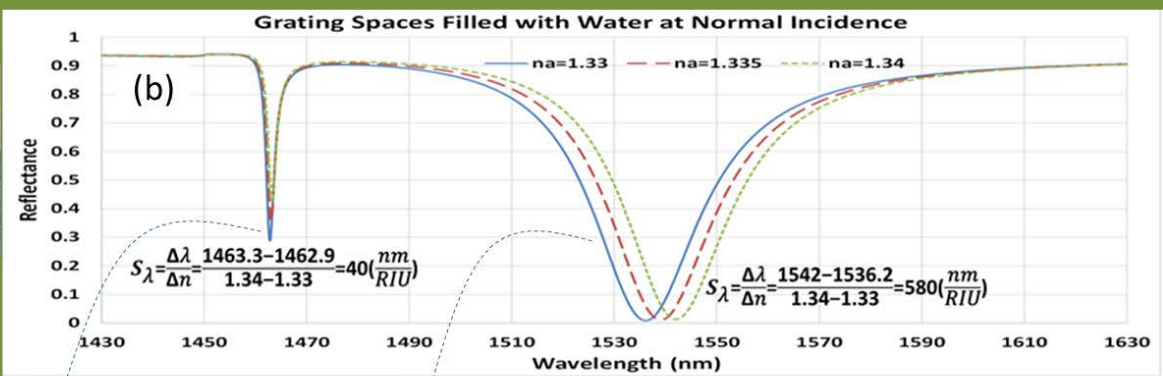
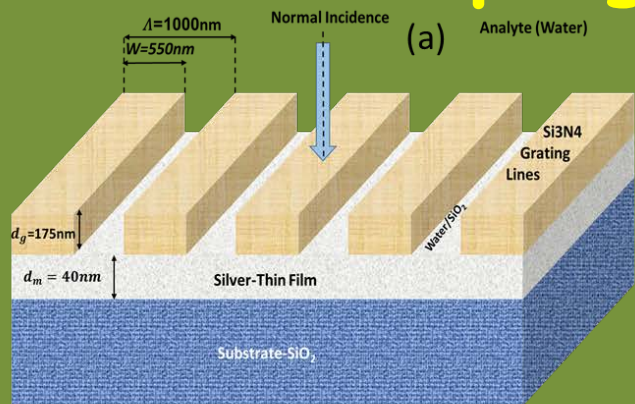


(c) Sample dip field distribution $(I/I_0)_{\max} \approx 10^3$ Reference dip field distribution



- Sachin K. Srivastava and Ibrahim Abdulhalim, *Opt. Lett.* 40, 2425-28 (2015).
- Olga Krasnykov et al., *Opt. Commu.* 284, 1435-1438 (2011).
- Alina Karabchevsky, et al., *Journal of Plasmonics*, 4, 281-292 (2009).

Self Referenced SPR Thin Dielectric Grating Coupling on Thin Metal Film



Summary and Future Trends

- **SPR biosensors have a large growing market**
- **Field of interest are environmental sensing and health**
- **SPR Physics/optics allows for many different modes with variety of improvements in the performance. All originates from the EM field distribution/enhancement**
- **SPR systems can be miniaturized made portable and cheap.**
- **For the future specific sensing should be developed more through binding layers development**